

Day-05

① Ramish walks \rightarrow 3km in 30 min

$$S = \frac{d}{t}$$

$$S = \frac{3}{0.5 \text{ hr}} = \boxed{6 \text{ km/hr} = \text{speed}}$$

② Train travels \rightarrow 50 km/hr
3 hrs \rightarrow ?

$$d = S \times t$$

$$= 50 \times 3$$

$$\boxed{d = 150 \text{ km}}$$

③ Train travels at 50 km/hr. ^{How} far will it go in 3 hr.

$$\text{Distance} = \text{speed} \times \text{Time}$$

$$= 50 \times 3$$

$$\boxed{d = 150 \text{ km}}$$

④ A cyclist covers 20 km in 1 hr 30 minutes.
What is his speed?

$$1 \text{ hr } 30 \text{ min} = 1.5 \text{ hr}$$

$$\text{Speed} = 20 / 1.5$$

$$\boxed{S = 13.33 \text{ km/hr}}$$

⑤ A boat goes 10 km downstream in 1 hr.
What is its speed downstream?

$$\text{Speed} = 10 \text{ km/hr}$$

$$\boxed{S = 10 \text{ km/hr}}$$

⑥ If a boat's speed in still water is 15 km/hr and stream speed is 5 km/hr, what is its speed upstream?

$$\text{Upstream speed} = 15 - 5 = 10 \text{ km/hr}$$

$$= \boxed{10 \text{ km/hr}}$$

⑦ A man walks 4 km upstream in 2 hrs.
What is his upstream speed?

$$\text{Speed} = 4 / 2$$

$$= \boxed{2 \text{ km/hr}}$$

$$\textcircled{8} \text{ Down stream, speed} = \frac{24}{2} \\ = 12 \text{ km/hr} \\ \text{Stream speed} = 12 - 10 = \underline{2 \text{ km/hr}}$$

$$\textcircled{9} \text{ speed} = \frac{300}{5} \\ s = \underline{60 \text{ km/hr}}$$

$$\textcircled{10} \text{ speed} = \frac{60}{3} \\ s = \underline{20 \text{ km/hr}}$$

$$\textcircled{11} \text{ Time} = \frac{\text{Distance}}{\text{speed}} \\ = \frac{240}{60} \\ t = \underline{4 \text{ hrs}}$$

$$\textcircled{2} \text{ Upstream speed} = \frac{30}{3} \\ = 10 \text{ km/hr}$$

$$\text{Downstream speed} = \frac{30}{2} \\ = 15 \text{ km/hr}$$

$$\text{Boat speed} = \frac{(15+10)}{2} \\ = \underline{12.5 \text{ km/hr}}$$

$$\text{Stream speed} = \frac{(15-10)}{2}$$

$$= \underline{2.5 \text{ km/hr}}$$

$$\textcircled{3} \text{ Upstream} = 20 - s = 15 \text{ km/hr} \\ = \underline{15 \text{ km/hr}}$$

$$\text{Downstream} = 20 + s \\ = \underline{25 \text{ km/hr}}$$

$$\textcircled{4} \text{ Speed} = \frac{\text{Distance}}{\text{Time}} \\ = \frac{120}{9} \\ = 13.33 \text{ m/s}$$

$$\text{Convert to km/hr} = 13.33 \times \frac{18}{5} \\ = \underline{48 \text{ km/hr}}$$

$$\textcircled{5} \text{ Relative speed} = \frac{(120+140)}{10} = \frac{260}{10} \\ = \underline{26 \text{ m/s}}$$

$$\textcircled{6} \text{ Upstream speed} = \frac{20}{4} = 5 \text{ km/hr}$$

$$\text{Downstream speed} = \frac{20}{3} \\ = 6.67 \text{ km/hr}$$

$$\text{Boat speed} = \frac{(5+6.67)}{2} \\ = \underline{5.8 \text{ km/hr}}$$

$$\begin{aligned} \text{Stream speed} &= ((6.67) - 5) / 2 \\ &= 0.83 \text{ km/hr} \end{aligned}$$

$$\textcircled{17} \text{ Downstream speed} = 5 + 2 = 7 \text{ km/hr}$$

$$\begin{aligned} \text{Time} &= 10 / 7 = 1.43 \text{ hr} \approx \\ &= 1 \text{ hour } 26 \text{ minutes} \end{aligned}$$

$$\textcircled{18} \text{ Let total distance} = 60 + 60 = 120 \text{ km}$$

$$\text{Time for 1st part} = 60 / 40 = 1.5 \text{ hr}$$

$$\text{Time for 2nd part} = 60 / 60 = 1 \text{ hr}$$

$$\text{Total time} = 2.5 \text{ hrs}$$

$$\begin{aligned} \text{Avg speed} &= \text{Total distance} \div \text{Total time} \\ &= 120 \div 2.5 \\ &= 48 \text{ km/hr} \end{aligned}$$

$$\textcircled{19} \text{ Downstream speed} = 48 / 3 = 16 \text{ km/hr}$$

$$\begin{aligned} \text{upstream speed} &= 48 / 4 \\ &= 12 \text{ km/hr} \end{aligned}$$

$$\text{Speed of boat} = ((16 + 12) / 2) = 14 \text{ km/hr}$$

$$\begin{aligned} \text{Speed of stream} &= ((16 - 12) / 2) \\ &= 2 \text{ km/hr} \end{aligned}$$

$$\textcircled{20} \text{ Total distance} = 100 + 200 = 300 \text{ m}$$

$$\begin{aligned} \text{speed} &= 60 \text{ km/hr} = (60 \times 1000) / 3600 \\ &= 16.67 \text{ m/s} \end{aligned}$$

$$\text{Time} = 300 / 16.67 \approx 18 \text{ seconds}$$

$$\textcircled{21} \text{ Let the boat speed} = x \text{ km/hr}$$

$$\text{Then downstream} = x + 2, \text{ upstream} = x - 2$$

$$\begin{aligned} \text{Time} &= 30 / (x + 2) + 20 / (x - 2) = \\ &= 5 \end{aligned}$$

Solve:-

$$\frac{30}{x + 2} + \frac{20}{x - 2} = 5$$

$$LCM = (x+2)(x-2)$$

Multiply throughout:

$$30(x-2) + 20(x-2) = 5(x^2-4)$$

$$30x - 60 + 20x + 40 = 5x^2 - 20$$

$$50x - 20 = 5x^2 - 20$$

$$5x^2 - 50x = 0$$

$$= x(x-10) = 0$$

$$= x = 10$$

Speed of boat = 10 km/hr.

$$\textcircled{22} \text{ Relative speed} = 60 + 40 = 100 \text{ km/hr.}$$

$$= 100 \times 1000 / 3600$$

$$= \underline{\underline{27.78 \text{ km/s}}}$$

$$\textcircled{23} \text{ Let boat speed} = x \text{ km/hr.}$$

$$\text{Then upstream speed} = x - 2$$

$$\text{Downstream} = x + 2$$

$$\text{Time diff} = 2 \text{ hrs.}$$

$$\frac{20}{x-2} - \frac{20}{x+2} = 2$$

Multiply by $(x-2)(x+2)$:

$$20(x+2) - 20(x-2) = 2(x^2-4)$$

$$20x + 40 - 20x + 40 = 2x^2 - 8$$

$$= 80 = 2x^2 - 8$$

$$= 88 \Rightarrow x^2 = 44$$

$$= x = \sqrt{44} \approx 6.63$$

$$\textcircled{24} \text{ Speed} = 72 \text{ km/hr.}$$

$$= (72 \times 1000) / 3600 = 20 \text{ m/s.}$$

$$\cdot \text{Length of train} = 20 \times 12 = 240 \text{ m.}$$

$$\cdot \text{Total length (train + platform).}$$

$$= 20 \times 18$$

$$= 360 \text{ m.}$$

$$\cdot \text{Platform length} = 360 - 240$$

$$= \underline{\underline{120 \text{ m}}}$$

$$\textcircled{25} \text{ Let stream speed} = x \text{ km/hr.}$$

$$\text{Then upstream} = 20 - x$$

$$\text{Downstream} = 20 + x$$

$$\frac{40}{20+x} - \frac{40}{20-x} = 1$$

Multiply by $(20-x)(20+x)$:

$$40(20+x) - 40(20-x) = (20^2 - x^2)$$

$$800 + 40x - 800 + 40x = 400 - x^2$$

$$80x = 400 - x^2$$

$$= x^2 + 80x - 400$$

$$= 1$$

Solve quadratic:-

$$x = \frac{-80 \pm \sqrt{80^2 + 4 \times 400}}{2}$$

$$= \frac{-80 \pm \sqrt{8000}}{2} = \frac{-80 \pm 89.44}{2}$$

speed of stream $\approx 4.72 \text{ km/hr}$