MaunaLoa

March 31, 2025

1 MaunaLoa Temperature Time Series

References: - ARIMA Model in Python Time Series Forecasting #6. Nachiketa Hebbar - ARIMA for Time Series Forecasting; A Complete Guide. Zaina Saadeddin - Time Series Forecasting with ARIMA: Everything You Need to Know!. Nayeem Islam

```
[]: # Install pmdarima library
# pmdarima does not support Numpy 2.0
import pmdarima as pm
```

[]: !python --version

Python 3.11.11

- python 3.11.11
- numpy 1.23.2
- pandas 2.2.2

```
[]: !pip uninstall numpy
```

```
Found existing installation: numpy 1.26.4
Uninstalling numpy-1.26.4:
Would remove:
    /usr/local/bin/f2py
    /usr/local/lib/python3.11/dist-packages/numpy-1.26.4.dist-info/*
    /usr/local/lib/python3.11/dist-
packages/numpy.libs/libgfortran-040039e1.so.5.0.0
    /usr/local/lib/python3.11/dist-
packages/numpy.libs/libopenblas64_p-r0-0cf96a72.3.23.dev.so
    /usr/local/lib/python3.11/dist-
packages/numpy.libs/libquadmath-96973f99.so.0.0.0
    /usr/local/lib/python3.11/dist-packages/numpy/*
Proceed (Y/n)? y
Successfully uninstalled numpy-1.26.4
```

```
[]: pip install numpy==1.23.2
```

Collecting numpy==1.23.2

```
Using cached
numpy-1.23.2-cp311-cp311-manylinux_2_17_x86_64.manylinux2014_x86_64.whl.metadata
(2.2 kB)
Using cached
numpy-1.23.2-cp311-cp311-manylinux_2_17_x86_64.manylinux2014_x86_64.whl (17.0 MB)
Installing collected packages: numpy
```

ERROR: pip's dependency resolver does not currently take into account all the packages that are installed. This behaviour is the source of the following dependency conflicts.

scipy 1.15.2 requires numpy<2.5,>=1.23.5, but you have numpy 1.23.2 which is incompatible.

jaxlib 0.5.1 requires numpy>=1.25, but you have numpy 1.23.2 which is incompatible.

treescope 0.1.9 requires numpy>=1.25.2, but you have numpy 1.23.2 which is incompatible.

plotnine 0.14.5 requires numpy>=1.23.5, but you have numpy 1.23.2 which is incompatible.

albucore 0.0.23 requires numpy>=1.24.4, but you have numpy 1.23.2 which is incompatible.

mizani 0.13.1 requires numpy>=1.23.5, but you have numpy 1.23.2 which is incompatible.

blosc2 3.2.0 requires numpy>=1.26, but you have numpy 1.23.2 which is incompatible.

pandas-stubs 2.2.2.240909 requires numpy>=1.23.5, but you have numpy 1.23.2 which is incompatible.

opency-python-headless 4.11.0.86 requires numpy>=1.23.5; python_version >= "3.11", but you have numpy 1.23.2 which is incompatible.

ml-dtypes 0.4.1 requires numpy>=1.23.3; python_version >= "3.11", but you have numpy 1.23.2 which is incompatible.

chex 0.1.89 requires numpy>=1.24.1, but you have numpy 1.23.2 which is incompatible.

opency-contrib-python 4.11.0.86 requires numpy>=1.23.5; python_version >= "3.11", but you have numpy 1.23.2 which is incompatible.

jax 0.5.2 requires numpy>=1.25, but you have numpy 1.23.2 which is incompatible. bigframes 1.41.0 requires numpy>=1.24.0, but you have numpy 1.23.2 which is incompatible.

imbalanced-learn 0.13.0 requires numpy<3,>=1.24.3, but you have numpy 1.23.2 which is incompatible.

xarray 2025.1.2 requires numpy>=1.24, but you have numpy 1.23.2 which is incompatible. $\ensuremath{\mathbf{3}}$

albumentations 2.0.5 requires numpy>=1.24.4, but you have numpy 1.23.2 which is

[]: | !pip uninstall pandas Found existing installation: pandas 2.2.3 Uninstalling pandas-2.2.3: Would remove: /usr/local/lib/python3.11/dist-packages/pandas-2.2.3.dist-info/* /usr/local/lib/python3.11/dist-packages/pandas/* Proceed (Y/n)? y Successfully uninstalled pandas-2.2.3 []: !pip install pandas==2.2.2 Collecting pandas==2.2.2 Using cached pandas-2.2.2-cp311-cp311-manylinux_2_17_x86_64.manylinux2014_x86_64.whl.metadata (19 kB) Requirement already satisfied: numpy>=1.23.2 in /usr/local/lib/python3.11/distpackages (from pandas==2.2.2) (1.26.4) Requirement already satisfied: python-dateutil>=2.8.2 in /usr/local/lib/python3.11/dist-packages (from pandas==2.2.2) (2.9.0.post0) Requirement already satisfied: pytz>=2020.1 in /usr/local/lib/python3.11/distpackages (from pandas==2.2.2) (2025.2) Requirement already satisfied: tzdata>=2022.7 in /usr/local/lib/python3.11/distpackages (from pandas==2.2.2) (2025.2) Requirement already satisfied: six>=1.5 in /usr/local/lib/python3.11/distpackages (from python-dateutil>=2.8.2->pandas==2.2.2) (1.17.0) Using cached pandas-2.2.2-cp311-cp311-manylinux_2_17_x86_64.manylinux2014_x86_64.whl (13.0 Installing collected packages: pandas Successfully installed pandas-2.2.2 []: !pip install pmdarima Requirement already satisfied: pmdarima in /usr/local/lib/python3.11/distpackages (2.0.4) Requirement already satisfied: joblib>=0.11 in /usr/local/lib/python3.11/distpackages (from pmdarima) (1.4.2) Requirement already satisfied: Cython!=0.29.18,!=0.29.31,>=0.29 in /usr/local/lib/python3.11/dist-packages (from pmdarima) (3.0.12) Requirement already satisfied: numpy>=1.21.2 in /usr/local/lib/python3.11/distpackages (from pmdarima) (1.26.4)

Requirement already satisfied: pandas>=0.19 in /usr/local/lib/python3.11/dist-

Requirement already satisfied: scipy>=1.3.2 in /usr/local/lib/python3.11/dist-

packages (from pmdarima) (2.2.2)

packages (from pmdarima) (1.15.2)

Requirement already satisfied: scikit-learn>=0.22 in

/usr/local/lib/python3.11/dist-packages (from pmdarima) (1.6.1)

```
Requirement already satisfied: statsmodels>=0.13.2 in
    /usr/local/lib/python3.11/dist-packages (from pmdarima) (0.14.4)
    Requirement already satisfied: urllib3 in /usr/local/lib/python3.11/dist-
    packages (from pmdarima) (2.3.0)
    Requirement already satisfied: setuptools!=50.0.0,>=38.6.0 in
    /usr/local/lib/python3.11/dist-packages (from pmdarima) (78.1.0)
    Requirement already satisfied: packaging>=17.1 in
    /usr/local/lib/python3.11/dist-packages (from pmdarima) (24.2)
    Requirement already satisfied: python-dateutil>=2.8.2 in
    /usr/local/lib/python3.11/dist-packages (from pandas>=0.19->pmdarima)
    (2.9.0.post0)
    Requirement already satisfied: pytz>=2020.1 in /usr/local/lib/python3.11/dist-
    packages (from pandas>=0.19->pmdarima) (2025.2)
    Requirement already satisfied: tzdata>=2022.7 in /usr/local/lib/python3.11/dist-
    packages (from pandas>=0.19->pmdarima) (2025.2)
    Requirement already satisfied: threadpoolctl>=3.1.0 in
    /usr/local/lib/python3.11/dist-packages (from scikit-learn>=0.22->pmdarima)
    Requirement already satisfied: patsy>=0.5.6 in /usr/local/lib/python3.11/dist-
    packages (from statsmodels>=0.13.2->pmdarima) (1.0.1)
    Requirement already satisfied: six>=1.5 in /usr/local/lib/python3.11/dist-
    packages (from python-dateutil>=2.8.2->pandas>=0.19->pmdarima) (1.17.0)
[]: # Load libraries
     import pandas as pd
     import numpy as np
```

1.1 Read Data: MaunaLoa Daily Temperatures

Shape of data (1821, 5)

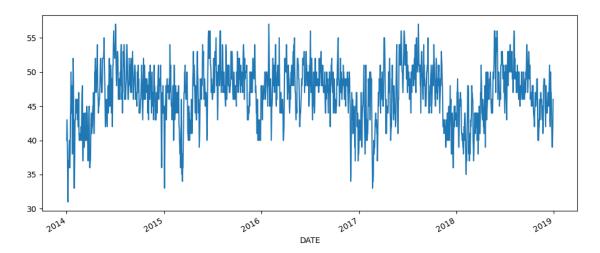
[]:		${\tt MinTemp}$	${\tt MaxTemp}$	AvgTemp	Sunrise	Sunset
	DATE					
	2014-01-01	33.0	46.0	40.0	657	1756
	2014-01-02	35.0	50.0	43.0	657	1756
	2014-01-03	36.0	45.0	41.0	657	1757

```
2014-01-04 32.0 41.0 37.0 658 1757
2014-01-05 24.0 38.0 31.0 658 1758
```

The dataset has 1,821 rows and 5 columns.

```
[]: # plot data
df['AvgTemp'].plot(figsize=(12,5))
```

[]: <Axes: xlabel='DATE'>



1.2 Is Data Stationary?

If P-vlaue < 0.05, data is stationary

If P-value > 0.05, data is not stationary. Data has an increasing for decreasing trend/p>

```
# Interpret the results
if dftest[1] > 0.05:
    print("The data is not stationary.")
else:
    print("The data is stationary.")
```

[]: # P-value should be as low as possible. < 0.05

ad_test(df['AvgTemp'])

- 1. ADF: -6.554680125068777
- 2. P-Value: 8.675937480199653e-09
- 3. Num of Lags: 12
- 4. Num of Observations Used for ADF Regression and Critical Values Calculation: 1808
- 5. Critical Values:

1%: -3.433972018026501 5%: -2.8631399192826676 10%: -2.5676217442756872

The data is stationary.

1.3 Find the Best ARIMA Model

```
[]: # Load auto_arima
from pmdarima import auto_arima
# ignore warnings
import warnings
warnings.filterwarnings("ignore")
```

```
[]: # Find the best ARIMA model
stepwise_fit = auto_arima(df['AvgTemp'], trace=True, suppress_warnings=True)
stepwise_fit.summary()
```

Performing stepwise search to minimize aic

```
ARIMA(2,0,2)(0,0,0)[0] intercept
                                  : AIC=8344.294, Time=4.38 sec
                                  : AIC=10347.755, Time=0.07 sec
ARIMA(0,0,0)(0,0,0)[0] intercept
                                  : AIC=8365.701, Time=0.29 sec
ARIMA(1,0,0)(0,0,0)[0] intercept
ARIMA(0,0,1)(0,0,0)[0] intercept
                                   : AIC=9136.225, Time=0.37 sec
                                   : AIC=19192.139, Time=0.04 sec
ARIMA(0,0,0)(0,0,0)[0]
                                  : AIC=8355.947, Time=2.16 sec
ARIMA(1,0,2)(0,0,0)[0] intercept
ARIMA(2,0,1)(0,0,0)[0] intercept
                                   : AIC=8356.308, Time=5.38 sec
                                  : AIC=8347.324, Time=3.77 sec
ARIMA(3,0,2)(0,0,0)[0] intercept
                                  : AIC=8318.606, Time=3.82 sec
ARIMA(2,0,3)(0,0,0)[0] intercept
ARIMA(1,0,3)(0,0,0)[0] intercept
                                  : AIC=8330.189, Time=5.47 sec
ARIMA(3,0,3)(0,0,0)[0] intercept
                                  : AIC=8310.514, Time=4.54 sec
ARIMA(4,0,3)(0,0,0)[0] intercept
                                  : AIC=8332.054, Time=5.42 sec
```

```
ARIMA(3,0,4)(0,0,0)[0] intercept
                                    : AIC=8317.479, Time=6.36 sec
ARIMA(2,0,4)(0,0,0)[0] intercept
                                   : AIC=8305.268, Time=4.84 sec
                                   : AIC=8296.961, Time=6.17 sec
ARIMA(1,0,4)(0,0,0)[0] intercept
ARIMA(0,0,4)(0,0,0)[0] intercept
                                    : AIC=8455.435, Time=1.28 sec
ARIMA(1,0,5)(0,0,0)[0] intercept
                                   : AIC=8295.814, Time=5.44 sec
ARIMA(0,0,5)(0,0,0)[0] intercept
                                   : AIC=8419.091, Time=1.78 sec
ARIMA(2,0,5)(0,0,0)[0] intercept
                                   : AIC=8302.138, Time=7.48 sec
                                    : AIC=8304.533, Time=0.62 sec
ARIMA(1,0,5)(0,0,0)[0]
```

Best model: ARIMA(1,0,5)(0,0,0)[0] intercept

Total fit time: 69.726 seconds

1		١.
L	_	١ ١

Dep. Variable:	y	No. Observations:	1821
Model:	SARIMAX(1, 0, 5)	Log Likelihood	-4139.907
Date:	Mon, 31 Mar 2025	AIC	8295.814
Time:	04:09:28	BIC	8339.871
Sample:	0	HQIC	8312.068
	- 1821		
Covariance Type:	opg		

	coef	std eri		$\mathbf{P} > \mathbf{z} $	[0.025]	0.975]
intercept	1.3625	0.397	3.429	0.001	0.584	2.141
ar.L1	0.9707	0.009	113.365	0.000	0.954	0.987
ma.L1	-0.1219	0.024	-5.083	0.000	-0.169	-0.075
ma.L2	-0.2155	0.024	-8.836	0.000	-0.263	-0.168
ma.L3	-0.2028	0.024	-8.424	0.000	-0.250	-0.156
ma.L4	-0.1345	0.023	-5.885	0.000	-0.179	-0.090
ma.L5	-0.0459	0.024	-1.879	0.060	-0.094	0.002
$\mathbf{sigma2}$	5.5010	0.172	31.927	0.000	5.163	5.839
Ljung-Box (L1) (Q):		Q):	0.00 Jar	que-Ber	a (JB):	21.33
Prob(Q):			0.99 Prob(JB) :		0.00	
Heteroskedasticity (H):			0.81 Ske	ew:		-0.18
Prob(H) (two-sided):			0.01 Ku	rtosis:		3.40

Warnings:

[1] Covariance matrix calculated using the outer product of gradients (complex-step).

The best arima model is ARIMA(1,0,5). - p: The number of past values (lags) considered in the AR term. 1 - d: The degree of differencing applied to the data. 0 - q: The number of past forecast errors included in the MA term. 5

[]: # Load ARIMA from statsmodels.tsa.arima.model import ARIMA

1.4 Split Data into Train and Test

```
[]: print(df.shape)
    train = df.iloc[:-30] # all values except the last 30 values
    test = df.iloc[-30:] #last 30 values

print(train.shape, test.shape)
```

(1821, 5) (1791, 5) (30, 5)

1.5 Train the Model

```
[]: model = ARIMA(train['AvgTemp'], order=(1,0,5))
model = model.fit()
model.summary()
```

[]:

Dep. Variable:	AvgTemp	No. Observations:	1791
Model:	ARIMA(1, 0, 5)	Log Likelihood	-4070.198
Date:	Mon, 31 Mar 2025	AIC	8156.395
Time:	02:17:28	BIC	8200.320
Sample:	0	HQIC	8172.614
	- 1791		
Covariance Type:	opg		

	v <u>-</u>					
	\mathbf{coef}	std err	${f z}$	$\mathbf{P} > \mathbf{z} $	[0.025]	0.975]
const	46.5856	0.758	61.454	0.000	45.100	48.071
ar.L1	0.9856	0.005	188.230	0.000	0.975	0.996
ma.L1	-0.1412	0.023	-6.124	0.000	-0.186	-0.096
ma.L2	-0.2268	0.024	-9.635	0.000	-0.273	-0.181
ma.L3	-0.2168	0.023	-9.251	0.000	-0.263	-0.171
ma.L4	-0.1479	0.023	-6.491	0.000	-0.193	-0.103
ma.L5	-0.0595	0.024	-2.438	0.015	-0.107	-0.012
$\mathbf{sigma2}$	5.5093	0.174	31.624	0.000	5.168	5.851
Ljung-Box (L1) (Q):		(Q):	0.00 Ja	rque-Be	ra (JB):	14.88
Prob(Q):			0.97 Prob(JB) :			0.00
Heteroskedasticity (H):			0.82 Sk	ew:		-0.15
Prob(H) (two-sided):			0.01 K ι	ırtosis:		3.33

Warnings:

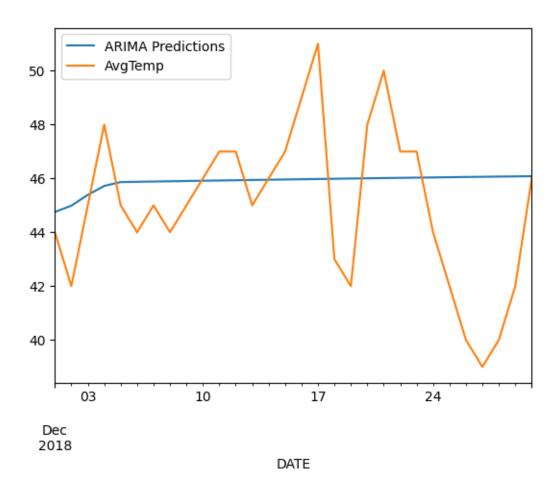
[1] Covariance matrix calculated using the outer product of gradients (complex-step).

```
[]: # Make a prediction on the test data then compare to actual

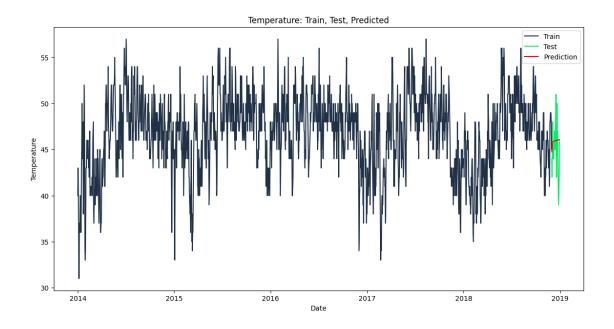
start=len(train)
end=len(train)+len(test)-1
#pred=model.predict(start=start,end=end,typ='levels').rename('ARIMALI
Predictions').rename('ARIMA Predictions')
```

```
pred=model.predict(start=start,end=end,typ='levels').rename('ARIMA Predictions')
     pred.index = df.index[start:end+1]
     print(pred)
    DATE
    2018-12-01
                   44.754109
    2018-12-02
                  44.987795
    2018-12-03
                  45.388741
    2018-12-04
                   45.721545
    2018-12-05
                  45.863733
    2018-12-06
                  45.874126
    2018-12-07
                   45.884370
    2018-12-08
                   45.894466
    2018-12-09
                   45.904417
    2018-12-10
                   45.914225
    2018-12-11
                   45.923891
    2018-12-12
                  45.933418
    2018-12-13
                  45.942808
    2018-12-14
                  45.952063
    2018-12-15
                  45.961185
    2018-12-16
                   45.970175
    2018-12-17
                  45.979036
    2018-12-18
                   45.987769
    2018-12-19
                  45.996377
    2018-12-20
                  46.004861
    2018-12-21
                  46.013222
    2018-12-22
                   46.021463
    2018-12-23
                   46.029586
                   46.037591
    2018-12-24
    2018-12-25
                   46.045481
    2018-12-26
                  46.053258
    2018-12-27
                  46.060923
    2018-12-28
                  46.068477
    2018-12-29
                  46.075922
    2018-12-30
                   46.083261
    Name: ARIMA Predictions, dtype: float64
[]: print(test['AvgTemp'])
    DATE
    2018-12-01
                  44.0
    2018-12-02
                  42.0
    2018-12-03
                   45.0
                   48.0
    2018-12-04
    2018-12-05
                  45.0
    2018-12-06
                  44.0
    2018-12-07
                  45.0
    2018-12-08
                  44.0
```

```
2018-12-09
                  45.0
    2018-12-10
                  46.0
    2018-12-11
                  47.0
    2018-12-12
                  47.0
                  45.0
    2018-12-13
                  46.0
    2018-12-14
                  47.0
    2018-12-15
    2018-12-16
                  49.0
    2018-12-17
                  51.0
    2018-12-18
                  43.0
    2018-12-19
                  42.0
    2018-12-20
                  48.0
    2018-12-21
                  50.0
                  47.0
    2018-12-22
    2018-12-23
                  47.0
    2018-12-24
                  44.0
    2018-12-25
                  42.0
    2018-12-26
                  40.0
    2018-12-27
                  39.0
    2018-12-28
                  40.0
    2018-12-29
                  42.0
    2018-12-30
                  46.0
    Name: AvgTemp, dtype: float64
[]: pred.plot(legend=True)
     test['AvgTemp'].plot(legend=True)
```



1.6 Plot Train, Test, & Predicted Data



```
[]: test['AvgTemp'].mean()
```

[]: 45.0

The average for the test data is 45.

```
[]: pred = pred[:len(test)]
  test_temp = test['AvgTemp'][:len(forecast)]

# Calculate RMSE

from sklearn.metrics import mean_squared_error
  rmse = np.sqrt(mean_squared_error(test_temp,pred))
  print(f"RMSE: {rmse: .4f}")
```

RMSE: 3.0005

On average predictions are off by +/-3 degrees.

1.7 Forecast Past the End of the Original Data

Forecast: 2018-12-31 to 2109-04-09

```
[]: # Forecast future value
forecast = model_fit.forecast(steps = 100)
print(forecast)
```

```
1791
            44.754109
    1792
           44.987795
    1793
            45.388741
    1794
            45.721545
    1795
            45.863733
    1886
            46.392716
    1887
            46.395493
    1888
            46.398231
    1889
            46.400928
            46.403587
    1890
    Name: predicted_mean, Length: 100, dtype: float64
[]: forecast.index = pd.date_range(start=df.index[-1], periods=101,__
      ⇔inclusive="right")
     print(forecast)
    2018-12-31
                  44.754109
    2019-01-01
                  44.987795
    2019-01-02
                  45.388741
    2019-01-03
                  45.721545
    2019-01-04
                  45.863733
    2019-04-05
                  46.392716
    2019-04-06
                  46.395493
    2019-04-07
                  46.398231
    2019-04-08 46.400928
    2019-04-09
                  46.403587
    Freq: D, Name: predicted_mean, Length: 100, dtype: float64
[ ]: last_date = train.index[-1]
     forecast_index = pd.date_range(last_date,periods=101, inclusive="right")
     # Define plot
     plt.figure(figsize=(14,7))
     plt.plot(train.index, train["AvgTemp"], label='Train', color="navy") # train_
     plt.plot(test.index, test["AvgTemp"], label='Test', color='#01ef63') # test data
     plt.plot(forecast_index,forecast, label='Forecast', color='red')
      ⇔forecasted data
     plt.title('Temperature: Train, Test, Forecast')
     plt.xlabel('Date')
     plt.ylabel('Temperature')
     plt.legend()
     plt.show()
```

