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HEAT TRANSFER

MECHANICAL ENGINEERING

Date of Test : 27/07/2023**ANSWER KEY >**

- | | | | | |
|--------|---------|---------|---------|---------|
| 1. (d) | 7. (b) | 13. (c) | 19. (c) | 25. (c) |
| 2. (d) | 8. (a) | 14. (b) | 20. (b) | 26. (d) |
| 3. (a) | 9. (c) | 15. (a) | 21. (a) | 27. (a) |
| 4. (d) | 10. (d) | 16. (b) | 22. (b) | 28. (c) |
| 5. (d) | 11. (b) | 17. (b) | 23. (a) | 29. (d) |
| 6. (a) | 12. (c) | 18. (a) | 24. (a) | 30. (c) |

DETAILED EXPLANATIONS

1. (d)

$$\eta = \frac{Q_{\text{actual}}}{Q_{\text{ideal}}} = \frac{\sqrt{hPkA}(T_b - T_{\infty})}{hA_{\text{fin}}(T_b - T_{\infty})} = \frac{\sqrt{hPkA}}{hPL} = \frac{1}{L} \sqrt{\frac{kA}{hP}}$$

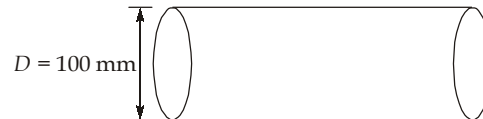
For circular fin

$$A = \frac{\pi}{4} d^2$$

$$P = \pi d$$

$$\eta = \frac{1}{L} \sqrt{\frac{kd}{4h}} = \frac{1}{2L} \sqrt{\frac{kd}{h}}$$

2. (d)



Diameter of steel pipe, $D = 100 \text{ mm}$

Nusselt number, $Nu = 20$

Thermal conductivity, $k = 0.06 \text{ W/mK}$

For horizontal pipe, $Nu = \frac{hD}{k}$

$$\Rightarrow 20 = \frac{h \times 0.1}{0.06}$$

Heat transfer coefficient, $h = 12 \text{ W/m}^2\text{K}$

3. (a)

$$\nu < \alpha$$

$$Pr = \frac{\nu}{\alpha}, \text{ so } Pr < 1$$

For $Pr < 1$, $\frac{\delta_t}{\delta_v} > 1$

$$\delta_t > \delta_v \text{ or } \delta_v < \delta_t$$

4. (d)

5. (d)

Critical radius of insulation, $r_c = \frac{k}{h_o}$

$$= \frac{0.5}{10} = 0.05 \text{ m} = 50 \text{ mm}$$

Maximum value of heat dissipation rate,

$$q_{\max} = \frac{\Delta T}{\frac{\ln\left(\frac{r_o}{r_i}\right)}{2\pi kL} + \frac{1}{hA_o}} = \frac{100 - 25}{\frac{\ln(50/0.5)}{2\pi \times 0.5 \times 1} + \frac{1}{2\pi \times \frac{50}{1000} \times 1 \times 10}} = 42.036 \text{ W/m}$$

6. (a)

Heat transfer rate through composite structural wall, $q_1 = -k_1 A \frac{\Delta T}{\delta_1} = -0.2 A \frac{\Delta T}{0.09}$

Heat transfer rate through masonry wall,

$$q_2 = -k_2 A \frac{\Delta T}{\delta_2} = -0.7 A \times \frac{\Delta T}{\delta_2}$$

As per given condition,

$$\begin{aligned} q_2 &= 0.6q_1 \\ \Rightarrow -0.7 A \times \frac{\Delta T}{\delta_2} &= 0.6 \times \left(-0.2 A \times \frac{\Delta T}{0.09} \right) \\ \delta_2 &= 0.525 \text{ m} = 525 \text{ mm} \end{aligned}$$

7. (b)

For parallel flow heat exchanger,

$$\varepsilon = \frac{1 - \exp(-NTU(1+C))}{1+C}$$

Put $C = 0$,

$$\begin{aligned} \varepsilon &= \frac{1 - \exp(-NTU)}{1} \\ \varepsilon &= 1 - \exp(-NTU) \end{aligned}$$

For counter flow heat exchanger,

$$\varepsilon = \frac{1 - \exp\{-NTU(1-C)\}}{1 - C \exp\{-NTU(1-C)\}}$$

Put $C = 0$,

$$\begin{aligned} \varepsilon &= \frac{1 - \exp\{-NTU(1-0)\}}{1 - 0 \times \exp\{-NTU(1-0)\}} \\ \varepsilon &= 1 - \exp(-NTU) \end{aligned}$$

So, expression:

$$\varepsilon = 1 - \exp(-NTU)$$

is valid for all the heat exchangers having zero capacity ratio.

8. (a)

$$\begin{aligned} \frac{k_Q [100 - T] A}{l} &= \frac{k_P [T - 0] A}{l} \\ k_P &= 4 k_Q \\ 100 - T &= 4T \\ 5T &= 100 \\ T &= 20^\circ\text{C} \end{aligned}$$

9. (c)

Reflectivity, $\rho = 0.4$

For opaque body,

$$\alpha + \rho = 1$$

$$\alpha + 0.4 = 1$$

$$\text{Absorptivity, } \alpha = 0.6 = \frac{G_{abs}}{G} = \frac{G_{abs}}{600}$$

Part of radiation absorbed,

$$G_{abs} = 0.6 \times 600 = 360 \text{ W/m}^2$$

10. (d)

For infinitely long fin,

$$\dot{q} = \sqrt{hPkA} (T_b - T_\infty)$$

For circular fin, $P = \pi D$

$$A = \frac{\pi D^2}{4}$$

So,

$$\dot{q} = \sqrt{h \times \pi D \times k \times \frac{\pi D^2}{4}} (T_b - T_\infty)$$

$$\dot{q} \propto \sqrt{k} D^{3/2}$$

$$\frac{\dot{q}_1}{\dot{q}_2} = \frac{\sqrt{k_1} D_1^{3/2}}{\sqrt{k_2} D_2^{3/2}} = \left(\frac{400}{250} \right)^{1/2} \left(\frac{D}{0.4D} \right)^{3/2} = 5$$

11. (b)

$$\frac{T(t) - T_\infty}{T_i - T_\infty} = e^{-bt}$$

$$\Rightarrow \frac{\frac{T_i + T_\infty}{2} - T_\infty}{T_i - T_\infty} = e^{-bt}$$

$$\Rightarrow \frac{1}{2} = e^{-bt}$$

Where $b = \frac{1}{\tau}$

$$\begin{aligned} \text{Time required, } t &= \frac{\ln 2}{b} \\ &= \tau \ln 2 = 10 \times 0.693 = 6.93 \text{ s} \end{aligned}$$

12. (c)

Mass flow rate of air, $\dot{m}_h = 1 \text{ kg/s}$

Specific heat at constant pressure of air, $c_{ph} = 1.005 \text{ kJ/kgK}$

$$\dot{m}_h c_{ph} = 1 \times 1.005 = 1.005 \text{ kW/K}$$

Mass flow-rate of water, $\dot{m}_c = 2 \text{ kg/s}$

$$c_{pc} = 4.18 \text{ kJ/kgK}$$

$$\dot{m}_c c_{pc} = 2 \times 4.18 = 8.36 \text{ kW/K}$$

Since, $\dot{m}_h c_{ph} < \dot{m}_c c_{pc}$

$$C_{\min} = \dot{m}_h c_{ph} = 1.005 \text{ kW/K}$$

Maximum heat transfer rate,

$$\begin{aligned} q_{\max} &= C_{\min}(T_{hi} - T_{ci}) \\ &= 1.005 \times (80 - 15) = 65.325 \text{ kW} \end{aligned}$$

13. (c)

Case I : $Re_1 = \frac{V_1 L_1}{\nu_1} = \frac{100 \times 1}{\nu_1} = \frac{100}{\nu_1}$

Case II : $Re_2 = \frac{V_2 L_2}{\nu_2} = \frac{20 \times 5}{\nu_2} = \frac{100}{\nu_2}$

For same fluid $\nu_1 = \nu_2$ and $Pr_1 = Pr_2$

We know that Nusselt number,

$$Nu = f(Re, Pr)$$

So, $Nu_1 = Nu_2$

$$\frac{h_1 L_1}{k_1} = \frac{h_2 L_2}{k_2}$$

$$h_2 = \frac{h_1 \times L_1}{L_2} \quad (K_1 = K_2)$$

Case I : $q''_1 = h_1(T_s - T_\infty)$

$$\frac{20,000}{(400 - 300)} = h_1$$

$$h_1 = 200 \text{ W/m}^2\text{K}$$

So, $h_2 = \frac{200 \times 1}{5} = 40 \text{ W/m}^2\text{K}$

14. (b)

Without shield

Radiation heat transfer rate,

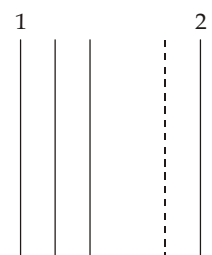
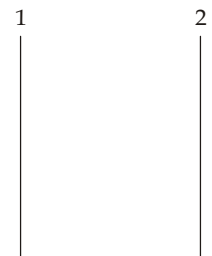
$$q = \frac{\sigma(T_1^4 - T_2^4)}{\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1}$$

Let number of shields be N .

With shield

Radiation heat transfer rate,

$$q' = \frac{\sigma(T_1^4 - T_2^4)}{\left(\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1\right) + N\left(\frac{2}{\epsilon} - 1\right)}$$



As per the conditions,

$$q' = (1 - 0.9)q$$

$$\frac{q}{q'} = \frac{1}{0.1} = 10$$

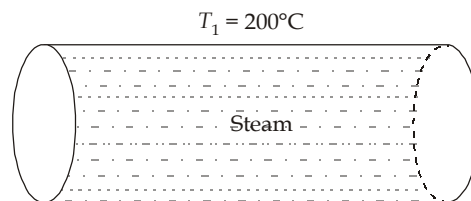
$$\frac{\left(\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1\right) + N\left(\frac{2}{\epsilon} - 1\right)}{\left(\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1\right)} = 10$$

$$\frac{\left(\frac{1}{0.8} + \frac{1}{0.6} - 1\right) + N\left(\frac{2}{0.29} - 1\right)}{\left(\frac{1}{0.8} + \frac{1}{0.6} - 1\right)} = 10$$

Number of shields, $N = 2.925$

$$N \simeq 3$$

15. (a)



Heat transfer rate due to radiation,

$$\begin{aligned} q &= \epsilon \sigma (T_1^4 - T_2^4) \\ &= 0.8 \times 5.67 \times 10^{-8} \times [(200 + 273)^4 - (25 + 273)^4] = 1912.7638 \text{ W/m}^2 \\ &= h_r (T_1 - T_2) \end{aligned}$$

where,

h_r = Radiation heat transfer coefficient

$$\Rightarrow 1912.7638 = h_r \times (200 - 25)$$

$$h_r = 10.93 \text{ W/m}^2\text{K}$$

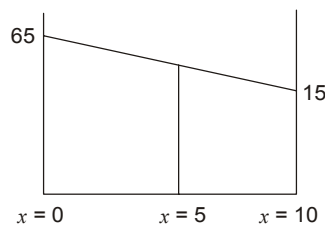
Convection heat transfer coefficient

$$h_c = 6 \text{ W/m}^2\text{-K}$$

So, combined heat transfer coefficient

$$= h_r + h_c = 10.93 + 6 = 16.93 \text{ W/m}^2\text{-K}$$

16. (b)



$$T - 65 = \frac{15 - 65}{10 - 0} [x - 0]$$

$$T = 65 - \frac{50}{10}x$$

$$T = 65 - 5x$$

at $x = 5 \text{ m}$

$$T = 65 - 25 = 40^\circ\text{C}$$

17. (b)

$$A_1 F_{12} = A_2 F_{21}$$

$$F_{21} = \frac{A_1}{A_2} \times F_{12} = \frac{\pi \left(0.75^2 - \left(\frac{0.25}{2} \right)^2 \right)}{2\pi \times (0.75)^2} \times F_{12}$$

$$F_{11} + F_{12} + F_{13} = 1$$

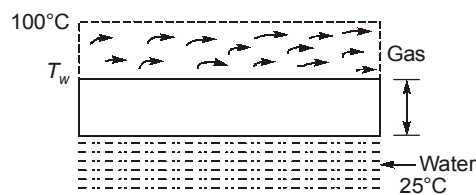
$$F_{1-1} = 0 \quad \text{and } F_{1-3} = 0$$

$$\therefore F_{12} = 1$$

$$F_{21} = \frac{\pi(0.75^2 - 0.125^2)}{2\pi \times 0.75 \times 0.75}$$

$$F_{21} = 0.486$$

18. (a)



$$\text{Rate of heat transfer} = \frac{T_g - T_w}{\Sigma R}$$

$$\Sigma R = \frac{1}{h_g} + \frac{L}{k} + \frac{1}{h_w} = \frac{1}{14500} + \frac{4 \times 10^{-3}}{95.5} + \frac{1}{2250}$$

$$\Sigma R = 5.553 \times 10^{-4} \text{ m}^2\text{K/W}$$

$$Q = \frac{100 - 25}{5.553 \times 10^{-4}} = 135063.4 \text{ W/m}^2$$

$$Q = (T_g - T_p) h_g$$

$$135063.4 = [100 - T_p] 14500$$

$$T_p = 90.7^\circ\text{C}$$

19. (c)

Minimum heat capacity rate,

$$C_{\min} = \dot{m}_c c_{pc} = 3 \times 4.2 = 12.6 \text{ kW/K}$$

Overall heat transfer coefficient, $U = 1600 \text{ W/m}^2\text{C}$ Heat transfer area, $A = 12 \text{ m}^2$

$$NTU = \frac{UA}{C_{\min}} = \frac{1600 \times 12}{12.6 \times 1000} = 1.5238$$

$$\text{Effectiveness, } \varepsilon = 1 - e^{-NTU} = 1 - e^{-(1.5238)} = 0.782$$

20. (b)

For steady state, $\frac{\partial T}{\partial t} = 0$

$$\therefore 0 = \frac{1}{r} \frac{\partial}{\partial r} \left(r \cdot \frac{\partial T}{\partial r} \right) + q$$

$$\frac{\partial}{\partial r} \left(r \cdot \frac{\partial T}{\partial r} \right) = -q \cdot r$$

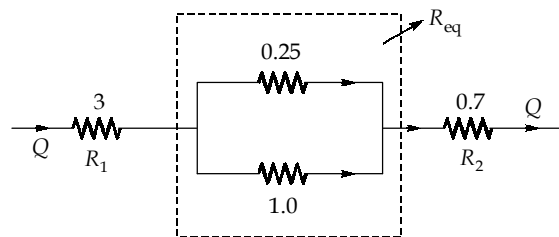
On integration,

$$r \cdot \left(\frac{\partial T}{\partial r} \right) = \frac{-qr^2}{2} + A$$

$$\frac{\partial T}{\partial r} = \frac{-qr}{2} + \frac{A}{r}$$

$$T(r) = \frac{-qr^2}{4} + A \ln r + B$$

21. (a)



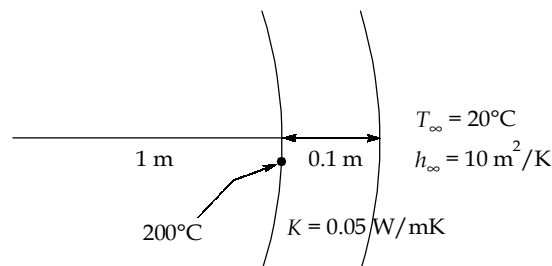
$$\frac{1}{R_{eq}} = \frac{1}{0.25} + \frac{1}{1}$$

$$R_{eq} = 0.2$$

$$R_{\text{total}} = R_1 + R_{eq} + R_2$$

$$R_{\text{total}} = 3 + 0.2 + 0.7 = 3.9$$

22. (b)



From steady state heat transfer,

$$\frac{200 - T}{\frac{\ln\left(\frac{r_2}{r_1}\right)}{2\pi KL}} = \frac{T - 20}{\frac{1}{h2\pi r_2 L}}$$

$$\frac{200 - T}{\frac{\ln\left(\frac{1.1}{1}\right)}{2\pi \times 0.05}} = \frac{T - 20}{\frac{1}{10 \times 2\pi \times 1.1}}$$

$$T = 28.1936^\circ\text{C}$$

23. (a)

Initially, $T_H = 1850 + 273 = 2123 \text{ K}$
 $Q = 25 \text{ W}, T_L = 500 + 273 = 773 \text{ K}$

$$25 = \sigma A (T_H^4 - T_L^4)$$

$$25 = \sigma A (2123^4 - 773^4)$$

$$\sigma A = \frac{25}{(2123^4 - 773^4)}$$

After some time, $T_H = 1500 + 273 = 1773 \text{ K}$
 $T_L = 750 + 273 = 1023 \text{ K}$

$$Q = \sigma_1 A (T_H^4 - T_L^4)$$

$$Q = \frac{25(1773^4 - 1023^4)}{(2123^4 - 773^4)} = 11 \text{ Watt}$$

24. (a)

We know that,

$$\text{Gr} = \frac{g\beta\Delta TL_c^3}{\nu^2}$$

$$\beta = \frac{1}{T_{\text{avg}}} = \frac{1}{161 + 273} = 2.304 \times 10^{-3} \text{ K}^{-1} \quad \left(T_{\text{avg}} = \frac{25 + 297}{2} = 161^\circ\text{C} \right)$$

For horizontal plate:

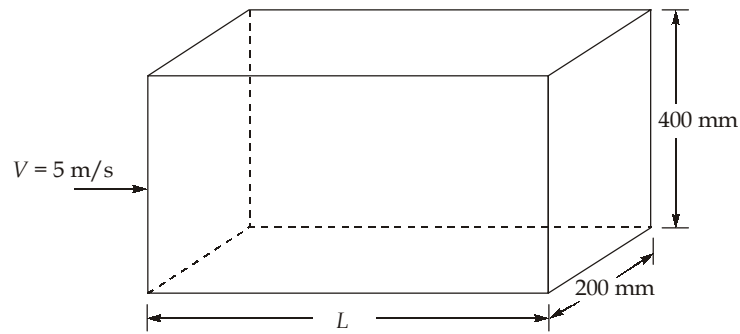
$$L_C = \frac{A_s}{p} = \frac{50 \times 50}{4 \times 50} = 12.5 \text{ cm or } 0.125 \text{ m}$$

So,

$$\text{Gr} = \frac{9.81 \times (2.304 \times 10^{-3}) \times 272 \times (0.125)^3}{(30 \times 10^{-6})^2}$$

$$= 133.184 \times 10^5$$

25. (c)



$$\text{Hydraulic diameter, } D_h = \frac{4A}{P} = \frac{4 \times 200 \times 400}{2(200 + 400)}$$

$$D_h = 266.667 \text{ mm}$$

$$\begin{aligned} \text{Reynolds number, } Re &= \frac{VD_h}{\nu} = \frac{5 \times 0.266667}{15.06 \times 10^{-6}} \\ &= 88.535 \times 10^3 > 2000 \end{aligned}$$

So, flow is turbulent,

$$\text{Prandtl number, } Pr = \frac{\nu}{\alpha} = \frac{15.06 \times 10^{-6}}{7.71 \times 10^{-2} / 3600} = 0.7032$$

For heating of fluid case,

$$\begin{aligned} Nu &= 0.023(Re)^{0.8}(Pr)^{0.4} \\ &= 0.023(88.535 \times 10^3)^{0.8}(0.7032)^{0.4} \\ Nu &= 181.239 \end{aligned}$$

$$\Rightarrow \frac{h \times D_h}{k} = 181.239$$

$$\frac{h \times 0.266667}{0.026} = 181.239$$

$$\Rightarrow h = 17.671 \text{ W/m}^2 \text{ } ^\circ\text{C}$$

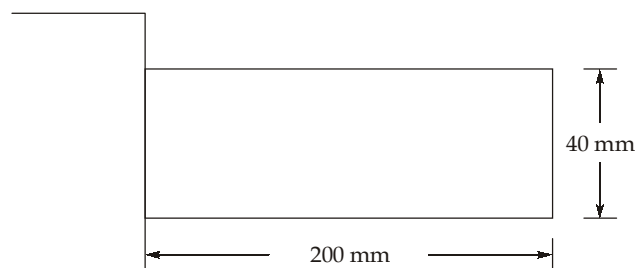
Heat transfer rate per unit length per unit temperature difference,

$$Q = h(PL)(\Delta T)$$

$$\frac{Q}{L\Delta T} = 17.671 \times 2(0.2 + 0.4)$$

$$\frac{Q}{L\Delta T} = 21.205 \text{ W/m}^\circ\text{C}$$

26. (d)



$$\text{Efficiency of fin, } \eta_{\text{fin}} = 40\%$$

Diameter of fin, $d = 40 \text{ mm}$

Cross-sectional area of fin, $A_b = \frac{\pi}{4} d^2$

$$= \frac{\pi}{4} \times 0.04^2 = 1.2566 \times 10^{-3} \text{ m}^2$$

Surface area of fin, $A_{\text{fin}} = \pi d l$

$$= \pi \times 0.04 \times 0.2 = 0.02513 \text{ m}^2$$

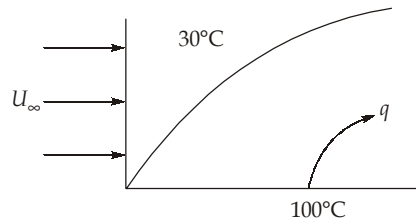
As we know,

$$\text{Effectiveness of fin, } \epsilon_{\text{fin}} = \eta_{\text{fin}} \frac{A_{\text{fin}}}{A_b}$$

$$= 0.4 \times \frac{0.02513}{1.2566 \times 10^{-3}} = 7.99$$

27. (a)

Velocity of air, $U_{\infty} = 30 \text{ m/s}$



$$\text{Reynold number, } Re_L = \frac{U_{\infty} L}{\nu} = \frac{30 \times L}{18.97 \times 10^{-6}}$$

$$= 1.5814 \times 10^6 L$$

...(1)

As we know,

$$\text{Drag force, } F_D = C_D \times \frac{1}{2} \rho U_{\infty}^2 A$$

$$10.5 = \frac{0.0742}{(1.5814 \times 10^6 L)^{1/5}} \times \frac{1}{2} \times 1.06 \times 30^2 \times L^2$$

$$10.5 = 2.0376 L^{(2 - 0.2)}$$

$$L^{1.8} = 5.1532$$

$$L = (5.1532)^{1/1.8}$$

$$L = 2.486 \text{ m}$$

\Rightarrow

From eq. (1)

$$Re_L = 1.5814 \times 10^6 \times 2.486$$

$$= 3.9314 \times 10^6$$

$$C_D = \frac{0.0742}{(3.9314 \times 10^6)^{1/5}} = 3.5604 \times 10^{-3}$$

By simple Reynolds analogy,

$$\overline{St} = \frac{C_D}{2}$$

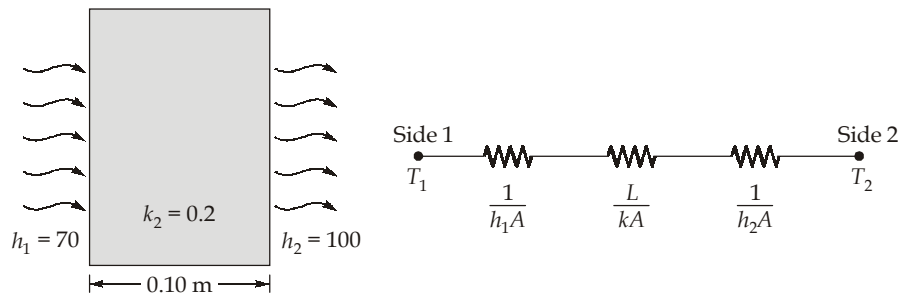
$$\Rightarrow \frac{\bar{h}}{\rho U_{\infty} c_p} = \frac{C_D}{2}$$

$$\begin{aligned} \Rightarrow \bar{h} &= \frac{3.5604 \times 10^{-3}}{2} \times 1.06 \times 30 \times 1.005 \times 1000 \\ &= 56.893 \text{ W/m}^2\text{K} \end{aligned}$$

28. (c)

$$Q = \frac{\Delta T}{R} = \frac{T_1 - T_2}{R}$$

$$R = \frac{1}{h_1 A} + \frac{1}{kA} + \frac{1}{h_2 A} = \frac{1}{70} + \frac{0.1}{0.2} + \frac{1}{100} = 0.5242^\circ\text{C/W}$$



$$\begin{aligned} T_1 - T_2 &= Q \times R = 100 \times 0.5242 \\ &= 52.42^\circ\text{C} \approx 52.4^\circ\text{C} \end{aligned}$$

29. (d)

$$Q_1 = A_1 [F_{12} (J_1 - J_2) + F_{1-3} (J_1 - J_3)]$$

$$J_1 = \sigma 550^4 = 5188.4 \text{ W/m}^2\text{K}$$

$$J_2 = 7500 \text{ W/m}^2$$

$$J_3 = 3200 \text{ W/m}^2$$

$$Q = 9(0.2 \times (5188.4 - 7500) + 0.8 \times (5188.4 - 3200)) = 10.15 \text{ kW}$$

30. (c)

$$T_o = T_w + \frac{q_G R^2}{4k}$$

$$T_o = 100^\circ\text{C} + \frac{3000}{\frac{\pi}{4} \times 1.2^2 \times 5} \times \frac{0.6^2}{4 \times 62} = 100.64^\circ\text{C}$$

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