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Question 1: How many disks can you handle with a timeout of 1 minute?

I can handle 5 disks.

In fact, using the command: `telingo hanoi.lp towers03.lp`

We can see that for 6 disks it takes a time of 109 seconds equals approximately 1 minute 49 seconds so the maximum of disks it can handle with a timeout of 1 minute is 5.

Question 2: For $n=2$ the solution takes 3 steps, for $n=3$ it takes 7 steps. Use the recursive relation above to find a formula for the length of the solution for an arbitrary n .

The length of solution will follow the formula $2^n - 1$ where n =number of the disks.

Because we know that the algorithm is:

If the disks are initially in A and we want to move them in C

- 1) Move the first $n-1$ disks from pole A to pole B using C.
- 2) Move the largest disk (disk n) from pole A to pole C.
- 3) Move the $n-1$ disks from pole B to pole C using A.

So we need $f(n-1)$ moves for the first step, 1 for the second, $f(n-1)$ for the third (where f is a function of the number of disks).

Thus,

Total moves = $f(n-1) + 1 + f(n-1) = 2 * f(n-1) + 1$

In addition, we know that $f(1)=1$ (because obviously to move one disk we need just one move).

So $f(2)=2*f(1)+1=2*1+1=3$

$f(3)=2*f(2)+1=2*3+1=7$

$f(4)=2*f(3)+1=2*7+1=15$

$f(5)=2*f(4)+1=2*15+1=31$

$f(6)=2*f(5)+1=2*31+1=63$

So, observing the results we can derive a general formula for the number of moves that is $f(n)=2^n - 1$.

Question 3: For $n=4$ how many steps are required if, instead of 3 poles, we have 5 poles (a, b, c, d, e) available? It requires 7 steps. But a notable change is that now we have more models, that makes sense because now we have more freedom on the choice of what pole to use as auxiliary.

Question 4: if we implement this control rule, is there any variation in the execution time?

With the constraint Time : 2.572s

Without the constraint Time : 2.735s

It is normal that the execution time decreases as I avoid making unnecessary moves.