

Tree learnign methods

output:

```
library(dplyr)
```

```
##  
## Attaching package: 'dplyr'  
## The following objects are masked from 'package:stats':  
##  
##   filter, lag  
## The following objects are masked from 'package:base':  
##  
##   intersect, setdiff, setequal, union
```

```
library(caret)
```

```
## Loading required package: lattice
```

```
## Loading required package: ggplot2
```

```
library(tree)
```

```
library(ggplot2)
```

1 Exploratory data analysis

```
data <- read.csv(params$myfile)
```

The data set contains data on 5631 compound where a solubility screen has been preformed where all compounds were classified as eather soluble of insoluble. Fro each compound 72 contineous variables were recorded.

A short exploratory data analysis is preformed to become familiar with the dateset.

```
summary(data)
```

```
##           x1           x2           x3           x4  
## Min.      : 265.5   Min.      : 219.6   Min.      :1.208   Min.      :1.069  
## 1st Qu.: 754.2   1st Qu.: 518.9   1st Qu.:1.447   1st Qu.:1.465  
## Median : 880.9   Median : 598.0   Median :1.469   Median :1.561  
## Mean      : 880.6   Mean      : 596.4   Mean      :1.472   Mean      :1.551  
## 3rd Qu.:1000.1   3rd Qu.: 674.9   3rd Qu.:1.493   3rd Qu.:1.646  
## Max.      :1903.1   Max.      :1275.7   Max.      :1.703   Max.      :2.251  
##  
##           x5           x6           x7           x8  
## Min.      : 657.5   Min.      : 248.9   Min.      : 76.0   Min.      : 17.0  
## 1st Qu.:1374.1   1st Qu.: 855.4   1st Qu.: 459.1   1st Qu.:175.8  
## Median :1560.4   Median :1000.9   Median : 575.8   Median :229.9  
## Mean      :1543.7   Mean      : 998.5   Mean      : 570.1   Mean      :230.9
```

```

## 3rd Qu.:1729.9 3rd Qu.:1149.1 3rd Qu.: 677.1 3rd Qu.:282.1
## Max. :3375.8 Max. :2329.4 Max. :1392.8 Max. :541.8
##
##          x9          x10          x11          x12
## Min.   : 0.00 Min.   : 0.00 Min.   : 0.00 Min.   : 0.00
## 1st Qu.: 84.12 1st Qu.: 41.50 1st Qu.:15.25 1st Qu.: 2.50
## Median :115.00 Median : 58.75 Median :22.50 Median : 5.00
## Mean   :116.37 Mean   : 59.70 Mean   :24.23 Mean   : 6.27
## 3rd Qu.:145.81 3rd Qu.: 75.38 3rd Qu.:30.56 3rd Qu.: 8.25
## Max.   :318.38 Max.   :188.88 Max.   :98.00 Max.   :36.00
##
##          x13          x14          x15          x16
## Min.   :0.00100 Min.   :0.0010 Min.   :0.0020 Min.   :0.0040
## 1st Qu.:0.03400 1st Qu.:0.0600 1st Qu.:0.0980 1st Qu.:0.1850
## Median :0.05200 Median :0.0910 Median :0.1500 Median :0.2830
## Mean   :0.06219 Mean   :0.1059 Mean   :0.1765 Mean   :0.3303
## 3rd Qu.:0.08100 3rd Qu.:0.1350 3rd Qu.:0.2250 3rd Qu.:0.4310
## Max.   :0.28600 Max.   :0.4800 Max.   :0.8800 Max.   :1.4670
##
##          x17          x18          x19          x20
## Min.   :0.0000 Min.   :0.0000 Min.   :0.0000 Min.   :0.0000
## 1st Qu.:0.2720 1st Qu.:0.3480 1st Qu.:0.4530 1st Qu.:0.5660
## Median :0.4140 Median :0.5210 Median :0.6860 Median :0.8800
## Mean   :0.4777 Mean   :0.5951 Mean   :0.7531 Mean   :0.9349
## 3rd Qu.:0.6325 3rd Qu.:0.7890 3rd Qu.:0.9850 3rd Qu.:1.2180
## Max.   :1.9010 Max.   :2.2390 Max.   :2.5560 Max.   :3.2330
##
##          x21          x22          x23          x24
## Min.   :1.860 Min.   :0.695 Min.   :0.1760 Min.   :0.0270
## 1st Qu.:2.430 1st Qu.:1.452 1st Qu.:0.7870 1st Qu.:0.3060
## Median :2.610 Median :1.697 Median :0.9680 Median :0.3850
## Mean   :2.611 Mean   :1.699 Mean   :0.9705 Mean   :0.3927
## 3rd Qu.:2.777 3rd Qu.:1.927 3rd Qu.:1.1435 3rd Qu.:0.4710
## Max.   :4.060 Max.   :3.239 Max.   :2.1090 Max.   :1.1060
##
##          x25          x26          x27          x28
## Min.   :0.0000 Min.   :0.0000 Min.   :0.00000 Min.   :0.00000
## 1st Qu.:0.1470 1st Qu.:0.0730 1st Qu.:0.02800 1st Qu.:0.00500
## Median :0.1910 Median :0.0980 Median :0.03700 Median :0.00800
## Mean   :0.1977 Mean   :0.1011 Mean   :0.04068 Mean   :0.01036
## 3rd Qu.:0.2430 3rd Qu.:0.1240 3rd Qu.:0.05000 3rd Qu.:0.01300
## Max.   :0.6660 Max.   :0.4010 Max.   :0.21100 Max.   :0.08500
##
##          x29          x30          x31          x32
## Min.   : 2.678 Min.   : 1.931 Min.   : 1.543 Min.   : 0.707
## 1st Qu.: 6.819 1st Qu.: 6.521 1st Qu.: 6.246 1st Qu.: 0.866
## Median : 7.219 Median : 6.882 Median : 6.569 Median : 1.500
## Mean   : 7.527 Mean   : 7.052 Mean   : 6.650 Mean   : 3.210
## 3rd Qu.: 8.033 3rd Qu.: 7.387 3rd Qu.: 6.968 3rd Qu.: 4.717
## Max.   :12.946 Max.   :11.980 Max.   :11.319 Max.   :17.292
##
##          x33          x34          x35          x36
## Min.   : 0.707 Min.   : 0.707 Min.   : 15.62 Min.   : 1.875
## 1st Qu.: 1.500 1st Qu.: 1.118 1st Qu.:212.50 1st Qu.:115.375

```

```

## Median : 3.162      Median : 2.121      Median :265.25      Median :144.000
## Mean   : 4.548      Mean   : 3.855      Mean   :270.73      Mean   :146.687
## 3rd Qu.: 7.159      3rd Qu.: 6.164      3rd Qu.:326.25      3rd Qu.:176.250
## Max.   :21.059      Max.   :21.651      Max.   :761.62      Max.   :379.500
##
##          x37          x38          x39          x40
## Min.    : 1.125      Min.    : 0.375      Min.    : 0.125      Min.    : 0.00
## 1st Qu.: 64.500      1st Qu.: 40.625      1st Qu.: 25.750      1st Qu.: 19.38
## Median : 83.250      Median : 54.000      Median : 36.250      Median : 28.12
## Mean    : 83.455      Mean    : 54.082      Mean    : 36.732      Mean    : 28.59
## 3rd Qu.:101.125      3rd Qu.: 67.375      3rd Qu.: 47.125      3rd Qu.: 37.00
## Max.    :212.875      Max.    :159.375      Max.    :136.625      Max.    :114.50
##
##          x41          x42          x43          x44
## Min.    : 0.00       Min.    : 0.000      Min.    : 0.454      Min.    : 0.616
## 1st Qu.: 13.62       1st Qu.: 9.875      1st Qu.:13.755      1st Qu.: 20.369
## Median : 20.88       Median :15.500      Median :21.045      Median : 29.984
## Mean    : 20.96       Mean    :15.468      Mean    :22.580      Mean    : 32.402
## 3rd Qu.: 27.50       3rd Qu.:20.625      3rd Qu.:29.450      3rd Qu.: 41.964
## Max.    :101.50       Max.    :89.625      Max.    :85.059      Max.    :115.804
##
##          x45          x46          x47          x48
## Min.    : 0.543      Min.    : 0.91       Min.    : 0.751      Min.    : 0.00
## 1st Qu.: 25.117      1st Qu.: 30.68      1st Qu.: 37.080      1st Qu.: 42.18
## Median : 35.880      Median : 44.48      Median : 54.345      Median : 61.22
## Mean    : 39.327      Mean    : 49.33      Mean    : 60.700      Mean    : 68.64
## 3rd Qu.: 50.449      3rd Qu.: 64.01      3rd Qu.: 78.532      3rd Qu.: 88.62
## Max.    :159.264      Max.    :210.14      Max.    :253.770      Max.    :275.60
##
##          x49          x50          x51          x52
## Min.    : 0.00       Min.    : 0.00       Min.    : 0.0000      Min.    : 0.000
## 1st Qu.: 47.45       1st Qu.: 53.99      1st Qu.: 0.9605      1st Qu.: 0.737
## Median : 70.16       Median : 79.66      Median : 1.4160      Median : 1.089
## Mean    : 78.58       Mean    : 89.11      Mean    : 1.6947      Mean    : 1.416
## 3rd Qu.:101.12       3rd Qu.:114.34      3rd Qu.: 1.9990      3rd Qu.: 1.639
## Max.    :341.64       Max.    :371.88      Max.    :171.1110     Max.    :216.500
##
##          x53          x54          x55          x56
## Min.    :11.61       Min.    : 0.007      Min.    : 484.6       Min.    :113.6
## 1st Qu.:17.37       1st Qu.: 1.139      1st Qu.:1092.6       1st Qu.: 420.5
## Median :18.81       Median : 2.172      Median :1250.9       Median : 511.5
## Mean    :18.84       Mean    : 3.372      Mean    :1358.5       Mean    : 541.4
## 3rd Qu.:20.25       3rd Qu.: 3.720      3rd Qu.:1417.2       3rd Qu.: 624.0
## Max.    :27.25       Max.    :346.750     Max.    :5949.9       Max.    :1766.2
##
##          x57          x58          x59          x60
## Min.    : 0.00       Min.    : 0.00       Min.    : 0.000      Min.    : 0.000
## 1st Qu.: 90.38       1st Qu.: 15.62      1st Qu.: 5.875      1st Qu.: 1.625
## Median :135.00       Median : 31.00      Median : 11.500      Median : 3.250
## Mean    :156.38       Mean    : 41.60      Mean    : 16.799      Mean    : 5.492
## 3rd Qu.:202.75       3rd Qu.: 59.12      3rd Qu.: 24.500      3rd Qu.: 8.000
## Max.    :709.12       Max.    :265.50      Max.    :155.250     Max.    :122.750
##
##          x61          x62          x63          x64

```

```
## Min.    : 0.0000    Min.    : 0.0000    Min.    : -3252.8    Min.    : -344.9
## 1st Qu.: 0.0000    1st Qu.: 0.0000    1st Qu.: 243.7     1st Qu.: 328.6
## Median : 0.2500    Median : 0.0000    Median : 322.1     Median : 457.0
## Mean   : 0.8435    Mean   : 0.1091    Mean   : 185.2     Mean   : 457.2
## 3rd Qu.: 1.1250    3rd Qu.: 0.0000    3rd Qu.: 391.1     3rd Qu.: 596.5
## Max.   :100.8750    Max.   :79.3750    Max.   : 727.6     Max.   :1200.4
##
##      x65           x66           x67           x68
## Min.    : -10.25    Min.    : 10.38     Min.    : 0.00      Min.    : -10.75
## 1st Qu.: 305.31    1st Qu.:134.00     1st Qu.: 67.75     1st Qu.: 36.50
## Median : 406.00    Median :185.88     Median : 98.00     Median : 53.00
## Mean   : 413.76    Mean   :189.30     Mean   : 99.57     Mean   : 54.21
## 3rd Qu.: 521.94    3rd Qu.:239.94     3rd Qu.:128.50     3rd Qu.: 69.62
## Max.   :1069.50    Max.   :511.12     Max.   :291.62     Max.   :161.88
##
##      x69           x70           x71           x72
## Min.    : -55.38    Min.    : -61.375   Min.    : 9.897     Min.    : 103.1
## 1st Qu.: 14.62     1st Qu.: 2.500     1st Qu.: 37.275    1st Qu.: 369.2
## Median : 21.75     Median : 4.875     Median : 43.828     Median : 431.5
## Mean   : 23.39     Mean   : 6.161     Mean   : 43.870     Mean   : 427.6
## 3rd Qu.: 29.62     3rd Qu.: 8.125     3rd Qu.: 50.443     3rd Qu.: 490.5
## Max.   : 90.38     Max.   : 34.875     Max.   :100.170     Max.   :1056.7
##
##                               NA's    :787
##
##      y
## Min.    : -1.0000
## 1st Qu.: -1.0000
## Median : -1.0000
## Mean   : -0.2406
## 3rd Qu.: 1.0000
## Max.   : 1.0000
##
```

In the summary one can see that the only variable that has missing values is x_{71} with a percentage of 13.97%. To perform analysis one can not have missing values hence we decided to substitute the *NA* values with the column mean instead of for example deleting the entire column or all rows with missing values.

```
library(zoo)
```

```
##
## Attaching package: 'zoo'

## The following objects are masked from 'package:base':
##
##      as.Date, as.Date.numeric
```

```
data <- na.aggregate(data) # set the average of the column on NA values
```

To check the variability of the data and how they are distributed we made violin plots. As we have a lot of variables the data is split with regards to the column mean in order to make the observation easier.

```
library(tidyr)
library(ggplot2)
library(dplyr)
```

```
subset0 <- data.frame(data$x51, data$x52, data$x61, data$x62) # mean less than 2 with high outliers
```

```
subset1 <- data.frame(data$x13, data$x14, data$x15, data$x16, data$x17, data$x18, data$x24, data$x25, data
```

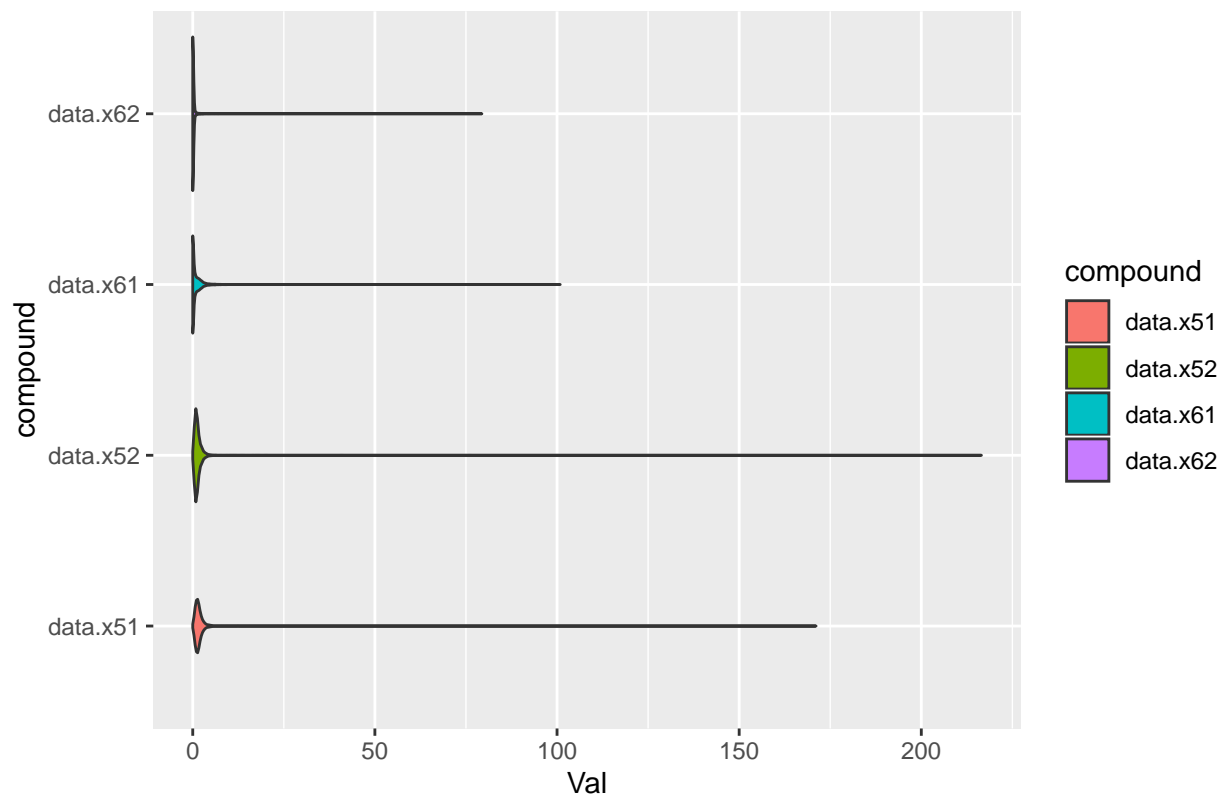
```

subset1.1 <- data.frame(data$x3, data$x4, data$x19, data$x20, data$x22, data$x23) # mean less than 2
subset2 <- data.frame(data$x12, data$x21, data$x29, data$x30, data$x31, data$x32, data$x33, data$x34, d
subset3 <- data.frame(data$x11, data$x39, data$x40, data$x41, data$x42, data$x43, data$x44, data$x45, d
subset4 <-data.frame(data$x10, data$x37, data$x38, data$x47, data$x48, data$x49, data$x50, data$x68) #
subset5 <- data.frame(data$x1, data$x2, data$x7, data$x8, data$x9, data$x35, data$x36, data$x56, data$x
subset6 <- data.frame(data$x5, data$x6, data$x55) # mean higher than 1000

subset0 %>%
  gather(key="compound", value="Val") %>%
  ggplot( aes(x=compound, y=Val, fill=compound)) +
    geom_violin()+
    coord_flip()+
    ggtitle("Plot means lower than 2 with large outliers")

```

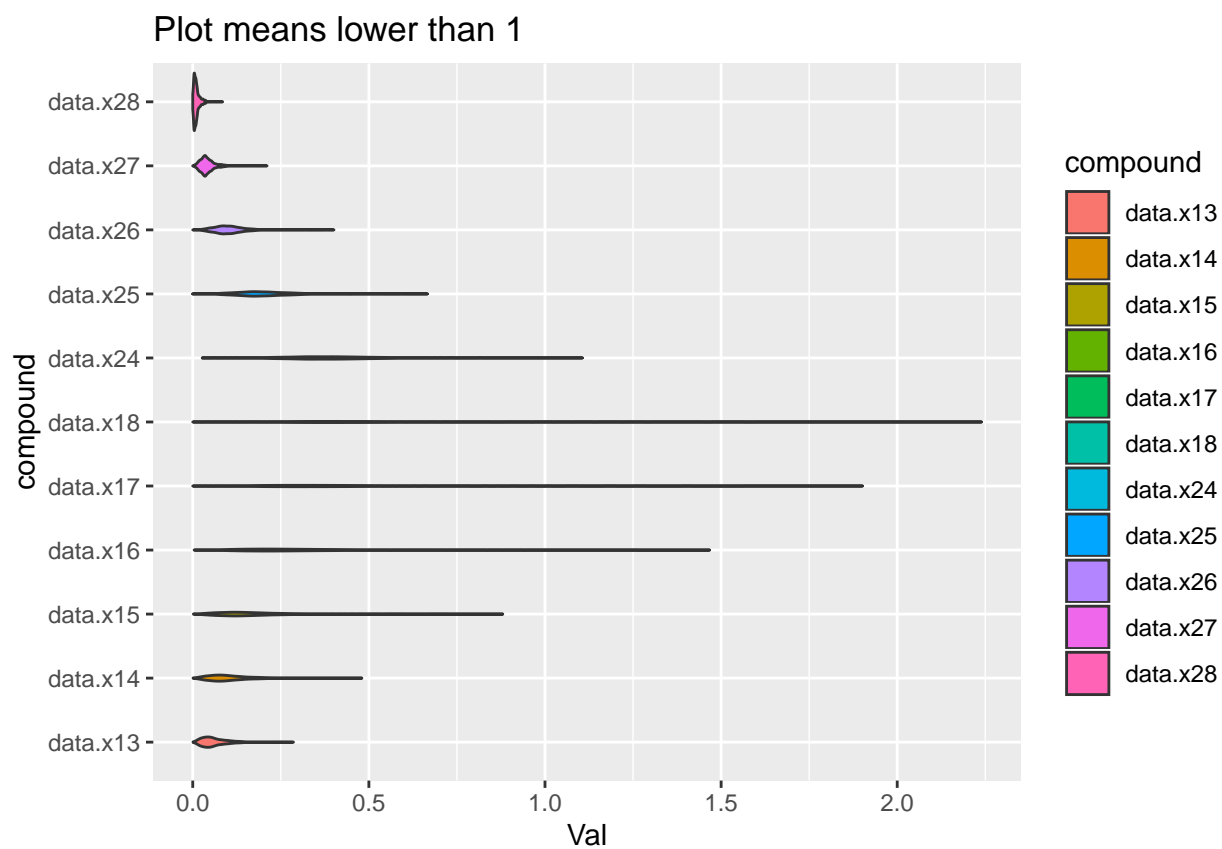
Plot means lower than 2 with large outliers



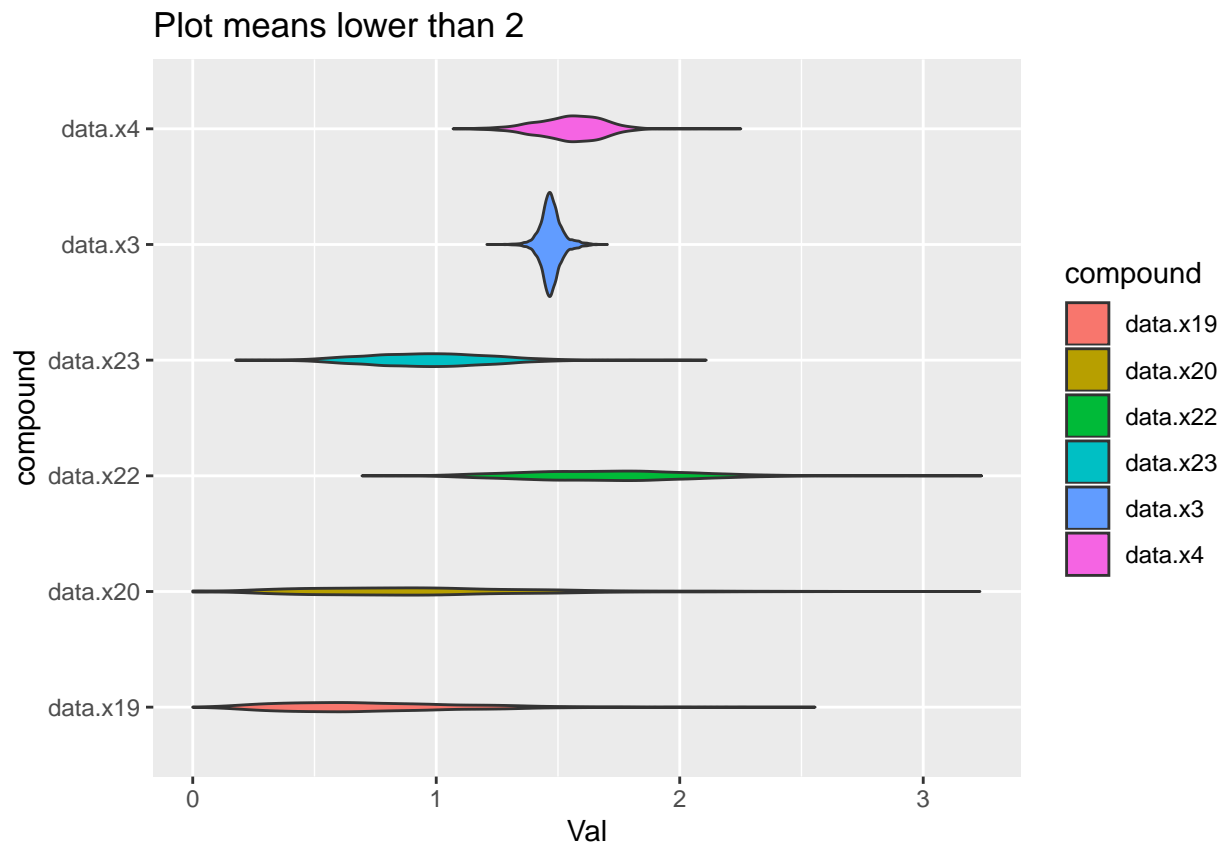
```

subset1 %>%
  gather(key="compound", value="Val") %>%
  ggplot( aes(x=compound, y=Val, fill=compound)) +
    geom_violin()+
    coord_flip()+
    ggtitle("Plot means lower than 1")

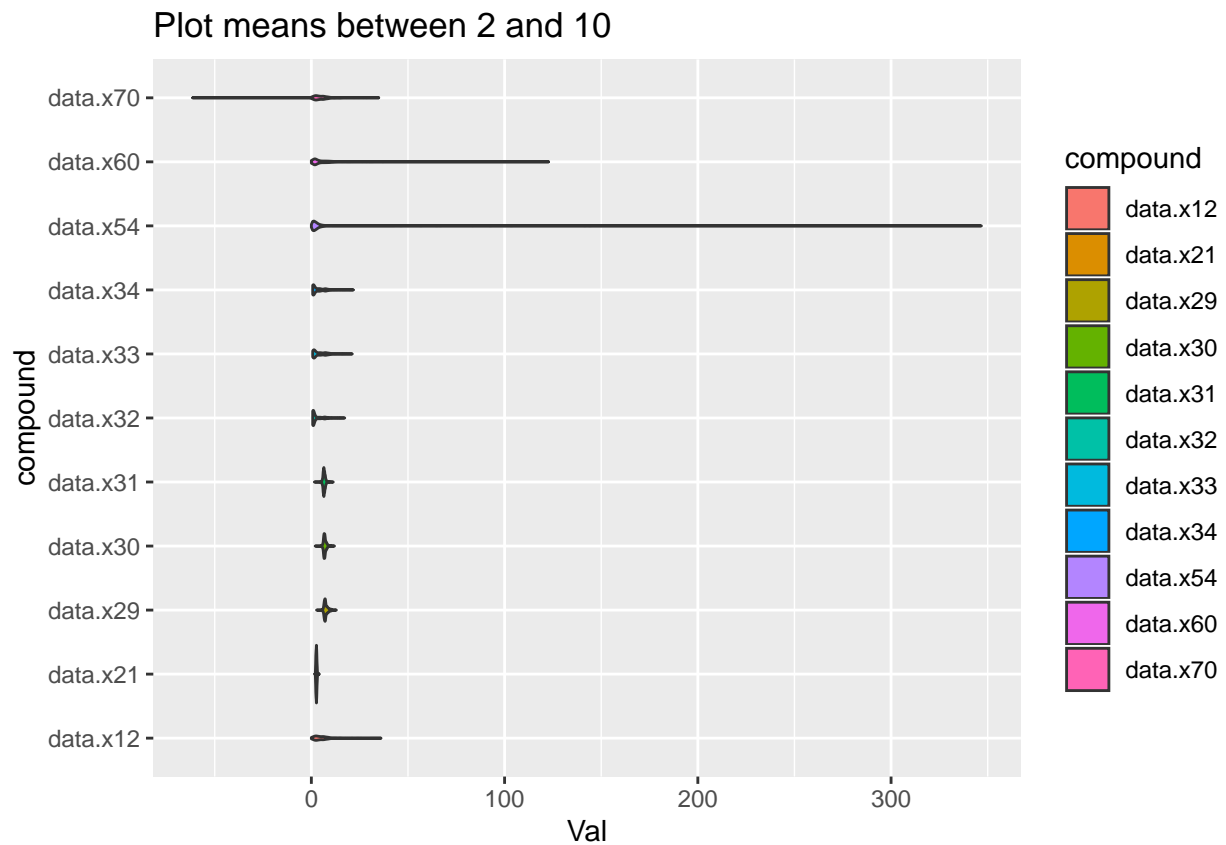
```



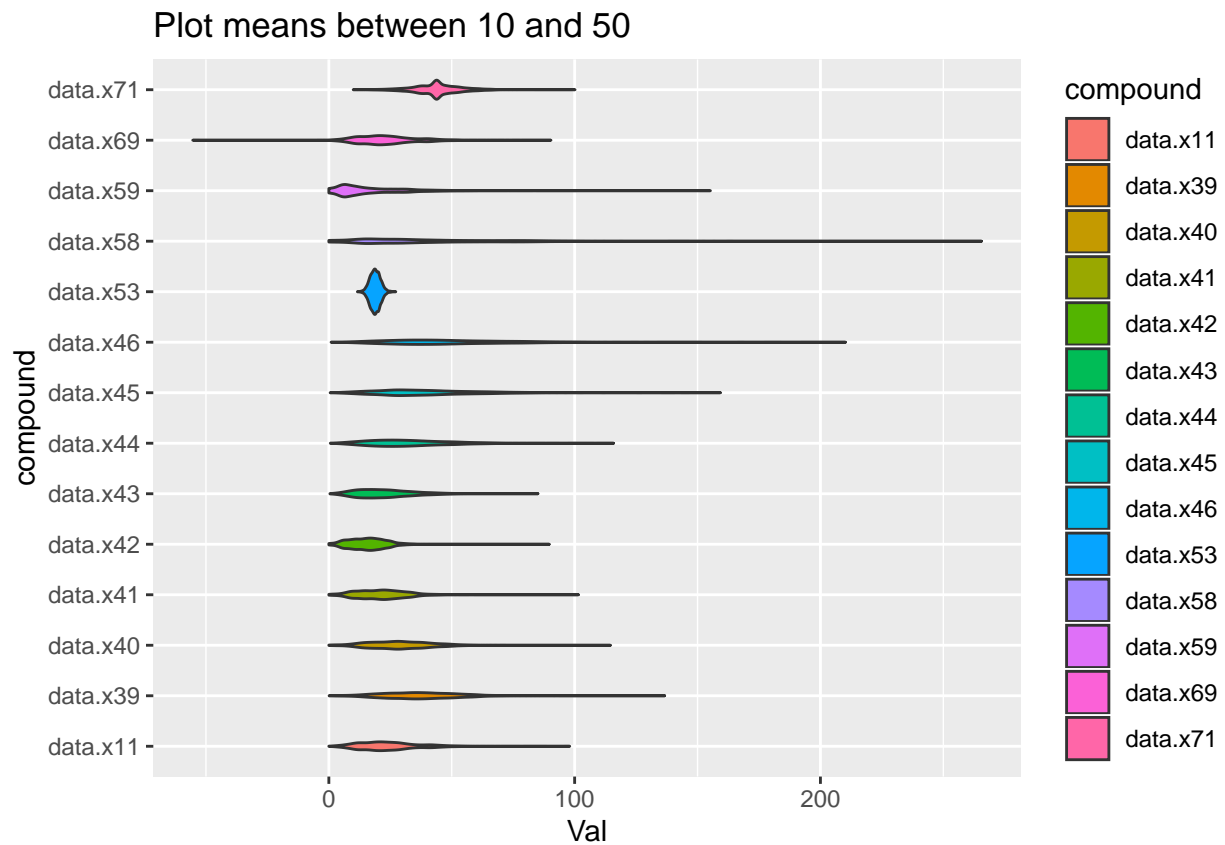
```
subset1.1 %>%
  gather(key="compound", value="Val") %>%
  ggplot( aes(x=compound, y=Val, fill=compound)) +
    geom_violin()+
    coord_flip()+
    ggtitle("Plot means lower than 2")
```



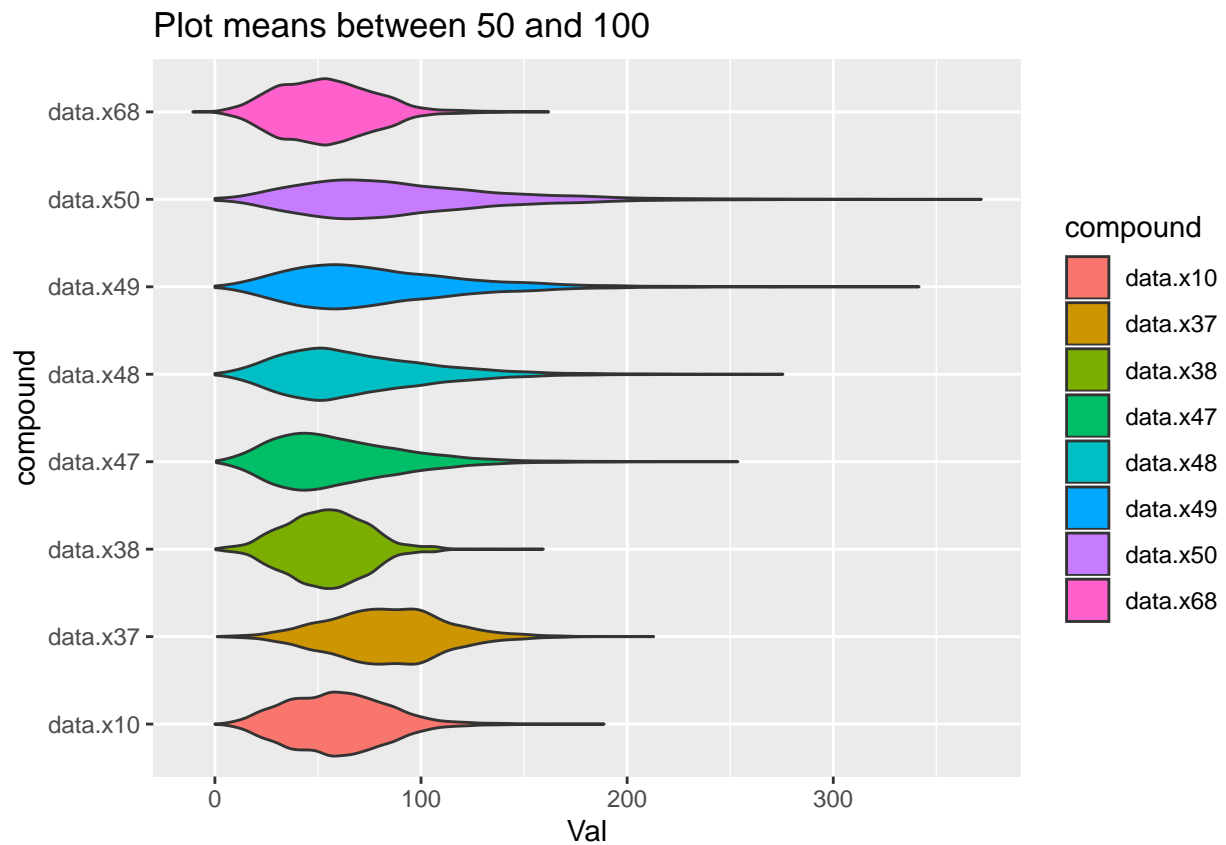
```
subset2 %>%  
  gather(key="compound", value="Val") %>%  
  ggplot( aes(x=compound, y=Val, fill=compound)) +  
    geom_violin()+  
    coord_flip()+  
    ggtitle("Plot means between 2 and 10")
```



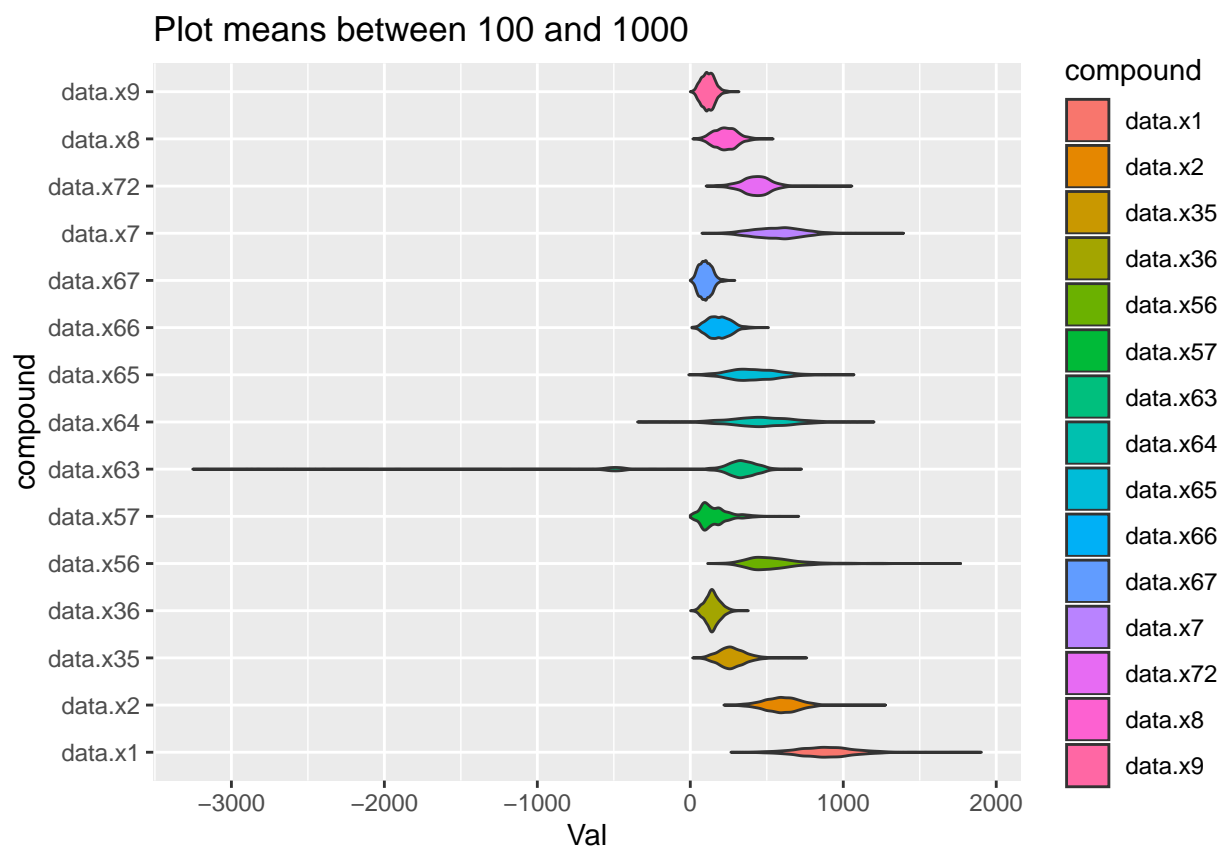
```
subset3 %>%
  gather(key="compound", value="Val") %>%
  ggplot( aes(x=compound, y=Val, fill=compound)) +
    geom_violin()+
    coord_flip()+
    ggtitle("Plot means between 10 and 50")
```

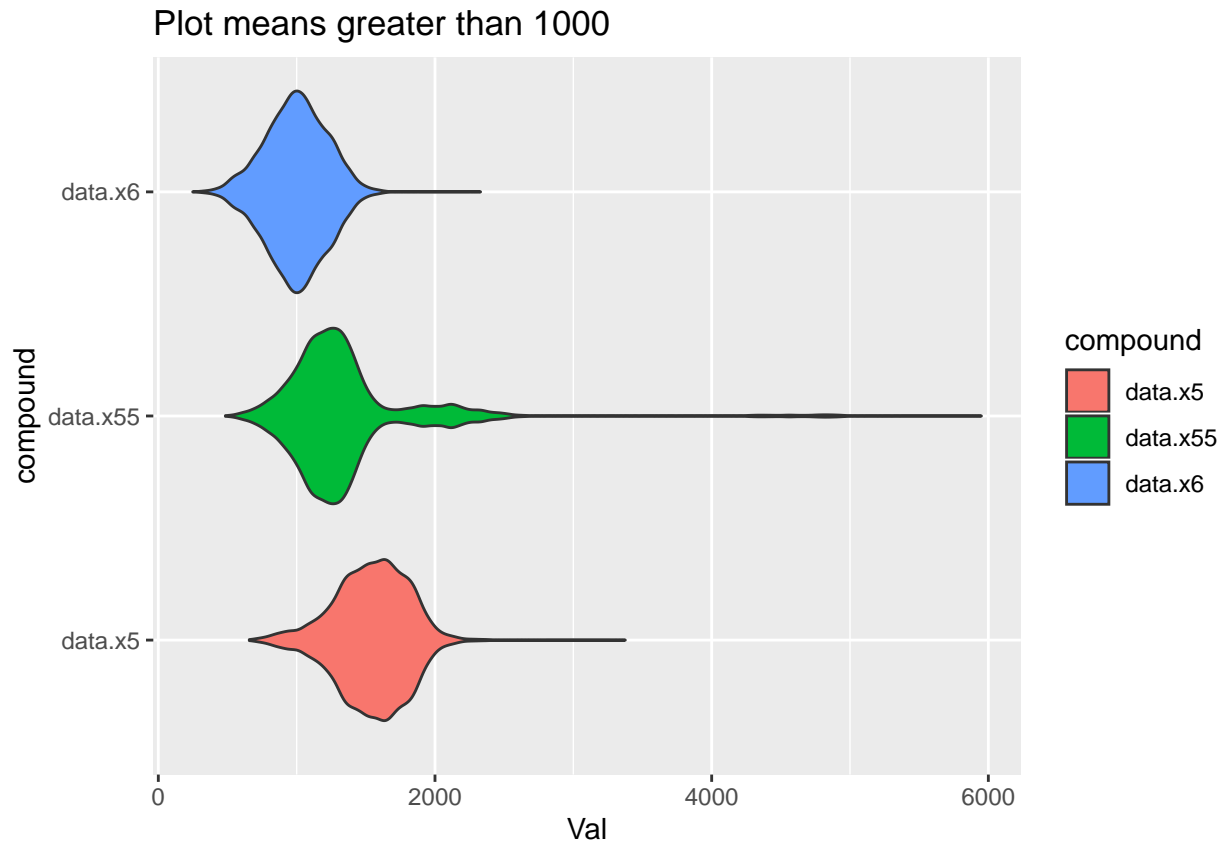
```
subset4 %>%
  gather(key="compound", value="Val") %>%
  ggplot( aes(x=compound, y=Val, fill=compound)) +
    geom_violin()+
    coord_flip()+
    ggtitle("Plot means between 50 and 100")
```



```
subset5 %>%
  gather(key="compound", value="Val") %>%
  ggplot( aes(x=compound, y=Val, fill=compound)) +
    geom_violin()+
    coord_flip()+
    ggtitle("Plot means between 100 and 1000")
```



```
subset6 %>%
  gather(key="compound", value="Val") %>%
  ggplot( aes(x=compound, y=Val, fill=compound)) +
    geom_violin()+
    coord_flip()+
    ggtitle("Plot means greater than 1000")
```



Looking at this violin plots it can be seen that a lot of the components have quite small variance. However we can see some high outliers which could be problematic. This is noted when moving on to further analysis.

A correlation table is done in order to check if there is a linear relation between the variables.

```
X <- data[, -73]
X <- scale(X)
```

```
C <- cor(X)
head(C)
```

```
##          x1          x2          x3          x4          x5          x6          x7
## x1  1.0000000  0.9922019  0.6617702  0.9132550  0.8548888  0.5157994  0.39866996
## x2  0.9922019  1.0000000  0.5686335  0.9562784  0.8789283  0.5519158  0.43840048
## x3  0.6617702  0.5686335  1.0000000  0.3229651  0.4089550  0.1306643  0.03110228
## x4  0.9132550  0.9562784  0.3229651  1.0000000  0.8826500  0.6045916  0.50541191
## x5  0.8548888  0.8789283  0.4089550  0.8826500  1.0000000  0.8586513  0.74276859
## x6  0.5157994  0.5519158  0.1306643  0.6045916  0.8586513  1.0000000  0.96017475
##          x8          x9          x10         x11         x12         x13         x14
## x1  0.37053247  0.3508783  0.3566473  0.3637045  0.3214353 -0.4874010 -0.4412800
## x2  0.39631857  0.3671058  0.3684962  0.3668381  0.3211978 -0.4959966 -0.4548166
## x3  0.07737273  0.1140231  0.1409133  0.1934261  0.1811551 -0.3076249 -0.2418498
## x4  0.43192191  0.3826158  0.3760261  0.3567108  0.3072873 -0.4949219 -0.4678345
## x5  0.61762760  0.5403826  0.5212293  0.4700830  0.3621697 -0.4756300 -0.5057987
## x6  0.82088533  0.7145723  0.6662820  0.5418295  0.3727688 -0.3217159 -0.4390745
##          x15         x16         x17         x18         x19         x20
## x1 -0.4197133 -0.4694502 -0.4998835 -0.5332395 -0.5931547 -0.5397476
## x2 -0.4387986 -0.4850215 -0.5105356 -0.5436700 -0.6023948 -0.5401801
```

```

## x3 -0.1829922 -0.2194932 -0.2595881 -0.2826530 -0.3369743 -0.3639192
## x4 -0.4658221 -0.4985059 -0.5089568 -0.5401488 -0.5942427 -0.5137649
## x5 -0.5110266 -0.4933989 -0.4697766 -0.4881575 -0.5128573 -0.4132727
## x6 -0.4954873 -0.4454225 -0.3917520 -0.3887633 -0.3432310 -0.2144998
##      x21      x22      x23      x24      x25      x26
## x1 -0.49678070 -0.4039201 -0.3237346 -0.24248698 -0.1924284 -0.13328099
## x2 -0.47403638 -0.3764538 -0.2923797 -0.22321575 -0.1811279 -0.12459983
## x3 -0.43498135 -0.4160630 -0.3947351 -0.28985380 -0.2160468 -0.16022319
## x4 -0.39236690 -0.2892218 -0.2015362 -0.16667586 -0.1455783 -0.09564338
## x5 -0.01120148  0.0705358  0.1109908  0.07521345  0.0586746  0.09325173
## x6  0.40825157  0.5423688  0.5802171  0.48708716  0.4154461  0.40732757
##      x27      x28      x29      x30      x31      x32      x33
## x1 -0.01551995  0.09940273  0.19675200  0.25112251  0.3008533  0.04373356  0.09138912
## x2 -0.01315373  0.10066136  0.20717237  0.26451246  0.3111918  0.04239189  0.08635702
## x3 -0.04147939  0.04079677  0.05430859  0.06614591  0.1159653  0.03081442  0.08641229
## x4 -0.00166872  0.10543667  0.22382082  0.28590732  0.3224404  0.03570327  0.07001654
## x5  0.14658482  0.17917834  0.25848656  0.31333691  0.3548803  0.03961313  0.08446086
## x6  0.35259032  0.26818768  0.28139613  0.32224847  0.3591088  0.04386218  0.08465656
##      x34      x35      x36      x37      x38      x39      x40
## x1  0.08896521  0.6820756  0.588985593  0.5412972  0.4387331  0.3510472  0.3527750
## x2  0.08388428  0.6545158  0.567458738  0.5330149  0.4452651  0.3653052  0.3660019
## x3  0.08159868  0.5876487  0.511231062  0.4178851  0.2814430  0.1921597  0.1988093
## x4  0.06602553  0.5503497  0.484876674  0.4822526  0.4348051  0.3774941  0.3753558
## x5  0.07562523  0.3920232  0.433586764  0.5038924  0.5154822  0.4957246  0.4869050
## x6  0.06449795 -0.1050620  0.006272814  0.1746825  0.2945501  0.3649717  0.3589584
##      x41      x42      x43      x44      x45      x46
## x1  0.3262755  0.3329922 -0.113127876 -0.075759064 -0.052079217 -0.017285553
## x2  0.3383110  0.3451567 -0.091967702 -0.055255219 -0.033390059 -0.004909783
## x3  0.1928582  0.1939332 -0.199395100 -0.174369793 -0.145792121 -0.090074135
## x4  0.3457763  0.3520189 -0.036802398 -0.003972388  0.013455127  0.025741495
## x5  0.4500299  0.4490919  0.009131573 -0.003541028  0.005375077  0.002855975
## x6  0.3366080  0.3374267  0.112826503  0.088358902  0.106307012  0.080491815
##      x47      x48      x49      x50      x51      x52
## x1  0.004612659  0.01290031  0.040463095  0.05750260 -0.12846114 -0.10529052
## x2  0.012436612  0.01863229  0.047561663  0.06365525 -0.12346116 -0.10419555
## x3 -0.058349687 -0.04449105 -0.034091551 -0.01518383 -0.15534114 -0.11855845
## x4  0.030363690  0.03080259  0.059784152  0.07348788 -0.10701945 -0.09779046
## x5 -0.012612957 -0.02070397  0.002859267  0.01161077 -0.06988990 -0.08493151
## x6  0.040425827  0.01920912  0.026639917  0.02167635  0.08409449  0.01540715
##      x53      x54      x55      x56      x57      x58
## x1  0.7088191  0.022163378  0.4054590  0.3331118  0.02361152 -0.091706155
## x2  0.7303931  0.015854938  0.4010131  0.3255883  0.01361591 -0.106121159
## x3  0.3254089  0.061837413  0.2935718  0.2590556  0.05826200 -0.004781807
## x4  0.7368525 -0.001592405  0.3633431  0.2863657 -0.01229390 -0.134420485
## x5  0.6599917 -0.030763847  0.4483741  0.4891974  0.19720934  0.031590740
## x6  0.4096258 -0.143687954  0.3615647  0.5053489  0.34541697  0.196832038
##      x59      x60      x61      x62      x63      x64
## x1 -0.098068220 -0.07000824  0.022004579 -0.005932764  0.008117355  0.26195724
## x2 -0.112731072 -0.08542620  0.008192976 -0.007850912  0.026062013  0.30795156
## x3 -0.008472751  0.01504489  0.073769032  0.006262774 -0.107475937 -0.09021364
## x4 -0.141075427 -0.11728239 -0.026746464 -0.014402946  0.070183183  0.40035722
## x5  0.012165637  0.02778423  0.069042310  0.035211567  0.038459279  0.49464514
## x6  0.181469488  0.19220134  0.141332366  0.061730205  0.059218953  0.63378100
##      x65      x66      x67      x68      x69      x70      x71

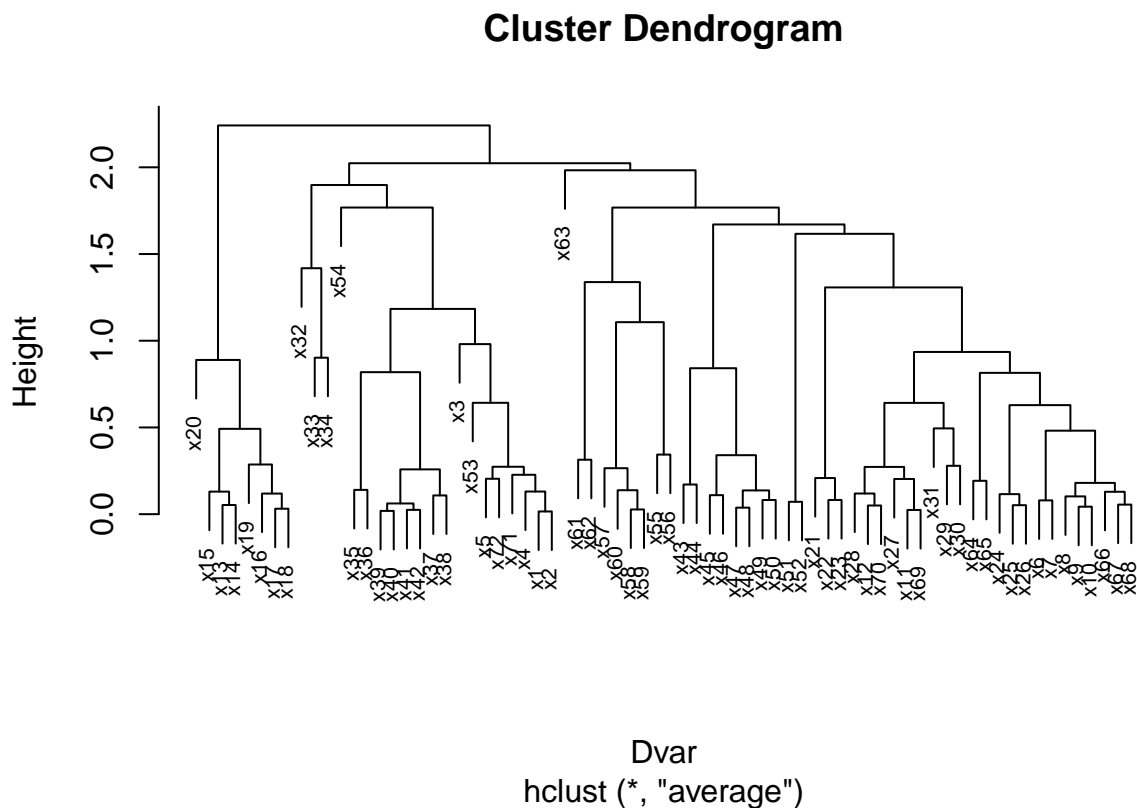
```

```
## x1 0.398177970 0.42471230 0.4003946 0.3869621 0.3663280 0.3217195 0.9284626
## x2 0.445344790 0.45797004 0.4225859 0.4030531 0.3716906 0.3219106 0.9122037
## x3 -0.003135893 0.08206638 0.1216271 0.1423389 0.1850402 0.1791729 0.6795407
## x4 0.530384895 0.50775816 0.4489942 0.4187291 0.3668999 0.3095062 0.8187867
## x5 0.648976376 0.62295240 0.5574405 0.5333876 0.4670753 0.3531464 0.7866585
## x6 0.784080981 0.75661837 0.6771354 0.6431088 0.5286311 0.3577971 0.4749514
##      x72
## x1 0.9068178
## x2 0.9010083
## x3 0.6009858
## x4 0.8355009
## x5 0.8979010
## x6 0.6817726
```

We have some variables that are linearly correlated. For example x1 and x2 have a correlation of NA.

Next a Cluster Dendrogram is produced in order to check graphically the distances between the variables. It clusters the variables with respect to their column mean.

```
Dvar<-as.dist(2*(1-C)) # as.dist is a generic function. Its default method handles objects inheriting
clusterVar<-hclust(Dvar,method= "average")
plot(clusterVar,labels=colnames(X),cex=0.65)
```



In this dendrogram it can be seen that there are a lot of clusters meaning a lot of the variables are close to each other with respect to the correlation mean distance. So it's saying, as we commented before that there is a lot of variables that are closely correlated.

As we have a lot of variables PCA analysis is performed in order to check the which variables explain much of the variability of the data.

```
pca <- princomp(X)
summary(pca)
```

```
## Importance of components:
##
##      Comp.1      Comp.2      Comp.3      Comp.4      Comp.5
## Standard deviation  4.2765825 3.8201475 2.61795519 2.36376354 2.17066070
## Proportion of Variance 0.2540612 0.2027239 0.09520704 0.07761626 0.06545284
## Cumulative Proportion 0.2540612 0.4567851 0.55199212 0.62960837 0.69506122
##
##      Comp.6      Comp.7      Comp.8      Comp.9      Comp.10
## Standard deviation  2.04486950 1.4696980 1.3852587 1.29838683 1.28371474
## Proportion of Variance 0.05808658 0.0300055 0.0266567 0.02341816 0.02289189
## Cumulative Proportion 0.75314780 0.7831533 0.8098100 0.83322816 0.85612006
##
##      Comp.11      Comp.12      Comp.13      Comp.14      Comp.15
## Standard deviation  1.23466275 1.09170557 1.0285509 0.92836109 0.91026746
## Proportion of Variance 0.02117587 0.01655601 0.0146959 0.01197232 0.01151019
## Cumulative Proportion 0.87729593 0.89385194 0.9085478 0.92052017 0.93203036
##
##      Comp.16      Comp.17      Comp.18      Comp.19
## Standard deviation  0.88929080 0.725888210 0.699707547 0.642445464
## Proportion of Variance 0.01098581 0.007319546 0.006801078 0.005733465
## Cumulative Proportion 0.94301617 0.950335719 0.957136797 0.962870262
##
##      Comp.20      Comp.21      Comp.22      Comp.23
## Standard deviation  0.610738144 0.603206698 0.516239961 0.483958538
## Proportion of Variance 0.005181491 0.005054485 0.003702098 0.003253576
## Cumulative Proportion 0.968051753 0.973106238 0.976808336 0.980061912
##
##      Comp.24      Comp.25      Comp.26      Comp.27
## Standard deviation  0.435023558 0.406718003 0.3561279 0.345128596
## Proportion of Variance 0.002628877 0.002297902 0.0017618 0.001654651
## Cumulative Proportion 0.982690789 0.984988690 0.9867505 0.988405142
##
##      Comp.28      Comp.29      Comp.30      Comp.31
## Standard deviation  0.318381534 0.296303303 0.26995339 0.2587110170
## Proportion of Variance 0.001408122 0.001219601 0.00101233 0.0009297678
## Cumulative Proportion 0.989813264 0.991032865 0.99204519 0.9929749626
##
##      Comp.32      Comp.33      Comp.34      Comp.35
## Standard deviation  0.2415662321 0.2287125425 0.2213461521 0.19680264
## Proportion of Variance 0.0008106196 0.0007266489 0.0006805947 0.00053803
## Cumulative Proportion 0.9937855822 0.9945122311 0.9951928258 0.99573086
##
##      Comp.36      Comp.37      Comp.38      Comp.39
## Standard deviation  0.1924752313 0.1728686108 0.163466497 0.1564707226
## Proportion of Variance 0.0005146291 0.0004151231 0.000371195 0.0003401033
## Cumulative Proportion 0.9962454849 0.9966606080 0.997031803 0.9973719063
##
##      Comp.40      Comp.41      Comp.42      Comp.43
## Standard deviation  0.1551350603 0.1470969135 0.1430641473 0.1249421784
## Proportion of Variance 0.0003343217 0.0003005742 0.0002843192 0.0002168517
## Cumulative Proportion 0.9977062280 0.9980068022 0.9982911215 0.9985079732
##
##      Comp.44      Comp.45      Comp.46      Comp.47
## Standard deviation  0.1192421416 0.1136811903 0.1019380236 0.0988889400
## Proportion of Variance 0.0001975169 0.0001795237 0.0001443501 0.0001358439
## Cumulative Proportion 0.9987054900 0.9988850138 0.9990293638 0.9991652077
##
##      Comp.48      Comp.49      Comp.50      Comp.51
## Standard deviation  0.0913520744 0.0884807831 0.0849282758 8.036697e-02
## Proportion of Variance 0.0001159262 0.0001087533 0.0001001957 8.972218e-05
## Cumulative Proportion 0.9992811339 0.9993898872 0.9994900830 9.995798e-01
##
##      Comp.52      Comp.53      Comp.54      Comp.55
## Standard deviation  7.670105e-02 7.404935e-02 6.740711e-02 6.365644e-02
```

```
## Proportion of Variance 8.172356e-05 7.617055e-05 6.311842e-05 5.628975e-05
## Cumulative Proportion 9.996615e-01 9.997377e-01 9.998008e-01 9.998571e-01
##                               Comp.56      Comp.57      Comp.58      Comp.59
## Standard deviation      5.988363e-02 4.475628e-02 4.326690e-02 3.956368e-02
## Proportion of Variance 4.981509e-05 2.782612e-05 2.600496e-05 2.174393e-05
## Cumulative Proportion 9.999069e-01 9.999347e-01 9.999608e-01 9.999825e-01
##                               Comp.60      Comp.61      Comp.62      Comp.63
## Standard deviation      2.580847e-02 1.602058e-02 1.168558e-02 1.086949e-02
## Proportion of Variance 9.252713e-06 3.565341e-06 1.896903e-06 1.641205e-06
## Cumulative Proportion 9.999918e-01 9.999953e-01 9.999972e-01 9.999989e-01
##                               Comp.64      Comp.65      Comp.66 Comp.67 Comp.68
## Standard deviation      9.084114e-03 4.675022e-08 3.102016e-08      0      0
## Proportion of Variance 1.146330e-06 3.036072e-17 1.336696e-17      0      0
## Cumulative Proportion 1.000000e+00 1.000000e+00 1.000000e+00      1      1
##                               Comp.69 Comp.70 Comp.71 Comp.72
## Standard deviation      0      0      0      0
## Proportion of Variance      0      0      0      0
## Cumulative Proportion      1      1      1      1
```

Looking to the principal components one can see that 17 components are needed in order to explain the 95% of the data variation.

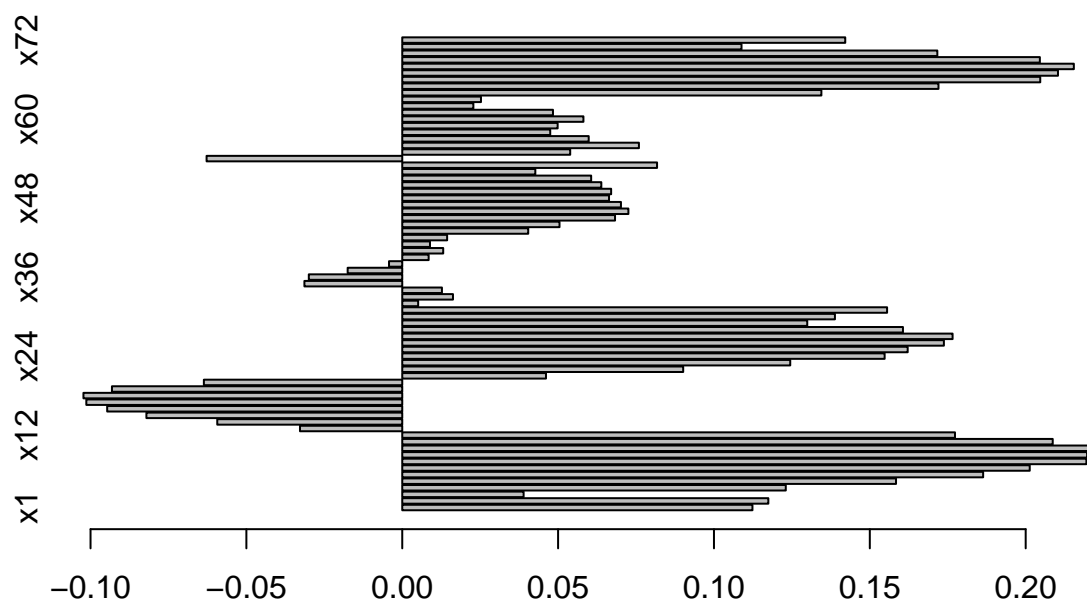
The next step is to check the importance that each variable has in each of the 17th principal components which we consider significant.

```
l <- data.frame(pca$loadings[,1:17])
head(l)
```

```
##           Comp.1      Comp.2      Comp.3      Comp.4      Comp.5      Comp.6
## x1 0.11234649 0.19199901 0.119100563 0.090254064 0.002409457 0.03854674
## x2 0.11744560 0.19155408 0.114877746 0.077021320 -0.003949036 0.02017171
## x3 0.03893855 0.13330638 0.092953342 0.127367942 0.038217303 0.11488100
## x4 0.12303975 0.17952297 0.098858603 0.040173983 -0.019053747 -0.02201165
## x5 0.15840681 0.16232073 -0.008475662 0.062796554 0.002610569 -0.07775550
## x6 0.18635406 0.06927434 -0.121906994 0.009531728 -0.040445182 -0.12250458
##           Comp.7      Comp.8      Comp.9      Comp.10      Comp.11      Comp.12
## x1 0.0799879285 0.136441085 0.03387566 0.023998931 0.08782882 0.006751505
## x2 0.0631368031 0.147832556 0.03114743 0.035611194 0.09003051 -0.024520631
## x3 0.1317884804 0.008044929 0.01837754 -0.072087509 0.02471100 0.187158157
## x4 0.0139682347 0.163066990 0.02441388 0.057984524 0.08283012 -0.097545867
## x5 -0.0005471538 0.194991159 0.05373537 0.020375652 0.04721878 -0.038316382
## x6 -0.0263493959 0.206543316 0.02617906 0.002537998 0.03023852 -0.043768161
##           Comp.13      Comp.14      Comp.15      Comp.16      Comp.17
## x1 0.007703451 0.02072805 1.012833e-02 0.026647670 0.07246095
## x2 0.002068803 0.02363510 4.046959e-05 -0.057899578 0.04172298
## x3 0.035755218 -0.01189155 6.349231e-02 0.546938191 0.22467173
## x4 -0.012076600 0.02588064 -2.206488e-02 -0.242715135 -0.03588205
## x5 0.093104799 -0.03530430 -1.567965e-02 -0.009450296 -0.07807828
## x6 0.121889939 -0.04036149 -1.993386e-02 0.011038690 -0.07530793
```

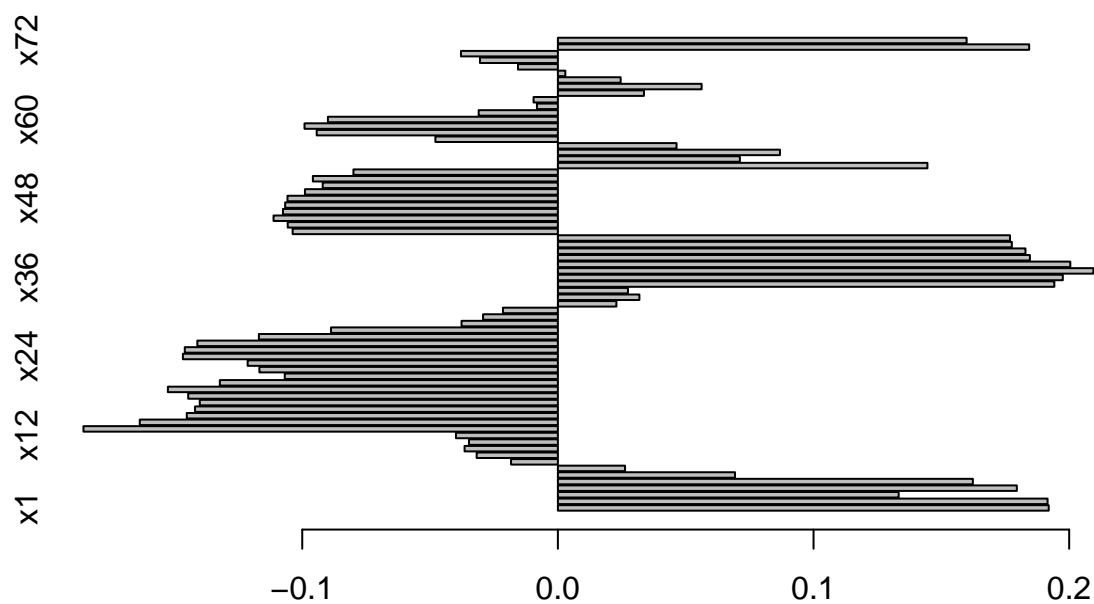
```
names <- row.names(l)
barplot(l[,1], names.arg = rownames(l), horiz = T)
title("1st Principal Component")
```


1st Principal Component



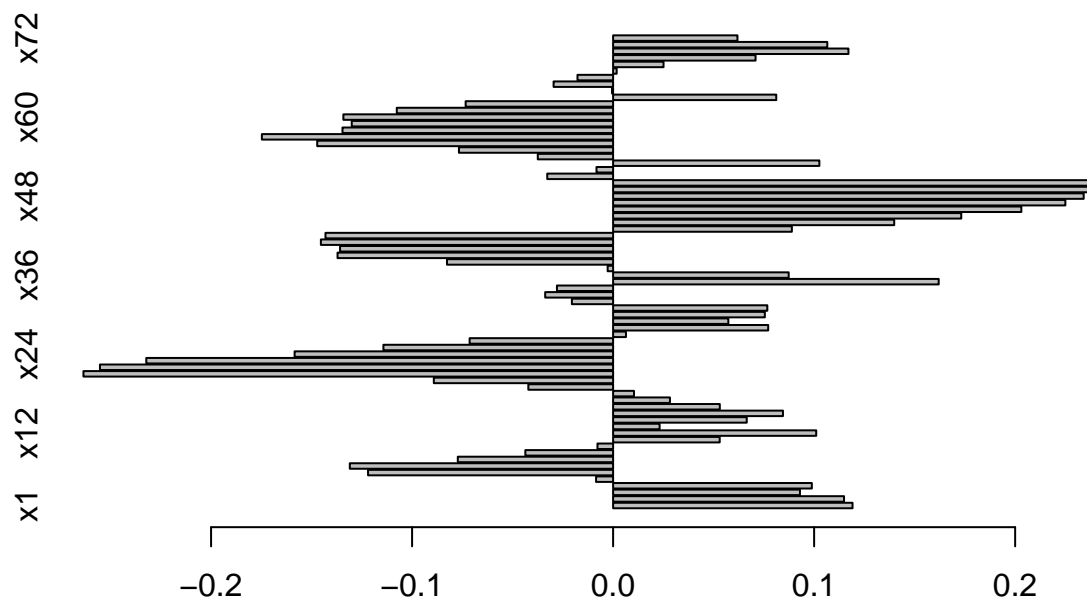
```
barplot(l[,2], names.arg = rownames(l), horiz = T)
title("2nd Principal Component")
```

2nd Principal Component



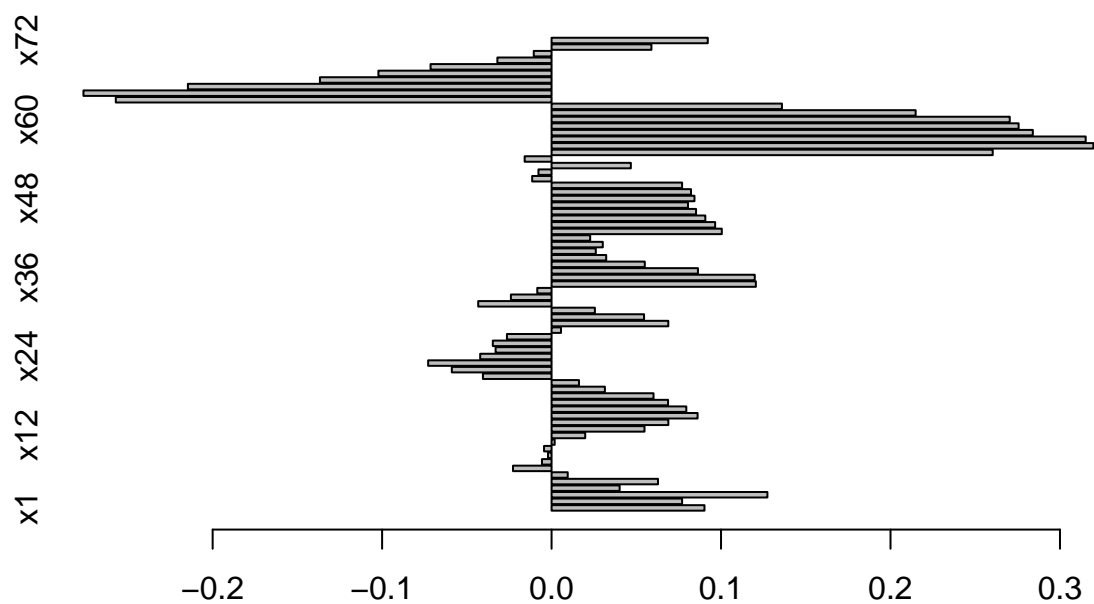
```
barplot(l[,3], names.arg = rownames(l), horiz = T)
title("3rd Principal Component")
```

3rd Principal Component



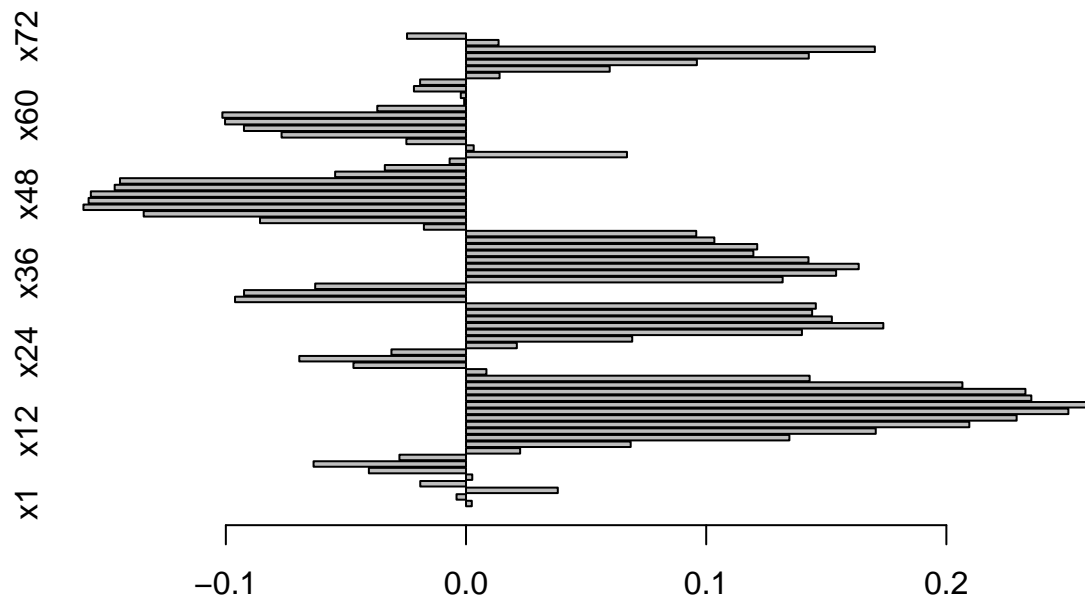
```
barplot(l[,4], names.arg = rownames(l), horiz = T)
title("4th Principal Component")
```

4th Principal Component



```
barplot(l[,5], names.arg = rownames(l), horiz = T)
title("5th Principal Component")
```

5th Principal Component

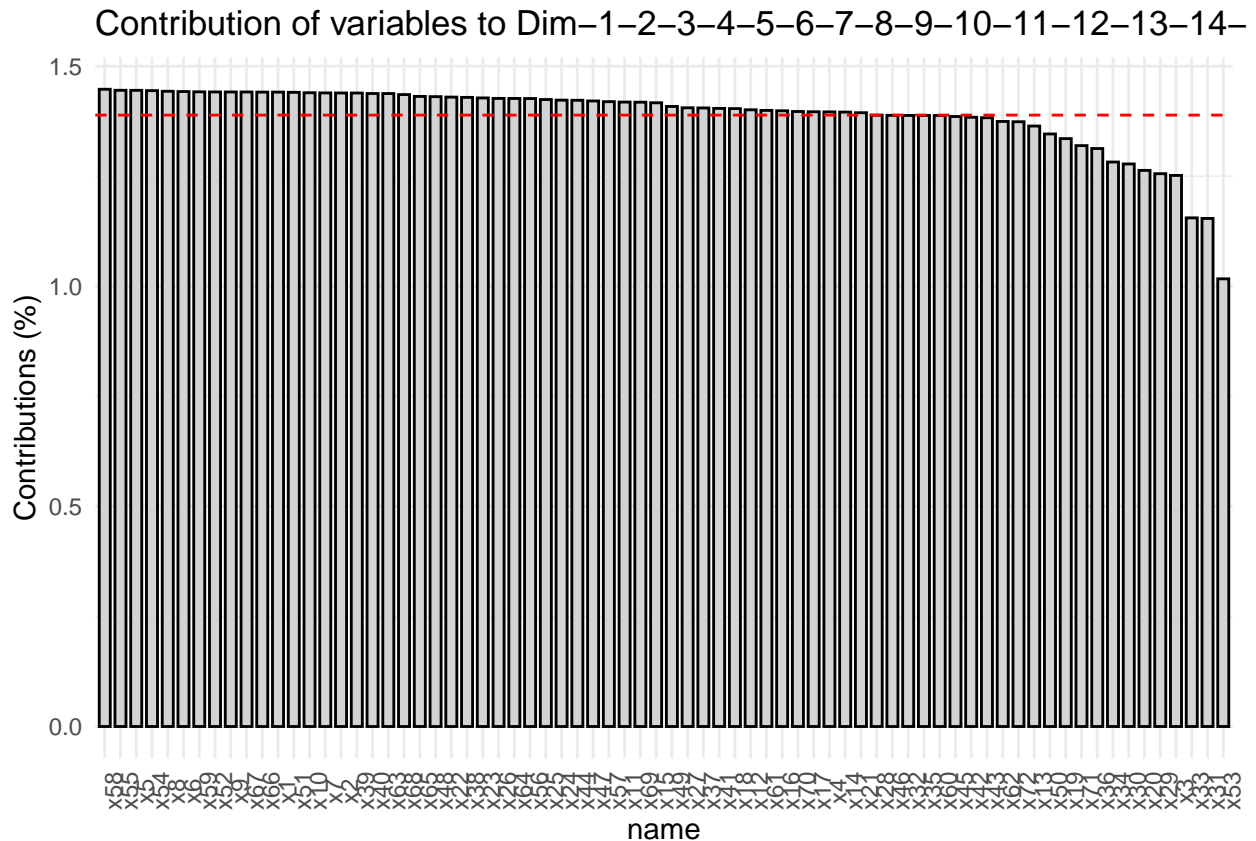


In this plots it can be seen that there is a lot of variables that contribute in each of the principal components. To know which are the most important variables and if there is any variable that can be removed from the dataset I am going to do a contribution plot in order to check if there is any variable that is not significantly contributing to any of the 17PC which explain the 95% of the variance.

```
library(factoextra)
```

```
## Welcome! Want to learn more? See two factoextra-related books at https://goo.gl/ve3WBa
```

```
contrib <- fviz_contrib(pca, choice="var", axes = 1:17,
  fill = "lightgray", color = "black") +
  theme_minimal() +
  theme(axis.text.x = element_text(angle=90))
contrib
```



```
contrib.data <- contrib$data[with(contrib$data, order(contrib)), ]
nsign <- contrib.data[1:13,]
nsign <- c(nsign$name)
```

We can see that there are 13 variables (53, 31, 33, 3, 29, 20, 30, 34, 36, 71, 19, 50, 13) with a non significant contribution to the principal components that explain the 95% of the variance of our dataset. This are the variables that following the PCA analysis can be removed. As it's seen there are a lot of variables whom one could consider removing from the original data however we decide to keep them and use this analysis to compare with the variables that are deemed unimportant when we do the pruned tree and the random forest analysis.

2 Splitting data

```
data$y=as.factor(data$y)

set.seed(params$seed)
pt <- params$partition

inTrain <- createDataPartition(y=data$y, p=pt, list=FALSE)
str(inTrain)

## int [1:2816, 1] 2 6 11 13 15 16 19 21 22 23 ...
## - attr(*, "dimnames")=List of 2
## ..$ : NULL
## ..$ : chr "Resample1"
```

```
training <- data[-inTrain,]
testing <- data[inTrain,]
nrow(training)
```

```
## [1] 2815
```

3 Pruned single tree:

```
tree.data <- tree(y~., data, subset= inTrain, split="deviance")
summary(tree.data)
```

```
##
## Classification tree:
## tree(formula = y ~ ., data = data, subset = inTrain, split = "deviance")
## Variables actually used in tree construction:
## [1] "x38" "x37" "x65" "x12" "x40"
## Number of terminal nodes: 6
## Residual mean deviance: 1.099 = 3089 / 2810
## Misclassification error rate: 0.2923 = 823 / 2816
```

```
set.seed(params$seed)
```

```
cv.data=cv.tree(tree.data)
```

```
names(cv.data)
```

```
## [1] "size" "dev" "k" "method"
```

```
cv.data
```

```
## $size
```

```
## [1] 6 5 4 3 2 1
```

```
##
```

```
## $dev
```

```
## [1] 3150.043 3176.539 3246.135 3253.552 3353.560 3740.975
```

```
##
```

```
## $k
```

```
## [1] -Inf 39.60449 49.90155 54.89454 117.21261 388.48898
```

```
##
```

```
## $method
```

```
## [1] "deviance"
```

```
##
```

```
## attr("class")
```

```
## [1] "prune" "tree.sequence"
```

One can see there is an increase in deviance as the number of nodes get smaller. Since it does not have that much sense to choose the actual minimum since this would not prune the tree at all we chose $n = 4$.

```
prune.data=prune.tree(tree.data,best=4)
```

```
summary(prune.data)
```

```
##
```

```
## Classification tree:
```

```
## snip.tree(tree = tree.data, nodes = 5:4)
```

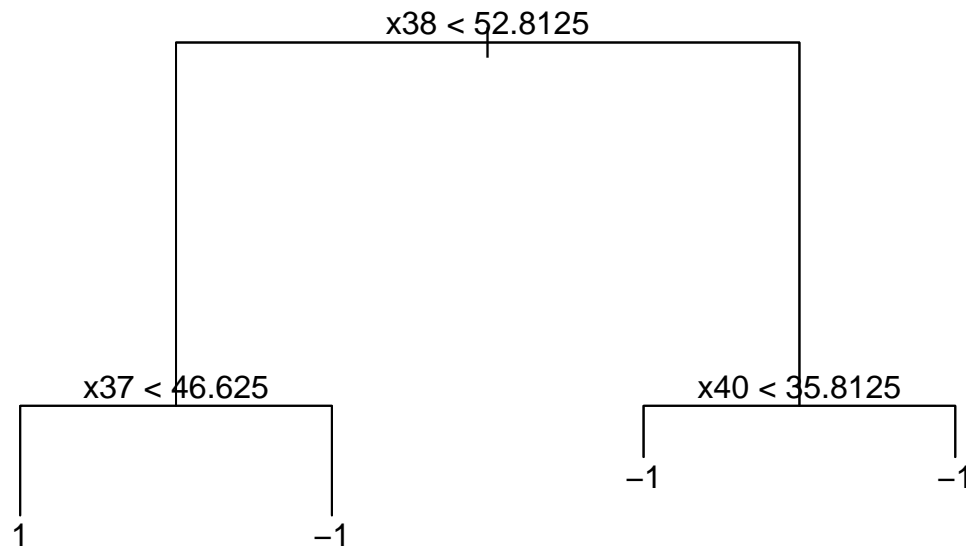
```
## Variables actually used in tree construction:
```

```
## [1] "x38" "x37" "x40"
```

```
## Number of terminal nodes: 4
```

```
## Residual mean deviance: 1.13 = 3178 / 2812
## Misclassification error rate: 0.3132 = 882 / 2816
```

```
plot(prune.data)
text(prune.data,pretty=0)
```



Make predictions on the test set to evaluate the classifier.

```
yhat_1=predict(prune.data,newdata=testing, type = "class")
res <- table(yhat_1,testing$y)
res
```

```
##
## yhat_1   -1    1
##        -1 1703  838
##         1   44  231
```

```
accrcy <- sum(diag(res)/sum(res))
```

The accuracy that we obtain in this model is 0.6867898.

Random forrest:

In the random forrest model one needs to decide how many variables *mtry* are assesed in each node and how many trees *ntree* are used in the forrest. Caret only has tuning for the number of parameters assesed in each node and this tuningprocess is quite slow. Therefor the decition is made to take a gready approch towards tuning these parameters. First we use tuning by caret to tune the number of variables. Then the optimum is chosen and used when tuning the number of trees. The order is decided this way since the number of parameters assesed in each node is said to hava a bigger inpack on the result than the number of trees.

A tunegrid is created with 15 values from 1:15 for *mtry* to tun the model. Our train function will change number of entry variable at each split according to the tunegrid. The default numebr of trees is 500.

```
#Very slow
library(randomForest)
```

```
## randomForest 4.6-14
```

```
## Type rfNews() to see new features/changes/bug fixes.
```

```
##
## Attaching package: 'randomForest'

## The following object is masked from 'package:ggplot2':
##
##      margin

## The following object is masked from 'package:dplyr':
##
##      combine

library(mlbench)
library(caret)
library(e1071)

control <- trainControl(method='repeatedcv',
                        number=10,
                        repeats=3,
                        search='grid')

tuneGrid <- expand.grid(.mtry = (1:15))

rf_gridsearch <- train(y ~ .,
                      data = training,
                      method = 'rf',
                      metric = 'Accuracy',
                      tuneGrid = tuneGrid,
                      trControl=control)

print(rf_gridsearch)

## Random Forest
##
## 2815 samples
## 72 predictor
## 2 classes: '-1', '1'
##
## No pre-processing
## Resampling: Cross-Validated (10 fold, repeated 3 times)
## Summary of sample sizes: 2533, 2534, 2533, 2534, 2533, 2533, ...
## Resampling results across tuning parameters:
##
##  mtry  Accuracy  Kappa
##  1     0.7806923 0.5099224
##  2     0.7848357 0.5232310
##  3     0.7848303 0.5246080
##  4     0.7849514 0.5253865
##  5     0.7867316 0.5301324
##  6     0.7838863 0.5242217
##  7     0.7840045 0.5244932
##  8     0.7830610 0.5230448
##  9     0.7860190 0.5298642
## 10     0.7844773 0.5263509
## 11     0.7823467 0.5223274
## 12     0.7856636 0.5294921
## 13     0.7869731 0.5324345
## 14     0.7824687 0.5231927
```

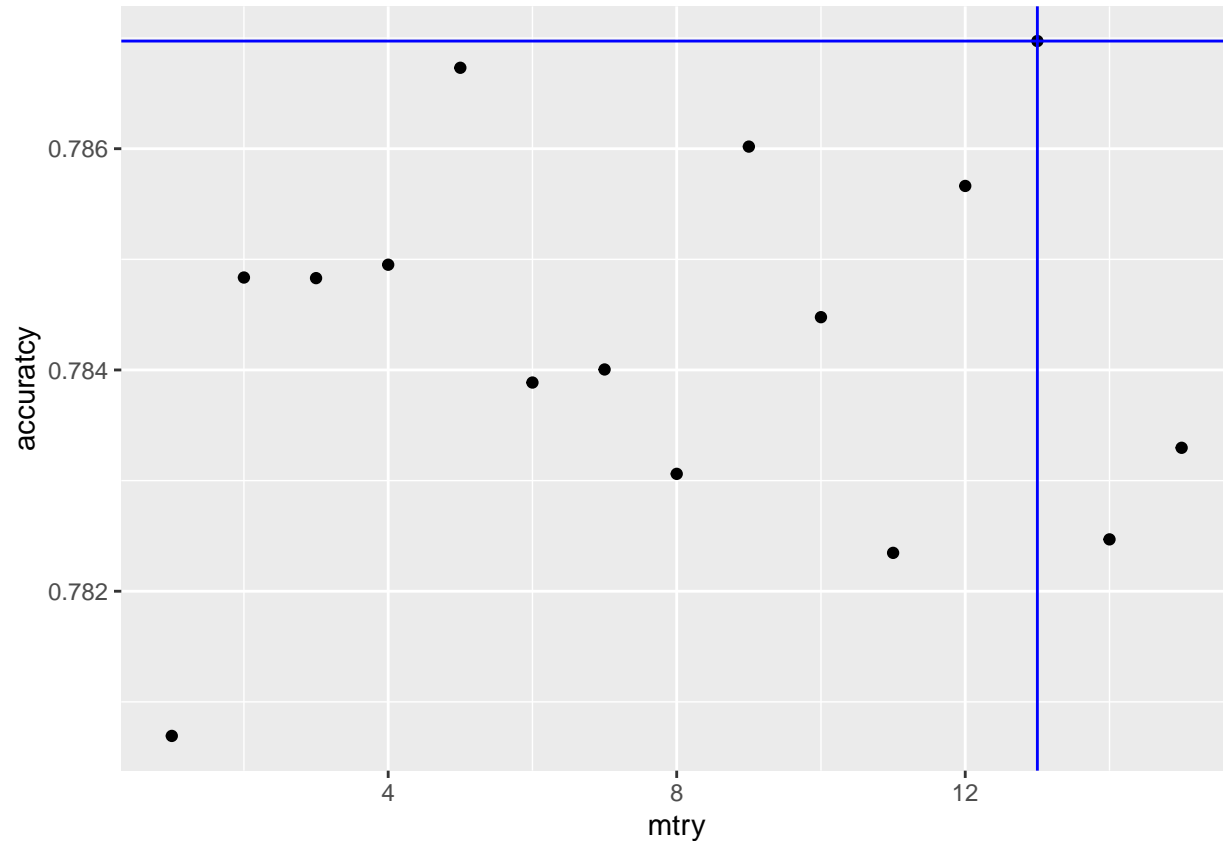
```
## 15 0.7832966 0.5249542
```

```
##
```

```
## Accuracy was used to select the optimal model using the largest value.
```

```
## The final value used for the model was mtry = 13.
```

```
ggplot(data = tibble(mtry= rf_gridsearch$results$mtry, accuracy = rf_gridsearch$results$Accuracy), aes
```



Eventually the optimum value for *mtry* is chosen automatically by the algorithm.

A loop is made to tune for *ntree* with the optimum value for *mtry*. This is also a rather slow process hence the decision is made to only check for number of trees that are multiples of 50.

```
mtry.opt <- which.max(rf_gridsearch$results$Accuracy)
```

```
accuracy.list <- rep(0, 20)
```

```
control <- trainControl(method='repeatedcv',  
                        number=10,  
                        repeats=3)
```

```
for (i in 1:20){  
  model <- train(y ~ .,  
                data = training,  
                method = 'rf',  
                metric = 'Accuracy',  
                tuneGrid = data.frame(mtry = mtry.opt),  
                ntree = i*50,  
                trControl=control)  
  yhat <- predict(model, newdata = testing, type = "raw")  
  res <- table(yhat,testing$y)
```



```

accuracy.list[i] <- sum(diag(res)/sum(res))
#print(sum(diag(res)/sum(res)))
}

```

As one can see with the exception of $n_{tree}=50$ there is very little difference in the performance of each iteration. This supports the assumption that *mtry* has a greater impact on the result.

```
x = seq(1,20)
```

```

ntree.opt = which.max(accuracy.list)
ntree.opt

```

```
## [1] 16
```

```
length(x)
```

```
## [1] 20
```

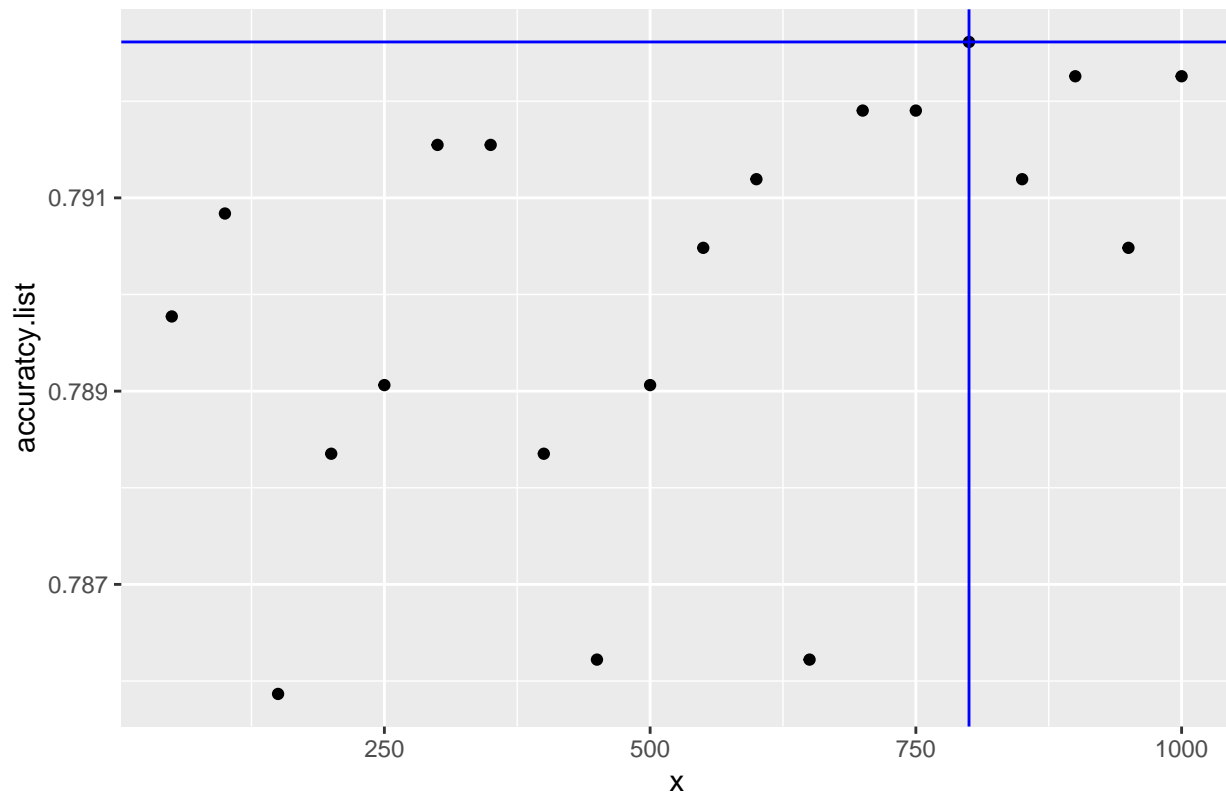
```
length(accuracy.list)
```

```
## [1] 20
```

```
ntree <- which.max(accuracy.list)*50
```

```
ggplot(data = tibble(x = seq(1, 20)*50, accuracy.list), aes(x, accuracy.list)) + geom_point() + geom_vline(xintercept = ntree)
```

Accuracy as a function of number of trees



There is not a very big difference in accuracy related to the choice of *n*.

```

control <- trainControl(method='repeatedcv',
                        number=10,

```

```

repeats=3)

rf_final <- train(y ~ .,
  data = training,
  method = 'rf',
  metric = 'Accuracy',
  ntree = ntree.opt,
  tuneGrid = data.frame(mtry = mtry.opt),
  trControl=control)

```

Make predictions with the final model and get accuracy statistics

```

yhat_final <- predict(rf_final, newdata = testing, type = "raw")
res <- table(yhat_final,testing$y)
res

```

```

##
## yhat_final  -1    1
##           -1 1531  409
##           1   216  660

```

```

accrcy_rf <- sum(diag(res)/sum(res))

```

Now the accuracy obtained is 0.778054. This is much higher thtn with the single tree from earlier.

Use varImp to get the variable importance, the 10 most important are shown.

```

varImp(rf_final)

## rf variable importance
##
##   only 20 most important variables shown (out of 72)
##
## Overall
## x38 100.00
## x40  97.54
## x37  80.62
## x41  64.60
## x72  48.90
## x42  42.14
## x59  42.09
## x64  40.57
## x71  37.88
## x36  36.72
## x39  34.70
## x57  33.17
## x58  32.75
## x21  30.41
## x50  30.04
## x63  30.03
## x47  29.36
## x65  28.64
## x51  28.51
## x19  28.34

```

Variables originally deamed less important by PCA analytics:

```
nsgn
```

```
## [1] 53 31 33 3 29 20 30 34 36 71 19 50 13
```

As one can see there are three variables x_{36} , x_{20} and x_{53} which are not important in the PCA analysis but when we do the random forest they are important.

5 Comparison of models:

The pruned tree had an accuracy of 0.6867898 while the random forest has an accuracy of 0.778054. The random forest performs significantly better.

6 Gradient Boosting

We are using gbm function: Generalized Boosted Regression Modeling To run gradient boosting algorithm we use a GLM function.

Concerning the use of the function :

- n.trees is equivalent to the number of iterations and the number of basis functions in the additive expansion.
- we use stumps to study iteration influence. This is obtained by choosing interaction.depth equal to 1.

Moreover, it is important to replace binary variables (due to the fact that we are working on a classification) $\{-1,1\}$ by $\{0,1\}$ from our training data set at the beginning to use this function and to fit the model.

```
library("ISLR")
library("gbm")
```

```
## Loaded gbm 2.1.5
```

```
library("pROC")
```

```
## Type 'citation("pROC")' for a citation.
```

```
##
```

```
## Attaching package: 'pROC'
```

```
## The following objects are masked from 'package:stats':
```

```
##
```

```
## cov, smooth, var
```

```
library(tidyr)
library(ggplot2)
library(dplyr)
```

```
set.seed(2)
```

```
#Replace binary variables by {0,1}
```

```
training$y <- ifelse(training$y== -1,0,1)
```

```
#Fitting the model & prediction
```

```
boost.compounds=gbm(y~.,data=training,distribution="adaboost",n.trees=2000,interaction.depth=1)
```

```
#Evaluating the error for testing data set
```

```
yhat_gbm_2000 =predict(boost.compounds,newdata=testing,n.trees=2000, type = "response")
```

```
yhat_gbm_2000 <- ifelse(yhat_gbm_2000 < 0.5,0,1)
res <- table(yhat_gbm_2000,testing$y)
accrcy_gbm_test_2000 <- sum(diag(res)/sum(res))
accrcy_gbm_test_2000
```

```
## [1] 0.7574574
```

```
#Evaluating the error for training data set
```

```
yhat_gbm_train_2000 =predict(boost.compounds,newdata=training,n.trees=2000, type = "response")
yhat_gbm_train_2000 <- ifelse(yhat_gbm_train_2000 < 0.5,0,1)
res <- table(yhat_gbm_train_2000,training$y)
accrcy_gbm_train_2000 <- sum(diag(res)/sum(res))
accrcy_gbm_train_2000
```

```
## [1] 0.8650089
```

As we can see, the accuracy rate is really higher on training data (0.7574574) set than on testing data set (0.8650089), which is expected due to the fact that the model is fitted on the training data set.

We should retain the missclassification rate of testing data set. We can notice that the model for 2000 iterations with stumps as trees is more efficient than a pruned single tree model but less efficient that with a forest trees model.

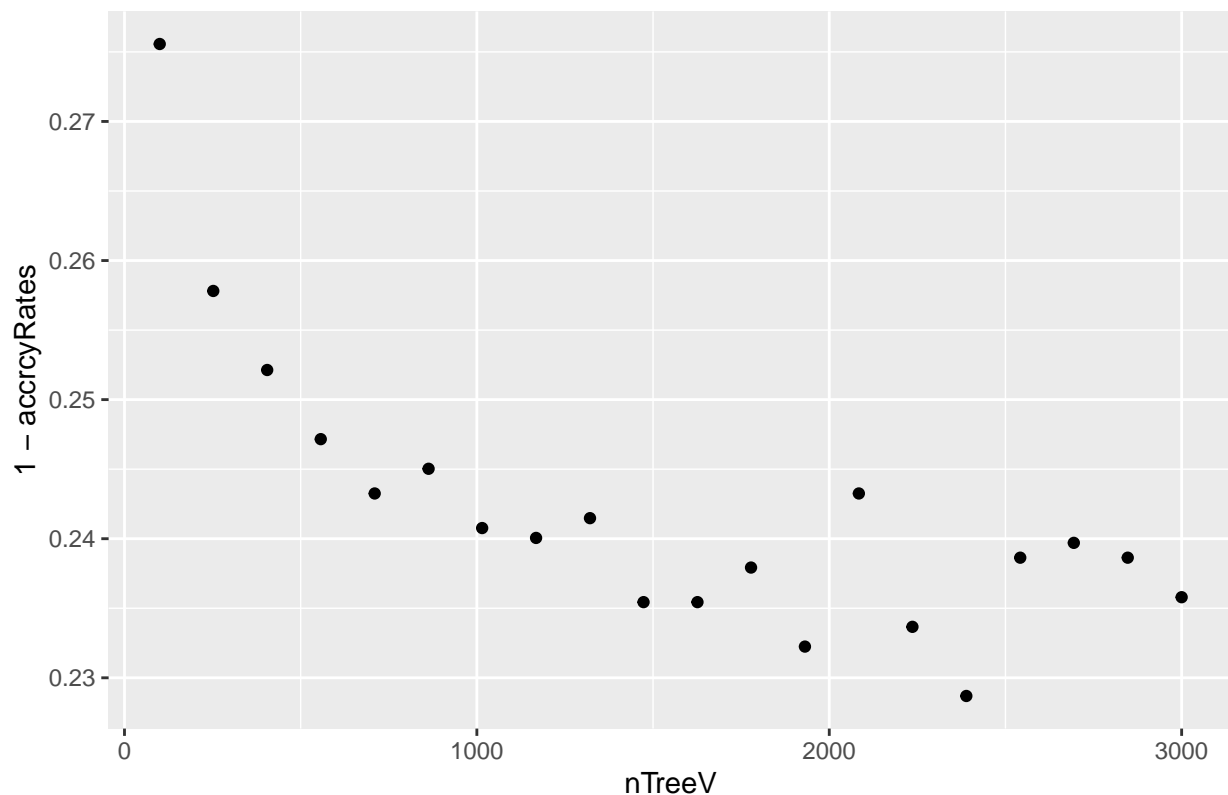
Then we can put forward the influence of the number of iterations (ie. the number of trees) on the missclassification on the testing data set:

```
sampling = 20
accrcyRates <- rep(0,sampling)
firstValue = 100
lastValue = 3000
nTreeV = floor(seq(from = firstValue, to = lastValue, by = (lastValue - firstValue)/(sampling-1)))

for (i in 1:sampling) {
  boost.compounds=gbm(y~.,data=training,distribution="adaboost",n.trees=nTreeV[i],interaction.depth=1)
  yhat_gbm =predict(boost.compounds,newdata=testing,n.trees=nTreeV[i], type = "response")
  yhat_gbm <- ifelse(yhat_gbm < 0.5,0,1)
  res <- table(yhat_gbm,testing$y)
  err_gbm <- sum(diag(res)/sum(res))
  accrcyRates[i] <- err_gbm
}

x <- data.frame(nTreeV,1-accrcyRates)
ggplot(x) + aes(x=nTreeV, y=1-accrcyRates) + geom_point()+ggtitle("Influence of iteration number on misclassification rate")
```

Influence of iteration number on missclassification



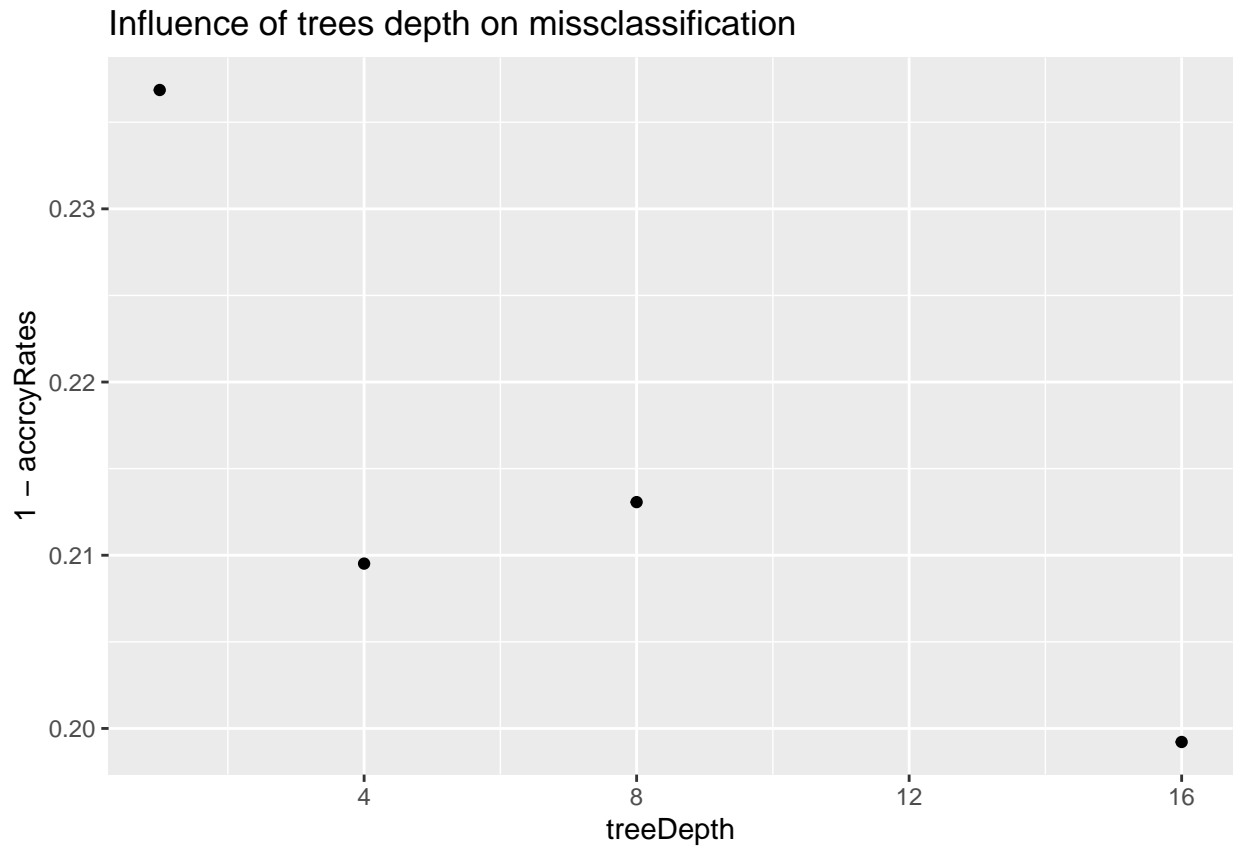
On this plot, as expected, we can notice that missclassification as a function of iteration number is more or less a decreasing function. We can also notice that above a certain number of iteration, the functions is almost constant.

We can then study the influence of trees maximum depth to optimize our solution :

```
#We take the n.tree value with the best accrcyRates
nTree <- nTreeV[which(max(accrcyRates)==accrcyRates)]
treeDepth <- c(1,4,8,16)
accrcyRates <- rep(0,length(treeDepth))

k <- 0
for (i in treeDepth) {
  k = k +1
  boost.compounds=gbm(y~.,data=training,distribution="adaboost",n.trees=nTree,interaction.depth=i)
  yhat_gbm =predict(boost.compounds,newdata=testing,n.trees=nTree, type = "response")
  yhat_gbm <- ifelse(yhat_gbm < 0.5,0,1)
  res <- table(yhat_gbm,testing$y)
  err_gbm <- sum(diag(res)/sum(res))
  accrcyRates[k] <- err_gbm
}

x <- data.frame(treeDepth,1-accrcyRates)
ggplot(x, aes(x=treeDepth, y=1-accrcyRates)) + geom_point()+ggtitle("Influence of trees depth on missclassification")
```



On this plot the decrease is also more or less decreadig with a minimum at 16.

In the best condition (which means with trees depth equal to 16) we can reach 0.8007812 of accuracy rate. This means that this algorithm is the most efficient among those explored in this report.

To conclude we can say that trees depth & iteration number are two factor which can be used to optimize our classification. Nevertheless, it important to be careful because both two factors are very greedy in ressource.