

## COMPUTER PROGRAMMING ASSIGNMENT SOLUTION

OSEI-SARFO HENRY

```
import numpy as np

L = 12 #length of beam in meters

w = 10 #intensity of load in KN/m

#Question a

#Bending moment(M) and shear force(V) at the first end, x=0

x = 0


$$M = (w * (-6 * x^{**2} + 6 * L * x - L^{**2})) / 12$$



$$V = w * (L / 2 - x)$$


m= 'The bending moment at x=0 is '

n= 'the shear force at x=0 is '

print()

print('(a.1)' + m + str(M) + ' and ', n + str(V))

#Bending moment(M) and shear force(V) at the first end, x=L=10

x = L


$$M = (w * (-6 * x^{**2} + 6 * L * x - L^{**2})) / 12$$



$$V = w * (L / 2 - x)$$


a= 'The bending moment at x=L is '

b= 'the shear force at x=L is '
```

```
print()
```

```
print('(a.2)' + m + str(M) + ' and ', n + str(V))
```

```
#Question b
```

```
"""
```

When the bending moment is zero, we get an expression  $x^2 - Lx + L^2/6 = 0$

```
"""
```

```
#from the expression
```

```
a = 1
```

```
b = -L
```

```
c = L**2/6
```

```
#Using the Almighty formula the two roots are;
```

```
discriminant = b**2 - 4*a*c
```

```
root_1b = (-b + np.sqrt(discriminant))/2*a
```

```
root_2b = (-b - np.sqrt(discriminant))/2*a
```

```
print()
```

```
print('(b) The points of contra-flexure are {0} and {1}'.format(root_1b,root_2b))
```

```
#Question c
```

```
"""
```

When the shear force is zero,  $x = L/2$

```
"""
```

```
x = L/2
```

```
print()
```

```
print('(c) The point at which V=0 is {}'.format(x))
```

#Question d

p = 0

s = 0.01

q = L + s

x = np.arange(p,q,s)

M = (w\*(-6\*x\*\*2 + 6\*L\*x-L\*\*2))/12

print()

print('(d) Using the initialized variable,the bending moment at each step in the array is {0}'.format(M))

#Question e

V = w\*(L/2 - x)

print()

print('(e) The shear force for each step along the span is {}'.format(V))

#Question f

"""

Let the absolute value of the bending moment array be AM

Also let the minimum AM be m\_AM

"""

AM = abs(M)

m\_AM = min(AM)

"""

When the bending moment is m\_AM, we get an expression  $x^2 - Lx + (L^2/6) + (2*m\_AM)/w = 0$

"""

#from the above expression

a = 1

b = -L

c = (L\*\*2/6)+(2\*m\_AM)/w

#Using the Almighty formula the two roots are;

discriminant = b\*\*2 - 4\*a\*c

root\_1f = (-b + np.sqrt(discriminant))/2\*a

root\_2f = (-b - np.sqrt(discriminant))/2\*a

print()

print('(f) The points along L at which the absolute values of the bending moment array is minimum are {0} and {1}'.format(root\_1f,root\_2f))

#Question g

"""

Let the relative errors be r\_e

"""

r\_e1 = ((root\_1b - root\_1f)/root\_1b\*100)

r\_e2 = ((root\_2f - root\_2b)/root\_2f\*100)

print()

print('(g) The relative errors between estimated points of contra-flexure are {0}% and {1}%'.format(r\_e1,r\_e2))

#Question h

"""

Let the maximum bending moment be max\_M and the minimum bending moment be min\_M

"""

#for the maximum

max\_M = max(M)

"""

When the bending moment is max\_M, we get an expression  $x^2 - Lx + (L^2/6) + (2 \cdot \text{max\_M})/w = 0$

"""

a = 1

b = -L

c =  $(L^2/6) + (2 \cdot \text{max\_M})/w$

#Using the Almighty formula the two roots are;

discriminant =  $b^2 - 4 \cdot a \cdot c$

root\_1 =  $(-b + \text{np.sqrt(discriminant)})/2 \cdot a$

root\_2 =  $(-b - \text{np.sqrt(discriminant)})/2 \cdot a$

print()

print('(h.1) The points at which the maximum bending moment occur are {0} and {1}'.format(root\_1, root\_2))

#for the minimum

min\_M = min(M)

"""

When the bending moment is min\_M, we get an expression  $x^2 - Lx + (L^2/6) + (2 \cdot \text{min\_M})/w = 0$

"""

a = 1

b = -L

c =  $(L^2/6) + (2 \cdot \text{min\_M})/w$

#Using the Almighty formula the two roots are;

discriminant =  $b^2 - 4 \cdot a \cdot c$

```
root_1 = (-b - np.sqrt(discriminant))/2*a
```

```
root_2 = (-b + np.sqrt(discriminant))/2*a
```

```
print()
```

```
print('(h.2) The points at which the minimum bending moment occur are {0} and  
{1}'.format(root_1,root_2))
```