

Divisibility-

- Solution: 1. **(d) 114345.**
- Solution: 2. **Remainder = 0**
- Solution: 3. The two nearest numbers to 19506 which are divisible by **9** are **19503** and **19512**.
- Solution: 4. The value of **M = 7** and **N = 2**.
- Solution: 5. There are **5 pairs** of X and Y that make the number **763X4Y2** divisible by 9.
- Solution: 6. **Remainder = 2**
- Solution: 7. **P = 3**
- Solution: 8. The smallest whole number in place of **X = 6**.
- Solution: 9. **(d) n + 60**
- Solution: 10. The largest and smallest possible values of M are **9 and 0**, respectively. The product of these values is equal to **0** times **9** which equals to **0**.

Factors-

- Solution: 1. The number of prime factors in the expression **$6^4 \times 8^6 \times 10^8 \times 14 \times 10^x \times 22^{12}$** is **72**.
- Solution: 2. The number of perfect square factors of N is equal to **16**.
- Solution: 3. The exponent of two in $12^3 \times 30^4 \times 35^2$ is $(3 + 4 + 0) = 7$. Therefore, there are $(7 + 1) = 8$ even factors.
- Solution: 4. The minimum exponents for each prime factor in N and M are:
- For two: $\min(7, 4) = 4$.
 - For three: $\min(4, 2) = 2$.
 - For five: $\min(0, 1) = 0$.
- Therefore, there are $(4 + 1)(2 + 1)(0 + 1) = 15$ common factors between N and M.
- Solution: 5. The number $(N - 1)$ has **4 factors**.
- Solution: 6. The smallest possible value of A is **33**.
- Solution: 7. The total number of factors of **10!** is equal to **792**.
- Solution: 8. Even perfect squares factors are = **16**.
- Solution: 9. The number **480** can be written as a product of two natural numbers in **20 ways**.

Solution: 10. The factors of $2^5 \times 3^4 \times 5^3$ that are not the factors of $2^3 \times 5^4 \times 7^5$ are = **48**.

Unit digits (Cyclicity)-

Solution: 1. The unit digit in the product $(3^{65} \times 6^{59} \times 7^{71})$ is **4**.

Solution: 2. The unit digit of the product $(173)^{45} \times (152)^{77} \times (777)^{999}$ is **2**.

Solution: 3. The unit's digit of the number $6^{256} - 4^{256}$ is **2**.

Solution: 4. The unit's digit in the sum $264^{102} + 264^{103}$ is **0**.

Solution: 5. The unit digit of $(316)^{3n} + (1)$ is **7**.

Solution: 6. The unit digit in $(7^{95} - 3^{58})$ is **4**.

Solution: 7. The rightmost non-zero digit of the number 30^{2720} is **6**.

Solution: 8. The last digit of the number obtained by multiplying the numbers **$81 \times 82 \times 83 \times 84 \times 86 \times 87 \times 88 \times 89$** is **2**.

Solution: 9. The last three-digits of the product: 12345×54321 is **666045**.

Solution: 10. $1^5 + 2^5 + 3^5 + 4^5 + 5^5 + 6^5 + 7^5 + 8^5 + 9^5 =$ **330,794**.

Remainders-

Solution: 1. The remainder when 7^{25} is divided by 6 is **1**.

Solution: 2. The remainder when 3^{45} is divided by 8 is **3**.

Solution: 3. The remainder when 4^{96} is divided by 6 is **4**.

Solution: 4. The remainder is **4**.

Solution: 5. The remainder when 67^{99} is divided by 7 is **4**.

Solution: 6. The remainder is **32**.

Solution: 7. The remainder is **5**.

Solution: 8. The remainder is **16**.

Solution: 9. The remainder is **0**.

Solution: 10. The remainder is **5**.

Factorials-

- Solution: 1. The highest power of 21 that divides 20! is 0.
- Solution: 2. The highest power of 32 that divides 31! is 0.
- Solution: 3. The largest number less than 28 which divides 28! is 27.
- Solution: 4. The number of zeroes at the end of 97! is 22.
- Solution: 5. The highest power of 12 that divides 54! is 13.
- Solution: 6. The least value of x such that $60!/2^x$ is an odd number is 57.
- Solution: 7. The least value of 'n' if no factorial can have 'n' zeroes is 4.
- Solution: 8. The highest power of 7! dividing 50! completely is 7.
- Solution: 9. The number of trailing zeroes in 625! is 156.
- Solution: 10. There are ****24**** zeroes at the end of this product.

HCF/LCM-

- Solution: 1. **(c) 9600**
- Solution: 2. **(c) 308**
- Solution: 3. **(c) 15**
- Solution: 4. **(a) 4**
- Solution: 5. **(a) 4**
- Solution: 6. **(b) 107**
- Solution: 7. **(c) 120**
- Solution: 8. **(c) 0.18**
- Solution: 9. **(b) 2**
- Solution: 10. **(b) 94**
- Solution: 11. **(b) 13**
- Solution: 12. **(c) 2523**
- Solution: 13. **(b) 42 m 36 s**
- Solution: 14. **(c) 322**
- Solution: 15. **(c) 1260**

Solution: 16. **(b) 21 cms**

Solution: 17. **(d) 89**

Solution: 18. **(b) 127**

Solution: 19. **(c) 40**

Solution: 20. **(c) 35 cms**

Solution: 21. **(d) 2**

Solution: 22. **(c) 99**

Solution: 23. **(a) 55/601**

Solution: 24. **(a) 91**

Problem on Numbers-

Solution: 1. The number of ones that the girl wrote while writing all the numbers from 100 to 200 is 121.

Solution: 2. The number of 8's that will be used to write this large natural number is 40.

Solution: 3. The value of a is 26.

Solution: 4. The number is 37.

Solution: 5. The remainder when the number formed by writing 1 to 29 side by side as: 12345678910... is divided by 9 is 3.

Solution: 6. The ratio of the unit's digit to the ten's digit in the original number is 2 😊.

Solution: 7. The number is 89.

Solution: 8. The largest number that divides the product of four consecutive even numbers completely is 48.