

Motivation

Symbolic computations are useful for theorists; now the same library can be used by both experimentalists and theorists.

A SymPy backend is a very different kind of backend because it's not numerical. We wanted to show that Vector is generic enough to support such far-flung use-cases.

NumPy arrays

Awkward arrays

Architecture

```
graph LR; A[SymPy vector classes] -- "Perform an operation" --> B[Shim layer mapping SymPy functions to NumPy functions]; C[Obj/NumPy/Awk vector classes] -- "Perform an operation" --> D[Compute functions duck typed]; B -- "Mapped function" --> D; D -- "Operate only on the data containers" --> E[wrap the result as a scalar, vector, or array of vectors]; E --> F[Perform Awkward and/or NumPy or SymPy operations on the result];
```

The diagram illustrates the architecture of the vectorization process. It starts with two input boxes: "SymPy vector classes" and "Obj/NumPy/Awk vector classes". The "SymPy vector classes" box has an arrow labeled "Perform an operation" pointing to a "Shim layer mapping SymPy functions to NumPy functions" box. The "Obj/NumPy/Awk vector classes" box has an arrow labeled "Perform an operation" pointing to a "Compute functions (duck typed)" box. The "Shim layer mapping SymPy functions to NumPy functions" box has an arrow labeled "Mapped function" pointing to the "Compute functions (duck typed)" box. From the "Compute functions (duck typed)" box, an arrow labeled "Operate only on the data containers" points down to a box labeled "wrap the result as a scalar, vector, or array of vectors". Finally, an arrow points from this box to a box labeled "Perform Awkward and/or NumPy or SymPy operations on the result".

Results

Computations on Object type vectors

Sympy vector classes as drop-in replacement

$$\frac{pt^3 \sin^2(\phi) \cos(\phi)}{\left(1 + \frac{1}{\sqrt{\frac{pt^2 \sin^2(\phi)}{M^2 + 0.25pt^2(1+e^{-2\eta})^{2e^{2\eta}}} + \frac{pt^2 \cos^2(\phi)}{M^2 + 0.25pt^2(1+e^{-2\eta})^{2e^{2\eta}}} + \frac{pt^2 \sinh^2(\eta)}{M^2 + 0.25pt^2(1+e^{-2\eta})^{2e^{2\eta}}} + 1}}\right)} + \dots$$

Symbolic calculations with the same API

`v.boost(v.to_beta3()).px.simplify()`

$$\frac{pt \left(1.0M^2 \sqrt{(M^2e^{2\eta} + 0.25pt^2e^{4\eta} + 0.5pt^2e^{2\eta} + 0.25pt^2)e^{-2\eta}e^{2\eta}} + 0.25pt^2 \sqrt{(M^2e^{2\eta} + 0.25pt^2e^{4\eta} + 0.5pt^2e^{2\eta} + 0.25pt^2)e^{-2\eta}e^{4\eta}} + 0.5pt^2 \sqrt{(M^2e^{2\eta} + 0.25pt^2e^{4\eta} + 0.5pt^2e^{2\eta} + 0.25pt^2)e^{-2\eta}e^{2\eta}} + 0.25pt^2 \sqrt{(M^2e^{2\eta} + 0.25pt^2e^{4\eta} + 0.5pt^2e^{2\eta} + 0.25pt^2)e^{-2\eta}e^{4\eta}} \right)}{\sqrt{(M^2e^{2\eta} + 0.25pt^2e^{4\eta} + 0.5pt^2e^{2\eta} + 0.25pt^2)e^{-2\eta}} \left(1.0M^2 \sqrt{\frac{1.0M^2e^{2\eta} + 0.25pt^2e^{4\eta} + 0.5pt^2e^{2\eta} + 0.25pt^2}{M^2}} \right)}$$

Results compatible with SymPy functions and methods

`v.boost(v.to_beta3()).px.subs({"pt": 1, "phi": 2, "eta": 3, "M": 4})`

$$\frac{\sqrt{\cos^2(2) + \sin^2(2) + 16 + \sinh^2(3) \cos(2)}}{\sqrt{1 + 0.015625(e^{-6} + 1)^2 e^6} \sqrt{-\frac{\sinh^2(3)}{16 + 0.25(e^{-6} + 1)^4 e^6} - \frac{\sin^2(2)}{16 + 0.25(e^{-6} + 1)^2 e^6} - \frac{\cos^2(2)}{16 + 0.25(e^{-6} + 1)^2 e^6} + 1}} + \left(1 + \frac{1}{\sqrt{-\frac{\sinh^2(3)}{16 + 0.25(e^{-6} + 1)^4 e^6} - \frac{\sin^2(2)}{16 + 0.25(e^{-6} + 1)^2 e^6} - \frac{\cos^2(2)}{16 + 0.25(e^{-6} + 1)^2 e^6} + 1}} \right) \frac{\cos(2) \sinh^2(3)}{(16 + 0.25(e^{-6} + 1)^2 e^6) \left(-\frac{\sinh^2(3)}{16 + 0.25(e^{-6} + 1)^4 e^6} - \frac{\sin^2(2)}{16 + 0.25(e^{-6} + 1)^2 e^6} - \frac{\cos^2(2)}{16 + 0.25(e^{-6} + 1)^2 e^6} + 1 \right)}$$

Use any SymPy functionality on the expressions

```
v.boost(v.to_beta3()).px.subs({...}).evalf()
-2.25409707330435
```

Evaluated results consistent with numerical backends

Integrations



Caveats

