4.6 Applications and the Perron-Frobenius Theorem