

## Complete API Documentation

# Reference Manual: Lossless Bayesian Network

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## Abstract

This reference manual provides complete API documentation for the Lossless Bayesian Network implementation. It includes detailed descriptions of all classes, methods, parameters, return values, and usage examples.

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# 1 Introduction

This reference manual documents the complete API of the Lossless Bayesian Network implementation. All classes, methods, and their usage are described in detail.

## 2 Header Files

### 2.1 node.hpp

Defines the `Node` class representing a variable in the Bayesian network.

### 2.2 cpt.hpp

Defines the `ConditionalProbabilityTable` class for storing conditional probability distributions.

### 2.3 bayesian\_network.hpp

Defines the `BayesianNetwork` class, the main interface for working with Bayesian networks.

## 3 Node Class

### 3.1 Overview

The `Node` class represents a variable in the Bayesian network with its possible states and parent relationships.

### 3.2 Public Members

Member	Type	Description
<code>name</code>	<code>std::string</code>	Variable name identifier
<code>states</code>	<code>std::vector&lt;std::string&gt;</code>	Vector of possible state names
<code>parentIds</code>	<code>std::set&lt;std::string&gt;</code>	Set of parent node IDs
<code>stateIndexMap</code>	<code>std::map&lt;std::string, int&gt;</code>	Mapping, state names to indices

### 3.3 Constructors

#### 3.3.1 Node()

Default constructor. Creates an empty node.

**Parameters:** None

**Returns:** Node instance

#### 3.3.2 Node(const std::string& nodeName, const std::vector<std::string>& nodeStates)

Constructor with name and states.

**Parameters:**

- `nodeName`: Name of the node
- `nodeStates`: Vector of possible state names

**Returns:** Node instance with initialized states

## 3.4 Methods

### 3.4.1 getStateIndex(const std::string& stateName) const

Get the index of a state by name.

**Parameters:**

- **stateName:** Name of the state

**Returns:** Index of the state (0-based), or -1 if not found

**Example:**

```
1 Node node("Disease", {"None", "Cold", "Flu"});  
2 int idx = node.getStateIndex("Cold"); // Returns 1
```

### 3.4.2 hasState(const std::string& stateName) const

Check if a state exists.

**Parameters:**

- **stateName:** Name of the state

**Returns:** true if state exists, false otherwise

### 3.4.3 getNumStates() const

Get number of possible states.

**Parameters:** None

**Returns:** Number of states

### 3.4.4 addParent(const std::string& parentId)

Add a parent node.

**Parameters:**

- **parentId:** ID of the parent node

**Returns:** void

### 3.4.5 removeParent(const std::string& parentId)

Remove a parent node.

**Parameters:**

- **parentId:** ID of the parent node

**Returns:** void

### 3.4.6 hasParent(const std::string& parentId) const

Check if node has a specific parent.

**Parameters:**

- **parentId:** ID of the parent node

**Returns:** true if parent exists, false otherwise

### 3.4.7 getNumParents() const

Get number of parent nodes.

**Parameters:** None

**Returns:** Number of parents

## 4 ConditionalProbabilityTable Class

### 4.1 Overview

The `ConditionalProbabilityTable` class stores conditional probabilities in a lossless, exact representation using multi-dimensional indexing.

### 4.2 Constructors

#### 4.2.1 ConditionalProbabilityTable()

Default constructor. Creates an empty CPT.

**Parameters:** None

**Returns:** CPT instance

#### 4.2.2 ConditionalProbabilityTable(const std::vector<size\_t>& dims)

Constructor with dimensions.

**Parameters:**

- **dims:** Vector of dimensions (last is node, others are parents)

**Returns:** CPT instance with initialized dimensions

**Example:**

```
1 // CPT for node with 2 parents (3 states each) and 2 node states
2 std::vector<size_t> dims = {3, 3, 2};
3 ConditionalProbabilityTable cpt(dims);
```

### 4.3 Methods

#### 4.3.1 setProbability(const std::vector<size\_t>& parentStates, size\_t nodeState, double prob)

Set probability for given parent and node state indices.

**Parameters:**

- **parentStates:** Vector of parent state indices
- **nodeState:** Index of node state
- **prob:** Probability value (must be in [0, 1])

**Returns:** void

**Throws:** `std::runtime_error` if probability is out of range or indices are invalid

**Example:**

```
1 // P(node=1 | parent1=0, parent2=2) = 0.75
2 cpt.setProbability({0, 2}, 1, 0.75);
```

#### 4.3.2 `getProbability(const std::vector<size_t>& parentStates, size_t nodeState) const`

Get probability for given parent and node state indices.

**Parameters:**

- `parentStates`: Vector of parent state indices
- `nodeState`: Index of node state

**Returns:** Probability value

**Throws:** `std::runtime_error` if indices are invalid

#### 4.3.3 `normalize()`

Normalize probabilities for each parent configuration. Ensures each conditional distribution sums to 1.0.

**Parameters:** None

**Returns:** void

**Example:**

```
1 cpt.setProbability({0}, 0, 0.6);  
2 cpt.setProbability({0}, 1, 0.4);  
3 cpt.normalize(); // Ensures sum = 1.0
```

#### 4.3.4 `isValid(double tolerance = 1e-6) const`

Validate that all conditional distributions sum to 1.0.

**Parameters:**

- `tolerance`: Tolerance for floating point comparison (default: 1e-6)

**Returns:** true if valid, false otherwise

#### 4.3.5 `getDimensions() const`

Get dimensions of the CPT.

**Parameters:** None

**Returns:** Vector of dimensions

#### 4.3.6 `getTotalSize() const`

Get total number of probability entries.

**Parameters:** None

**Returns:** Total size

## 5 BayesianNetwork Class

### 5.1 Overview

The `BayesianNetwork` class is the main interface for working with Bayesian networks. It provides network construction, inference, and I/O capabilities.

## 5.2 Constructors

### 5.2.1 BayesianNetwork()

Default constructor. Creates an empty network.

**Parameters:** None

**Returns:** BayesianNetwork instance

## 5.3 Network Construction Methods

### 5.3.1 addNode(const std::string& nodeId, const std::string& nodeName, const std::vector<std::string>& states)

Add a node to the network.

**Parameters:**

- **nodeId:** Unique identifier for the node
- **nodeName:** Name of the node
- **states:** Vector of possible state names

**Returns:** void

**Throws:** std::runtime\_error if node ID already exists

**Example:**

```
1 network.addNode("Disease", "Disease", {"None", "Cold", "Flu"});
```

### 5.3.2 addEdge(const std::string& parentId, const std::string& childId)

Add an edge from parent to child.

**Parameters:**

- **parentId:** ID of parent node
- **childId:** ID of child node

**Returns:** void

**Throws:** std::runtime\_error if:

- Parent or child node does not exist
- Adding edge would create a cycle
- Attempting to add self-loop

**Example:**

```
1 network.addEdge("Disease", "Symptom");
```

### 5.3.3 setCPT(const std::string& nodeId, const ConditionalProbabilityTable& cpt)

Set conditional probability table for a node.

**Parameters:**

- **nodeId:** ID of the node
- **cpt:** Conditional probability table

**Returns:** void

**Throws:** std::runtime\_error if node does not exist

## 5.4 Inference Methods

### 5.4.1 `getConditionalProbability(const std::string& nodeId, const std::string& nodeState, const std::map<std::string, std::string>& parentStates) const`

Get conditional probability.

**Parameters:**

- `nodeId`: ID of the node
- `nodeState`: State of the node
- `parentStates`: Map of parent IDs to their states

**Returns:** Conditional probability  $P(\text{nodeState} \mid \text{parentStates})$

**Throws:** `std::runtime_error` if:

- Node does not exist
- CPT not set for node
- Missing or invalid parent states
- Invalid node state

### 5.4.2 `computeJointProbability(const std::map<std::string, std::string>& assignment) const`

Compute joint probability for a full assignment.

**Parameters:**

- `assignment`: Map of node IDs to their states

**Returns:** Joint probability  $P(\text{assignment})$

**Throws:** `std::runtime_error` if assignment is incomplete

**Example:**

```
1 std::map<std::string, std::string> assignment;  
2 assignment["Disease"] = "Flu";  
3 assignment["Symptom"] = "Yes";  
4 double prob = network.computeJointProbability(assignment);
```

### 5.4.3 `variableElimination(const std::vector<std::string>& queryNodes, const std::map<std::string, std::string>& evidence) const`

Variable elimination for exact inference.

**Parameters:**

- `queryNodes`: Vector of node IDs to query
- `evidence`: Map of observed node IDs to their states

**Returns:** Map from query assignments to their probabilities (normalized)

**Example:**

```
1 std::map<std::string, std::string> evidence;  
2 evidence["Symptom"] = "Yes";  
3 std::vector<std::string> query = {"Disease"};  
4 auto results = network.variableElimination(query, evidence);
```

## 5.5 Utility Methods

### 5.5.1 `getNode(const std::string& nodeId) const`

Get node by ID.

**Parameters:**

- `nodeId`: ID of the node

**Returns:** Const reference to the node

**Throws:** `std::runtime_error` if node does not exist

### 5.5.2 `getNodeIds() const`

Get all node IDs.

**Parameters:** None

**Returns:** Vector of node IDs

### 5.5.3 `generateAssignments(const std::vector<std::string>& nodeIds, std::vector<std::map<std::string>& assignments) const`

Generate all possible assignments for given nodes.

**Parameters:**

- `nodeIds`: Vector of node IDs
- `assignments`: Output vector of assignments

**Returns:** void

**Throws:** `std::runtime_error` if any node does not exist

## 5.6 File I/O Methods

### 5.6.1 `saveToFile(const std::string& filename) const`

Save network to file.

**Parameters:**

- `filename`: Output filename

**Returns:** void

**Throws:** `std::runtime_error` if file cannot be opened

### 5.6.2 `loadFromFile(const std::string& filename)`

Load network from file.

**Parameters:**

- `filename`: Input filename

**Returns:** void

**Throws:** `std::runtime_error` if file cannot be loaded

## 6 Error Handling

All methods that can fail throw `std::runtime_error` exceptions with descriptive error messages. Common error conditions include:

- Node does not exist
- Invalid state names
- Cycle detection (invalid DAG)
- Invalid probability values
- Missing CPTs
- File I/O errors

## 7 Usage Examples

### 7.1 Complete Example

```
1 #include "bayesian_network.hpp"
2 #include <iostream>
3
4 int main() {
5     BayesianNetwork network;
6
7     // Add nodes
8     network.addNode("Disease", "Disease", {"None", "Cold", "Flu"});
9     network.addNode("Symptom", "Fever", {"No", "Yes"});
10
11    // Add edge
12    network.addEdge("Disease", "Symptom");
13
14    // Create CPT
15    std::vector<size_t> dims = {3, 2};
16    ConditionalProbabilityTable cpt(dims);
17    cpt.setProbability({0}, 0, 0.9); // P(No|None)
18    cpt.setProbability({0}, 1, 0.1); // P(Yes|None)
19    cpt.setProbability({1}, 0, 0.7); // P(No|Cold)
20    cpt.setProbability({1}, 1, 0.3); // P(Yes|Cold)
21    cpt.setProbability({2}, 0, 0.2); // P(No|Flu)
22    cpt.setProbability({2}, 1, 0.8); // P(Yes|Flu)
23    cpt.normalize();
24    network.setCPT("Symptom", cpt);
25
26    // Prior for Disease
27    std::vector<size_t> diseaseDims = {3};
28    ConditionalProbabilityTable diseaseCPT(diseaseDims);
29    diseaseCPT.setProbability({}, 0, 0.7);
30    diseaseCPT.setProbability({}, 1, 0.2);
31    diseaseCPT.setProbability({}, 2, 0.1);
32    diseaseCPT.normalize();
33    network.setCPT("Disease", diseaseCPT);
34
35    // Inference
36    std::map<std::string, std::string> evidence;
37    evidence["Symptom"] = "Yes";
```

```

38     std::vector<std::string> query = {"Disease"};
39     auto results = network.variableElimination(query, evidence);
40
41     // Display results
42     for (const auto& pair : results) {
43         std::cout << "P(Disease=" << pair.first.at("Disease")
44             << ")_=_ " << pair.second << std::endl;
45     }
46
47     return 0;
48 }

```

## 8 Performance Notes

- Variable elimination has exponential time complexity in the worst case
- CPT storage is exponential in the number of parents
- Topological ordering minimizes computation during inference
- State lookup is  $O(1)$  via hash maps

## 9 Copyright

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