Tutorial sheet -1

Sol 1: - Asymptotic Notation :

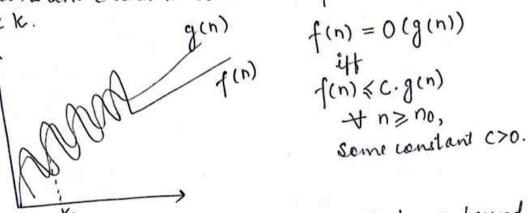
- These notations are used to tell the complexity of an algorithm when the inhet is well lave.

algorithm when the input is very large.

It describes the algorithm effectioned and performance in a meaningful may. It describes the schaviour of time or space complexity for large instance characteristics.

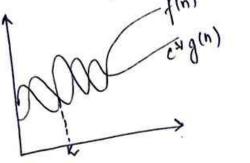
· The asymptotic notation of an algorithm is classified into 5 types:

(i) Big oh notation (0): (Asymptotic upper Bound) The function f(n) = O(g(n)), if and only if there exist a the constant C and k such that $f(n) \leq C^* g(n)$ for all $n \geq k$. g(n) = O(g(n))



(ii) Big Omega notation (Ω): (A symptotic lenur bound)

The punction $f(n) = \Omega(g(n))$, iff there exists a +ue constant C and C such that $f(n) \geq C * g(n)$ for all C, C and C such that $f(n) \geq C * g(n)$ for all C, C and C such that



 $f(n) = \Omega g(n)$ iff $f(n) \ge c \cdot g(n)$ $\forall n \ge n \in Some$ const < >0. (iii) Big theta notation (0): (Asymptotic tight bound) The function f(n) = O(g(n)), iff there existe a +ne constant (1, (2 & k such that (1" g(n) < f(n) < (2" g(n) for all", Cz g (n)
c, g (n) f(n) = 0 (g(n)) c, g(n) < f(n) < 62.g(n) + n > max(n,, n,) (iv) Small-oh (o):- 0 gives us upper bound. 1(n) < c g (n) Jan. + n>no & +c>0 $n = O(n^2)$ n < 0.001 n2 no. (v) small-omega (co): lour bound AAA (1.9(n) f(n) = wg(n) f(n) > c.g(n) * n>no & +c>0 $n^2 = \omega(n)$. \$012:- for (i= 1 to ba) ? i=i*2; Time complexity for a loop means no. of times loop has

- For the about loop, the loop will run for the following values of 1:- $\frac{1}{\text{value}} = \frac{1}{2} = \frac{1}{2}$ e=1,2,4,8,16,32,...,2k thumlans k times ie 2k=n K lag 2 = lag n $k = \log n$ $\lceil \log_2 2 = 1$. i. T. C = 0 (log n) $Sol3:- T(n) = \{3T(n-1), n>0.\}$ By forward substitution, T(n) = 3T(n-1) T(0) = 1 T(1) - 3T(1-1) = 3710) T(2) = 3T(2-1) = 3 * 3 = 32 T(3) - 3T(3-1) = 37(2) $= 3^{3}3^{2} = 3^{3}.$ T(n) = 3n.

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. T. C = O(3")
1014: - T(n) = { 2T(n-1)-1 , n>0
  By forward substitution,
      T(0) = 1
      T(1) = 2 T(1-1) -1
            = (2 - 1)
       T(2) = 2T(2-1) - 1
            = 2 T(1) - 1
            = 2 (2-1) -1
            =2^2-2^1-1
       T(3) = 2T(3-1) -1
            = 2T(2) - 1
             = 2 (22 -21-1) -1
             -2^3-2^2-2'-1
              2^{n}-2^{n-1}-2^{n-2}-2^{n-3}-2^{2}-2^{1}-2^{0}
       \Rightarrow 2^{n} - (2^{n} - 1)
       = 2×-2×+1-1
  :. T.C = 1
 1015: int = 1, s=1;
           nehile (s<=n)
              1++;
              s = s+i;
printf ("#");
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The value of i increases by one for the it. tis
 value contained in's at the it iteration is the
dum of the first 'i' + we integer of k is the total no.
 of iterations taken by any program then while loop
   terminates if: 1+2+3+...+k.
       = \left[ \left[ \left( k + 1 \right) \right] \right] > n
       40, k=0(5n)
:. T. c = O(5n)
1016: uoid function (int n)
           int i, count = 0;
           for (i=1; ≥i<=n°,i++) 0(n)
   Time complixity :- O(n).
Sol7: - void function (int n)
           int i, i, k, went =0;
           for ( i= n/2; i <= n; i++)
                                           O (logn)
              for(j=1;j<=n;j=j*2)
                 for(k=1; k<=n; k= k*2) 0 (log n)
                      count ++;
       J. c = log n * log n = Onlog2n)
        T. C = O (n log2 n)
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$018: - function (int n)
              if (n==1)
                return; for (\ell=1 \text{ to } n)
                                            O(n) times
                     for (j=1 ton) o(n) times
                        { prints(" *");
             function (n-3);
    Jine complexity: - O(n2) ans.
 solq:- upid function (int n)

\begin{cases}
\text{for } (i=1 \text{ for } n) \\
\text{for } (i=1; j < = n; j=j+1)
\end{cases}

\begin{cases}
\text{o(n)}
\end{cases}

                      printf("*");
       T. c = O(n) * o(n) = O(n2)
          T. C = 0 (n2)
  $0110: nk is O(c") aus.
      n^k = O(c^r)
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