

## 4.4 Optimization

Absolute Extrema of a function  $f$ .

If  $f(x) \leq f(c)$  (resp.  $f(x) \geq f(c)$ ) for all  $x$  in the domain of  $f$ , then  $f(c)$  is called the absolute maximum <sup>value</sup> of  $f$ . ~~(resp. absolute minimum value)~~ (resp. absolute minimum ~~value~~).

### Theorem (Extreme Value Theorem)

If a function  $f$  is continuous on a closed interval  $[a, b]$ , then  $f$  has both an absolute maximum value and an absolute minimum value on  $[a, b]$ .

Closed Interval Method: This gives us the algo for finding absolute max/min on a closed, bounded interval  $[a, b]$ . <sup>They</sup> ~~It~~ always exists by the theorem above.

- ① Find critical numbers that lie in open interval  $(a, b)$ .  
(Next, we will treat these as well as  $a$  &  $b$  as crit. pts.)
- ② Compute  $f$  at each critical number; compute  $f(a)$ ,  $f(b)$ .
- ③ The largest out of these is absolute max.  
The least " " " is absolute min.