

$$\left. \begin{array}{l} \boxed{E_0} = \text{---} \\ \boxed{E_1} = \boxed{S} \text{---} \\ \boxed{E_2} = \boxed{S} \boxed{S} \text{---} \end{array} \right\} \boxed{E_h} = \boxed{S^h} \text{---} \quad h \in \mathbb{Z}_3$$

$$C_3: S^3 = I$$

$$R_3: SZ = ZS$$

Lem 8 By definition & C_3 , we have 24 (1) $\boxed{S} \boxed{E_0} = \boxed{E_1}$

$$(2) \quad \boxed{S} \boxed{E_1} = \boxed{E_2}$$

$$(3) \quad \boxed{S} \boxed{E_2} = \boxed{E_0}$$

$$\text{Proof: 24. (1)/(2)/(3). LHS} = \boxed{S} \boxed{E_h} := \boxed{S} \boxed{S^h}$$

$$= \boxed{S^{h+1}} =: \boxed{E_{h+1}} = \text{RHS.}$$

$$\text{Note that 24. (3). LHS} := \boxed{S} \boxed{S} \boxed{S} \stackrel{C_3}{=} \text{---} =: \boxed{E_0} = 24. (3). \text{ RHS.}$$

□

Lem 9 By definition & R_3 , we have 25. (1) $\boxed{Z} \boxed{E_0} = \boxed{E_0} \boxed{Z}$

$$(2) \quad \boxed{Z} \boxed{E_1} = \boxed{E_1} \boxed{Z}$$

$$(3) \quad \boxed{Z} \boxed{E_2} = \boxed{E_2} \boxed{Z}$$

$$\text{Proof: 25. (1)/(2)/(3). LHS} = \boxed{Z} \boxed{E_h} := \boxed{Z} \boxed{S^h} \stackrel{R_3}{=} \boxed{S^h} \boxed{Z}$$

$$=: \boxed{E_h} \boxed{Z} = \text{RHS.}$$

□