

- [4] • Escribir la función más débil  $P = wp(S, Q)$   
 • Mostrar formalmente que la  $P$  elegida es correcta

②  $S \equiv \text{if } (a < 0) \text{ then } b := a \text{ else } b := -a \text{ fi}$

$Q \equiv (b = -|a|)$

Herramientas:

• 4: si  $S = \text{if } B \text{ then } S1 \text{ else } S2 \text{ endif}$ ,

$wp(S, Q) \equiv \text{def } (B) \wedge ((B \wedge wp(S1, Q)) \vee (\neg B \wedge wp(S2, Q)))$

$wp(S, b = -|a|) \stackrel{(4)}{=}$

$\text{def } (a < 0) \wedge (((a < 0) \wedge \overbrace{wp(b := a, Q)}^{[1]}) \vee (\neg(a < 0) \wedge \overbrace{wp(b := -a, Q)}^{[2]}))$

[1]  $wp(b := a, b = -|a|) \stackrel{(1)}{=}$

$\text{def } (a) \wedge (b = -|a|)^a \equiv \boxed{a = -|a|}$

[2]  $wp(b := -a, b = -|a|) \equiv \text{def } (-a) \wedge -a = -|a| \equiv$

$\boxed{-a = -|a|}$

luego

$\underbrace{((a < 0) \wedge a = -|a|)}_T \vee \underbrace{((a \geq 0) \wedge -a = -|a|)}_T \equiv \boxed{\text{True}}$

tenemos entonces que  $wp(S, Q) = \text{True}$