

CODE :

```
def knapSack_dp(m, W, P, n):
    """
    Solves the 0/1 Knapsack problem using Dynamic Programming (Tabulation).

    m: Knapsack capacity
    W: List of item weights
    P: List of item profits (values)
    n: Number of items
    """
    # Create a 2D DP table V[i][w] to store max profit for first i items and capacity w
    # (n+1 rows for items 0 to n, m+1 columns for weights 0 to m)
    V = [[0 for _ in range(m + 1)] for _ in range(n + 1)]

    # Fill the dp table using the recurrence relation
    #  $V[i][w] = \max(V[i-1][w], P[i-1] + V[i-1][w - W[i-1]])$ 
    for i in range(1, n + 1):
        # Current item's profit and weight (using 0-based indexing for lists P and W)
        p_i = P[i-1]
        w_i = W[i-1]
        for w in range(m + 1):
            if w_i <= w:
                # Case 1: Item i is included
                profit_with_i = p_i + V[i-1][w - w_i]
                # Case 2: Item i is NOT included
                profit_without_i = V[i-1][w]
                V[i][w] = max(profit_without_i, profit_with_i)
            else:
                # Item i cannot be included (weight w_i is greater than current capacity w)
                V[i][w] = V[i-1][w]

    # Print the DP table (similar to the format in the document)
    print("DP Table (Item i vs. Capacity w):")
    # Header: Capacity w
    print(" | ", end="")
    for w in range(m + 1):
        print(f"{w:2}", end=" ")
    print("\n" + "---" * (m + 3))
    # Body: Item i
    for i in range(n + 1):
        print(f"{i:2} | ", end="")
        for w in range(m + 1):
            print(f"{V[i][w]:2}", end=" ")
        print()

    # Backtrack to find selected items
    selected = [0] * n
    current_w = m
    max_profit = V[n][m]

    for i in range(n, 0, -1):
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# Check if the profit came from the previous row (item i was NOT included)
if V[i][current_w] == V[i-1][current_w]:
    # Item i was NOT included
    selected[i-1] = 0
else:
    # Item i WAS included
    selected[i-1] = 1
    # Subtract item's weight and move to the state before including it
    current_w -= W[i-1]

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# Print selected items
print("\n--")
print("Sequence of Decisions (x1, x2, x3, x4):")
print(f"Items: {selected} (1: included, 0: not included)")
# Print maximum value
print(f"Maximum Profit: {max_profit}")

return max_profit

```

Driver code

```

P = [1, 2, 5, 6] # Profits
W = [2, 3, 4, 5] # Weights
m = 8 # Knapsack capacity
n = len(P) # Number of items

```

```
knapSack_dp(m, W, P, n)
```

OUTPUT :

```
(base) kjcoemr@kjcoemr-HP-Pro-SFF-280-G9-Desktop-PC:~/Desktop/BE-15\$ python knapsack_dynamic_programming.py
```

DP Table (Item i vs. Capacity w):

	0	1	2	3	4	5	6	7	8
0	0	0	0	0	0	0	0	0	0
1	0	0	1	1	1	1	1	1	1
2	0	0	1	2	2	3	3	3	3
3	0	0	1	2	5	5	6	7	7
4	0	0	1	2	5	6	6	7	8

Sequence of Decisions (x1, x2, x3, x4):

Items: [0, 1, 0, 1] (1: included, 0: not included)

Maximum Profit: 8

```
(base) kjcoemr@kjcoemr-HP-Pro-SFF-280-G9-Desktop-PC:~/Desktop/BE-15\$
```