

A new SymPy backend for Vector: uniting experimental and theoretical physicists

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Vector

A Python library for JIT-compilable mathematical manipulations of Lorentz vectors, especially arrays of vectors, in a NumPy-like way.

NumPy arrays

Awkward arrays

12 coordinate systems - cartesian, cylindrical, pseudorapidity, and any combination of these with time or proper time for 4D vectors.

Uses conventions set up by ROOT's TLorentzVector and Math::LorentzVector.

Integrations

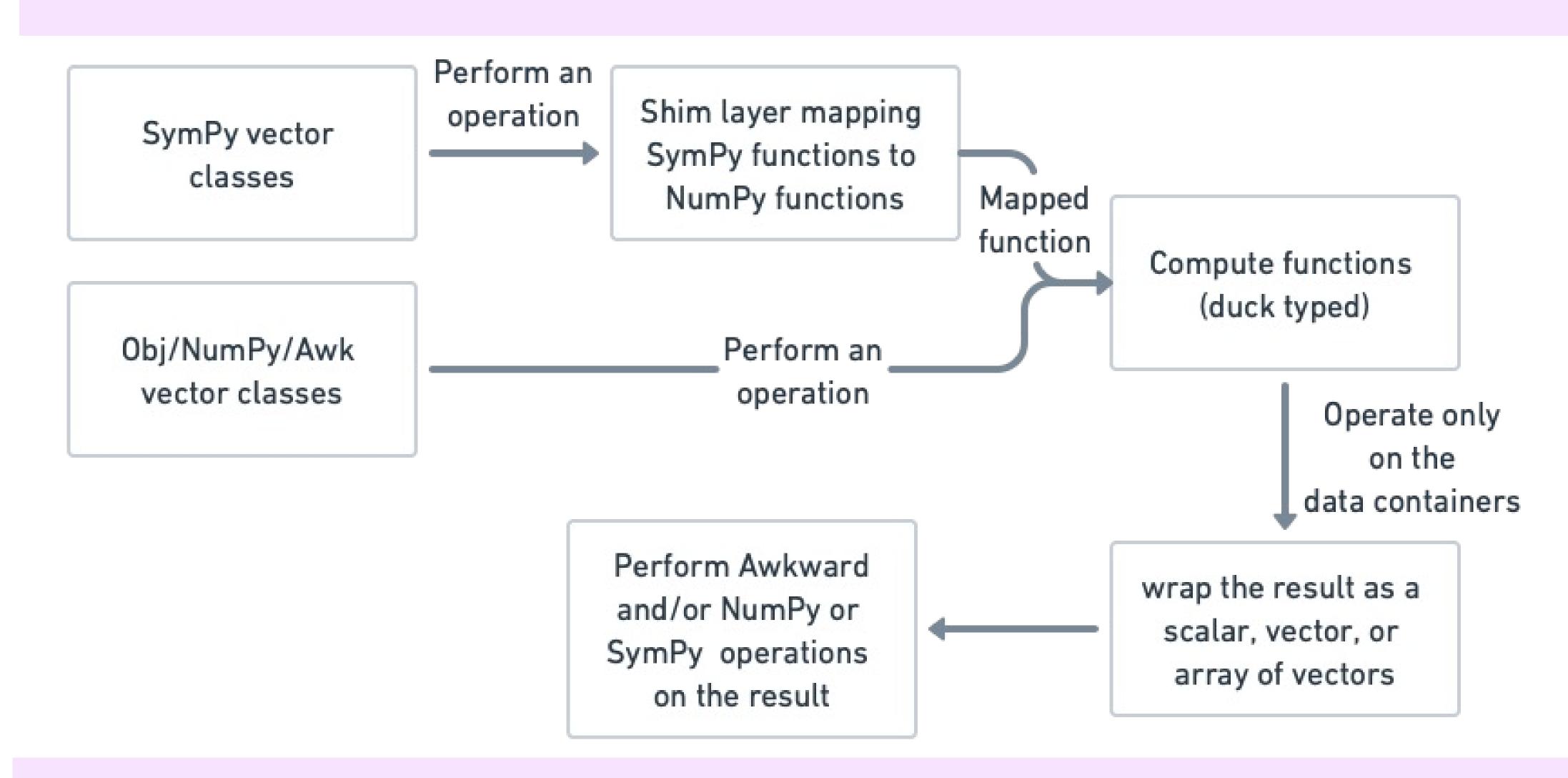


Motivation

Symbolic computations are useful for theorists; now the same library can be used by both experimentalists and theorists.

A SymPy backend is a very different kind of backend because it's not numerical. We wanted to show that Vector is generic enough to support such far-flung usecases.

Architecture



Results

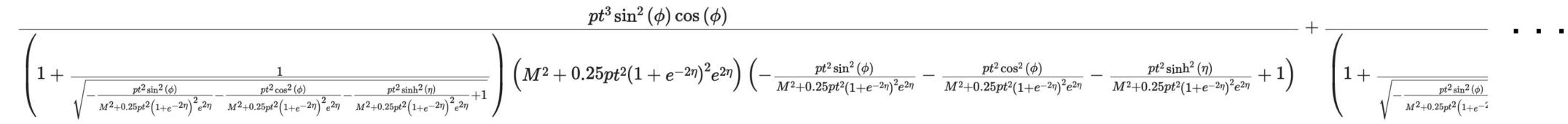
```
v = vector.MomentumObject(pt=1, phi=2, eta=3, M=4)
v.boost(v.to_beta3()).px
np.float64(-2.2540970733043526)
```

pt, phi, eta, M = sympy.symbols("pt phi eta M")
v = vector.MomentumSympy4D(pt=pt, phi=phi, eta=eta, M=M)

Sympy vector classes as drop-in replacement

Computations on Object type vectors

v.boost(v.to_beta3()).px



Symbolic calculations with the same API

```
 \begin{array}{c} \text{V.boost(v.to\_beta3()).px.simplify()} \\ & \underline{pt\left(1.0M^2\sqrt{(M^2e^{2\eta}+0.25pt^2e^{4\eta}+0.5pt^2e^{2\eta}+0.25pt^2)e^{-2\eta}e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta}+0.25pt^2e^{2\eta
```

Results compatible with SymPy functions and methods

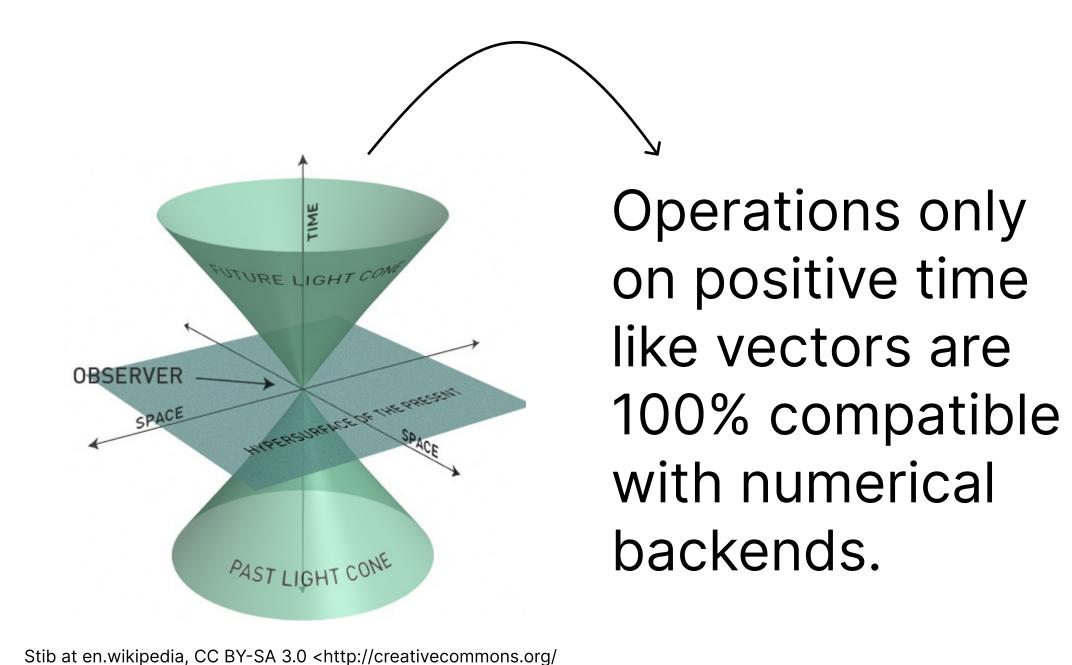
```
 \frac{\sqrt{\cos^2(2) + \sin^2(2) + 16 + \sinh^2(3)}\cos(2)}{\sqrt{1 + 0.015625(e^{-6} + 1)^2e^6}\sqrt{-\frac{\sinh^2(3)}{16 + 0.25(e^{-6} + 1)^2e^6} - \frac{\sin^2(2)}{16 + 0.25(e^{-6} + 1)^2e^6} - \frac{\cos^2(2)}{16 + 0.25(e^{-6} + 1)^2e^6} + 1}} + \frac{\cos(2)\sinh^2(3)}{\sqrt{1 + \frac{\sinh^2(3)}{16 + 0.25(e^{-6} + 1)^2e^6} - \frac{\sin^2(2)}{16 + 0.25(e^{-6} + 1)^2e^6} - \frac{\cos^2(2)}{16 + 0.25(e^{-6} + 1)^2e^6} + 1}}} + \frac{1}{\sqrt{-\frac{\sinh^2(3)}{16 + 0.25(e^{-6} + 1)^2e^6} - \frac{\cos^2(2)}{16 + 0.25(e^{-6} + 1)^2e^6} - \frac{\cos^2(2)}{16 + 0.25(e^{-6} + 1)^2e^6} - \frac{\sin^2(3)}{16 + 0.25(e^{-6} + 1)^2e^6} - \frac{\cos^2(2)}{16 + 0.25(e^{-6} + 1)^2e^6} - \frac{\sin^2(3)}{16 + 0.25(e^{-6} + 1)^2e^6} - \frac{\cos^2(2)}{16 + 0.25(e^{-6} + 1)^2e^6} - \frac{\cos^2(2
```

Use any SymPy functionality on the expressions

v.boost(v.to_beta3()).px.subs({...}).evalf()

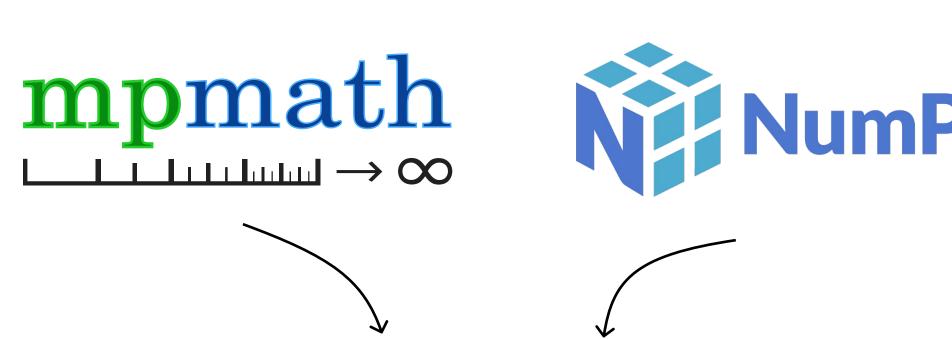
Evaluated results consistent with numerical backends

Caveats



-2.25409707330435

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SymPy uses mpmath for numerical computations which has more floating point precision than NumPy, producing slightly different numerical results.