COMP9020

Foundations of Computer Science

Acknowledgement of Country

I would like to acknowledge and pay my respect to the Bedegal people who are the Traditional Custodians of the land on which UNSW is built, and of Elders past and present.

COMP9020 20T3 Staff

Lecturer: Paul Hunter

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Lectures: Tuesdays 3-5pm and Fridays 11am-1pm Consults: Mondays 12-1pm and Thursdays 8-9pm

Research: Theoretical CS: Algorithms, Formal verification



Online arrangements

Lectures:

- Zoom: https://unsw.zoom.us/j/96612524105
- Recordings available on echo360 (through Moodle)

Consultations:

- Collaborate (through Moodle)
- Group-based, student-driven
- Wiki for questions

Other points of contact:

- Course forums
- Email



What you can expect from me

What is this course about?

What is Computer Science?



Course Aims

Computer Science is about \(\text{you decide} \)

This course aims to increase your level of mathematical maturity to assist with the fundamental problem of **finding**, **formulating**, **and proving** properties of programs.

Course Aims

The actual content is taken from a list of subjects that constitute the basis of the tool box of every serious practitioner of computing:

•	number theory	week 1
•	sets and languages	week 2
•	relations and functions	week 3
•	recursion; algorithmic analysis	week 4
•	induction	week 5
•	logic	week 7
•	graph theory	week 8
•	combinatorics	week 9
•	probability and expectation	week 10

Course Material

All course information is placed on the course website

www.cse.unsw.edu.au/~cs9020/

Content includes:

- Lecture slides and recordings
- Quizzes and Assignments
- Course Forums
- Practice questions
- Challenge questions
- Study groups



Course Material

Textbooks:

- KA Ross and CR Wright: Discrete Mathematics
- E Lehman, FT Leighton, A Meyer: Mathematics for Computer Science

Assessment Summary

50% exam, 40% assignments, 10% quizzes:

- 9 quizzes, worth up to 1.67 marks each
- 3 assignments, worth up to 13.33 marks each
- final exam (24 hours) worth up to 50 marks

Quizzes are available for 48 hours before the Monday lecture. Assignments due on Tuesdays of weeks 5, 8 and 11.

You must achieve 40% on the final exam to pass

Your final score will be taken from your 6 best quiz results, 3 assignments and final exam.



Late policy and Special Consideration

All assessments are submitted through the course website

Lateness policy

- Assignments: 10% off raw mark per 12 hours or part thereof
- Quizzes: Late submissions not accepted
- Exam: 25% off raw mark per 15 minutes or part thereof

If you cannot meet a deadline through illness or misadventure you need to apply for Special Consideration.



More information

View the course outline at:

https://webcms3.cse.unsw.edu.au/COMP9020/20T2/outline

Particularly the sections on **Student conduct** and **Plagiarism**.



What I will expect from you

Assessments

To achieve good marks in this course you need to demonstrate:

- Your understanding of the material
- Your ability to work with the material

NB

How you get an answer is as, if not more important than what the answer is.



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Mathematical communication

Guidelines for good mathematical writing

Mathematical writing should be:

- Clear
- Logical
- Sensical



Examples

Example (Bad) Ex1 6) 72 c) 12 Ex 2: (A 1B) U (B \A) = (A \B) \(\lambda \) (B \A) = (A \B) \(\lambda \) (B \A) = (A \B) \(\lambda \) (A \ Ex3 a) ks b) No c) Yes d) No e) Yes Ex4 a) True b) False

Examples

Example (Good)

Ex. 2

$$(A \setminus B) \cup (B \setminus A) = (A \cap B^c) \cup (B \cap A^c)$$

$$= ((A \cap B^c) \cup B) \cap ((A \cap B^c) \cup A^c)$$

$$= (A \cup B) \cap (B^c \cup B)$$

$$\cap (A \cup A^c) \cap (B^c \cup A^c)$$

$$= (A \cup B) \cap (A^c \cup B^c)$$

$$= (A \cup B) \cap (A \cap B)^c$$

$$= (A \cup B) \setminus (A \cap B)$$
(Def.)

Examples

Example (Good)

Ex. 4a

We will show that if R_1 and R_2 are symmetric, then $R_1 \cap R_2$ is symmetric.

Suppose $(a, b) \in R_1 \cap R_2$.

Then $(a, b) \in R_1$ and $(a, b) \in R_2$.

Because R_1 is symmetric, $(b, a) \in R_1$; and because R_2 is symmetric, $(b, a) \in R_2$.

Therefore $(b, a) \in R_1 \cap R_2$.

Therefore $R_1 \cap R_2$ is symmetric.



Proofs

A large component of your work in this course is giving **proofs** of **propositions**.

A **proposition** is a statement that is either true or false.

Example

Propositions:

- 3+5=8
- All integers are either even or odd
- There exist a, b, c such that 1/a + 1/b + 1/c = 4

Not propositions:

- 3 + 5
- x is even or x is odd
- 1/a + 1/b + 1/c = 4

Proposition structure

Common proposition structures include:

```
If A then B (A \Rightarrow B)
A if and only if B (A \Leftrightarrow B)
For all x, A (\forall x.A)
There exists x such that A (\exists x.A)
```

 \forall and \exists are known as **quantifiers**.

Proofs

A large component of your work in this course is giving **proofs** of **propositions**.

A proof of a proposition is an argument to convince the reader/marker that the proposition is true.

A **proof** of a proposition is a finite sequence of logical steps, starting from base assumptions (**axioms** and **hypotheses**), leading to the proposition in question.



Proofs

Example

Prove: $3 \times 2 = 2 \times 3$

$$3 \times 2 = (2+1) \times 2$$

$$= (2 \times 2) + (1 \times 2)$$

$$= (1 \times 2) + (2 \times 2)$$

$$= 2 + (2 \times 2)$$

$$= (2 \times 1) + (2 \times 2)$$

$$= 2 \times (1+2)$$

$$= 2 \times 3.$$

Starting from the proposition and deriving true is not valid.

Example

```
Prove: 0 = 1
```

Does this mean that 0 = 1?



Make sure each step is logically valid

Example

So
$$25-45 = 16-36$$

So $5^2-2\cdot 5\cdot \frac{9}{2} = 4^2-2\cdot 4\cdot \frac{9}{2}$
So $5^2-2\cdot 5\cdot \frac{9}{2}+\left(\frac{9}{2}\right)^2 = 4^2-2\cdot 4\cdot \frac{9}{2}+\left(\frac{9}{2}\right)^2$
So $(5-\frac{9}{2})^2 = (4-\frac{9}{2})^2$
So $5-\frac{9}{2} = 4-\frac{9}{2}$

Does this mean that 5 = 4?



Make sure each step is logically valid

Example

Suppose a = b. Then,

$$a^{2} = ab$$
So
$$a^{2} - b^{2} = ab - b^{2}$$
So
$$(a - b)(a + b) = (a - b)b$$
So
$$a + b = b$$
So
$$a = 0$$

This is true no matter what value *a* is given at the start, so does that mean everything is equal to 0?

For propositions of the form $\forall x.A$ where x can have infinitely many values:

- You cannot enumerate infinitely many cases in a proof.
- Only considering a finite number of cases is not sufficient.

Example

For all
$$n$$
, $n^2 + n + 41$ is prime

True for n = 0, 1, 2, ..., 39. Not true for n = 40.



The order of quantifiers matters when it comes to propositions:

Example

- For every number x, there is a number y such that y is larger than x
- There is a number y such that for every number x, y is larger than x

Proof strategies: direct proof

Proposition form	You need to do this
$A \Rightarrow B$	Assume A and prove B
$A \Leftrightarrow B$	Prove "If A then B" and "If B then A"
$\forall x.A$	Show A holds for every possible value of x
$\exists x.A$	Find a value of x that makes A true

Proof strategies: contradiction

To prove A is true, assume A is false and derive a contradiction. That is, start from the negation of the proposition and derive false.

Example

Prove: $\sqrt{2}$ is irrational

Proof: Assume $\sqrt{2}$ is rational ...



Proposition form	Its negation
A and B	
A or B	
$A \Rightarrow B$	
$A \Leftrightarrow B$	
$\forall x.A$	
$\exists x.A$	

Proposition form	Its negation
A and B	not A or not B
A or B	
$A \Rightarrow B$	
$A \Leftrightarrow B$	
$\forall x.A$	
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Proposition form	Its negation
A and B	not A or not B
A or B	not A and not B
$A \Rightarrow B$	A and not B
$A \Leftrightarrow B$	A and not B , or B and not A
$\forall x.A$	
$\exists x.A$	

Proposition form	Its negation
A and B	not A or not B
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$A \Rightarrow B$	A and not B
$A \Leftrightarrow B$	A and not B , or B and not A
$\forall x.A$	$\exists x. \text{ not } A$
$\exists x.A$	

Proposition form	Its negation
A and B	not A or not B
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$A \Rightarrow B$	A and not B
$A \Leftrightarrow B$	A and not B , or B and not A
$\forall x.A$	$\exists x. \text{ not } A$
$\exists x.A$	$\forall x. \text{ not } A$

Proof strategies: contrapositive

To prove a proposition of the form "If A then B" you can prove "If not B then not A"

Example

Prove: If $m + n \ge 73$ then $m \ge 37$ or $n \ge 37$.



Proof strategies: dealing with \forall

How can we check infinitely many cases?

- Choose an arbitrary element: an object with no assumptions about it (may have to check several cases)
- Induction (see week 8)

Example

Prove: For every integer n, n^2 will have remainder 0 or 1 when divided by 4.

Note: "Arbitrary" is not the same as "random".

