

Method

1. Bisection Method

Aim: The bisection method is used to find the roots of a polynomial equation. It separates the interval and subdivides the interval in which the root of equation lies. The principle behind this method is the intermediate value theorem for continuous functions.

Pseudocode:

```
clc
f = input('Enter non-linear equations: ');
a = input('Enter first guess: ');
b = input('Enter second guess: ');
n = input('Number of iteration: ');
if f(a) * f(b) < 0
    for i = 1:n
        c = (a + b) / 2
        if f(a) * f(c) < 0
            b = c;
```

else if $f(b) * f(c) < 0$

$a = c$;

end

end

else

disp('No root between given brackets')

end

[Input]

$$f = x^2 - 5x + 2;$$

$$a = 0;$$

$$b = 1;$$

$$n = 20;$$

[Output]

Method

2: Experiment Name: False Position Method

Aim: An algorithm for finding roots which retains that prior estimate for which the function value has opposite sign from the function value at the current best estimate of the root. In this way, the method of false position keeps the root bracketed.

Pseudocode:

f = input('Enter non-linear equation:');

a = input('Enter first guess:');

b = input('Enter second guess:');

if $f(a) * f(b) < 0$

for $i = 1:n$

$$c = \frac{a(f(b)) - b(f(a))}{f(b) - f(a)}$$

if $f(a) * f(c) < 0$

$b = c$;

else if $f(b) * f(c) < 0$

$a = c$;

end

end

else

disp('No root between given brackets');

end

[input]

$f = \cos(x) - x$;

$a = 0.5$

$b = 1$

$n = 20$

[output]

Method

3: Experiment Name: Newton Raphson Method

Aim: The Newton-Raphson method (also known as Newton's method) is a way to quickly find a good approximation for the root of a real valued function $f(x)=0$. It uses the idea that a continuous and differentiable function can be approximated by a straight line tangent to it.

Pseudocode:

$$f = x^2 + 2x + 3;$$

$$df = 2x + 2;$$

$$e = 10^4;$$

$$x_0 = 0;$$

$$n = 10;$$

if $df(x_0) \approx 0$

for $i = 1 : n$

$x_1 = x_0 - (f(x_0) / df(x_0))$

fprintf('x%.2 = %.4f \n', i, x1)

if $abs(x_1 - x_0) < e$

break

end

$x_0 = x_1$;

end

else

disp('Newton, Rapshon Failed');

end

Method:

3. Experiment Name: Secant Method

Aim: In numerical analysis, the secant method is a root finding algorithm that uses a succession of roots of secant lines to better approximate a root of a function f . The secant method can be thought of as a finite-difference approximation of Newton's method.

Pseudocode:

clc;

$f = @(x) (x^2 - 2);$

$x_0 = \text{input}('Enter x_0:');$

$x_1 = \text{input}('Enter x_1:');$

$tol = \text{input}('Enter tolerance:');$

$itr = \text{input}('Enter Iteration:');$

$P = 0;$

for $i = 1: itr$

$$x_2 = (x_0 * f(x_1) - x_1 * f(x_0)) / (f(x_1) - f(x_0));$$

if $\text{abs}(x_2 - x_1) < \text{tol}$

$p = 1;$

$k = i;$

break;

else

$x_0 = x_1;$

$x_1 = x_2;$

end

end

if $p == 1$

fprintf('Solution is %.f at iteration %i',
x2, k)

else

fprintf('No convergent solution exist
in the given number iteration')

end

[Input]

$x_0 = 0.5$

$x_1 = 5$

tolerance = 0.0001

iteration = 10

5. Experiment Name: Fixed Point Method

Aim: Fixed point method allows us to solve nonlinear one variable equations. We build an iterative method, using a sequence which converges to a fixed point of $g(x)$, this fixed point is the exact solution of $f(x) = 0$.

Pseudocode:

clc

$g = @(x) (2^x + 2) / 5;$

$x_0 = \text{input}('Enter initial values: ');$

$e = 0.0001;$

$n = \text{input}('Enter Iteration: ');$

for $i = 1:n$

$x_1 = g(x_0);$

if $\text{abs}(x_1 - x_0) < e$

$\text{fprintf}('x \%d = \%4.5f \backslash n', i, x_i);$

break

end $x_0 = x_1; \text{end}$

Method

G: Experiment Name: Basic Gauss Elimination Method

Aim: The goal of Gaussian elimination is to get the matrix in row echelon form. If a matrix is in row echelon form, that means that, reading from left to right, each row will start with at least one more zero term than the row above it.

Pseudocode:

```
A = input('Enter your coefficient matrix:');  
B = input('Enter source vector:');  
N = length(B);  
X = zeros(N, 1);  
Aug = [A B]  
for j = 1:N-1
```

for $i = j+1 : N$

$m = \text{Aug}(i, j) / \text{Aug}(j, j);$

$\text{Aug}(i, :) = \text{Aug}(i, :) - m \times \text{Aug}(j, :);$

end

end

Aug

$X(N) = \text{Aug}(N, N+1) / \text{Aug}(N, N);$

for $k = N-1 : 1 : 1$

$X(k) = (\text{Aug}(k, N+1) - \text{Aug}(k, k+1 : N) \times$
 $X(k+1 : N)) / \text{Aug}(k, k);$

end

X

Method

7. Experiment Name: Jacobi Iteration Method

Aim: In Numerical linear algebra, the Jacobi method is an iterative algorithm for determining the solutions of a strictly diagonally dominant system of linear equations. Each diagonal element is solved for, and an approximate value is plugged in. The process is then iterated until it converges.

Pseudocode:

```
A = input('Enter co-efficient matrix A:');  
B = input('Enter source vector B:');  
p = input('Enter initial guess vector:');  
n = input('Enter no of Iterations:');  
e = input('Enter Tolerance:');  
N = length(B);  
X = zeros(N, 1);
```

```
for j = i : n
```

```
for i = 1 : N
```

```
x(i) = (B(i) / A(i, i)) - (A(i, [1:i-1, i+1:N]) * P([1:i-1, i+1:N])) / A(i, i);
```

```
end
```

```
fprintf('Iteration no %d\n', i)
```

```
if abs(x - p) < e
```

```
break
```

```
end
```

```
p = x;
```

```
end;
```