

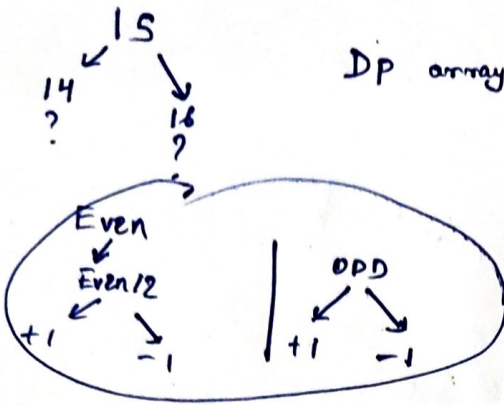
Question 1

13 $\xrightarrow{1}$ 14 $\xrightarrow{7}$ 7 $\xrightarrow{1}$ 8 $\xrightarrow{4}$ 4 $\xrightarrow{2}$ 2 $\xrightarrow{1}$ 1
 13 $\xrightarrow{1}$ 12 $\xrightarrow{6}$ 6 $\xrightarrow{3}$ 3 $\xrightarrow{1}$ 2 $\xrightarrow{1}$ 1

$x+1$ $x-1$

10 $\xrightarrow{5}$ 5 \rightarrow
 18 $\xrightarrow{9}$ 9
 20 $\xrightarrow{10}$ 10 $\xrightarrow{5}$ 5
 44 $\xrightarrow{22}$ 22 $\xrightarrow{11}$ 11
 6+3+2
 5+1+3

DP array \rightarrow $\begin{bmatrix} 0 & 1 & 2 & 3 & \dots \\ 0 & 0 & 1 & \dots \end{bmatrix}$



Bottom up:

$$\text{cost}[0] = 0$$

$$\text{cost}[1] = 0$$

$$\text{cost}[2] = \frac{2}{1} + \text{cost}[1] = 1$$

$$\text{cost}[3] = 1 + \min[\text{cost}[2], \text{cost}[4]]$$

~~we don't calculate cost of upper index (+1) so can't be used here~~

~~TOP-DOWN~~

~~cost function~~

$$\text{cost}[i] = \text{if } i \text{ is odd} \rightarrow \text{cost}[i] = \max[1 + \min[\text{cost}[i-1], \text{cost}[\frac{i+1}{2}]]]$$

cost[4] \rightarrow can be split to $\frac{4}{2} + \text{cost}[2]$ which we know at index $i=3$.

for (i)

$i \neq \text{even}$

$$\text{cost}[i] = 1 + \text{cost}[\frac{i}{2}]$$

$i = \text{odd}$

$$\text{cost}[i] = 1 + \min[\text{cost}[i-1], 1 + \text{cost}[\frac{i+1}{2}]]$$

correction given in whatsapp, even number split cost = 1

$$5 \rightarrow 1 + (3, 3^x)$$

Ⓟ

$$7 \rightarrow 1 + (6, 4+2+1)$$

$$8 \rightarrow 4+2+1$$

$$9 \rightarrow$$

$$14 \rightarrow 7+$$

$$1 + 8 + 7$$