

$$E(\boldsymbol{\theta}) = \frac{1}{2} \sum_{i}^{N} ||\mathbf{y}_{i}^{*} - \mathbf{y}_{i}(\boldsymbol{\theta})||^{2} \qquad \text{The energy to be minimized}$$

$$\mathbf{y}(\boldsymbol{\theta}) = \mathbf{r}(\boldsymbol{\theta}) \; \mathbf{Y}(\boldsymbol{\theta}) \qquad \text{Network's forward mapping}$$

$$\mathbf{y} = \begin{bmatrix} \vdots & \vdots & \vdots \\ -\mathbf{y}^{j} & - \\ \vdots & \vdots & \vdots \end{bmatrix} \qquad \text{Matrix of outputs for all routes}$$

$$\mathbf{y}^{j} = \sigma\left(\mathbf{P}^{j}\mathbf{x}\right) \qquad \text{Intermediate output for j-th route}$$

$$\mathbf{r} = \sigma\left(\mathbf{R}\mathbf{x}\right) \qquad \text{Soft routing weights}$$

$$\Delta\boldsymbol{\theta}_{t+1} := -\rho \left. \frac{\partial E}{\partial \boldsymbol{\theta}} \right|_{t} \qquad \text{The parameter update rule}$$

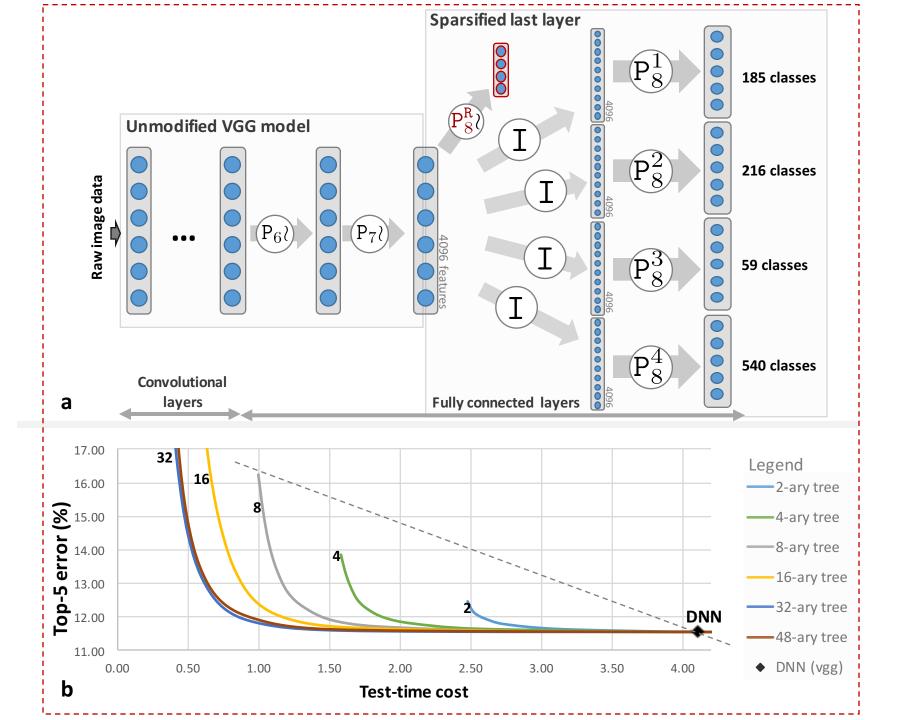
$$\boldsymbol{\theta} := \left\{\mathbf{R}, \left\{\mathbf{P}^{j}\right\}\right\} \qquad \text{The parameters to be optimized}$$

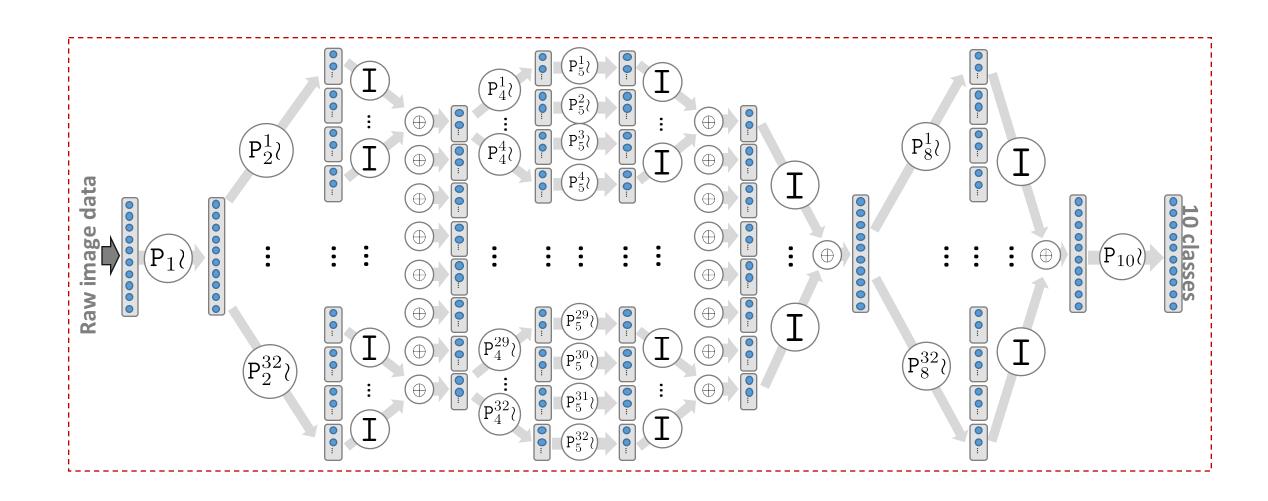
$$\mathcal{T} = \left\{(\mathbf{x}_{1}, \mathbf{y}_{1}^{*}), \dots, (\mathbf{x}_{i}, \mathbf{y}_{i}^{*}), \dots, (\mathbf{x}_{N}, \mathbf{y}_{N}^{*})\right\} \qquad \text{The labelled training set}$$

Chain rule to compute partial derivatives for gradient descent

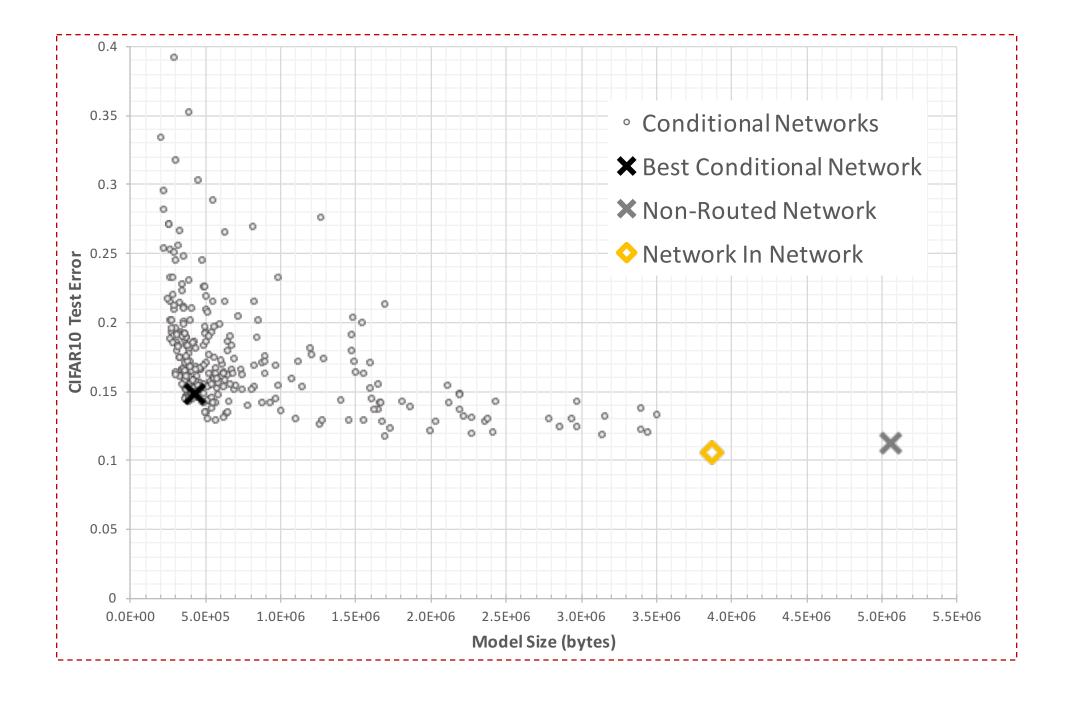
$$\begin{split} \boldsymbol{\phi}^j &:= \mathbf{P}^j \mathbf{x} & \mathbf{y}^j = \sigma(\boldsymbol{\phi}^j) \\ \frac{\partial E}{\partial \boldsymbol{\theta}} &= \frac{\partial E}{\partial \mathbf{y}} \, \frac{\partial \mathbf{y}}{\partial \boldsymbol{\theta}} = \frac{\partial E}{\partial \mathbf{y}} \left(\frac{\partial \mathbf{r}}{\partial \mathbf{R}} \mathbf{Y} + \sum_j \, r(j) \, \frac{\partial \mathbf{y}^j}{\partial \boldsymbol{\phi}^j} \frac{\partial \boldsymbol{\phi}^j}{\partial \mathbf{P}^j} \right) \end{split}$$

Routing weights influence the back-propagating errors differently for different routes

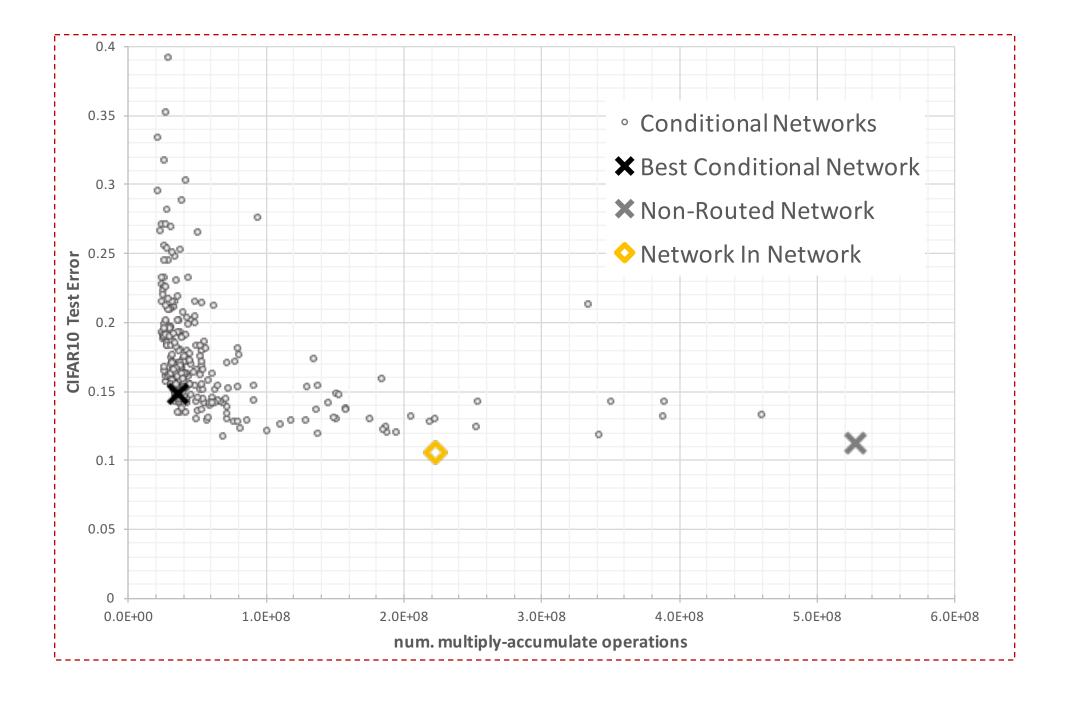




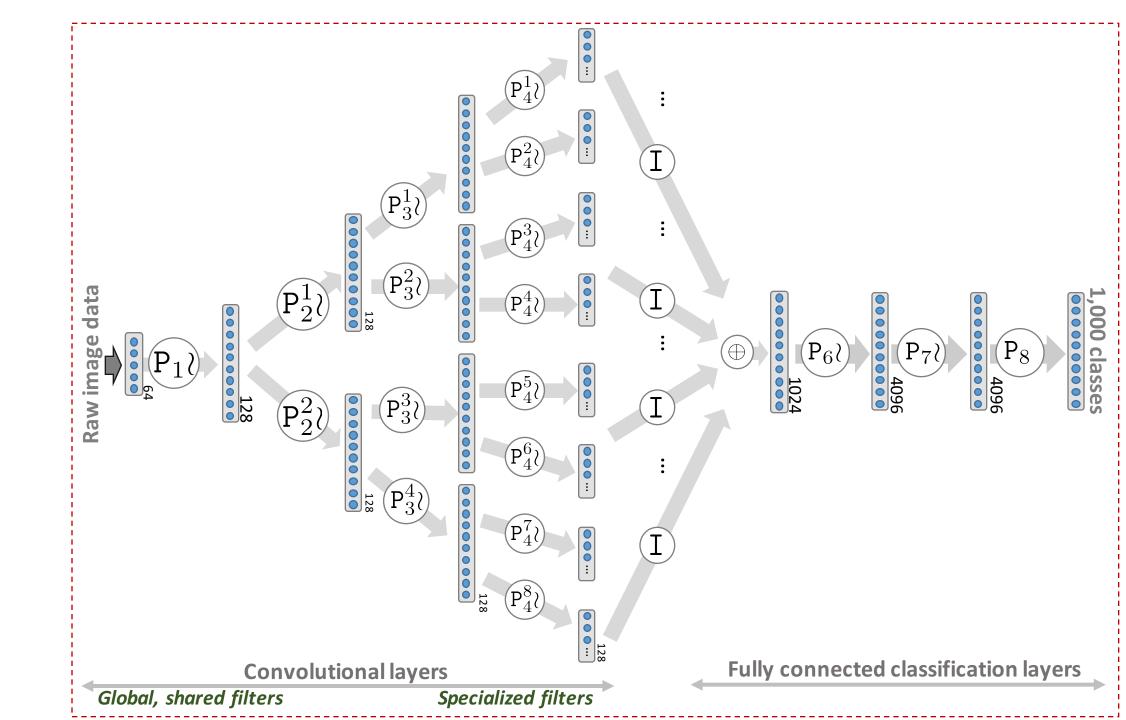
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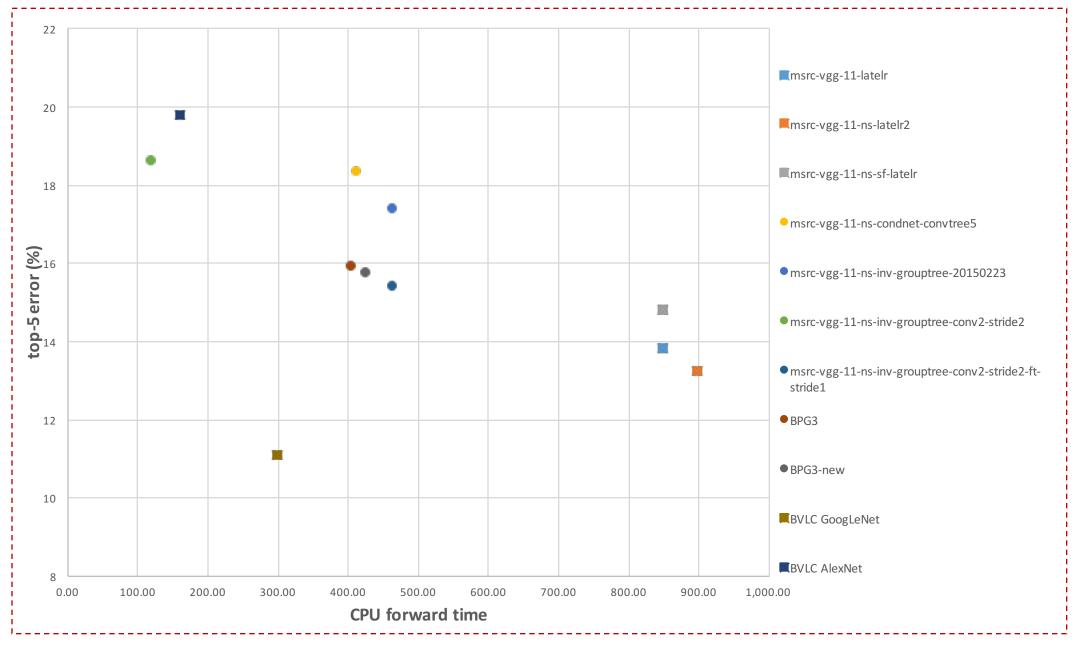
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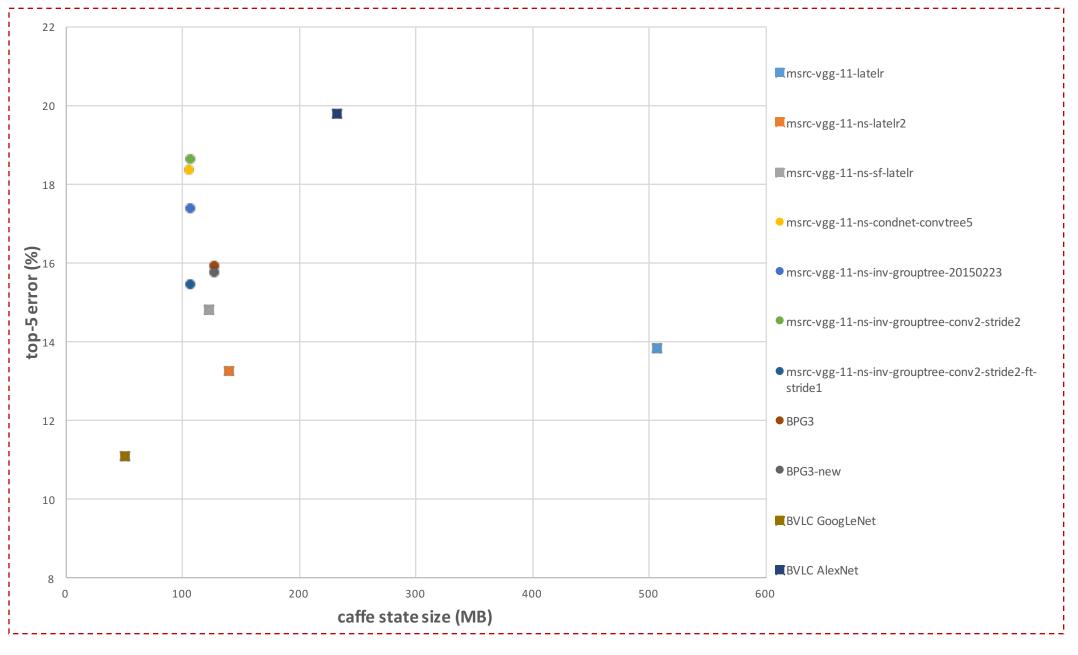
ImageNet



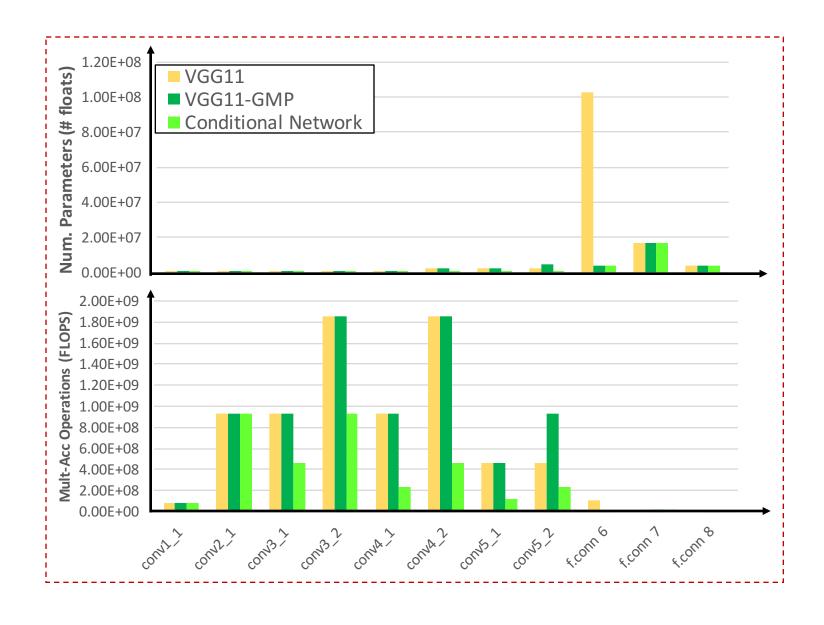
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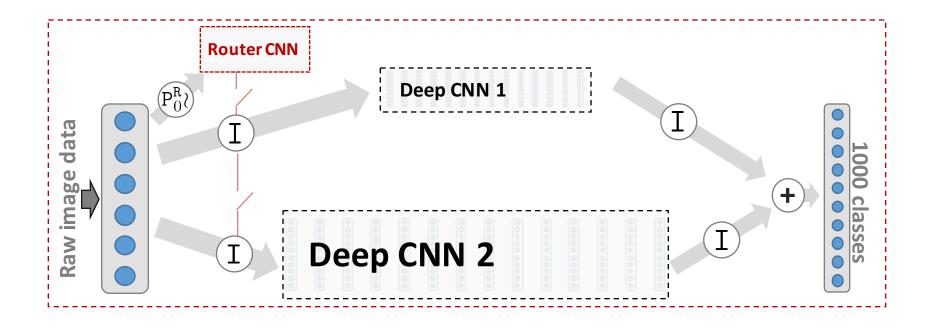
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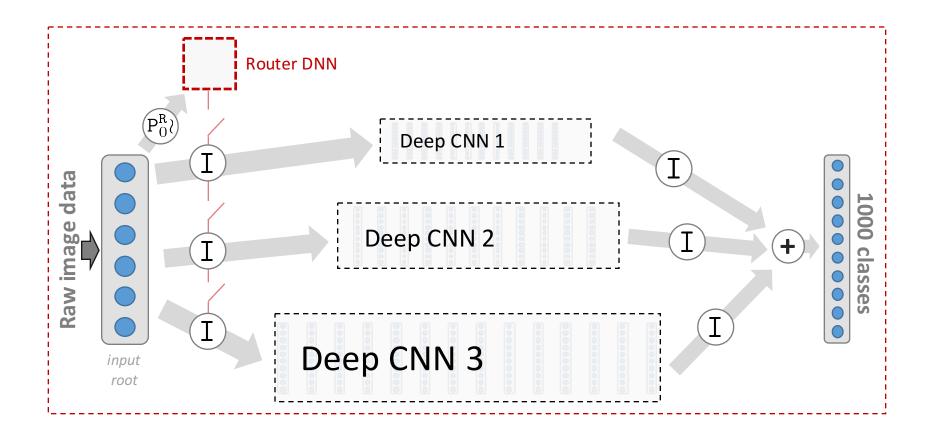
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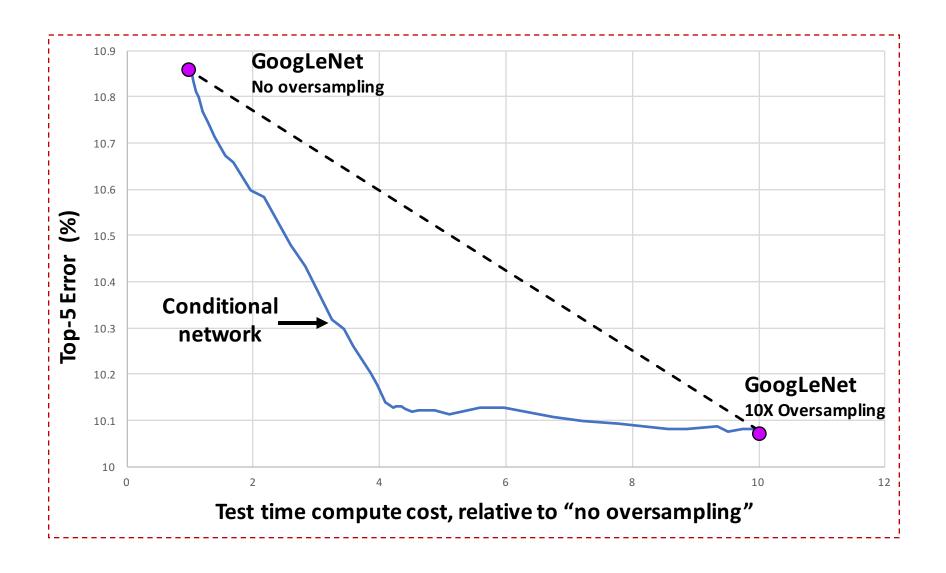


Mixing



Mixing





OLD unused

