

# COMP 250

## INTRODUCTION TO COMPUTER SCIENCE

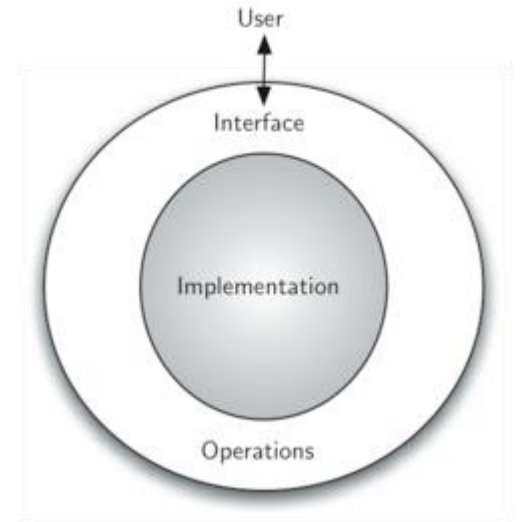
### Lecture 16 – Queues

Roman Sarrazin-Gendron, Winter 2020

Slides very much based on Michael Langer and Giulia Alberini

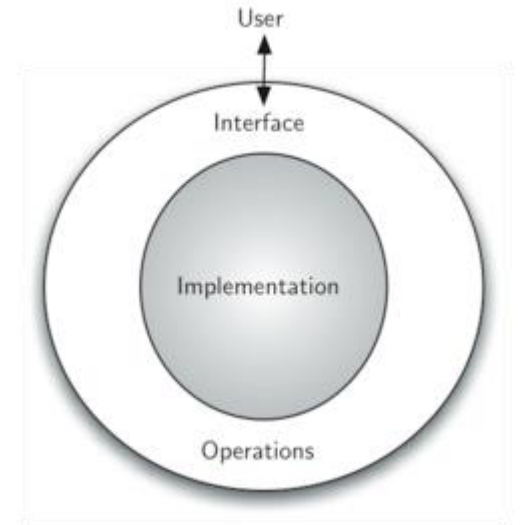
# REMINDER: ABSTRACT DATA TYPES

- Type/class of object defined by values and operations from the perspective of the user
- Completely independent of implementation and language (more abstract than data structures)
- Puts the focus on the essential tasks towards solving a problem.



# REMINDER: ABSTRACT DATA TYPES (ADT)

- Type/class of object defined by values and operations from the perspective of the user
- Completely independent of implementation and language (more abstract than data structures)
- **Goal** : force the user to only use efficient operations by restricting number of functions available.
  - Many ADTs are specialized to specific problems/data



# REMINDER : STACKS

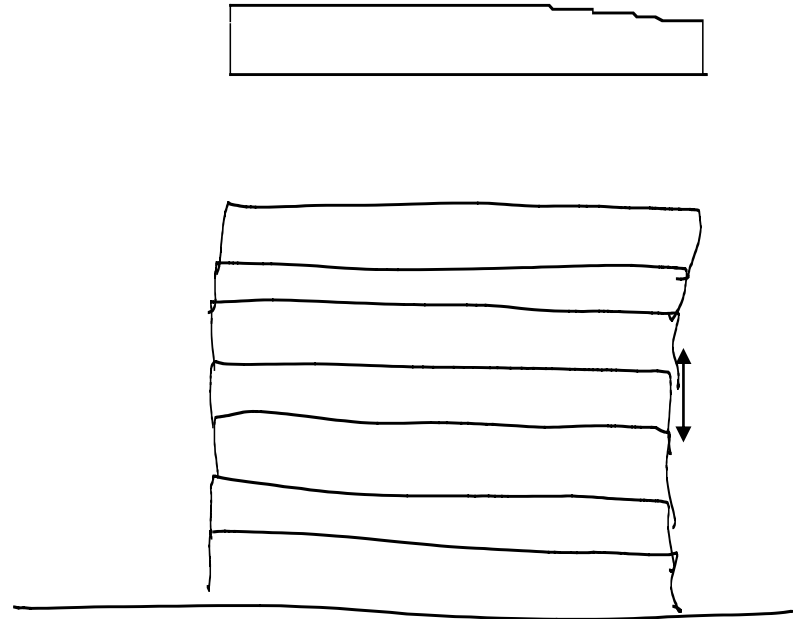
## Stack

push(e)

pop()

**LIFO**

(last in, first out)



- By implementing a Stack with an ArrayList and making push and pop execute addLast and removeLast, we make sure the user never uses inefficient methods like addFirst, and guarantee a good execution time.

# ADT (ABSTRACT DATA TYPE)

- **List**

add(i,e), remove(i), get(i), set(i), .....

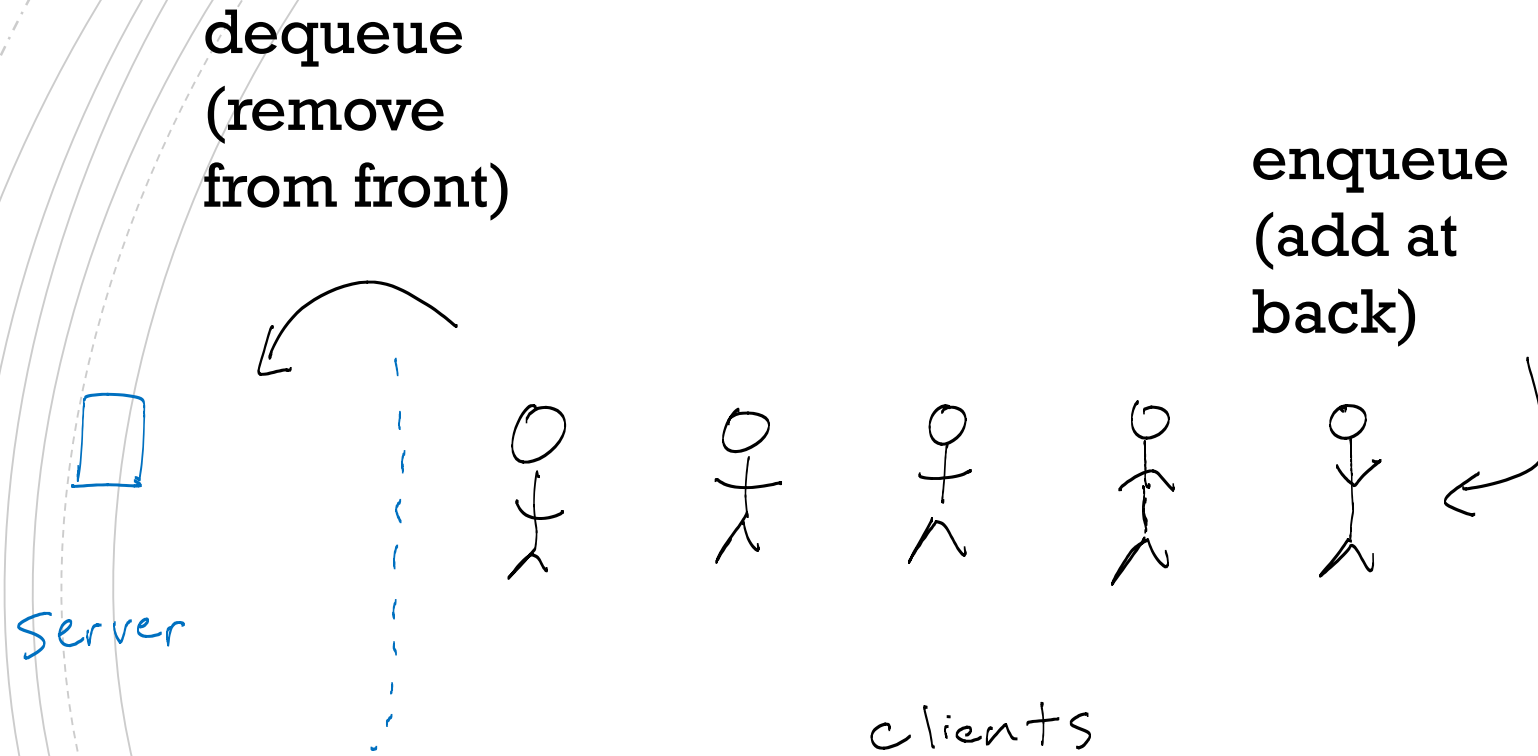
- **Stack**

push, pop(), ..

- **Queue**

enqueue( e ), dequeue()

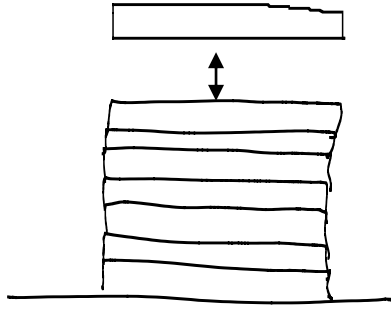
# QUEUE



# EXAMPLES

---

- keyboard buffer
- printer jobs
- CPU processes (applications do not run in parallel)
- web server
- .....



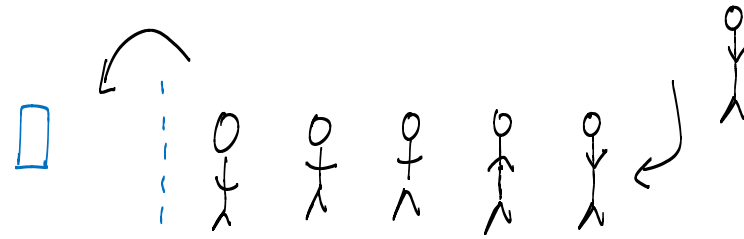
## Stack

push(e)

pop()

**LIFO**

(last in, first out)



## Queue

enqueue( e )

dequeue()

**FIFO**

(first in, first out)

“first come, first serve”



## EXERCISE : IMPLEMENT A QUEUE WITH A STACK

```
enqueue( e ){           // add element
:
}

dequeue() {             // remove 'oldest' element
:
}
```

Write pseudocode for these two methods that uses a stack, namely use the operations `push(e)`, `pop()`, `isEmpty()`.

# HINT FOR EXERCISE

top

i  
h  
g  
f  
e  
d  
c  
b  
a

Use a second stack.



**S**

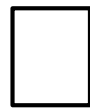
tmpS

# HINT FOR EXERCISE

top

i  
h  
g  
f  
e  
d  
c  
b  
a

**s**



**tmpS**

→  

```
while ( ! s.isEmpty() ){  
    tmpS.push( s.pop(  
    ) )  
}
```



**s**

a  
b  
c  
d  
e  
f  
g  
h  
i

**tmpS**

# QUEUE EXAMPLE

**enqueue( a )**

**a**

**enqueue( b )**

**ab**

**dequeue( )**

**b**

# QUEUE EXAMPLE

enqueue( a )	a
enqueue( b )	ab
dequeue( )	b
enqueue( c )	bc
enqueue( d )	bcd
enqueue( e )	bcde
dequeue( )	cde
enqueue( f )	cdef
enqueue( g )	cdefg

# HOW TO IMPLEMENT A QUEUE?

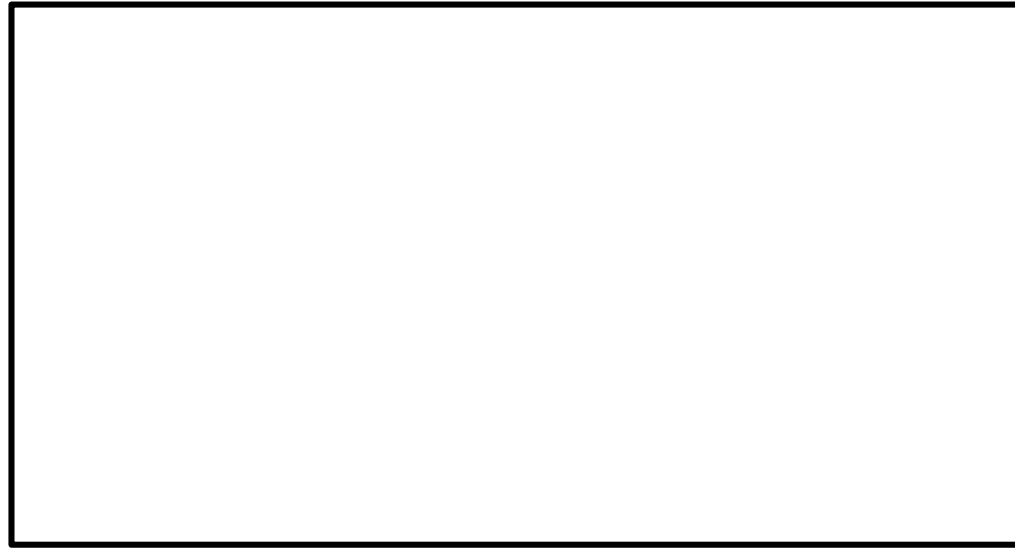
enqueue(e)

dequeue()

singly linked list

doubly linked list

array list



# — HOW TO IMPLEMENT A QUEUE? —

	enqueue(e)	dequeue()
singly linked list	addLast(e)	removeFirst()
doubly linked list	(unnecessary)	
array list		

# HOW TO IMPLEMENT A QUEUE?

	enqueue(e)	dequeue()
singly linked list	addLast(e)	removeFirst()
doubly linked list	(unnecessary)	
array list	addLast(e)	<b>removeFirst()</b>

**SLOW**



# QUEUES AND ARRAYLISTS

Implementing a queue with an array list. **(BAD)**

length = 4

0123 indices



enqueue ( a )

a---

enqueue ( b )

ab--

dequeue ( )

b---

**Requires shift**

# QUEUES AND ARRAYLISTS

length = 4

0123 indices



enqueue ( a )

a---

enqueue ( b )

ab--

dequeue ( )

b---

Requires shift

enqueue ( c )

bc--

enqueue ( d )

bcd-

enqueue ( e )

bcde

dequeue ( )

cde-

Requires shift

# Implementing a queue with an array list. (BAD)

length = 4

0123 indices



enqueue ( a )

a---

enqueue ( b )

ab--

dequeue ( )

b---

enqueue ( c )

bc--

enqueue ( d )

bcd-

enqueue ( e )

bcde

dequeue ( )

cde-

enqueue ( f )

cdef

enqueue ( g )

cdefg---

**requires expansion**

# Implementing a queue with an **expanding array**. (also **BAD**)

Use **head** and **tail** indices  
(**tail** = **head** + size - 1)

enqueue ( a )	a---	( 0 , 0 )
enqueue ( b )	ab--	( 0 , 1 )
dequeue ( )	-b--	( 1 , 1 )
enqueue ( c )	-bc-	( 1 , 2 )
enqueue ( d )	-bcd	( 1 , 3 )
enqueue ( e )	?	

# Implementing a queue with an **expanding array**. (also **BAD**)

Use **head** and **tail** indices  
(**tail** = **head** + size - 1)

enqueue ( a )	a---	( 0 , 0 )
enqueue ( b )	ab--	( 0 , 1 )
dequeue ( )	-b--	( 1 , 1 )
enqueue ( c )	-bc-	( 1 , 2 )
enqueue ( d )	-bcd	( 1 , 3 )
enqueue ( e )	-bcde---	( 1 , 4 )
dequeue ( )	--cde---	( 2 , 4 )
enqueue ( f )	--cdef--	( 2 , 5 )
enqueue ( g )	--cdefg-	( 2 , 6 )



**Make  
bigger  
array and  
copy to it.**

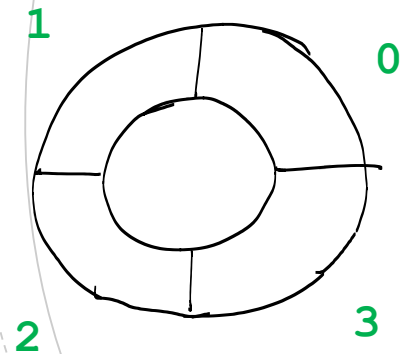
## ALTERNATIVES?

- **An expanding array is an inefficient usage of space.**
- **A better idea is....**

# CIRCULAR ARRAY

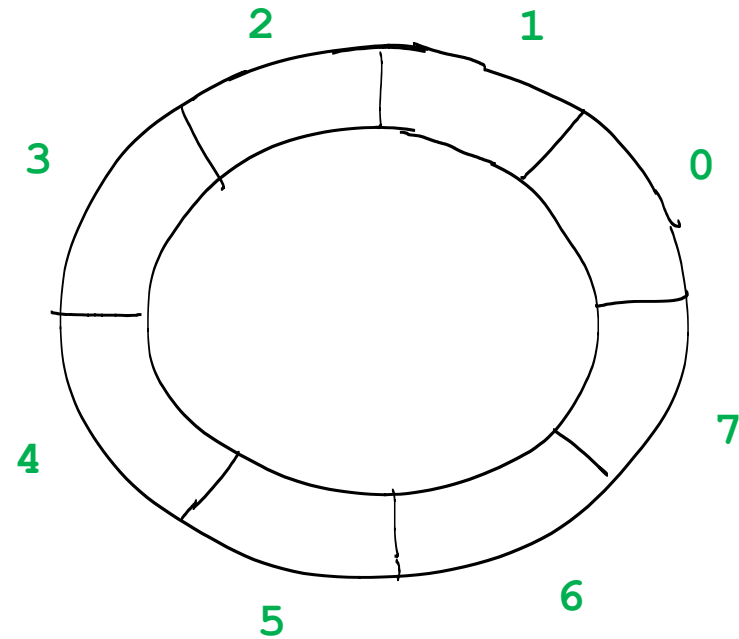
length = 4

0123



length = 8

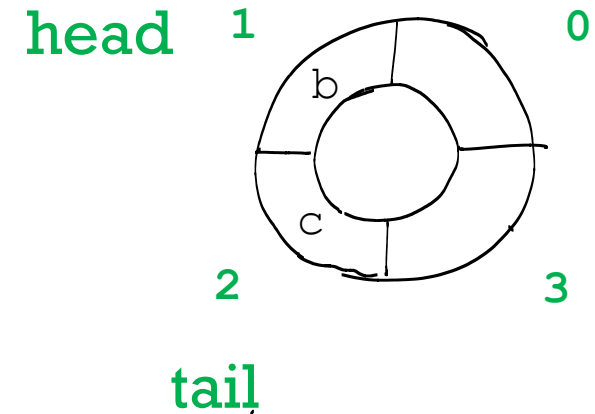
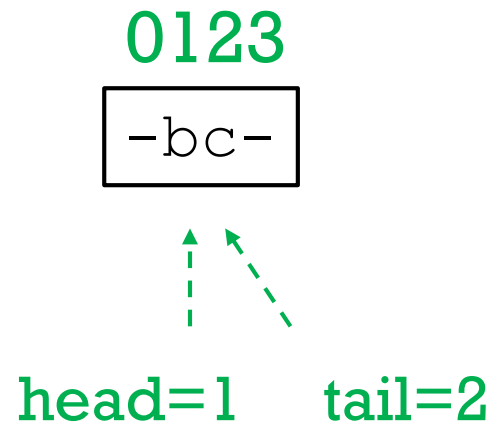
01234567



# CIRCULAR ARRAY

$$\text{tail} = (\text{head} + \text{size} - 1) \% \text{length}$$

```
enqueue ( a  
enqueue ( b )  
dequeue ()  
enqueue ( c )
```

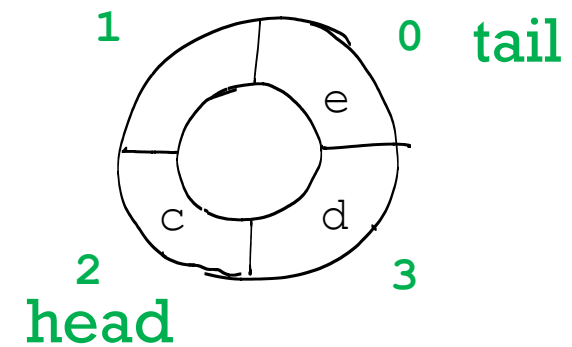
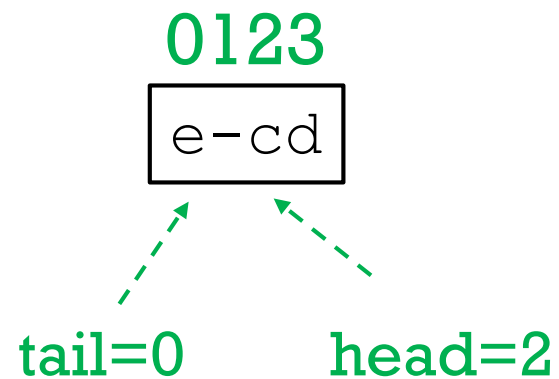




# CIRCULAR ARRAY

$$\text{tail} = (\text{head} + \text{size} - 1) \% \text{length}$$

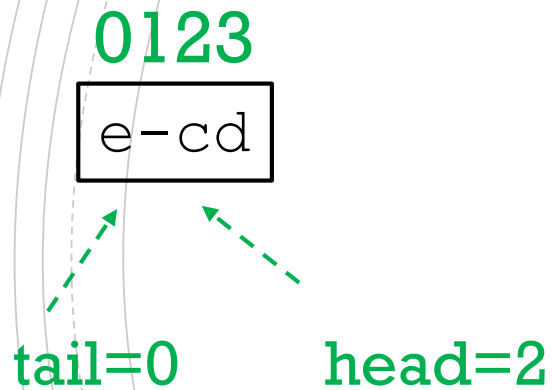
```
enqueue( a )  
enqueue( b )  
dequeue( )  
enqueue( c )  
enqueue( d )  
enqueue( e )  
dequeue( )
```



# CIRCULAR ARRAY

$\text{tail} = (\text{head} + \text{size} - 1) \% \text{length}$

```
enqueue( element ){  
    if (size < length)  
        queue[ (tail + 1) % length] = element  
    else .... // coming up  
    size = size+1  
}
```



```
dequeue(){ // check if empty omitted  
    element = queue[head]  
    head = (head + 1) % length  
    size = size-1  
    return element  
}
```

# Implementing a queue with a **circular** array

**(GOOD)**

$$\text{tail} = (\text{head} + \text{size} - 1) \% \text{length}$$

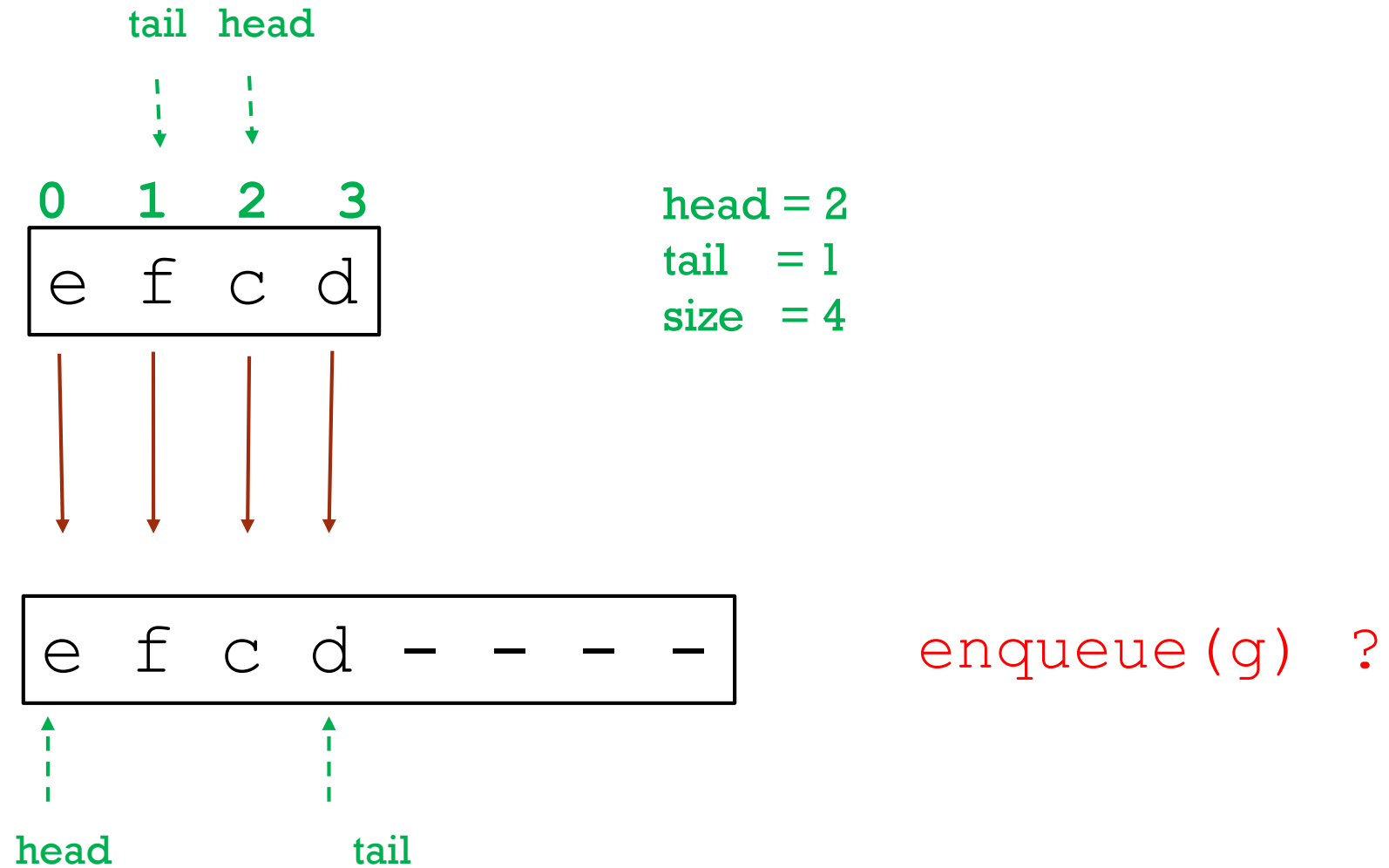
	array	(head, tail, size)
enqueue ( a )	a---	(0, 0, 1)
enqueue ( b )	ab--	(0, 1, 2)
dequeue ( )	-b--	(1, 1, 1)
enqueue ( c )	-bc-	(1, 2, 2)
enqueue ( d )	-bcd	(1, 3, 3)
enqueue ( e )	ebcd	(1, 0, 4)
dequeue ( )	e-cd	(2, 0, 3)
enqueue ( f )	efcd	(2, 1, 4)

# Implementing a queue with a **circular** array

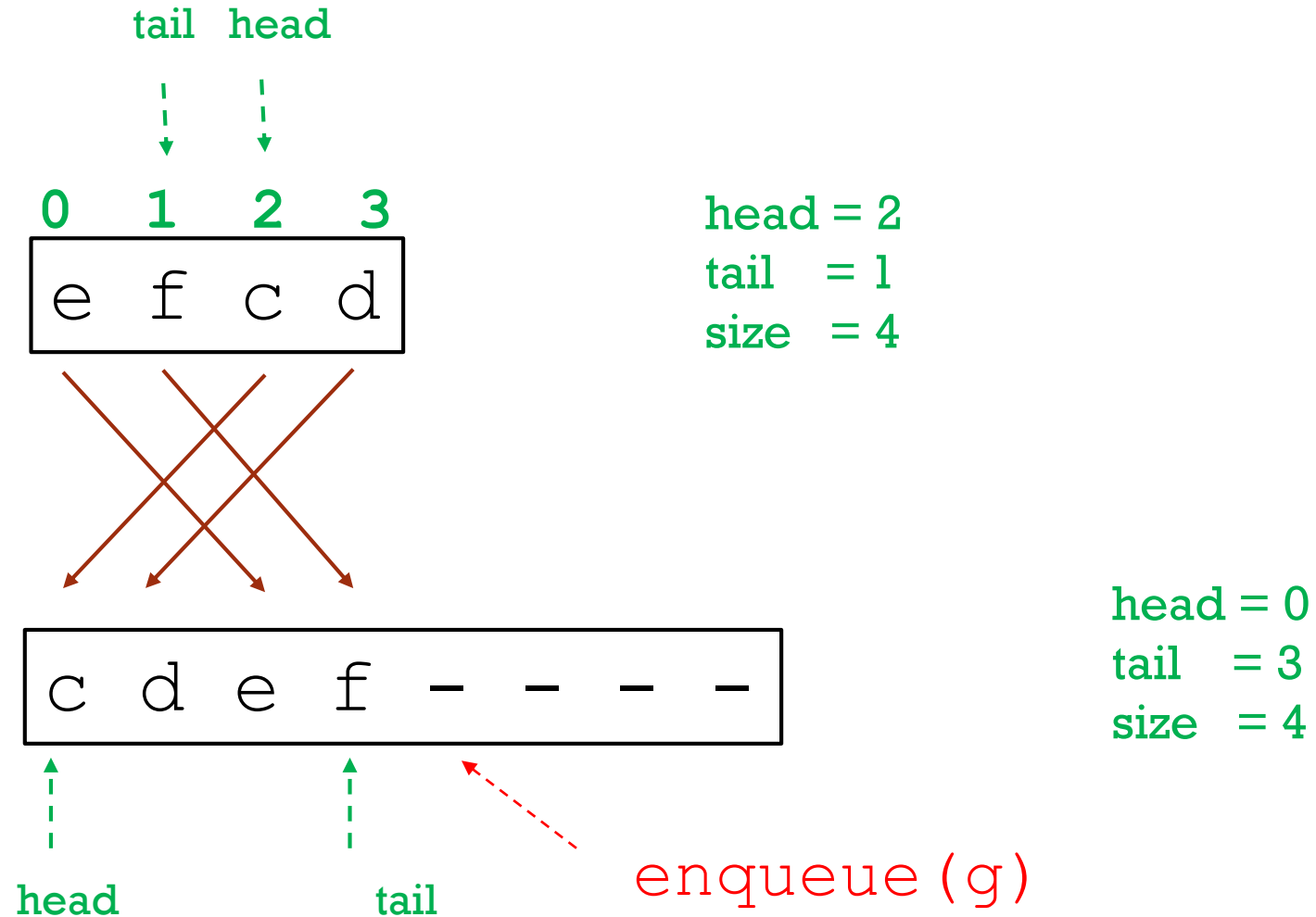
$$\text{tail} = (\text{head} + \text{size} - 1) \% \text{length}$$

	array	(head, tail, size)
enqueue ( a )	a---	(0, 0, 1)
enqueue ( b )	ab--	(0, 1, 2)
dequeue ( )	-b--	(1, 1, 1)
enqueue ( c )	-bc-	(1, 2, 2)
enqueue ( d )	-bcd	(1, 3, 3)
enqueue ( e )	ebcd	(1, 0, 4)
dequeue ( )	e-cd	(2, 0, 3)
enqueue ( f )	efcd	(2, 1, 4)
<b>enqueue ( g )</b>	<b>?</b>	

Increase length of array and copy? **BAD**



Increase length of array. Copy so that head moves to front.  
**(GOOD)**



## EXTENDING CIRCULAR ARRAY

```
enqueue( element ){  
    if ( queue.size == queue.length) {  
        // increase length of array  
  
        create a bigger array tmp[ ] // e.g. 2*length  
        for i = 0 to queue.length - 1  
            tmp[i] = queue[ (head + i) % queue.length ]  
        head = 0  
        queue = tmp  
    }  
    queue[size] = element  
    queue.size = queue.size + 1  
}
```

# WHAT DO WE DO IF THE QUEUE IS EMPTY?

$$\text{tail} = (\text{head} + \text{size} - 1) \% \text{length}$$

What happens when `size == 0` ?

	array	( <span style="color: green;">head</span> , <span style="color: green;">tail</span> , size)
Initial state	----	( <span style="color: green;">0</span> , <span style="color: green;">3</span> , 0)
enqueue( a )	a---	(0, 0, 1)
enqueue( b )	ab--	(0, 1, 2)
dequeue()	-b--	(1, 1, 1)
dequeue()	--- <div style="display: flex; justify-content: center; align-items: center; gap: 20px;"><div style="text-align: center;"><span style="color: green;">↑</span> <span style="color: green;">tail</span></div><div style="text-align: center;"><span style="color: green;">↑</span> <span style="color: green;">head</span></div></div>	( <span style="color: green;">2</span> , <span style="color: green;">1</span> , 0)



# — STACK AND QUEUES IN JAVA —

- Java has a stack class : <https://docs.oracle.com/javase/7/docs/api/java/util/Stack.html>
  - Push, pop, isEmpty, peek
- Java does NOT have a queue class, but it has a queue **interface**, implemented by different queue classes.
  - You will discuss interfaces on Monday with Giulia.

# SCOPE OF THE COURSE

- We will not discuss Java packages/classes for ADTs
  - We will never ask you to write a program using the Stack class in Java.
  - We can ask you to write your own Stack class and manipulate it.
    - This is what we did with Homework 2!
- The objective of the course is to understand how ADTs work and why we use them.

# QUIZ 2 TODAY!

- You have until 8PM today to submit the quiz
- **Monday- Wednesday:** two last classes about Java (with Giulia)
- **Next Friday:** new topic! We start discussing induction and recursion.