Final Project: Spotify Tracks

The Objective:

This project's purpose is to apply what we learned from the course and to practice our data communication skills. My goal is to tell a story through data and statistics.

Dataset Description:

The dataset I will use to conduct my analysis was taken from <u>kaggle.com</u>. The original dataset has a range of 125 different genres and their audio features that were popular between the years of 2022-1970. For this project, I randomly selected <u>149 tracks</u> to test the relationship between popularity and music features.

Chosen Variables:

- **Popularity:** The popularity of a track is the dependent variable being measured and tested in this study. The popularity of a track is a value between 0 and 100, with 100 being the most popular.
- **Duration**: is the track length in milliseconds
- **Danceability**: describes the track's appropriateness for dancing based on rhythm and beat. A value of 0 is the least danceable and 1.0 is the most danceable.
- Loudness: is the overall intensity of sound in a track measured in decibels (dB)
- **Energy**: is a measure from 0.0 to 1.0 and represents a measure of activity. An energetic track would give the listener a feeling of the track moving fast and producing an energetic feeling like a rock song for example.
- **Tempo:** The estimated tempo is the track beats per minute (BPM).

Introduction:

Spotify has mentioned the popularity of songs on Spotify is based on the frequent number of recent listens (*How we generate popular tracks*). However, the ranking of songs doesn't provide insight to the artist or the listener as to why people enjoy listening to the song. What if there is a formula that causes a song to increase in popularity? What if there are specific music attributes that affect a song's popularity? As a data analyst at City Records music label, your job is to discover and propose questions about what makes listeners hum along to a song, play it repeatedly, and whether there is a formula to produce a popular song.

Module 1:

The sample data of 149 Spotify songs are normally distributed. Find the probability of selecting a song that scored above 80 in popularity. Round to the nearest three decimal places.

$$SD = 21.756$$

$$z = (x - \overline{x}) / SD$$

$$z = 1.425$$

 $\begin{array}{c|cc} x & 80 \\ \hline SD & 21.756 \\ \hline \overline{x} & 48.987 \\ \hline z & 1.425 \\ \hline Probability & .077 \\ Above & Probability & .923 \\ \hline Probability & .923 \\ \hline Probability & .923 \\ \hline \end{array}$

The probability of selecting a song that scored above 80 is .077.

n	149
---	-----

Module 2:

City Records music label requires you to report what score a Spotify track would need to make it into the top 40 percentile. Additionally, conduct a 95% confidence interval for popularity and calculate if we have the necessary sample size to ensure we have an accurate representation of the population.

SD	21.756
Za/2	1.96
Е	3.493

E = margin of error =
$$Za/2 \sigma/\sqrt{n} = 3.493$$

$$n = (Za/2 * \sigma / E)^2 = 149$$

Score needed to make it into the Top 40	95% Confidence Interval for popularity	Necessary Sample Size
54.499	51.51 to 57.99	n= 149

Module 3:

At City Records, we believe popular songs that rank above 54.499 are short, catchy, and high-energy songs that would be played at a party. Is there sufficient evidence to support our claim at a significance level of .05. Calculate the test statistic and p-values, round the answer to three decimal places, and clarify the decision (μ 1 represents songs above 54.499, μ 2 represents all songs).

Ho:
$$\mu 1 = \mu 2$$

- 1. Popular songs have a shorter duration than the average songs (Ha: μ 1 < μ 2).
- 2. Popular songs have more danceability than average songs (Ha: $\mu 1 > \mu 2$).
- 3. Popular songs are louder than average songs (Ha: $\mu 1 > \mu 2$).
- 4. Popular songs have more energy than average songs (Ha: $\mu 1 > \mu 2$).
- 5. Popular songs have more tempo than average songs (Ha: $\mu 1 > \mu 2$).

	1. Duration	2. Danceability	3. Loudness	4. Energy	5. Tempo
Test statistic t	.313	.392	.629	-1.155	853
P-Value	.378	.348	.266	.126	.198

I performed a one-sample t-test to determine if there was a statistically significant difference in means. I found the means to not have a significant difference. All p-values were above .05. We failed to reject the null hypotheses. There is insignificant evidence to support the idea that all popular songs are short, high-energy party songs.

Module 4:

City Records is interested in more inferences from the Spotify dataset. Using the ANOVA procedure, find if there is any difference between the means of the song attributes. Explain your analysis.

Anova: Single	Factor					
SUMMARY						
Groups	Count	Sum	Average	Variance		
popularity	149	7299	48.9865772	473.337656		
duration_ms	149	33774848	226676.832	4710769748		
danceability	149	88.471	0.5937651	0.02429001		
energy	149	91.2267	0.61225973	0.05328626		
loudness	149	-1207.512	-8.1041074	16.9535481		
tempo	149	17626.839	118.300933	813.847587		
ANOVA						
Source of Variati	SS	df	MS	F	P-value	F crit
Between Gro	6.3782E+12	5	1.2756E+12	1624.74695	0	2.22418428
Within Group	6.9719E+11	888	785128509			
Total	7.0754E+12	893				

After using the ANOVA procedure, I received a p-value of 0. This indicates there is at least one group that differs significantly. These results might seem contradictory to the t-test performed earlier upon request. However, ANOVA tests are typically better at detecting differences than performing individual t-tests. Additionally, there is a chance we encountered an error because we did not adjust the significance level for each test.

Module 5:

City Records desires to predict the popularity of a Spotify song based on song attributes. Provide a regression equation for predicting song popularity and interpret your findings.

EXCEL MODEL 1:

SUMMARY O	UTPUT							
Regression	Statistics							
Multiple R	0.29895673							
R Square	0.08937513							
Adjusted R S	0.0575351							
Standard Err	21.1211773							
Observations	149							
ANOVA								
	df	SS	MS	F	Significance F			
Regression	5	6261.08276	1252.21655	2.80700507	0.01890994			
Residual	143	63792.8904	446.104129					
Total	148	70053.9732						
	Coefficients	tandard Erroi	t Stat	P-value	Lower 95%	Upper 95%	Lower 95.0%	Upper 95.0%
Intercept	74.1774449	17.9147133	4.14058788	5.8948E-05	38.7655709	109.589319	38.7655709	109.589319
duration_ms	2.669E-05	2.8056E-05	0.95131911	0.34304755	-2.877E-05	8.2148E-05	-2.877E-05	8.2148E-05
danceability	13.5373983	13.2793436	1.01943279	0.30971914	-12.711776	39.7865732	-12.711776	39.7865732
energy	-28.057655	10.0580061	-2.7895842	0.00599736	-47.939237	-8.1760728	-47.939237	-8.1760728
loudness	1.43891115	0.60062106	2.39570544	0.01788231	0.25166818	2.62615412	0.25166818	2.62615412
tempo	-0.0882431	0.0635449	-1.3886733	0.16709127	-0.2138518	0.0373656	-0.2138518	0.0373656

T-stat = -1.977 Rejection Region = t < -1.977 or t > 1.977

We can conclude from the first regression model that energy and loudness have statistically significant effects on the dependent variable popularity. However, outliers have a significant impact on the R-squared and adjusted R-square which could indicate why the R-square is low and the model does not explain the relationships between variables as effectively.

In addition, it's essential to remove insignificant variables to improve the model's performance. I used the SAS program to select the best regression model for predicting song popularity and to provide City Records with a more in-depth analysis (Appendix A).

More specifically, I used stepwise and backward stepwise selection which are variable selection procedures (Appendix B, figures 1-4). The procedure consists of testing different combinations of variables that improve the adjusted R-square while limiting RMSE. Using these tools I was able to simplify the regression model and verify accuracy.

To conclude, Model 3 performed the best with an adjusted R-square of .0613, R-square of .0803, and RMSE of 21.0795 (Appendix B, figure 5). Based on statistical evidence, there is a relationship between popularity and the independent variables energy, loudness, and tempo.

Regression equation =

 \hat{y} = 89.7795999 -28.142122(energy) + 1.66243768(loudness) - .0852923(tempo)

	SAS Code						
data	data music;						
	y x1 x2 x3	x4 x5;					
datali							
У	x1	x2 x3 x4	x5				
61		0.485 0.723 -6.565	167.845				
54		0.397 0.538 -6.503	154.342				
0		0.627 0.562 -6.268	95.054				
80		0.603 0.67 -3.882	107.993				
85		0.913 0.603 -4.892	123.061				
61 64		0.408 0.314 -7.729 0.79 0.728 -6.523	105.096 110.059				
54		0.675 0.931 -3.432	124.008				
72		0.484 0.368 -7.784	92.923				
88		0.561 0.431 -8.81 143.875					
82		0.559 0.559 -6.425	72.498				
84		0.609 0.378 -9.828	100.418				
0		0.629 0.664 -10.517	139.975				
0		0.604 0.741 -5.571	153.947				
82		0.918 0.585 -7.781	131.966				
84		0.724 0.818 -3.747	77.004				
85		0.76 0.703 -5.412	95.99 <mark>7</mark>				
3	201573	0.512 0.796 -4.075	171.01 <mark>4</mark>				
89	174000	0.548 0.816 -4.209	95.39				
88	238805	0.761 0.525 -6.9 80.87					
84	203807	0.695 0.884 -2.278	103.014				
58	225310	0.638 0.731 -4.537	89.928				
59	351425	0.365 0.449 -13.516	103.643				
58	328854	0.314 0.478 -7.201	199.631				
58		0.66 0.926 -3.452	109.997				
59		0.798 0.636 -10.52	139.98				
59		0.461 0.5 -9.828	76.176				
61		0.728 0.861 -5.852	87.46 <mark>7</mark>				
62		0.522 0.74 -7.018	92.618				
69		0.484 0.059 -25.084	89.329				
78		0.414 0.428 -11.097	145.075				
70		0.307 0.0381 -28.197					
51		0.347 0.799 -6.371	162.575				
52	159066		89.964				
36	120413	0.628 0.52 -8.331	89.97				
50 30	244120	0.51 0.42 -8.014 0.423 0.617 -6.458	125.898 142.042				
44	401773 258482	0.513 0.81 -6.826	142.042 121.015				
24	350000	0.205 0.181 -18.639	72.184				
48	261229	0.523 0.535 -11.394	159.903				
55	336932	0.254 0.527 -9.225	147.561				
42	242840	0.451 0.952 -3.186	95.985				
24	118000	0.254 0.996 -21.444	107.921				
42	209920	0.571 0.853 -6.589	126.016				
84	205946	0.649 0.716 -5.371	99.988				
79		0.886 0.672 -4.394	91.976				
30	268736	0.628 0.027 -13.64	122.007				

```
205658 0.49 0.674 -7.276
                                         122.807
        256680 0.316 0.413 -12,216
60
                                         155.69
        265386 0.47 0.271 -7.636
51
                                         145.902
73
        230666 0.676 0.461 -6.746
                                         87.917
55
        149610 0.42 0.166 -17.235
                                         77,489
57
        210826 0.438 0.359 -9.734
                                         76.332
71
        201933 0.266 0.0596
                                 -18.515 181.74
82
        198853 0.618 0.443 -9.681
                                         119.949
58
        214240 0.688 0.481 -8.807
                                         98.017
74
        229400 0.407 0.147 -8.822
                                         141.284
80
        242946 0.703 0.444 -9.331
                                         150.96
        205594 0.442 0.632 -6.77 78.899
56
74
        244800 0.627 0.363 -8.127
                                         99.905
69
        240165 0.483 0.303 -10.058
                                         133.406
52
        198712 0.489 0.314 -9.245
                                         124.234
62
        248448 0.691 0.234 -6.441
                                         87.103
56
        188133 0.755 0.78 -6.084
                                         120.004
58
        244986 0.489 0.561 -7.933
                                         83.457
56
        129750 0.706 0.112 -18.098
                                         110.154
77
        180750 0.658 0.9 -3.479
                                         156.096
74
        198173 0.749 0.862 -3.494
                                         97.982
53
        272639 0.462 0.217 -11.436
                                         120.971
79
        173947 0.902 0.582 -5.902
                                         107.005
68
        192280 0.692 0.881 -2.563
                                         103.053
64
        189546 0.683 0.947 -1.717
                                         100.024
        537653 0.372 0.426 -8.421
                                         123.993
66
76
        227478 0.904 0.723 -5.224
                                         145.013
64
        203056 0.765 0.77 -3.16 103.005
52
        150139 0.495 0.484 -10.923
                                         126.632
50
                                         125.939
        213571 0.659 0.633 -5.343
54
        183100 0.852 0.967 -1.661
                                         124.024
59
        149213 0.85 0.734 -6.415
                                         103.027
69
        225012 0.72 0.824 -5.086
                                         165.996
51
        266959 0.667 0.545 -8.088
                                         147.988
53
        341177 0.403 0.56 -7.46 155.701
74
        221573 0.82 0.852 -2.567
                                         109.036
52
        255186 0.664 0.637 -4.338
                                         93.137
52
        261000 0.591 0.828 -10.309
                                         89.981
67
        178529 0.878 0.777 -3.702
                                         139.989
52
        250124 0.59 0.908 -4.137
                                         87.989
67
        139213 0.852 0.762 -4.448
                                         131.958
63
        185508 0.519 0.352 -8.332
                                         78.943
40
        164571 0.809 0.464 -8.716
                                         140.006
        238064 0.667 0.645 -8.727
38
                                         123.994
39
        200145 0.541 0.84 -10.416
                                         137.04
39
        162384 0.734 0.551 -10.879
                                         144.058
38
        259339 0.388 0.498 -9.165
                                         84.567
56
        220506 0.857 0.628 -5.58 101.987
39
        214256 0.537 0.417 -11.937
                                         73.916
39
        203600 0.404 0.448 -10.731
                                         98.503
40
        281566 0.389 0.516 -9.313
                                         165.68
39
        214200 0.716 0.671 -9.517
                                         100.021
39
        247720 0.495 0.969 -3.376
                                         179.729
39
        120122 0.811 0.731 -4.085
                                         100.017
40
        140700 0.727 0.423 -12.411
                                         100.038
```

```
192000 0.78 0.721 -7.042
                                         79.996
40
        194567 0.772 0.652 -8.125
                                         127.027
39
        232041 0.5 0.912 -5.725
                                         139.865
39
        229200 0.707 0.885 -5.133
                                         120.032
40
        480000 0.717 0.898 -7.52 137.024
49
        193596 0.541 0.839 -7.141
                                         123.984
29
        358669 0.632 0.983 -6.276
                                         129.995
21
        204687 0.433 0.816 -5.507
                                         131.287
30
        279000 0.62 0.585 -7.233
                                         124.137
53
        162580 0.709 0.74 -5.783
                                         124.144
21
        354666 0.563 0.879 -7.16 180.009
47
        147230 0.393 0.94 -3.894
                                         129.958
36
        182553 0.658 0.857 -5.625
                                         140.985
49
        236712 0.519 0.874 -4.219
                                         145.944
3
        165249 0.684 0.429 -10.107
                                         96.016
27
        141665 0.697 0.535 -6.314
                                         91.905
26
        186635 0.641 0.4 -6.74 84.981
                                         96.978
10
        143004 0.774 0.657 -6.587
8
        113454 0.74 0.503 -9.669
                                         82.473
25
        144494 0.756 0.4 -8.383
                                         88.983
31
        134579 0.742 0.254 -15.696
                                         150.029
8
        155581 0.648 0.439 -10.652
                                         172.073
10
        144381 0.703 0.56 -6.529
                                         95.092
51
        191293 0.462 0.722 -5.134
                                         173.941
34
        295333 0.428 0.312 -14.24
                                         126.75
32
        230840 0.558 0.492 -10.173
                                         111.488
55
        284493 0.283 0.657 -8.557
                                         97.991
                                         133.942
23
        208828 0.54 0.77 -5.597
50
        231853 0.641 0.757 -4.867
                                         87.995
63
        332506 0.46 0.162 -17.142
                                         122.767
23
        341200 0.565 0.772 -8.436
                                         89.984
25
        270706 0.573 0.908 -4.369
                                         117.107
61
        205306 0.568 0.849 -10.472
                                         130.746
24
        195626 0.7 0.496 -8.64 100.058
23
        222738 0.583 0.643 -6.531
                                         120.116
23
        428266 0.524 0.951 -6.851
                                         108.1
23
        321200 0.478 0.471 -7.923
                                         204.643
23
        186826 0.675 0.452 -11.492
                                         127.901
23
        212573 0.786 0.517 -14.507
                                         136.923
25
        219866 0.622 0.714 -11.152
                                         159.948
25
        245706 0.373 0.849 -6.352
                                         114.792
24
        184466 0.496 0.507 -8.384
                                         101.117
23
        230272 0.576 0.672 -9.332
                                         112.799
25
        264773 0.515 0.926 -8.01 136.62
55
        244306 0.53 0.873 -10.572
                                         126.16
0
        266383 0.505 0.87 -9.392
                                         112.102
52
        184866 0.678 0.375 -6.992
                                         89.994
proc reg data = work.music;
   model y = x1 x2 x3 x4 x5 /cli clm;
run;
proc reg data = work.music;
   model y = x1 x2 x3 x4 x5 / vif r;
run;
```

```
proc reg data = work.music;
    model y = x1 x2 x3 x4 x5 / selection=stepwise
slentry=0.25 slstay=0.15;
run;

proc reg data = work.music;
    model y = x1 x2 x3 x4 x5 / SELECTION=BACKWARD
slstay=0.15;
run;
proc reg data = work.music;
    model y = x1 x2 x3 x4 x5 / selection = adjrsq Best = 13
CP RMSE;
run;
proc reg data = work.music;
    model y = x1 x2 x3 x4 x5 / selection = rsquare Best = 2
adjrsq CP RMSE;
run;
```

APPENDIX B:

The REG Procedure Model: MODEL1 Dependent Variable: y

Number of Observations Read	150
Number of Observations Used	149
Number of Observations with Missing Values	1

Stepwise Selection: Step 1

Variable x5 Entered: R-Square = 0.0164 and C(p) = 9.4654

Analysis of Variance						
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F	
Model	1	1146.33396	1146.33396	2.45	0.1200	
Error	147	68908	468.75945			
Corrected Total	148	70054				

Variable	Parameter Estimate	Standard Error	Type II SS	F Value	Pr > F
Intercept	60.52752	7.59023	29809	63.59	<.0001
x5	-0.09756	0.06238	1146.33396	2.45	0.1200

Bounds on condition number: 1, 1

Stepwise Selection: Step 2

Variable x4 Entered: R-Square = 0.0304 and C(p) = 9.2586

Analysis of Variance						
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F	
Model	2	2130.76983	1065.38491	2.29	0.1049	
Error	146	67923	465.22742			
Corrected Total	148	70054				

Variable	Parameter Estimate	Standard Error	Type II SS	F Value	Pr > F
Intercept	66.13714	8.48815	28244	60.71	<.0001
x4	0.62713	0.43112	984.43586	2.12	0.1479
х5	-0.10201	0.06222	1250.43151	2.69	0.1033

Bounds on condition number: 1.0024, 4.0097

Figure 1: Stepwise Selection 1 and 2

Stepwise Selection: Step 3

Variable x3 Entered: R-Square = 0.0803 and C(p) = 3.4284

Analysis of Variance									
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F				
Model	3	5623.87491	1874.62497	4.22	0.0068				
Error	145	64430	444.34551						
Corrected Total	148	70054							

Variable	Parameter Estimate	Standard Error	Type II SS	F Value	Pr > F
Intercept	89.77960	11.82873	25598	57.61	<.0001
х3	-28.14212	10.03717	3493.10508	7.86	0.0057
x4	1.66244	0.56024	3912.57660	8.81	0.0035
х5	-0.08529	0.06110	865.79231	1.95	0.1649

Bounds on condition number: 1.788, 13.717

Stepwise Selection: Step 4

Variable x5 Removed: R-Square = 0.0679 and C(p) = 3.3692

Analysis of Variance									
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F				
Model	2	4758.08260	2379.04130	5.32	0.0059				
Error	146	65296	447.23213						
Corrected Total	148	70054							

Variable	Parameter Estimate	Standard Error	Type II SS	F Value	Pr > F
Intercept	80.70075	9.91212	29645	66.29	<.0001
х3	-29.50953	10.02165	3877.74429	8.67	0.0038
x4	1.68392	0.56184	4017.38407	8.98	0.0032

Bounds on condition number: 1.771, 7.0841

All variables left in the model are significant at the 0.1500 level.

The stepwise method terminated because the next variable to be entered was just removed.

	Summary of Stepwise Selection											
Step	Variable Entered	Variable Removed	Number Vars In	Partial R-Square	Model R-Square	C(p)	F Value	Pr > F				
1	х5		1	0.0164	0.0164	9.4654	2.45	0.1200				
2	x4		2	0.0141	0.0304	9.2586	2.12	0.1479				
3	х3		3	0.0499	0.0803	3.4284	7.86	0.0057				
4		x5	2	0.0124	0.0679	3.3692	1.95	0.1649				

Figure 2: Stepwise Selection 3 and 4

The REG Procedure Model: MODEL1 Dependent Variable: y

Number of Observations Read	150
Number of Observations Used	149
Number of Observations with Missing Values	1

Backward Elimination: Step 0

All Variables Entered: R-Square = 0.0894 and C(p) = 6.0000

Analysis of Variance									
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F				
Model	5	6261.08276	1252.21655	2.81	0.0189				
Error	143	63793	446.10413						
Corrected Total	148	70054							

Variable	Parameter Estimate	Standard Error	Type II SS	F Value	Pr > F
Intercept	74.17744	17.91471	7648.21797	17.14	<.0001
x1	0.00002669	0.00002806	403.72783	0.91	0.3430
x2	13.53740	13.27934	463.61069	1.04	0.3097
х3	-28.05765	10.05801	3471.48421	7.78	0.0060
x4	1.43891	0.60062	2560.37207	5.74	0.0179
x5	-0.08824	0.06354	860.27324	1.93	0.1671

Bounds on condition number: 2.029, 37.794

Backward Elimination: Step 1

Variable x1 Removed: R-Square = 0.0836 and C(p) = 4.9050

Analysis of Variance									
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F				
Model	4	5857.35493	1464.33873	3.28	0.0131				
Error	144	64197	445.80985						
Corrected Total	148	70054							

Variable	Parameter Estimate	Standard Error	Type II SS	F Value	Pr > F
Intercept	82.23789	15.77918	12109	27.16	<.0001
x2	8.95158	12.36944	233.48002	0.52	0.4704
х3	-28.04084	10.05467	3467.33446	7.78	0.0060
x4	1.52109	0.59418	2921.63805	6.55	0.0115
х5	-0.07668	0.06235	674.23065	1.51	0.2208

Bounds on condition number: 1.987, 24.238

Figure 3: Backward Elimination 0 and 1

Backward Elimination: Step 2

Variable x2 Removed: R-Square = 0.0803 and C(p) = 3.4284

Analysis of Variance									
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F				
Model	3	5623.87491	1874.62497	4.22	0.0068				
Error	145	64430	444.34551						
Corrected Total	148	70054							

Variable	Parameter Estimate	Standard Error	Type II SS	F Value	Pr > F
Intercept	89.77960	11.82873	25598	57.61	<.0001
х3	-28.14212	10.03717	3493.10508	7.86	0.0057
x4	1.66244	0.56024	3912.57660	8.81	0.0035
x5	-0.08529	0.06110	865.79231	1.95	0.1649

Bounds on condition number: 1.788, 13.717

Backward Elimination: Step 3

Variable x5 Removed: R-Square = 0.0679 and C(p) = 3.3692

Analysis of Variance						
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F	
Model	2	4758.08260	2379.04130	5.32	0.0059	
Error	146	65296	447.23213			
Corrected Total	148	70054				

Variable	Parameter Estimate	Standard Error	Type II SS	F Value	Pr > F
Intercept	80.70075	9.91212	29645	66.29	<.0001
х3	-29.50953	10.02165	3877.74429	8.67	0.0038
x4	1.68392	0.56184	4017.38407	8.98	0.0032

Bounds on condition number: 1.771, 7.0841

All variables left in the model are significant at the 0.1500 level.

	Summary of Backward Elimination							
Step	Variable Removed	Number Vars In	Partial R-Square	Model R-Square	C(p)	F Value	Pr > F	
1	x1	4	0.0058	0.0836	4.9050	0.91	0.3430	
2	x2	3	0.0033	0.0803	3.4284	0.52	0.4704	
3	x5	2	0.0124	0.0679	3.3692	1.95	0.1649	

Figure 4: Backward Elimination 2 and 3

The REG Procedure Model: MODEL1 Dependent Variable: y

Adjusted R-Square Selection Method

Number of Observations Read	150
Number of Observations Used	149
Number of Observations with Missing Values	1

Number in Model	Adjusted R-Square	R-Square	C(p)	Root MSE	Variables in Model
3	0.0613	0.0803	3.4284	21.07950	x3 x4 x5
4	0.0582	0.0836	4.9050	21.11421	x2 x3 x4 x5
5	0.0575	0.0894	6.0000	21.12118	x1 x2 x3 x4 x5
4	0.0573	0.0828	5.0392	21.12406	x1 x3 x4 x5
2	0.0552	0.0679	3.3692	21.14786	x3 x4
3	0.0548	0.0740	4.4164	21.15148	x2 x3 x4
4	0.0515	0.0771	5.9284	21.18916	x1 x2 x3 x4
3	0.0491	0.0683	5.3019	21.21579	x1 x3 x4
4	0.0265	0.0528	9.7394	21.46594	x1 x2 x3 x5
3	0.0221	0.0419	9.4542	21.51475	x2 x3 x5
3	0.0211	0.0409	9.6105	21.52592	x1 x2 x3
2	0.0205	0.0337	8.7419	21.53250	x2 x3
2	0.0171	0.0304	9.2586	21.56913	x4 x5

Figure 5: Summary of all Regression Models

Reference

How we generate popular tracks. Spotify. (n.d.). https://support.spotify.com/us/artists/article/how-we-generate-popular-tracks/