

# *Efficient Concurrent Aggregate Queries*

*Concurrent Computing*

*Gal Sela, EPFL*

# Multi-Element Queries



- Snapshots    The numbers 1, 3, 7, 8, and 11 are displayed in green rounded squares, representing a snapshot of the data.

# Multi-Element Queries



- Snapshots, range queries
- Aggregate queries

size    5                      i-th item    4-th  $\Rightarrow$

Summarize a range of items with consecutive keys  
into a succinct value

# Aggregate Queries Applications

size 5

collections and maps  
in Java

i-th item 4-th  $\Rightarrow$  8

access sortedcontainer[i]  
in Python

implemented using order-statistic tree

similar augmented trees

in some text editors  
to access the cursor's location

Augmented trees – used in  
interval trees, link/cut trees, tango trees etc.

# Concurrent Snapshots



1

3

7

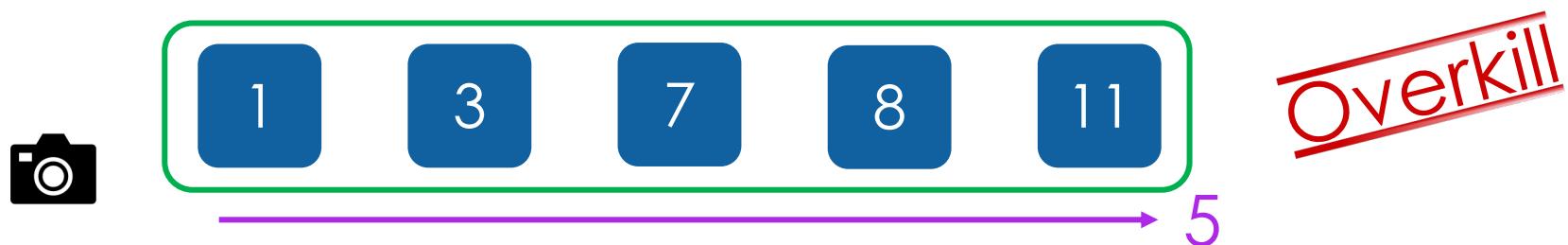
8

11

Extensive research  
in the last 35 years

# Concurrent Aggregate Queries

Could be implemented using **snapshot**



- ✓ Correct: linearizable
- ✗ Inefficient:  $\theta(\text{num of elements})$

# Concurrent Aggregate Queries



- ✓ Correct
- ✓ Efficient

*difficult!* Emerging research

# Concurrent Aggregate Queries

Correct and efficient – difficult!

Emerging research

Concurrent size [OOPSLA'22]

Wait-free trees with asymptotically-efficient range queries [IPDPS'24]

Concurrent aggregate queries [DISC'24]

Lock-free augmented trees [DISC'24]

# Concurrent Aggregate Queries

Correct and efficient – difficult!

Emerging research

For sets and dictionaries

# Concurrent Size

*Gal Sela and Erez Petrank*

OOPSLA'22

# Concurrent Size

Difficult due to concurrent updates

1

3

4

6

...



ins(3)

del(1)



ins(4)

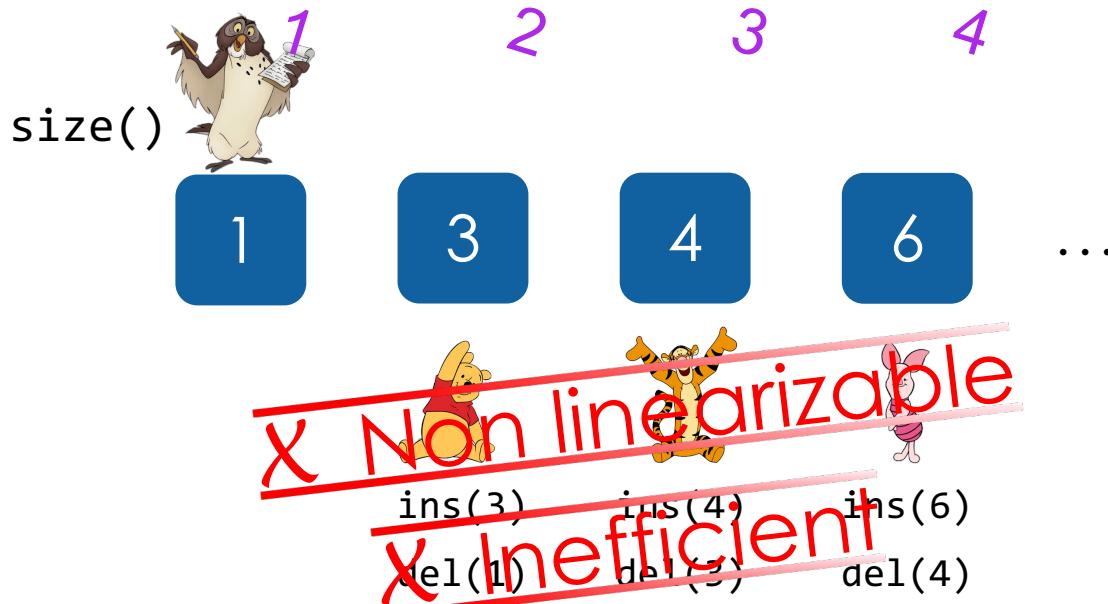
del(3)



ins(6)

del(4)

# Concurrent Size



ConcurrentLinkedQueue

ConcurrentLinkedDeque

# Concurrent Size

*For efficiency:* Metadata  
for computing size



ConcurrentSkipListMap

ConcurrentHashMap

# Concurrent Size

For efficiency: Metadata  
for computing size

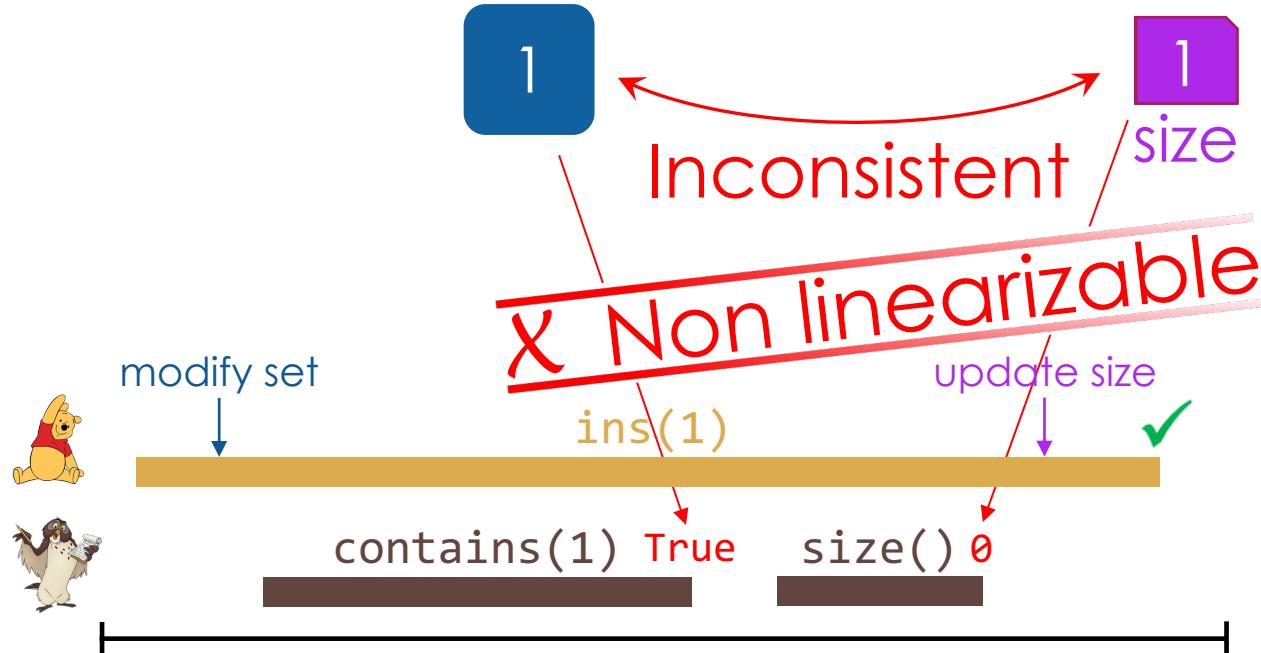


✓ Efficient

What about Correctness?

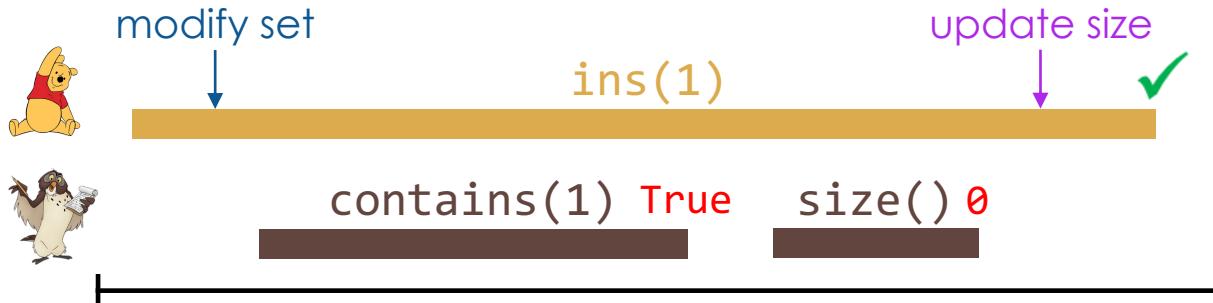
# Size as Metadata

Maintained  
by ins & del: modify set then update size



# Linearizability

Each operation appears to happen at once during its interval.



# Negative Size

Maintained  
by ins & del:      modify set    then    update size

1

3

4

6

...

-2  
size



size()



del(1)

ins(3)



del(3)

ins(4)



del(4)

ins(6)

X Incorrect

# Negative Size

## ConcurrentHashMap

```
public int size() {
    long n = sumCount();
    return ((n < 0L) ? 0 :
        (n > (long)Integer.MAX_VALUE) ? Integer.MAX_VALUE :
        (int)n);
}

public boolean isEmpty() {
    return sumCount() <= 0L; // ignore transient negative values
}
```

## ConcurrentSkipListMap

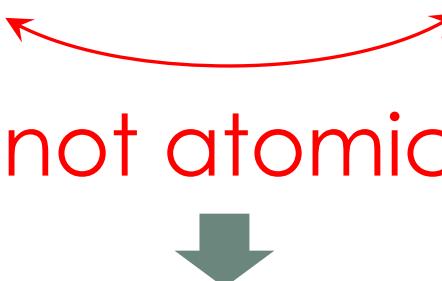
```
final long getAdderCount() {
    LongAdder a; long c;
    do {} while ((a = adder) == null &&
        !ADDER.compareAndSet(this, null, a = new LongAdder()));
    return ((c = a.sum()) <= 0L) ? 0L : c; // ignore transient negatives
}

public int size() {
    long c;
    return ((baseHead() == null) ? 0 :
        ((c = getAdderCount()) >= Integer.MAX_VALUE) ?
        Integer.MAX_VALUE : (int) c);
}
```

# Size as Metadata

Maintained  
by `ins` & `del`:    modify set    then    update size

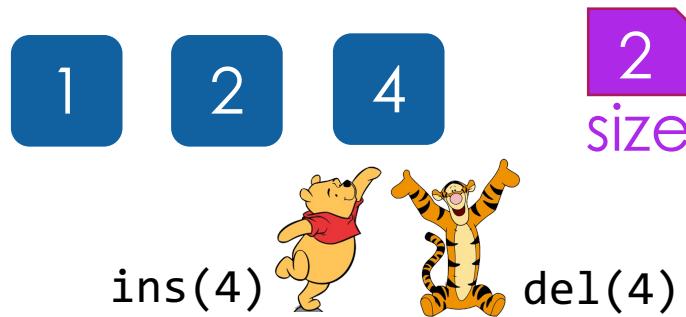
The problem:    not atomic



incorrect size

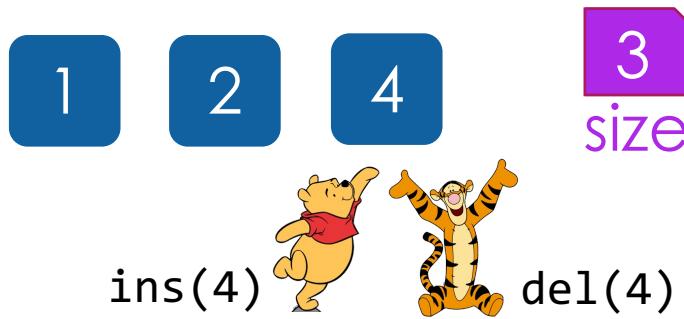
# Concurrent Size

- ✓ For efficiency: metadata
- ✓ For correctness: atomically update data structure & metadata:  
ins / del linearized at metadata update



# Concurrent Size

- ✓ For efficiency: metadata
- ✓ For correctness: atomically update data structure & metadata
- ✓ For progress:



# Concurrent Size

- ✓ For efficiency: metadata
- ✓ For correctness: atomically update data structure & metadata
- ✓ For progress:



How update metadata exactly once?

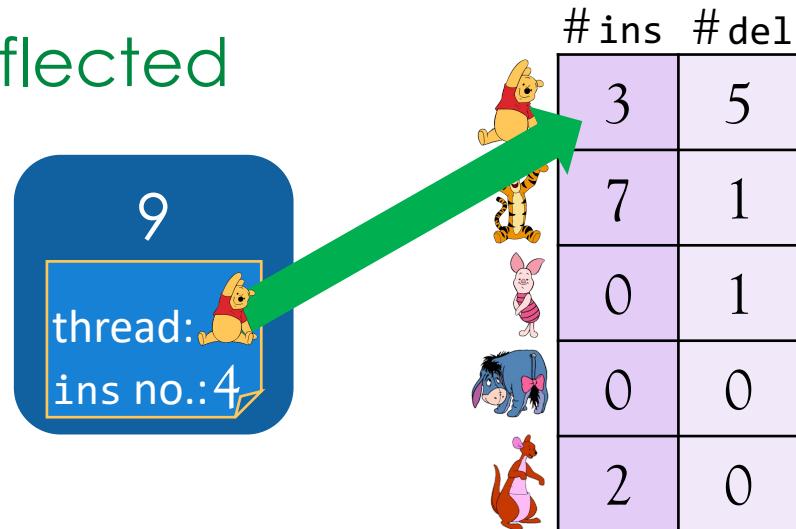
Using suitable metadata → Threads can determine whether reflects certain op, otherwise update

# Metadata: Monotonically Increasing Counters

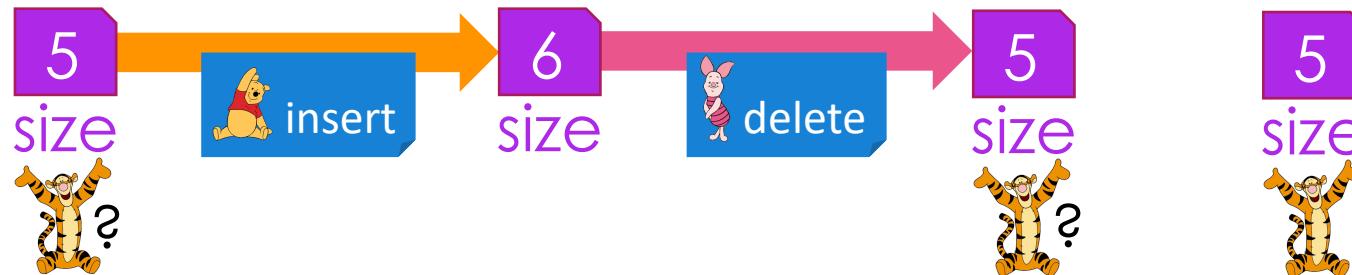
	# ins	# del
	3	5
	7	1
	0	1
	0	0
	2	0

# Metadata: Monotonically Increasing Counters

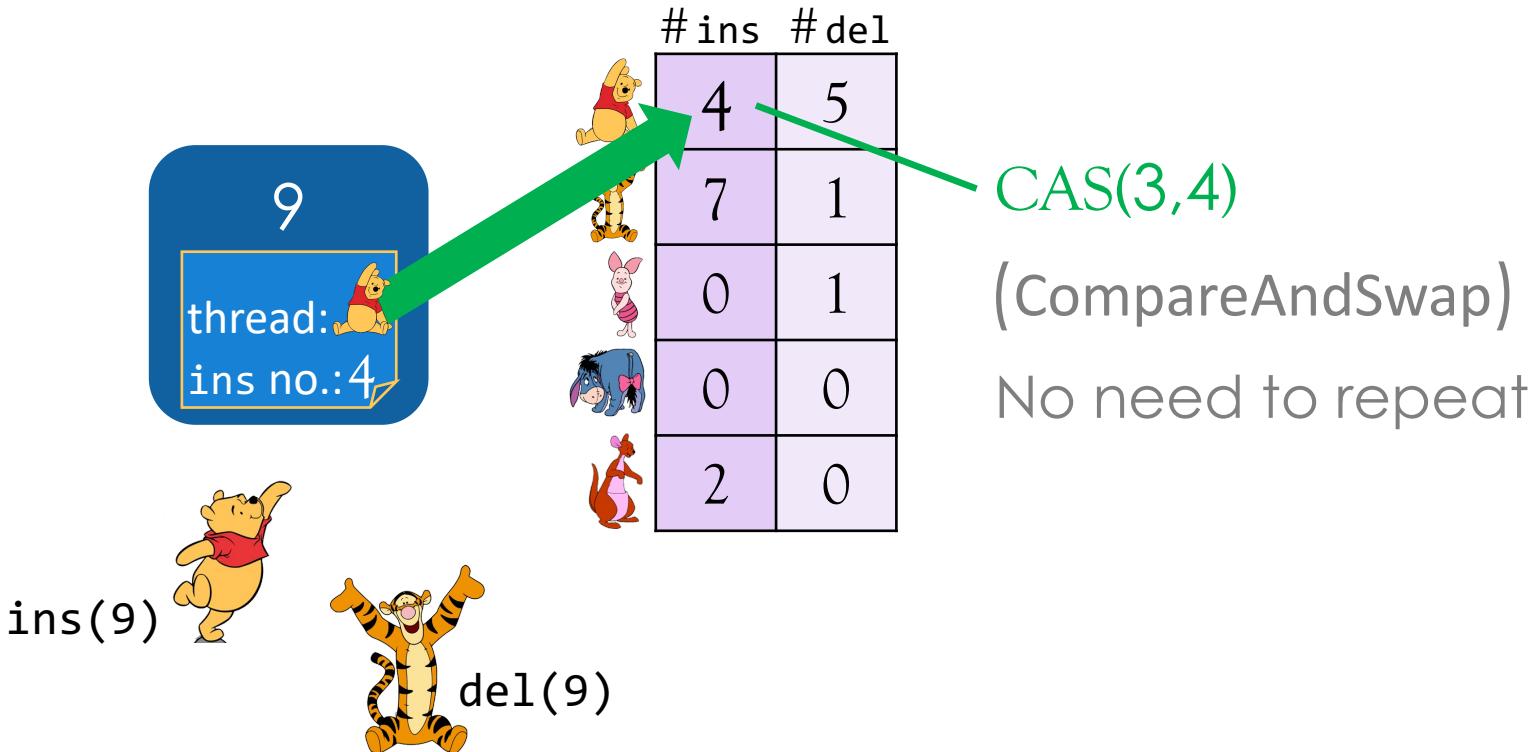
Easy to detect if certain op is reflected



Unlike size field, or even  $\#ins - \#del$  per thread



# Metadata: Monotonically Increasing Counters



# Compute Size from Metadata

	#ins	#del
	3	5
	7	1
	0	1
	0	0
	2	0

$$\text{size} = \sum (\#ins - \#del)$$



# Compute Size from Metadata requires snapshot

ins(9)



del(9)



#ins #del

1	0
0	0
0	0
0	0
0	1

$$\text{size} = \sum(\#\text{ins} - \#\text{del}) = -1$$



# Compute Size from Metadata requires snapshot

	# ins	# del
	1	0
	0	0
	0	0
	0	0
	0	1

Traversal → inconsistent size

Need small linearizable snapshot

not of all items ☺

$$\text{size} = \sum (\# \text{ins} - \# \text{del})$$



# Compute Size from Metadata requires snapshot

	# ins	# del
	1	0
	0	0
	0	0
	0	0
	0	1

Traversal → inconsistent size

Need small linearizable snapshot

Jayanti [2005], Petrank & Timnat [2013]

$$\text{size} = \sum (\# \text{ins} - \# \text{del})$$



# Efficient Size

Our size mechanism



Snapshot-based size



Adaptation of BST  
by Wei et al. [2021]

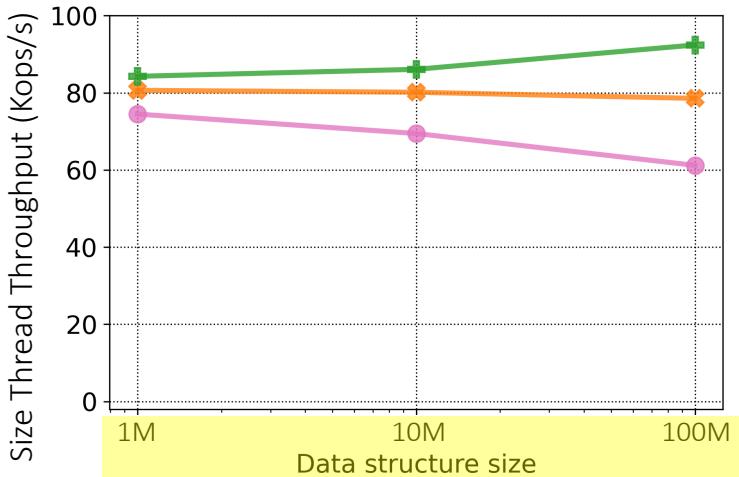
Skiplist by Petrank  
& Timnat [2013]



# Efficient Size

## Our size mechanism

—●— SizeHashTable    —◆— SizeBST    —+— SizeSkipList

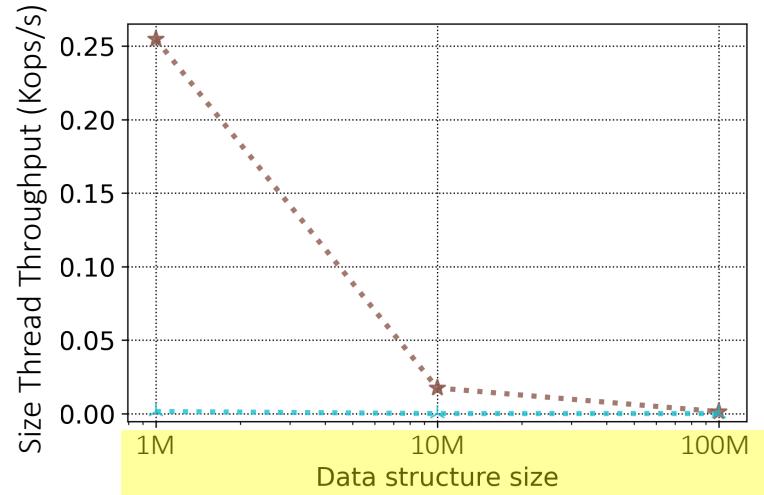


31 threads:  
1 thread:

3% ins, 2% del, 95% contains  
size → measure its throughput

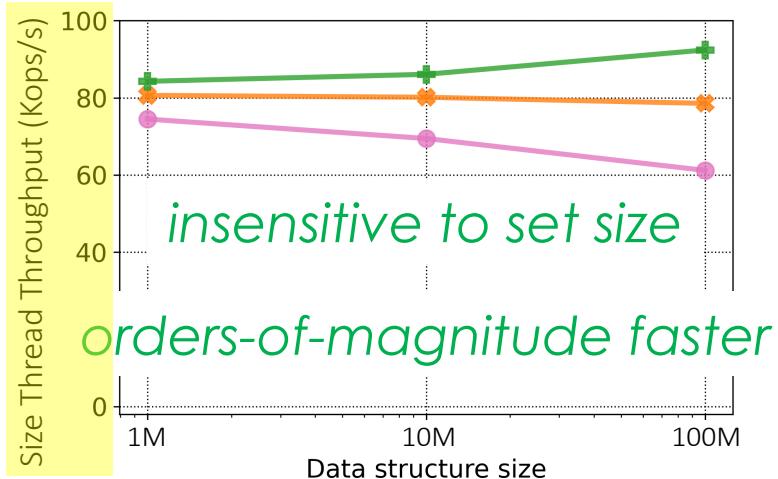
## Snapshot-based size

—★— VcasBST-64    —△— SnapshotSkipList



# Efficient Size

## Our size mechanism



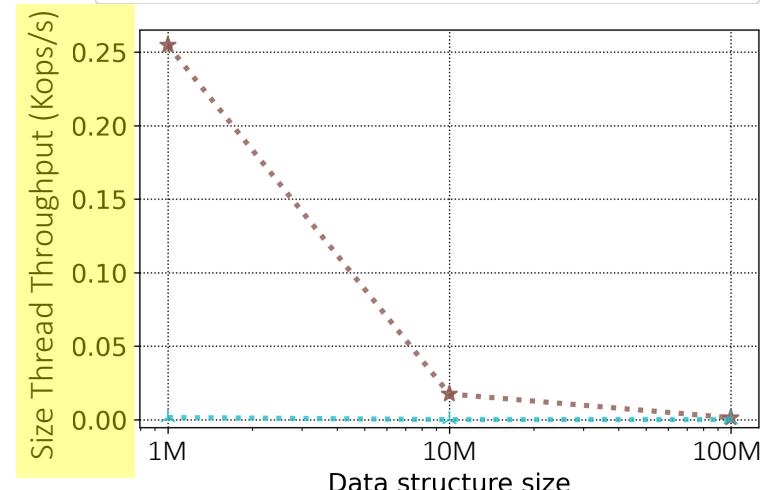
31 threads:

1 thread:

3% ins, 2% del, 95% contains

size → measure its throughput

## Snapshot-based size



# Concurrent Size / Main Ideas

- ✓ Efficient (using metadata)
- ✓ Correct (using atomic update of set & metadata + metadata snapshot)
- ✓ Preserves progress (using  )
- ✗ Incurs overhead on ins, del, contains

Similar ideas in tree aggregate queries

# Trees

Set or dictionary

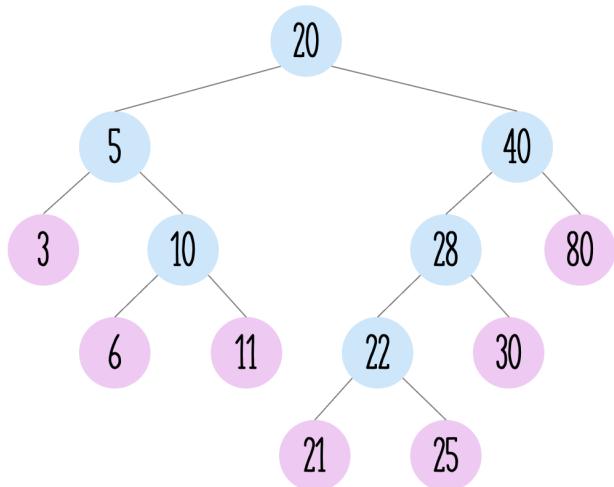
Keys



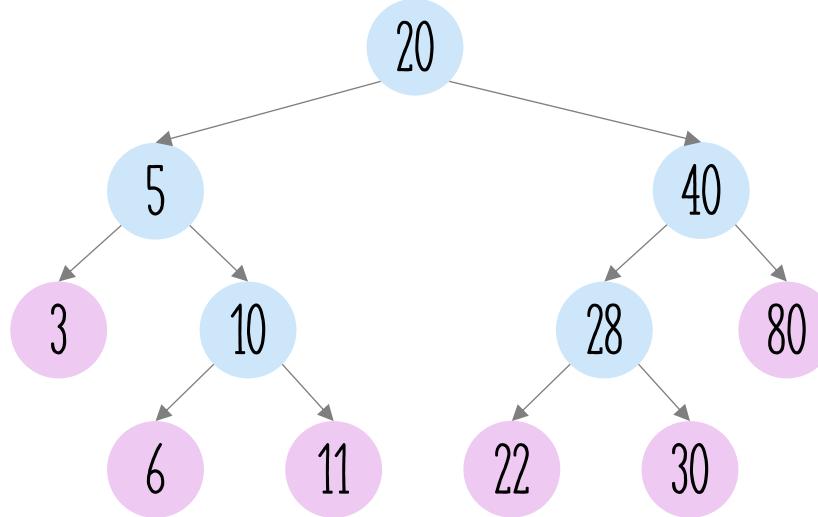
# Trees

Set or dictionary represented by binary search tree

Keys



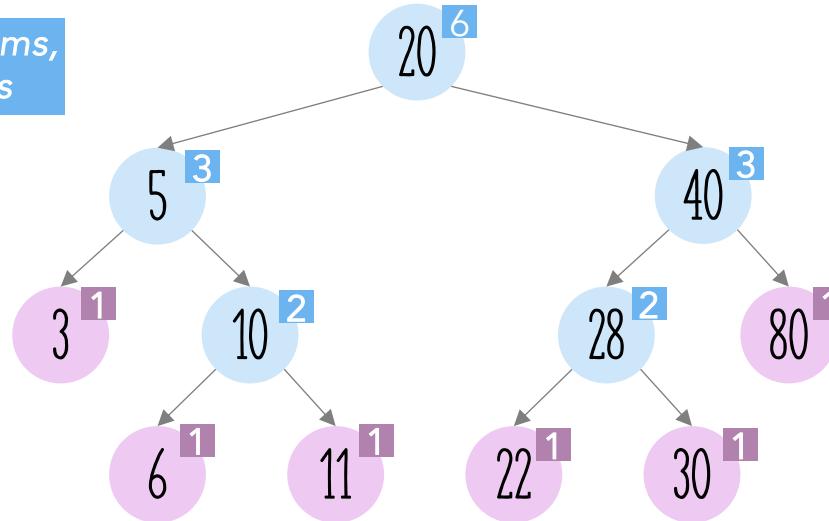
# Tree Aggregate Queries



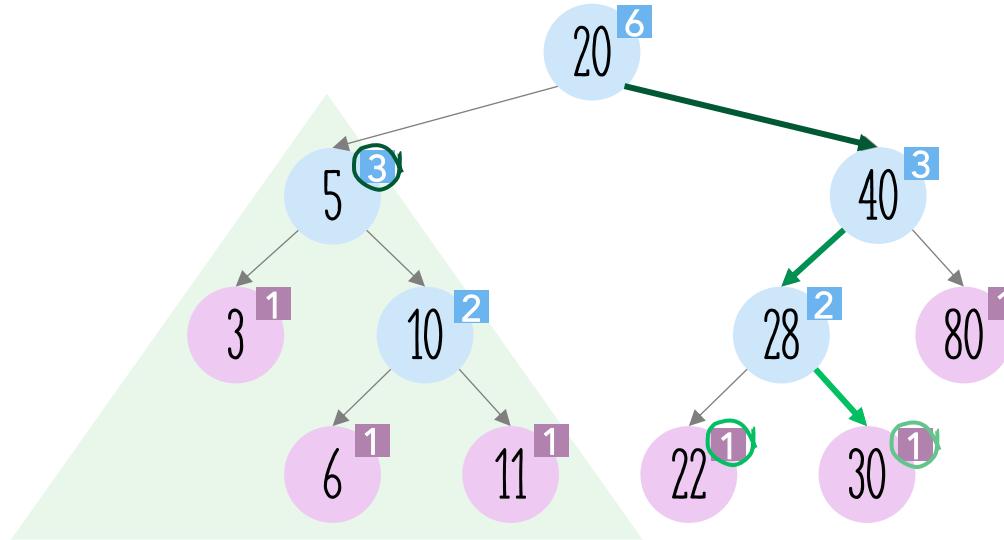
$\text{index}(30) = 5$

# Efficient Tree Aggregate Queries

*function of subtree's items,  
e.g., number of items*



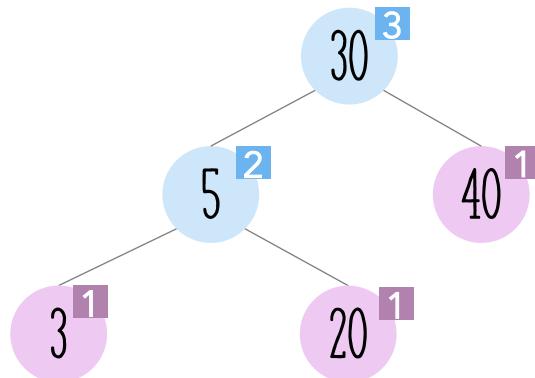
# Efficient Tree Aggregate Queries



$$\text{index}(30) = 3 + 1 + 1 = 5$$

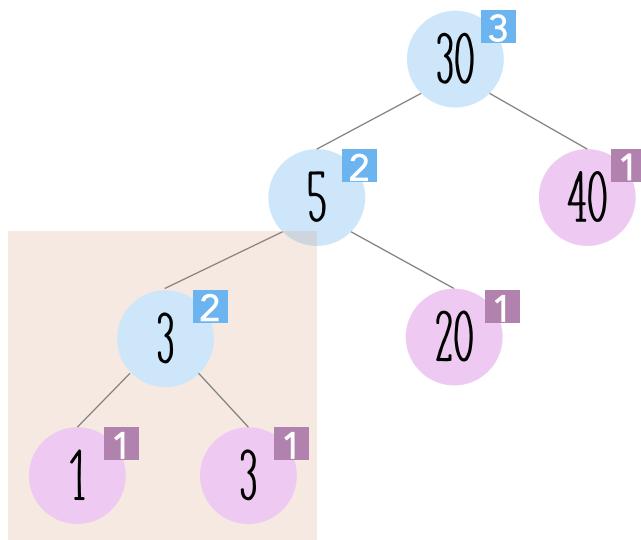
# Concurrent Tree Aggregate Queries

ins(1)



# Concurrent Tree Aggregate Queries

ins(1)

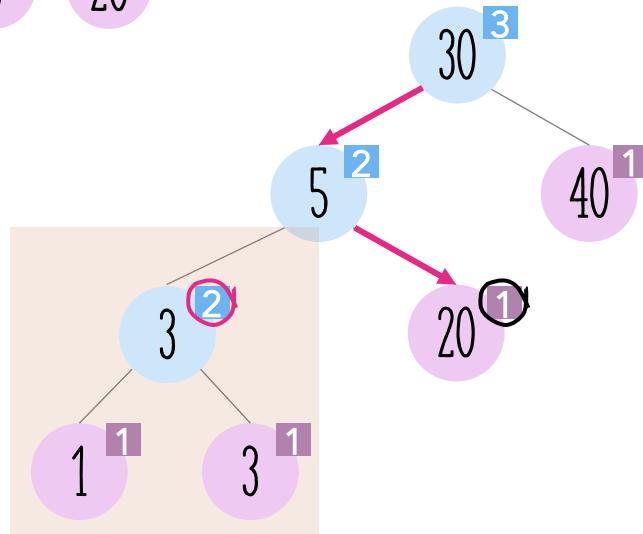


# Concurrent Tree Aggregate Queries

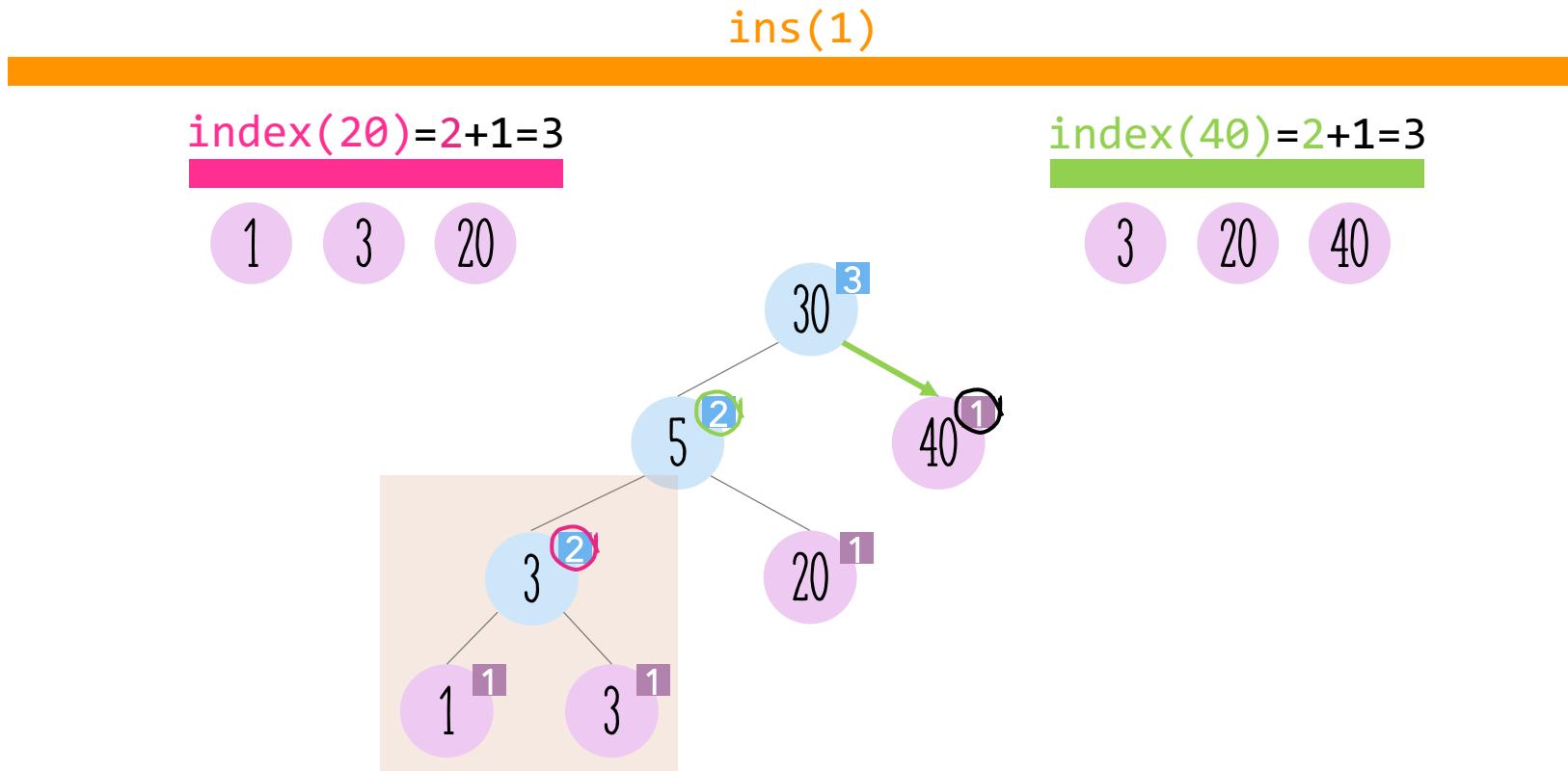
ins(1)

index(20)=2+1=3

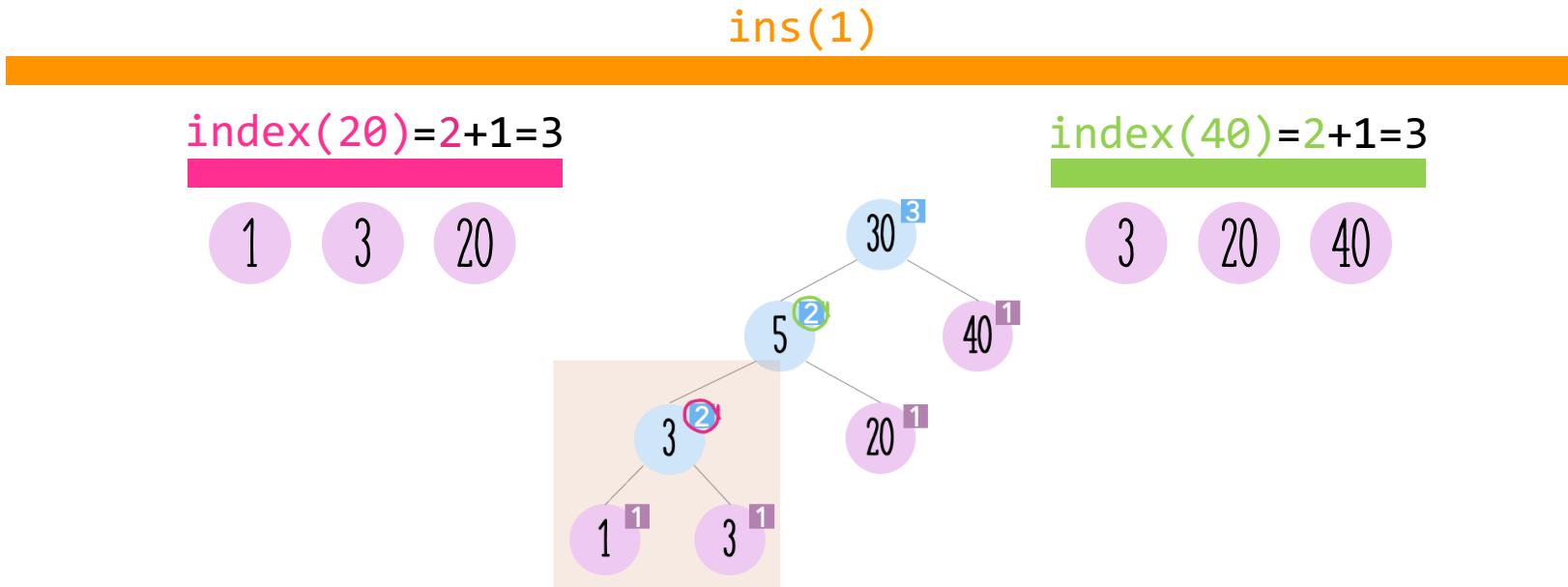
1    3    20



# Concurrent Tree Aggregate Queries



# Concurrent Tree Aggregate Queries



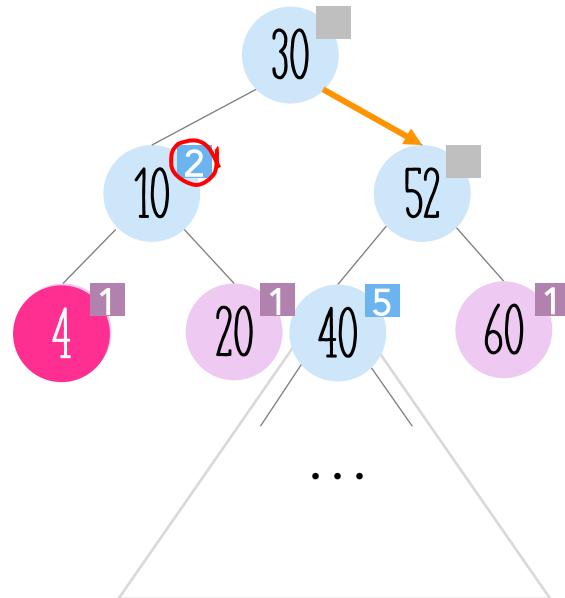
Problem: Some queries observe ins(1), others don't

Need atomic update of tree and all metadata

# Concurrent Tree Aggregate Queries

index(60)=2

del(4)



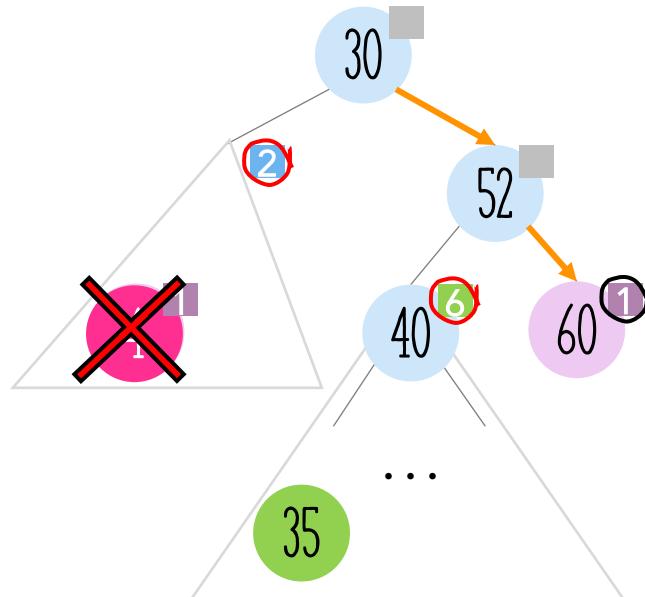
# Concurrent Tree Aggregate Queries

index(60)=2

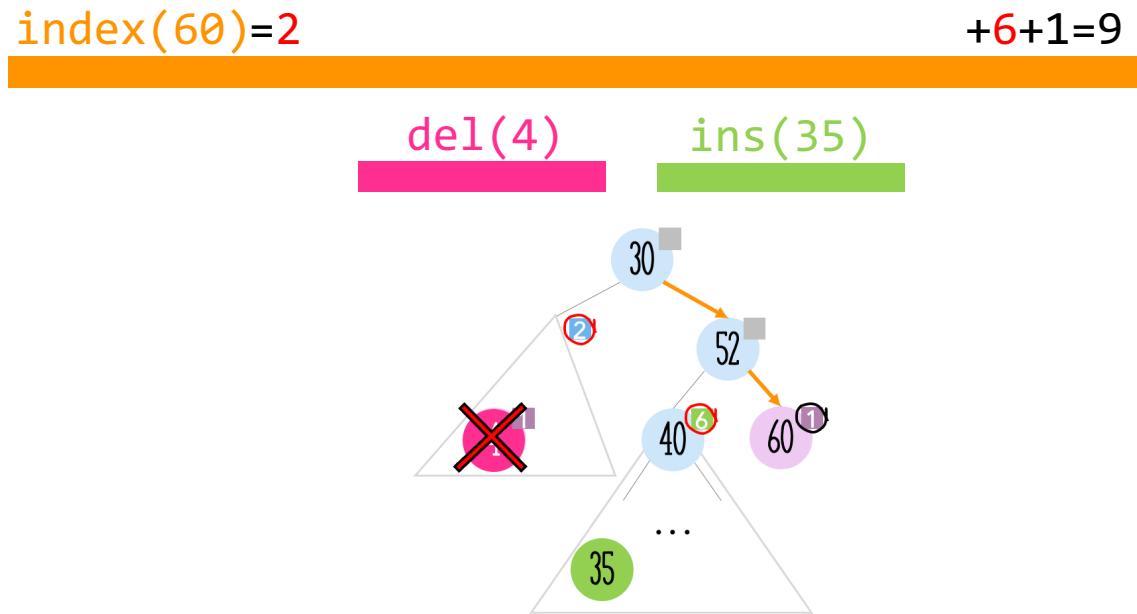
+6+1=9

del(4)

ins(35)



# Concurrent Tree Aggregate Queries



Problem: The query sees new updates after missing old updates

Queries should obtain a snapshot view of the traversed path

# Concurrent Tree Aggregate Queries

*Problem:* Updates modify multiple locations

→ Some queries see an update, others don't

Need atomic update of tree and all metadata

*Problem:* Queries read multiple values

→ Queries might see new updates after missing old updates

Queries should obtain a snapshot view of the traversed path

# Wait-Free Trees with Asymptotically-Efficient Range Queries

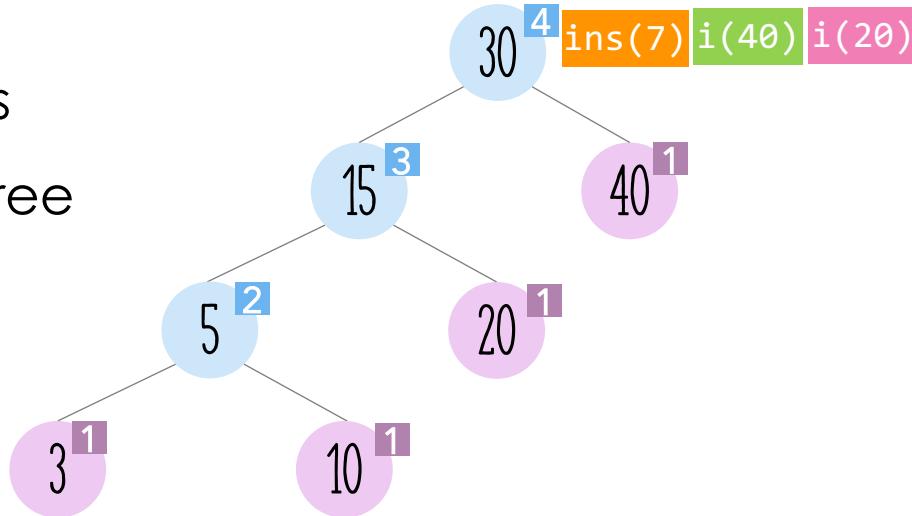
*Ilya Kokorin, Victor Yudov, Vitaly Aksenov, and Dan Alistarh,*

IPDPS'24

# Concurrent Tree Aggregate Queries

Kokorin, Yudov, Aksenenov, and Alistarh

Op queues in all nodes  
with ops to apply to subtree

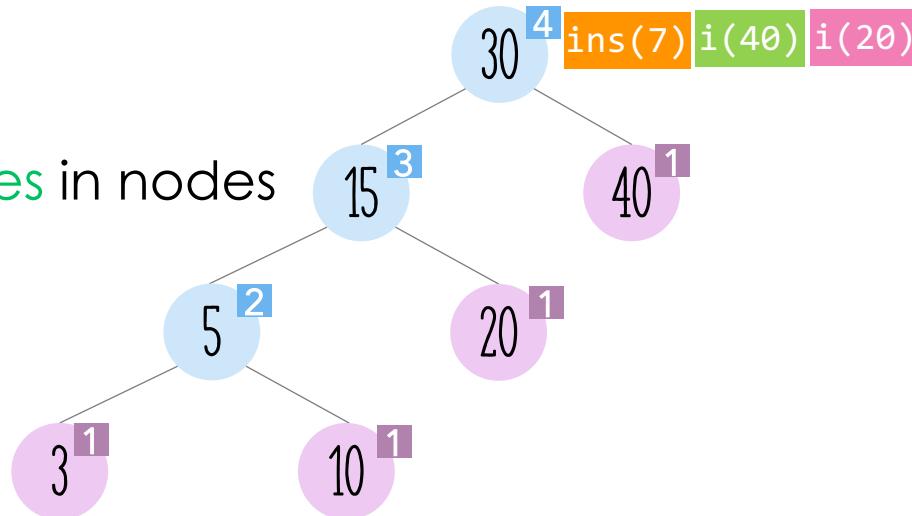


# Concurrent Tree Aggregate Queries

Kokorin, Yudov, Aksenov, and Alistarh

Serialize on root

Advance through op queues in nodes  
while helping others

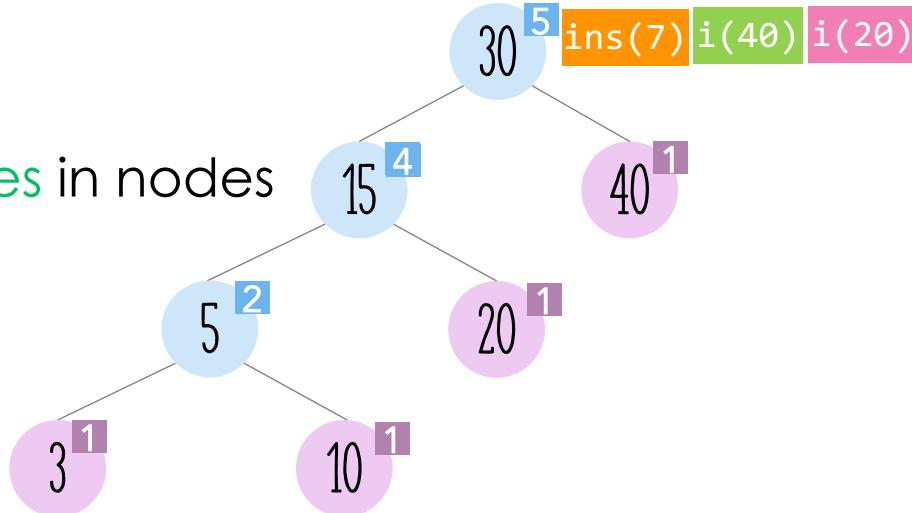


# Concurrent Tree Aggregate Queries

Kokorin, Yudov, Aksenov, and Alistarh

Serialize on root

Advance through op queues in nodes  
while helping others



# Concurrent Tree Aggregate Queries

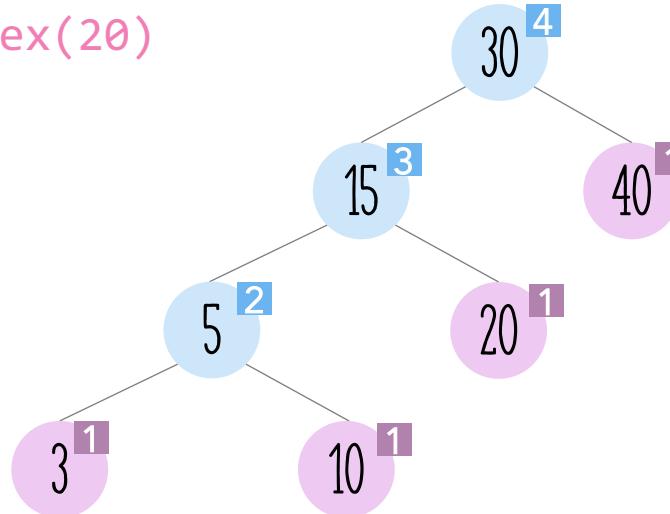
Kokorin, Yudov, Aksenov, and Alistarh

ins(7)    index(40)    index(20)

Goal:

index(40), index(20)

consider ins(7)

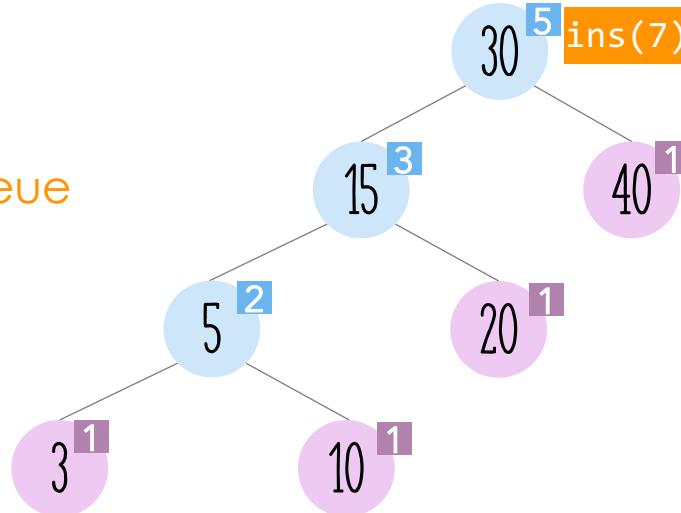


# Concurrent Tree Aggregate Queries

Kokorin, Yudov, Aksakov, and Alistarh

ins(7)  
ts=11

Serialize op: Add to root queue  
and obtain timestamp

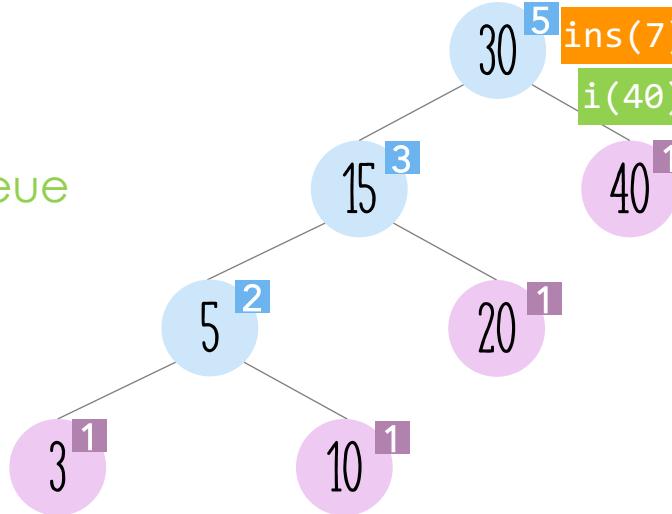


# Concurrent Tree Aggregate Queries

Kokorin, Yudov, Aksenov, and Alistarh

$\text{ins}(7)$      $\text{index}(40)$   
ts=11               ts=12

Serialize op: Add to root queue  
and obtain timestamp

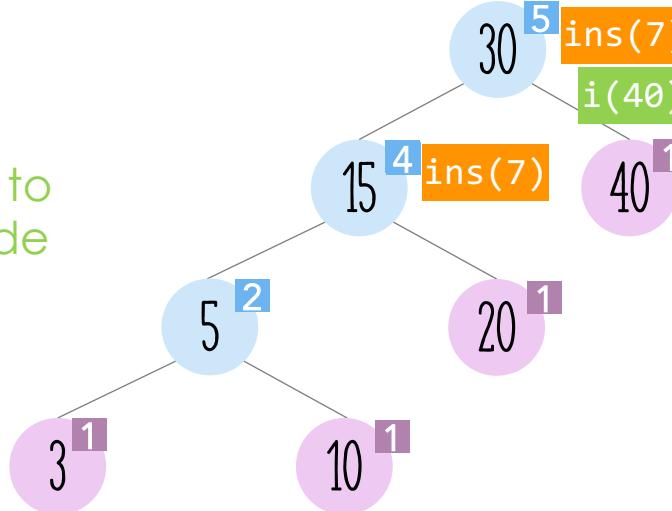


# Concurrent Tree Aggregate Queries

Kokorin, Yudov, Aksenenov, and Alistarh

$\text{ins}(7)$      $\text{index}(40)$   
 $\text{ts}=11$                  $\text{ts}=12$

Advance all operations up to  
ts=12 in each traversed node

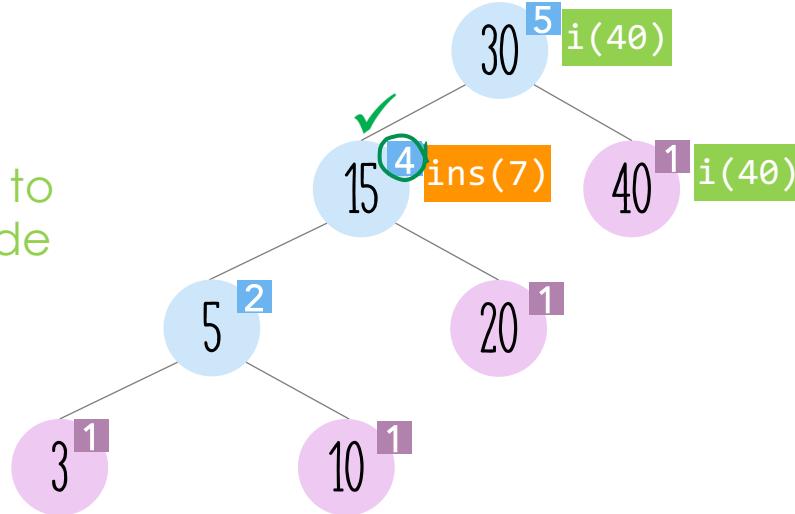


# Concurrent Tree Aggregate Queries

Kokorin, Yudov, Aksenenov, and Alistarh

$\text{ins}(7)$      $\text{index}(40)$   
 $\text{ts}=11$                  $\text{ts}=12$

Advance all operations up to  
 $\text{ts}=12$  in each traversed node

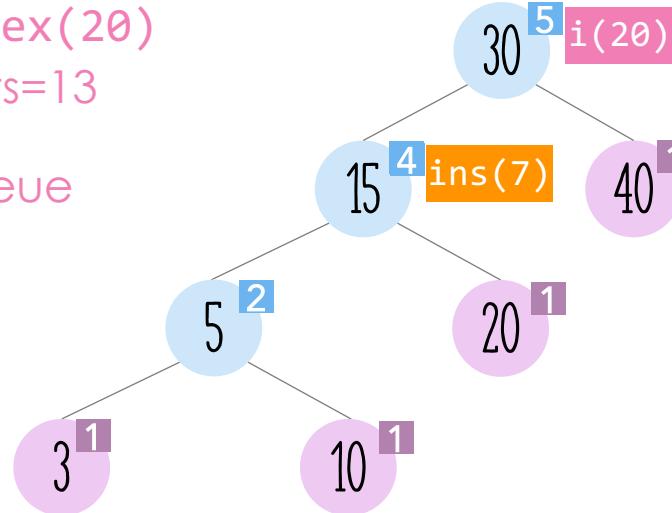


# Concurrent Tree Aggregate Queries

Kokorin, Yudov, Aksenenov, and Alistarh

ins(7)    index(40)    index(20)  
ts=11       ts=12       ts=13

Serialize op: Add to root queue  
and obtain timestamp

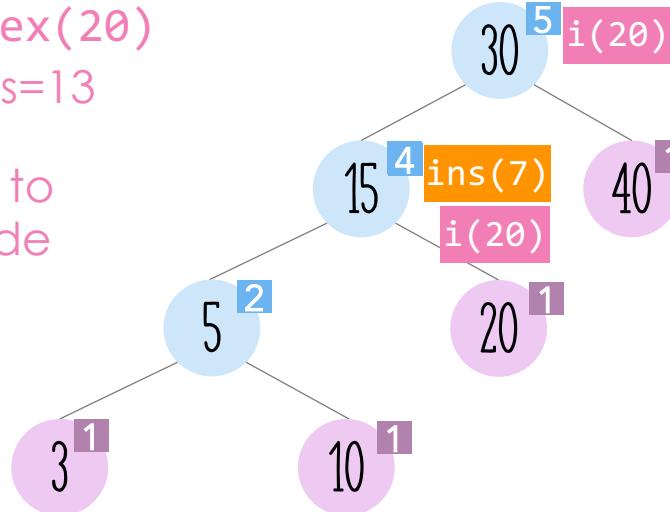


# Concurrent Tree Aggregate Queries

Kokorin, Yudov, Aksenenov, and Alistarh

ins(7)    index(40)    index(20)  
ts=11        ts=12        ts=13

Advance all operations up to  
ts=13 in each traversed node

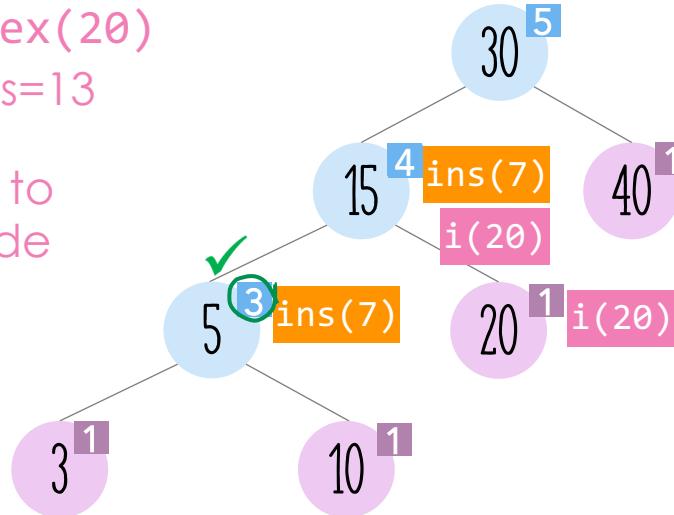


# Concurrent Tree Aggregate Queries

Kokorin, Yudov, Aksenenov, and Alistarh

$\text{ins}(7)$      $\text{index}(40)$      $\text{index}(20)$   
ts=11               ts=12               ts=13

Advance all operations up to  
ts=13 in each traversed node



# Concurrent Tree Aggregate Queries

Kokorin, Yudov, Aksenov, and Alistarh

ins(7)      index(40)      index(20)  
ts=11            ts=12            ts=13

Goal:

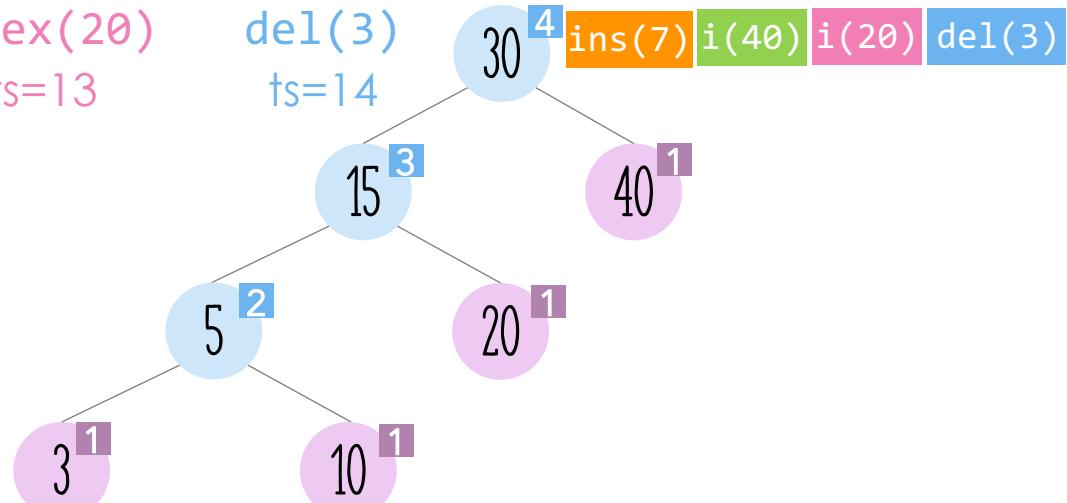
index(40), index(20)

consider ins(7)

Goal:

index(40), index(20)

don't consider del(3)



# Concurrent Tree Aggregate Queries

Kokorin, Yudov, Aksenov, and Alistarh

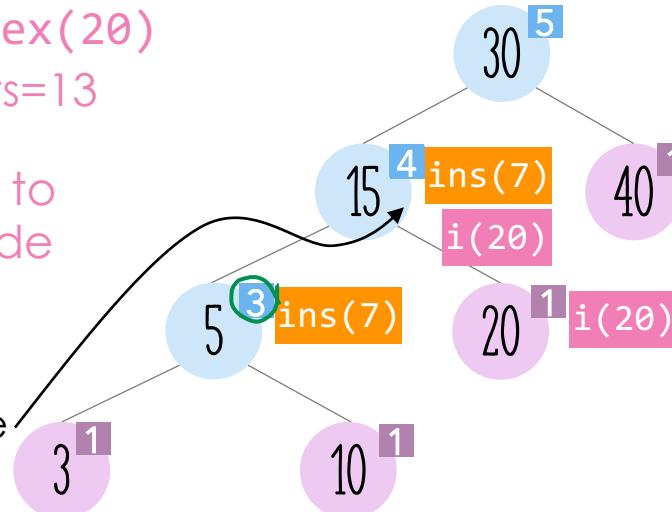
ins(7)  
ts=11

index(20)  
ts=13

Advance all operations up to  
ts=13 in each traversed node

Thanks to timestamps:

- index(20) keeps executing
- ins(7) doesn't enqueue here



# Concurrent Tree Aggregate Queries

Kokorin, Yudov, Aksenov, and Alistarh

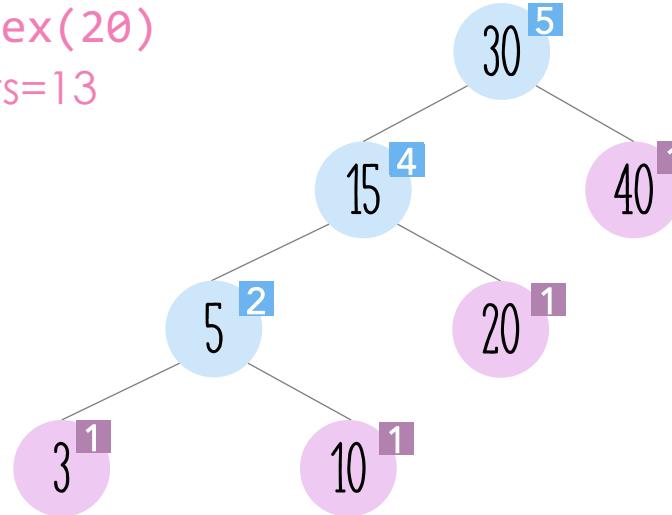
## Main Ideas

- ❖ Op queues in all nodes
- ❖ Serialize on root
- ❖ Advance through op queues in nodes while helping others to form virtual snapshot view

# Concurrent Tree Aggregate Queries

Kokorin, Yudov, Aksenov, and Alistarh

ins(7)      index(40)      index(20)  
ts=11            ts=12            ts=13



No support for failing operations

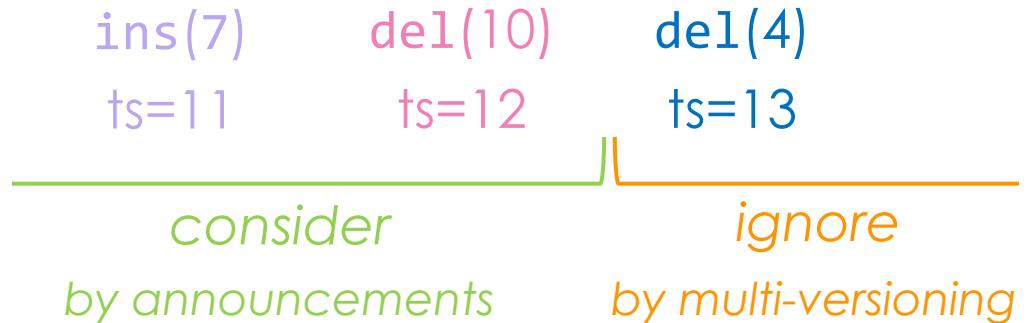
# Concurrent Aggregate Queries

*Gal Sela and Erez Petrank*

*DISC'24*

# Timestamps

Ongoing update operations

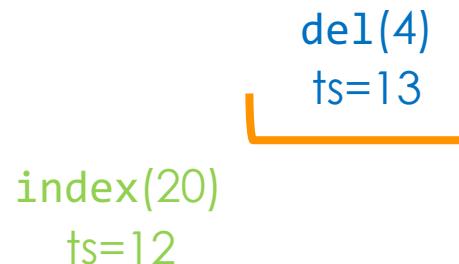


Aggregate queries

index(20)  
ts=12

# Multi-Versioning

to ignore concurrent updates  
with bigger timestamps



Similar to multi-versioning for snapshots

Wei et al. [PPoPP'21]

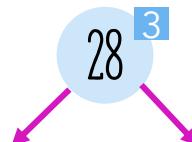
# Multi-Versioning

to ignore concurrent updates  
with bigger timestamps

index(20)  
ts=12

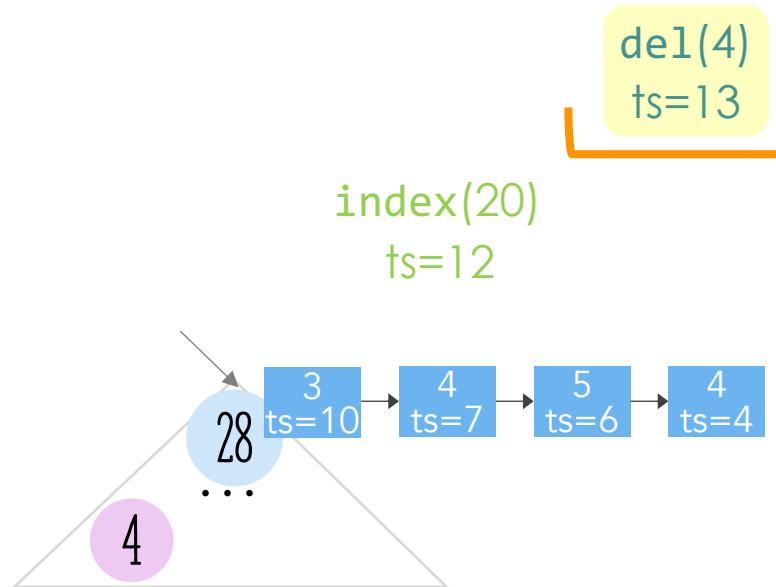
del(4)  
ts=13

aggregate value, child pointers → version lists



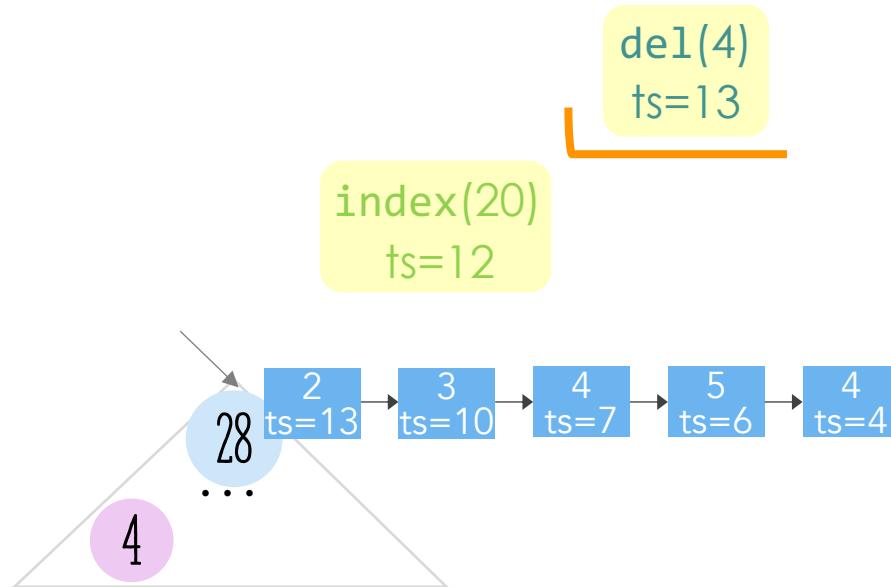
# Multi-Versioning

to ignore concurrent updates  
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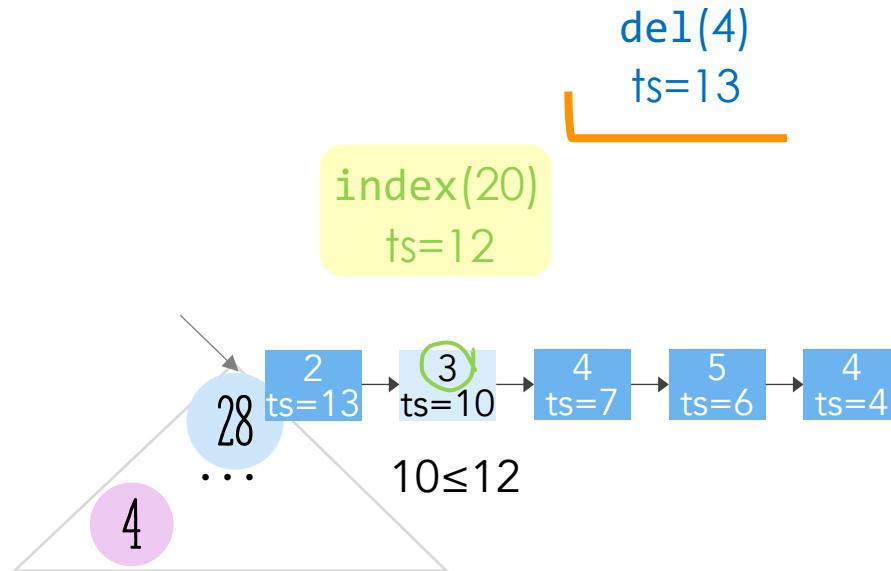
# Multi-Versioning

to ignore concurrent updates  
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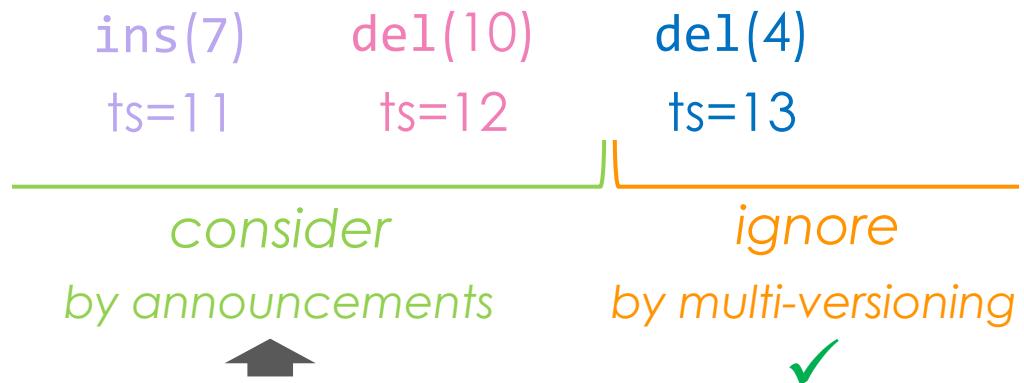
# Multi-Versioning

to ignore concurrent updates  
with bigger timestamps



# Timestamps

Ongoing update operations



Aggregate queries

index(20)  
ts=12

# Announcements

to consider concurrent updates  
with timestamps  $\leq$  query

Ongoing update operations

ins(7)

ts=11



del(10)

ts=12



Aggregate queries



index(20)  
ts=12

# Concurrent Aggregate Queries

## Design Main Ideas

- ❖ Timestamps
- ❖ Multi-versioning
- ❖ Announcements

2 implementing algorithms – optimizing either  
*update time or aggregate query time*

# Timestamps in FastQueryTree

By enqueueing to announcement queue



# Timestamps in FastUpdateTree

global  
timestamp

3

Incremented  
by aggregate  
queries

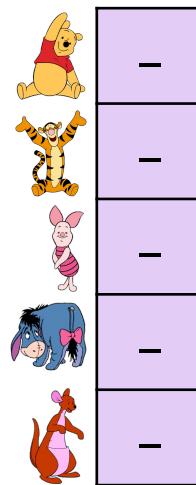
# Timestamps in FastUpdateTree

global  
timestamp

3

Incremented  
by aggregate  
queries

announcement  
array

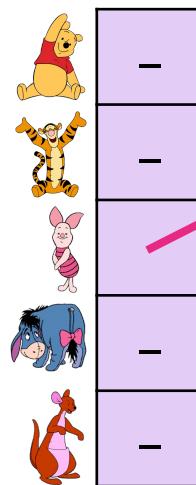


# Timestamps in FastUpdateTree

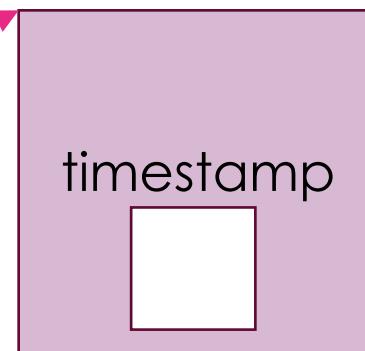
global  
timestamp

3

announcement  
array



announcement

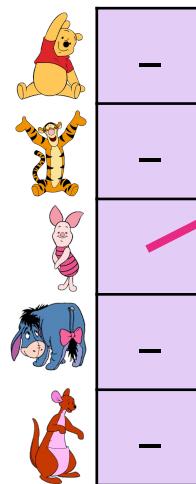


# Timestamps in FastUpdateTree

global  
timestamp

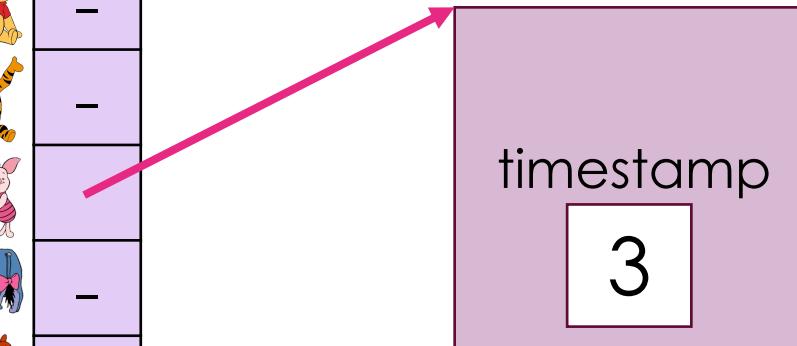
3

announcement  
array



announcement

timestamp  
3

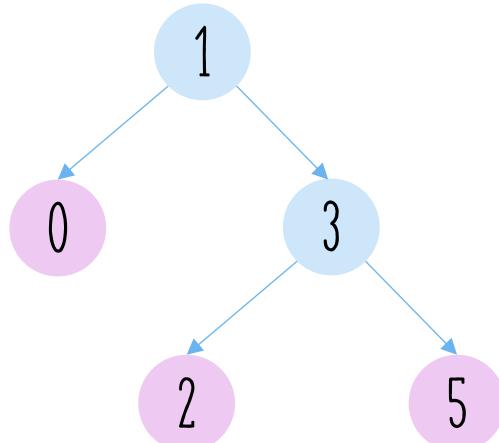


# Lock-Free Augmented Trees

*Panagiota Fatourou and Eric Ruppert*

DISC'24

# Lock-Free Augmented Trees

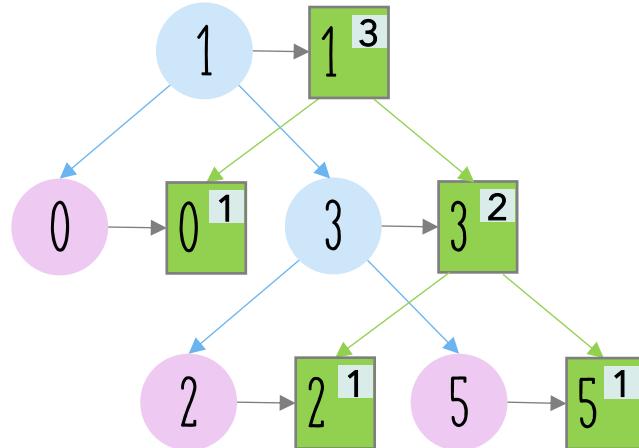


## Multi-versioning

- ❖ No version lists
- ❖ No timestamps
  - Order determined by arrival at root

# Lock-Free Augmented Trees

ins(4)

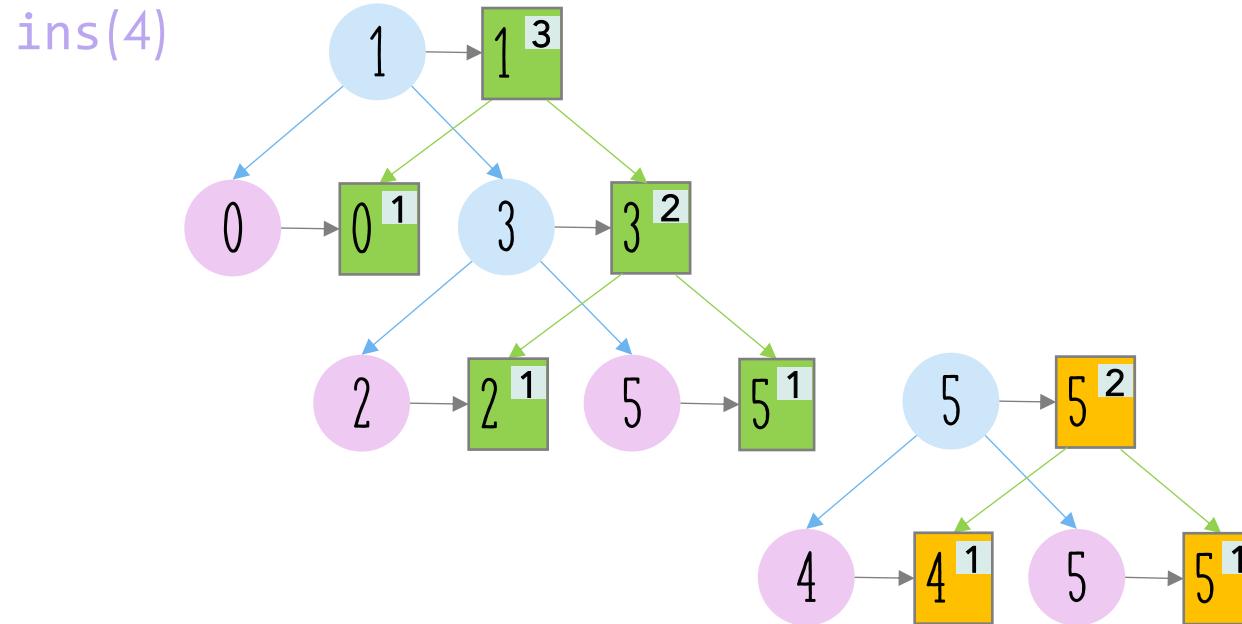


Multi-versioning

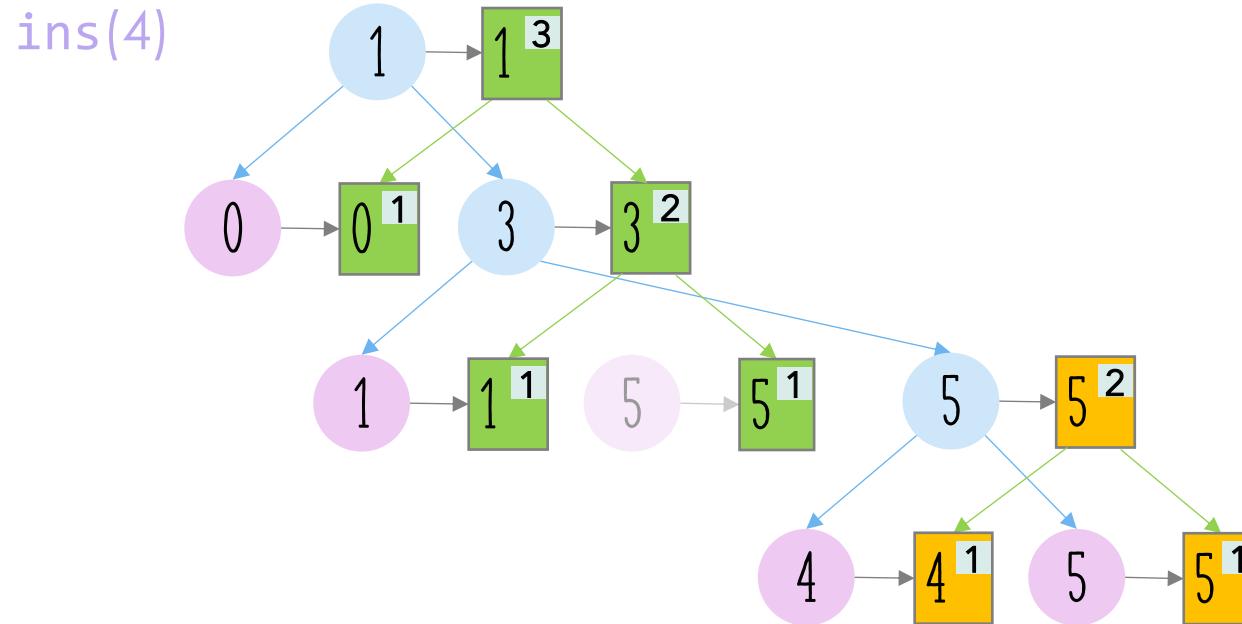
Tree replication

with aggregate metadata

# Lock-Free Augmented Trees

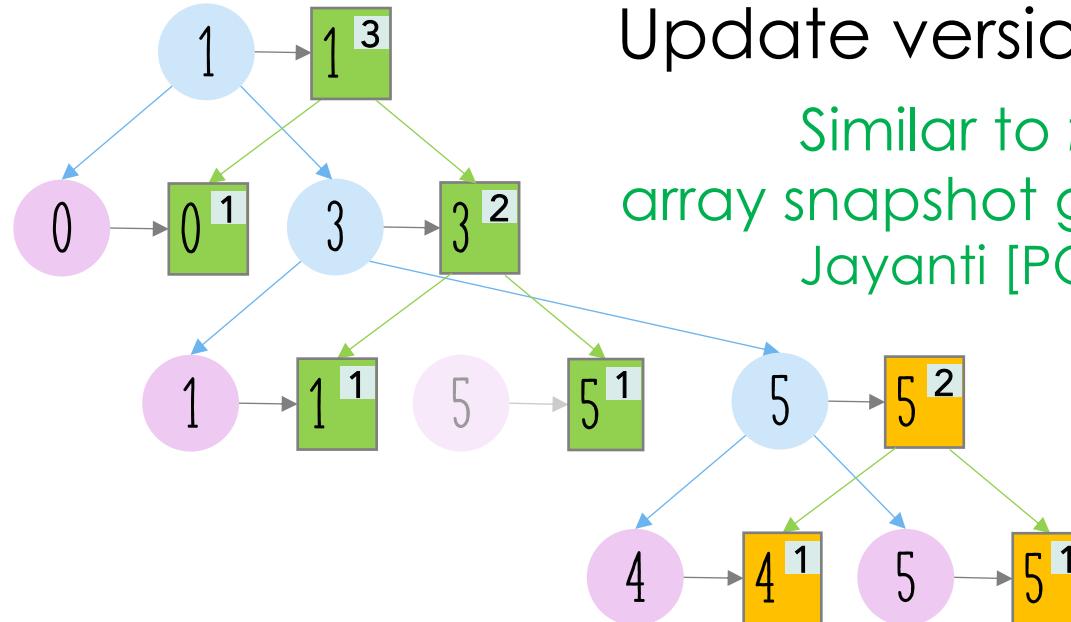


# Lock-Free Augmented Trees



# Lock-Free Augmented Trees

ins(4)

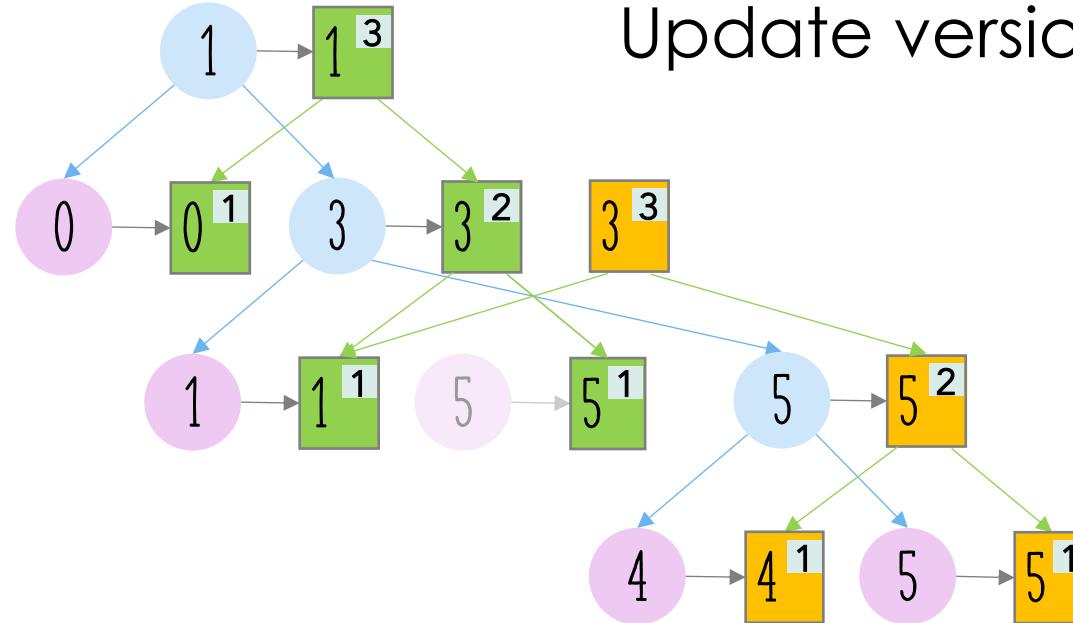


Update versions upwards

Similar to *f*-Arrays  
array snapshot generalization  
Jayanti [PODC'02]

# Lock-Free Augmented Trees

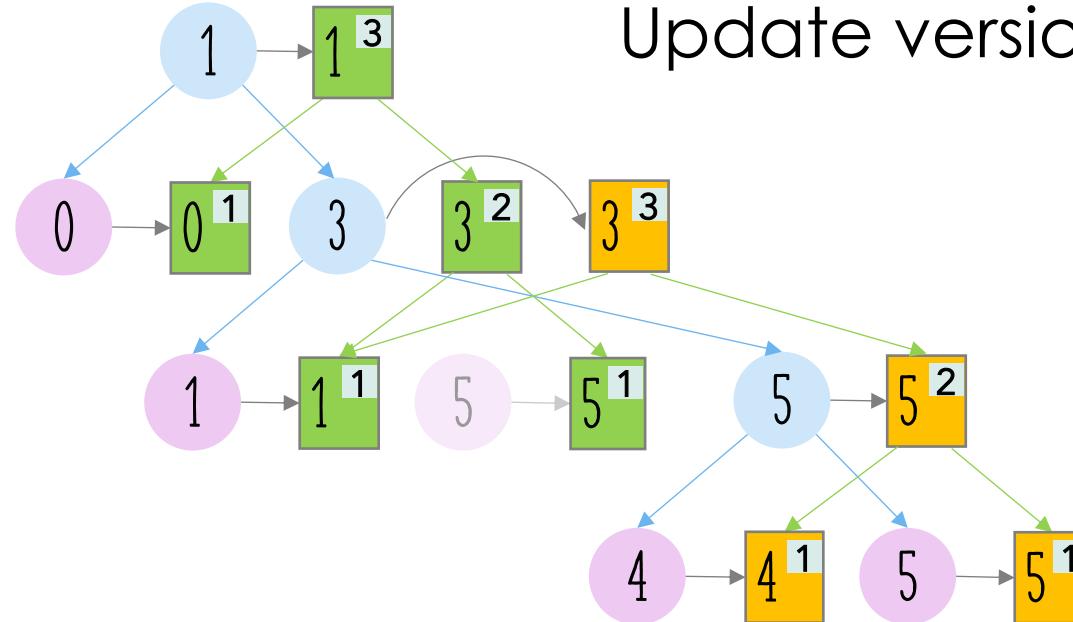
ins(4)



Update versions upwards

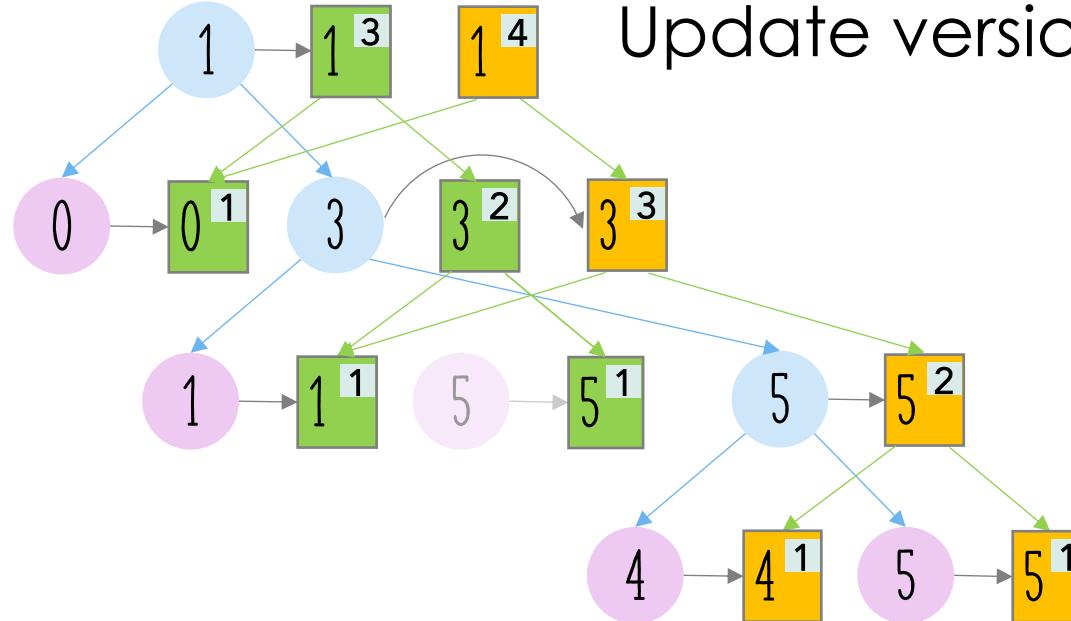
# Lock-Free Augmented Trees

ins(4)



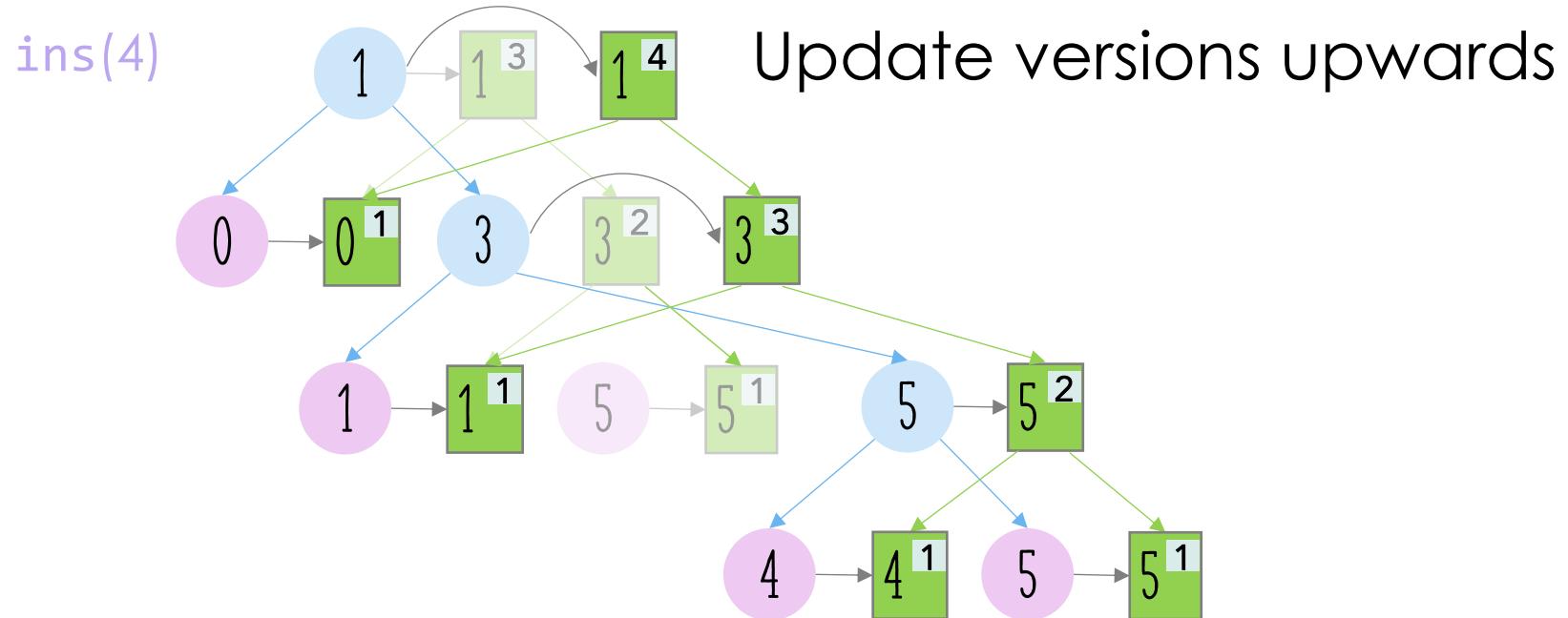
# Lock-Free Augmented Trees

ins(4)

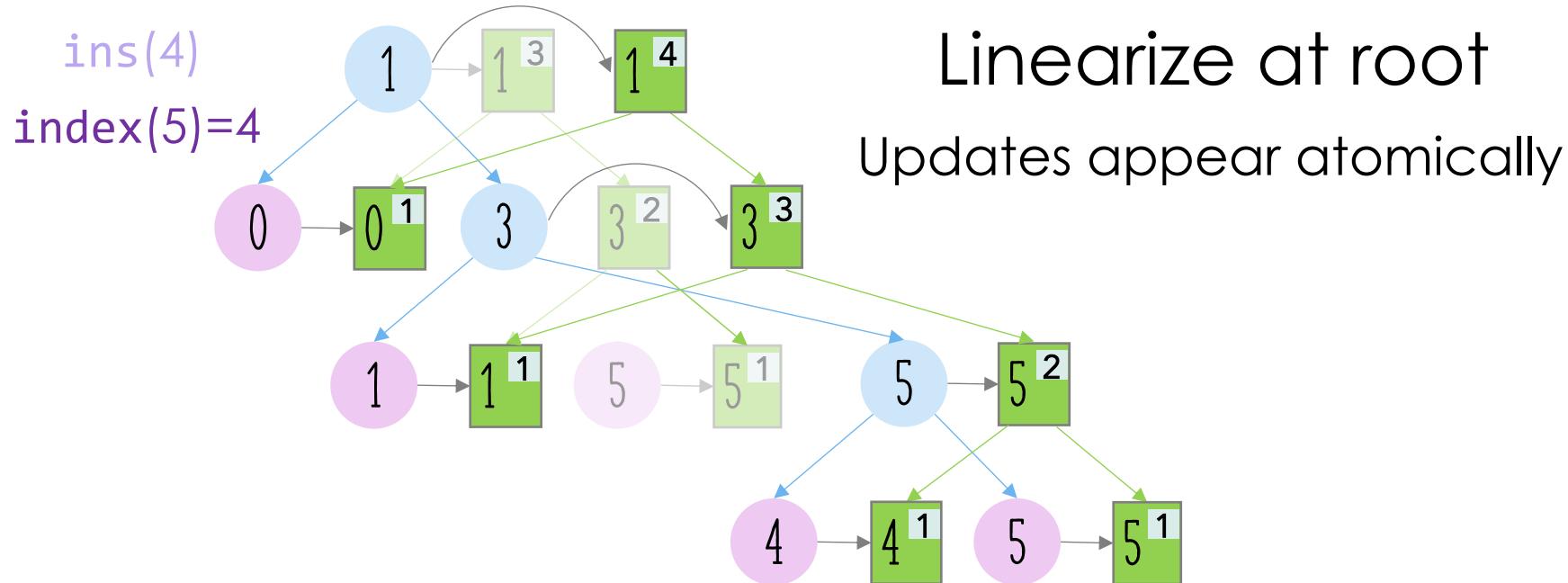


# Update versions upwards

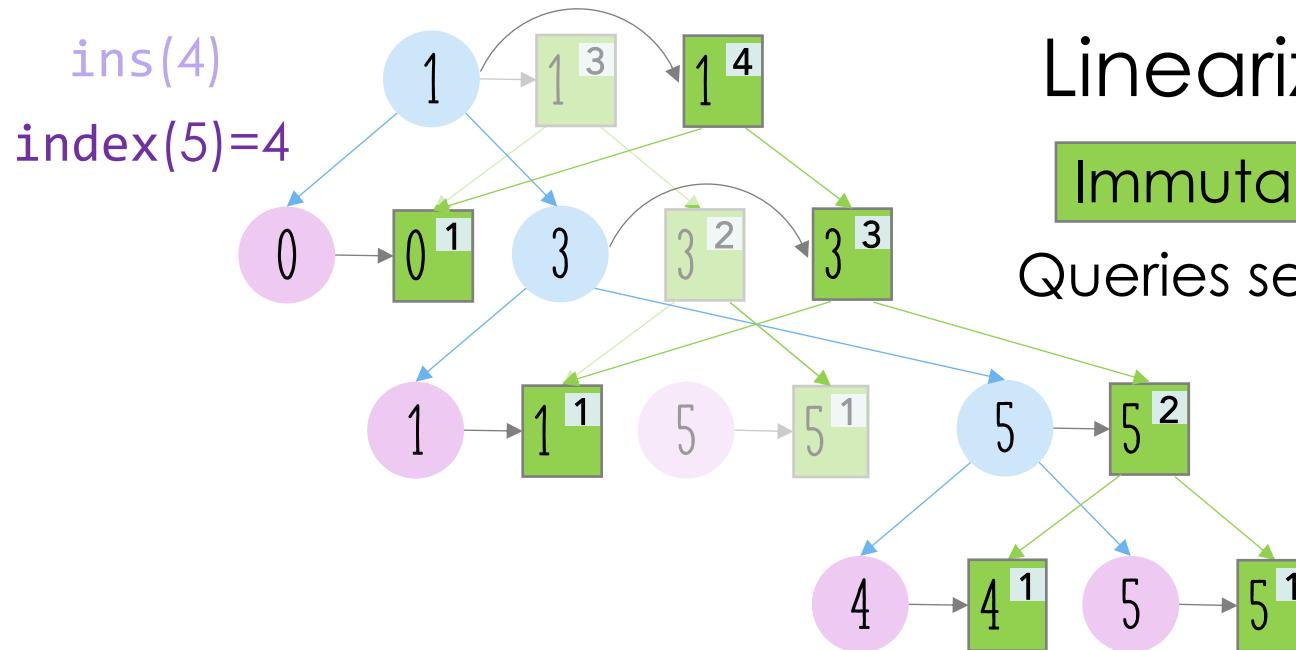
# Lock-Free Augmented Trees



# Lock-Free Augmented Trees



# Lock-Free Augmented Trees



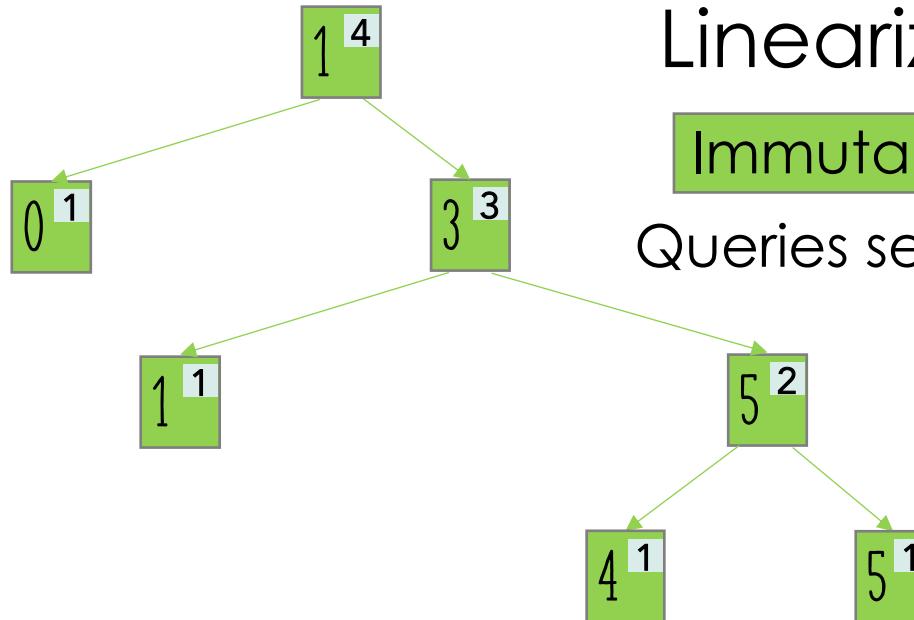
Linearize at root

Immutable versions

Queries see a snapshot

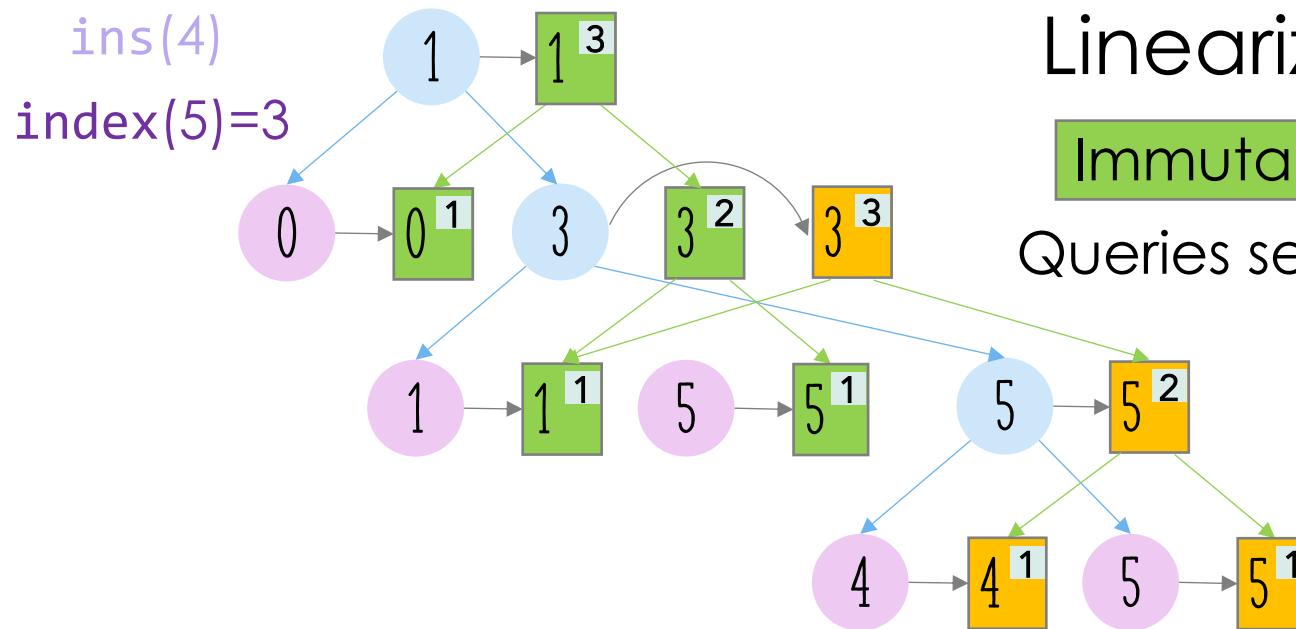
# Lock-Free Augmented Trees

$\text{ins}(4)$   
 $\text{index}(5)=4$



Linearize at root  
Immutable versions  
Queries see a snapshot

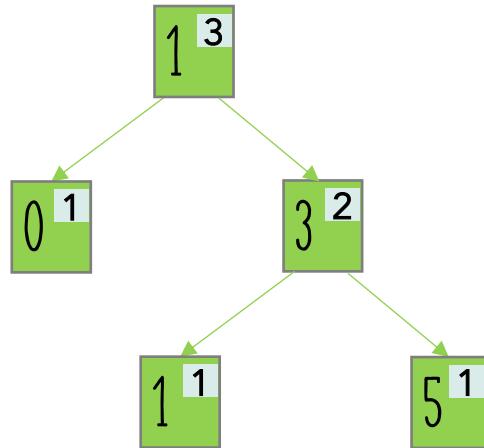
# Lock-Free Augmented Trees



Linearize at root  
Immutable versions  
Queries see a snapshot

# Lock-Free Augmented Trees

$\text{ins}(4)$   
 $\text{index}(5)=3$



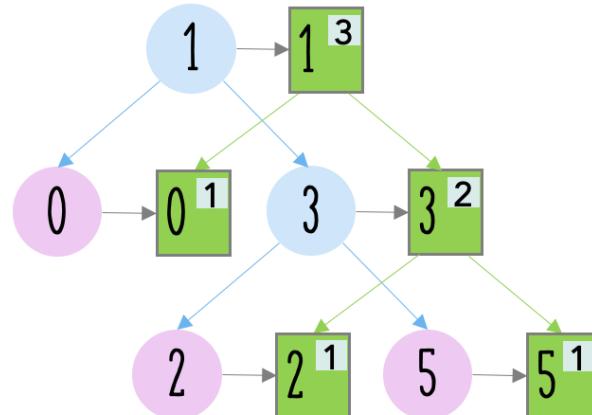
Linearize at root  
Immutable versions  
Queries see a snapshot

# Lock-Free Augmented Trees

## Main Ideas

### Multi-versioning

- ❖ No version lists
- ❖ No timestamps
  - Order determined by arrival at root



# Outlook

- ❖ Fast solutions (to be used in libraries)
  - ❖ Reduce overhead, possibly relax progress or correctness
  - ❖ Investigate trade-offs
    - ❖ between time of existing ops and aggregate queries
    - ❖ time-space

# Outlook

- ❖ Fast solutions (to be used in libraries)
- ❖ Memory management for multi-versioning
- ❖ Apply to more data structures
- ❖ Apply to more operations (not only queries)