



Pimpri Chinchwad Education Trust's
Pimpri Chinchwad College of Engineering, Pune
Department of Mechanical Engineering



Continuous Assessment Sheet

Course Name: Numerical Methods and Optimization (BME6413) Class: T.Y. B. Tech Mechanical Academic Year: 2022-23
Semester: VI

Name of Student: Aarthab · Mayur. Patil

Class: T.Y

Div.: C

Roll No.: TYMTEB 228

Sr. No.	Title of Assignment/ Experiment	Start Date	Completion Date	Knowledge (10)	Skill (10)	Attitude (5)	Total
1	<u>Introduction to MATLAB</u>		<u>13/2/24</u>				<u>25</u>
2	<u>Roots of Equations</u>		<u>13/2/24</u>				
3	<u>Multidimensional Functions</u>		<u>21/2/24</u>				
4	<u>Numerical Integration</u>		<u>21/2/24</u>				
5	<u>Curve Fitting</u>		<u>21/2/24</u>				
6	<u>Interpolation</u>		<u>16/2/24</u>				
7	<u>Orthogonality & Hermitian Functions</u>		<u>16/2/24</u>				
8	<u>Laplace</u>		<u>16/2/24</u>				
9	<u>Method of Lines</u>		<u>16/2/24</u>				
							<u>Total =</u>

Signature of Student

Signature of Course Teacher

PIMPRI CHINCHWAD EDUCATION TRUST'S
PIMPRI CHINCHWAD COLLEGE OF ENGINEERING
Sector No. 26, Pradhikaran, Nigdi, Pune - 411044

Department Of Mechanical Engineering
Year and Course TY N M O Sem Roll No. : TYMEB228

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This is certify that Shri. Sachin. Shreey. Patil has carried out the
above mentioned Numerical method & optimization Practicals / Term Work
in the Mechanical Department of Pimpri Chinchwad College of Engineering, Pune-44.

Date : 16/09/24

Subject Incharge Head of Department
Pimpri Chinchwad College of Engineering, Pune - 44

PIMPRI CHINCHWAD EDUCATION TRUST'S
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Department Of Mechanical Engineering
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This is certify that Shri. Sarthak Alfrey. Patil has carried out the
 above mentioned Numerical methods & optimization by Practicals / Term Work
 in the Mechanical Department of Pimpri Chinchwad College of Engineering, Pune-44.

Date: 16/04/24

X Subject Incharge Head of Department
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Safsh

Assignment no 1

Introduction to Matlab:-

1) What is Matlab:-

→ Matlab is a proprietary multi-paradigm programming language & numeric computing environment developed by Mathworks. Matlab allows matrix manipulations, plotting of functions & data, implementation of algorithms, creation of user interfaces & interfacing with programs written in other languages.

2) Commands in Matlab:-

a) Commands for Managing the session:-

Commands	Purposes
cic	Clear command window
clear	Remove variables from memory
exist	Check for existence of file
global	Declares variables to be global
help	Search for a help topic
lookfor	Searches help entries keywords
quit	Stop matlab
who	Lists current variables
whos	Lists current variables (long displays)

b) Commands for working with system :-

Commands	Purpose
cd	Changes current display
data	Display current data
delete	Deletes a file
diary	Switches on
dir	Lists all files in current directory
load	Loads workspace variables from file
path	Display search path
pwd	Display current directory
scine	Scenes workspace variables in a file
type	Display content of a file
which	Lists all matlab file in current directory
Wkread	Reads .WKS spreadsheet file.

c) Input & Output Commands :-

Commands	Purpose
disp	Display contents of an array/string
fscanf	Read formatted data from a file
format	Controls screen-display format
fprint	Performs formatted writes to file
input	Disp prompts & circuit for input
;	Suppresses screen printing

c) Vector, matrix & array commands :-

Commands	Purpose
cat	Concatenates arrays.
find	Finds indices of nonzero elements.
linspace	Creates regularly spaced vectors.
logspace	Creates logarithmically spaced vectors.
prod	Product of each column.
sort	Sorts each column.
size	Computes array size.
sum	Sums each column.
dot	Computes matrix dot products.
det	Computes determinant of an array.

e) Plotting Commands :-

Commands	Purpose
axis	sets axis limits
fplot	Intelligent plotting of functions
grid	Display gridlines
plot	Generates xy plot
print	Prints plot or saves plot to a file
xlabel	Add text label to x-axis
ylabel	Add text label to y-axis
gtext	Enables label placement by mouse.
legend	length placement by mouse.

3) Matlab symbols :-

Symbol	Role
+	Addition
+	Unary plus
-	Subtraction
.*	Element wise multiplication
*	Matrix multiplication
./	Element wise right division
\	Matrix right division
.\	Element wise left division
\`	Matrix left division
.^	Element wise power
^	Matrix power
.'	Transpose
'	Complex conjugated Transpose
==	Equal to
~=	Not Equal to
>	Greater than
>=	Greater than or equal
<	Less than
<=	Less than or equal
&	Find logical AND
	Find logical OR
&&	Find logical AND (with short circuitting)
	Find logical OR (with short circuitting)
~	Find logical NOT
:	Comma
::	Colon / semi-colon

7) inbuilt functions:

length	Computes no of elements
size	Compute array size
max/min	Returns largest/smallest element
sum	Sums each column
prod	Product of each column
abs	Absolute value
mean	Return the mean over all element
std	Return the standard deviation
cumsum	Returns the cumulative sum
round	Specify the type of rounding.
ceil	rounds values to nearest integer toward positive infinity.
floor	rounds values to nearest integer less than equal to element.

5) Branches, loop & flow control:

1) If else statement:

The if statement evaluates a logical expression & executes a group of statements when the expression is true. The optional else if & else keyword provide for the execution of alternative groups of statements. An end keyword, which matches the if, terminates the last group of statements. The groups of statements are delineated by the four keywords - no braces or brackets are involved.

2) Switch & case - statement:

The switch statement executes groups of statements based on the values of a variables or expression. The keywords case & otherwise delineate the groups only the first matching case is executed. There must be an end to match the switch.

3) For loop:

The for loop repeats a group of statement a fixed, predetermined no of times. A matching end delineates statement.

4) While loop: The while loop repeats a group of statements an indefinite no of times under control of logical condition. A matching end delineates the statement.

Q) Flowchart symbols :-

Symbols



Name

start/End

Function

An oval representation of start & end.



Arrow

A line is connector between the representative shape that shows relationship



Input/Output

A parallelogram represents input or output.



Decision

A diamond symbolizes a decision



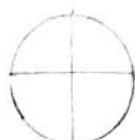
Process

A rectangle shape indicates process.



Connector

Indicates an inspection point.



OR

Logical OR



Swing
Function

Logical AND



Assignment no: 2

Bisection method

- Q) find a root of eqn $x^3 - 4x - 9 = 0$ using bisection method with accuracy 0.001

→ Let

$$y = f(x) = x^3 - 4x - 9$$

assume

$$x = 2 \text{ then } y = f(x) = -9$$

$$x = 3 \text{ then } y = f(x) = 6$$

1st iteration

$$x_1 = 2 \quad f(x_1) = -9$$

$$x_2 = 3 \quad f(x_2) = 6$$

$$x_3 = \frac{x_1 + x_2}{2} \\ = \frac{2+3}{2} = 2.5$$

$$f(x_3) = -3.375$$

$$(x_2 - x_1) = 1 > 0.001$$

2nd iteration

$$x_1 = 2.5 \quad f(x_1) = -3.375$$

$$x_2 = 3 \quad f(x_2) = 6$$

$$x_3 = \frac{x_1 + x_2}{2}$$

$$x_3 = \frac{2.5 + 3}{2} = 2.75$$

$$f(x_3) = 0.7698 > 0.001$$

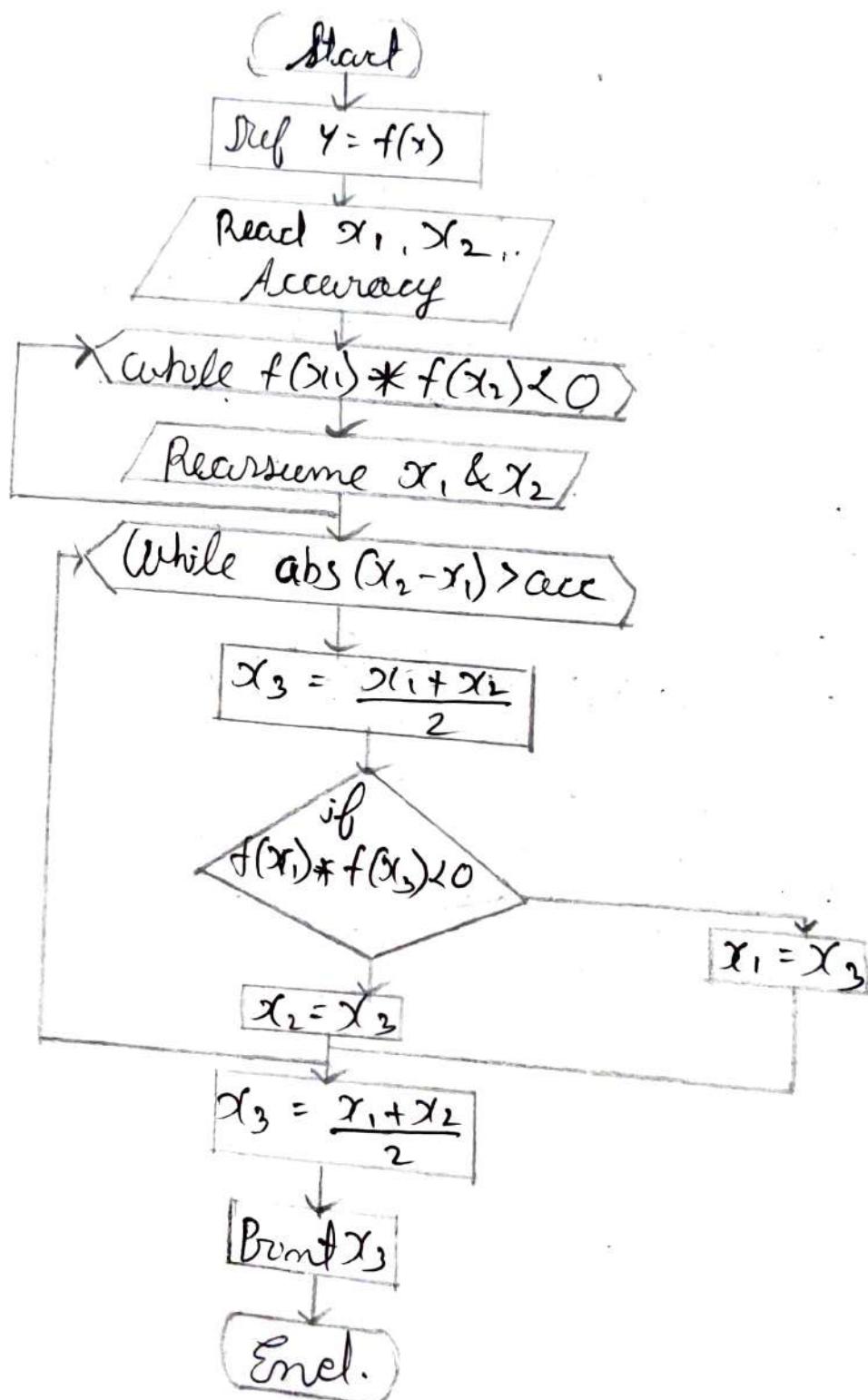
Iteration	x_1	x_2	$f(x_1)$	$f(x_2)$	x_3	$(x_2 - x_1)$
1	2	3	-9	6	2.5	1
2	2.5	3	-3.375	6	2.75	0.5
3	2.5	2.75	-3.375	0.7968	2.625	0.25
4	2.625	2.75	-1.4121	0.7968	2.687	0.125
5	2.687	2.715	-0.3341	0.7968	2.7187	0.125
6	2.687	2.718	-0.3341	0.2209	2.7031	0.031
7	2.703	2.718	-0.0610	0.2209	2.7109	0.015
8	2.7031	2.7109	-0.001	0.0799	2.7070	0.007
9	2.7031	2.7070	-0.061	0.009	2.7050	0.003
10	2.7056	2.7070	-0.0260	0.009	2.7060	0.002
11	2.7060	2.70703	-0.0084	0.009	2.7065	0.001

∴ Root of equation is 2.7065

Algorithm {Bisection Method}

- 1) Define $f(x)$ & number of iteration required n .
- 2) Given the two intervals x_1, x_2 such that $f(x_1) * f(x_2) < 0$
also $f(x_1)$ & $f(x_2)$ must must have opposite sign.
- 3) Find next approximation value of root using formula. $x_3 = \frac{x_1 + x_2}{2}$
- 4) Check $|x_3 - x_1| <$ accuracy.
- 5) Check $f(x_1) * f(x_3) > 0$
if yes $x_1 = x_3$
if not $x_2 = x_3$
- 6) Repeat step 3, 4, 5 for n times.
- 7) Write root of given equation x_3
- 8) End.

Homekant-Berechnen



6/2/24 12:10 AM C:\Us...\\BisectionmethodAssignment2.m 1 of 1

%NAME: Sarthak Abhay Patil
%ROLL NO:TYMEB228
%BATCH:B4

```
f=inline('x^2+8*x-4');
x1=input('enter the value of x1:');
x2=input('enter the value of x2:');
n=input('enter the number of iteration:');
y1=f(x1)
y2=f(x2)
while((y1*y2)>0)
    x1=input('enter the value of x1 again:');
    x2=input('enter the value of x2 again:');
    y1=f(x1)
    y2=f(x2)
end
for i=1:n
    x3=(x1+x2)/2
    y3=f(x3)
    if((y1*y3)<0)
        x2=x3
        y2=y3
    else
        x1=x3
        y1=y3
    end
end
fprintf('print root x3=%f',x3);
```



```
>> BisectionmethodAssignment2  
enter the value of x1:0  
enter the value of x2:1  
enter the number of iteration:8
```

```
y1 =
```

```
-4
```

```
y2 =
```

```
5
```

```
x3 =
```

```
0.5000
```

```
y3 =
```

```
0.2500
```

```
x2 =
```

```
0.5000
```

```
y2 =
```

```
0.2500
```

```
x3 =
```

```
0.2500
```

```
y3 =
```

```
-1.9375
```

```
x1 =
```

```
0.2500
```

```
x2 =
```

```
-1.9375
```

B) Newton-Raphson Method:-

Q) Solve $e^x \cos(x) - 1.2 = 0$ using NR Method take 5 decimal accuracy (0.0001)

→ Sol :-

$$1) y = f(x) = e^x \cos(x) - 1.2$$

2) Assume x_1 ,

$$\text{Let } x_1 = 1$$

$$F(x_1) = 0.268$$

$$\begin{aligned} F'(x_1) &= e^x \cos x + e^x (-\sin x) \\ &= e^x (\cos x - \sin x) \end{aligned}$$

$$\text{Therefore, } F'(x_1) = -0.8186$$

$$F''(x_1) = -2e^x \sin x,$$

$$F''(x_1) = -4.574$$

3) Check by convergence criteria

$$\frac{|F(x_1)|}{[F'(x_1)]^2} \leq 2$$

$$\frac{0.268 \times (-4.574)}{(-0.8186)^2} = -1.8293$$

$$\therefore -1.8293 \leq 1$$

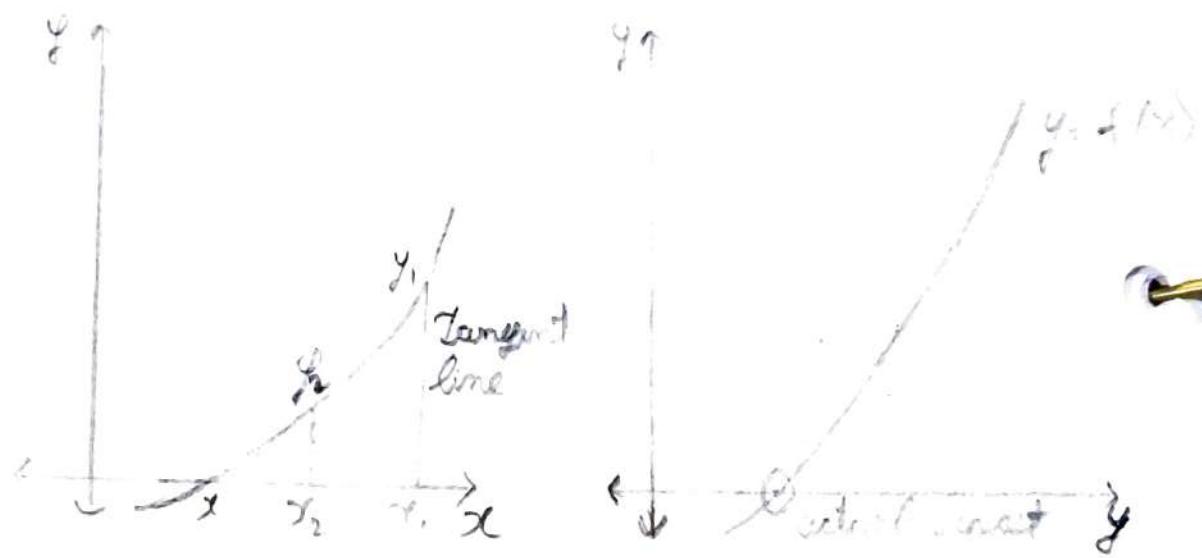
— satisfied

$$\therefore x_1 = 1$$

$$\begin{aligned} 4) x_2 &= x_1 - F(x_1)/F'(x_1) \\ &= 1 - (0.268 / (-0.8186)) \end{aligned}$$

$$\therefore x_2 = 1.327$$

Graphical Representation of Newton Raphson method:-



5)

$|x_2 - x_1|$ & accuracy
Here

$$|1.327 - 1| = 1.327 > 0.001 - \text{acc}$$

$$\therefore x_1 = x_2$$

New $x_1 = 1.327$ & same procedure is repeated
until accuracy is achieved.

No	x_1	$F(x_1)$	$F'(x_1)$	x_2	$F(x_2)$	$ x_2 - x_1 $
1)	1	0.2667	-0.8167	1.3282	-0.2433	0.3282
2)	1.3282	-0.2433	-2.0283	1.2218	-0.0395	0.1064
3)	1.2218	-0.0395	-2.7571	1.2023	-1.24 \times 10^{-3}	0.0195
4)	1.2023	-1.24 \times 10^{-3}	-1.9057	1.2016	3.59 \times 10^{-5}	7 \times 10^{-4}
5)	1.2016	3.59 \times 10^{-5}	-1.9013	1.2016	3.59 \times 10^{-5}	0

∴ Therefore,

Root of given eqn $e^x \cos(x) - 1.2 = 0$
is 1.2016

~~Algorithm~~ [Bisection Method] [Newton-Raphson].

- 1) Define $f(x)$ & no. number of iteration required n .
- 2) Assume initial guess x_1 .
- 3) Calculate single & double derivatives of function $f(x)$ i.e. $f'(x)$, $f''(x)$
- 4) Check convergence criteria
$$\frac{f(x_1) * f''(x_1)}{[f'(x_1)]^2} \leq 1 \quad \text{true}$$

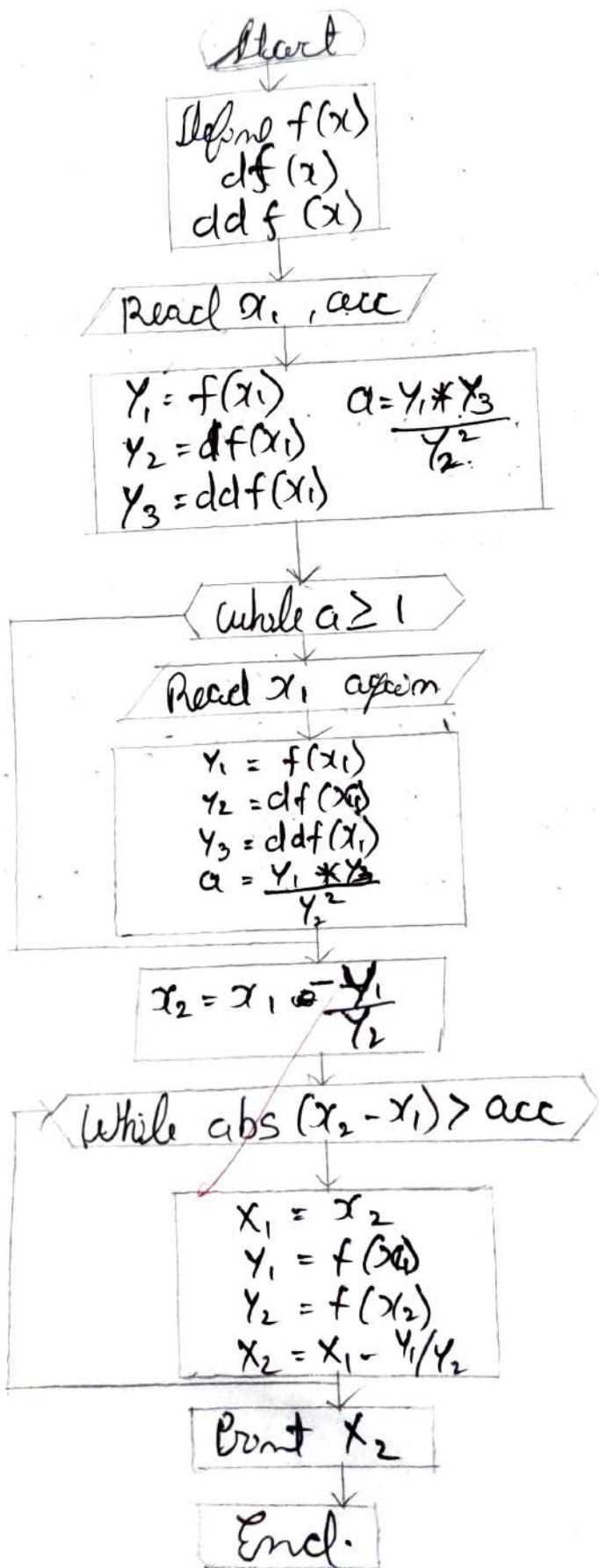
if ≤ 1 initial guess is correct else repeat step 2, 3 & 4 for correct initial guess
- 5) Calculate the root (approx) by using formula $x_{(n+1)} = x_n - \frac{f(x_n)}{f'(x_n)}$
- 6) if $(x_{n+1} - x_n) <$ accuracy, then root of given equation else repeat steps nos 4
- 7) End.

Algorithm [Bisection method] [Newton Raphson]

- 1) Define $f(x)$ & no number of iteration required ' n '.
- 2) Assume initial guess x_1 .
- 3) Calculate single & double derivatives of functions $f(x)$ i.e $f'(x)$ & $f''(x)$
- 4) Check convergence criteria
$$\frac{|f(x_i) - f''(x_i)|}{|f'(x_i)|^2} \leq i \text{ true}$$

if 2nd initial guess is correct else repeat step 2, 3 & 4 for correct initial guess.
- 5) Calculate the root (approx) by using formula $x_{(n+1)} = x_n - \frac{f(x_n)}{f'(x_n)}$
- 6) if $(x_{n+1} - x_n) <$ Accuracy, then root of given equation else repeat steps 5
- 7) End.

Flowchart: Newton Raphson



%NAME: Sarthak Abhay Patil

%ROLL NO:TYMEB228

%BATCH:B4

```
f=inline('exp(x)*cos(x)-1.2');
df=inline('exp(x)*(cos(x)-sin(x))');
ddf=inline('(-2)*exp(x)*sin(x)');

x1=input('Enter initial value:');
acc=input('Enter the accuracy:');
while f(x1)*ddf(x1)/df(x1)^2>1
    x1=input('Enter initial value again');
end
x2=x1-f(x1)/df(x1)
while abs(x2-x1)>acc
    x1=x2
    x2=x1-f(x1)/df(x1)
end
fprintf('Root of equation x2=%f',x2)
```



```
>> NewtonsRaphsonAssignment2  
Enter initial value:1  
Enter the accuracy:0.0001
```

```
x2 =
```

```
1.3282
```

```
x1 =
```

```
1.3282
```

```
x0 =
```

```
1.3218
```

```
x1 =
```

```
1.3218
```

```
x2 =
```

```
1.3218
```

```
x1 =
```

```
1.3218
```

```
x2 =
```

```
1.3218
```

```
x1 =
```

```
1.3218
```

```
x2 =
```

```
1.3218
```

```
Final answer = x1=1.321800
```

Assignment No 3

#

Simultaneous Equation:-

In Numerical methods & optimization the simultaneous equation method refers to solving a system of equations simultaneously to find the values of unknown variables that satisfies all equations in system.

c)

Gauss - Elimination Method :-

- This method is used to solve system of linear equations by systematically transforming equations to matrix representation by row operations & then back substituting to find the solution. It is versatile but can be computationally intensive for large systems.

b)

Thomas Algorithm for Tri-diagonal Matrix :-

- Tri-diagonal method is specifically designed for solving systems of equations where the coefficient matrix is tri-diagonal.
- Non-zero element only on main & adjacent to main diagonal.

c)

Gauss - Seidel Method:-

It is an iterative technique for solving systems of simultaneous linear equations.
It is useful for large & sparse systems.

#1 Numericals :-

1) Gauss Elimination Method

$$2x + 4y + 3z = 13$$

$$3x + 6y + 2z = 16$$

$$1x + 3y + 2z = 9$$

Re-arranging the above equation

$$3x + 4y + 2z = 16 \quad \text{--- (1)}$$

$$2x + 4y + 3z = 13 \quad \text{--- (2)}$$

$$1x + 3y + 2z = 9 \quad \text{--- (3)}$$

Nature

$$\begin{bmatrix} 3 & 4 & 1 \\ 2 & 4 & 3 \\ 1 & 3 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 16 \\ 13 \\ 9 \end{bmatrix}$$

$$R_2 \rightarrow R_2 - \frac{R_1}{a_{11}} \times a_{21}$$

$$R_3 \rightarrow R_3 - \frac{R_1}{a_{11}} \times a_{31}$$

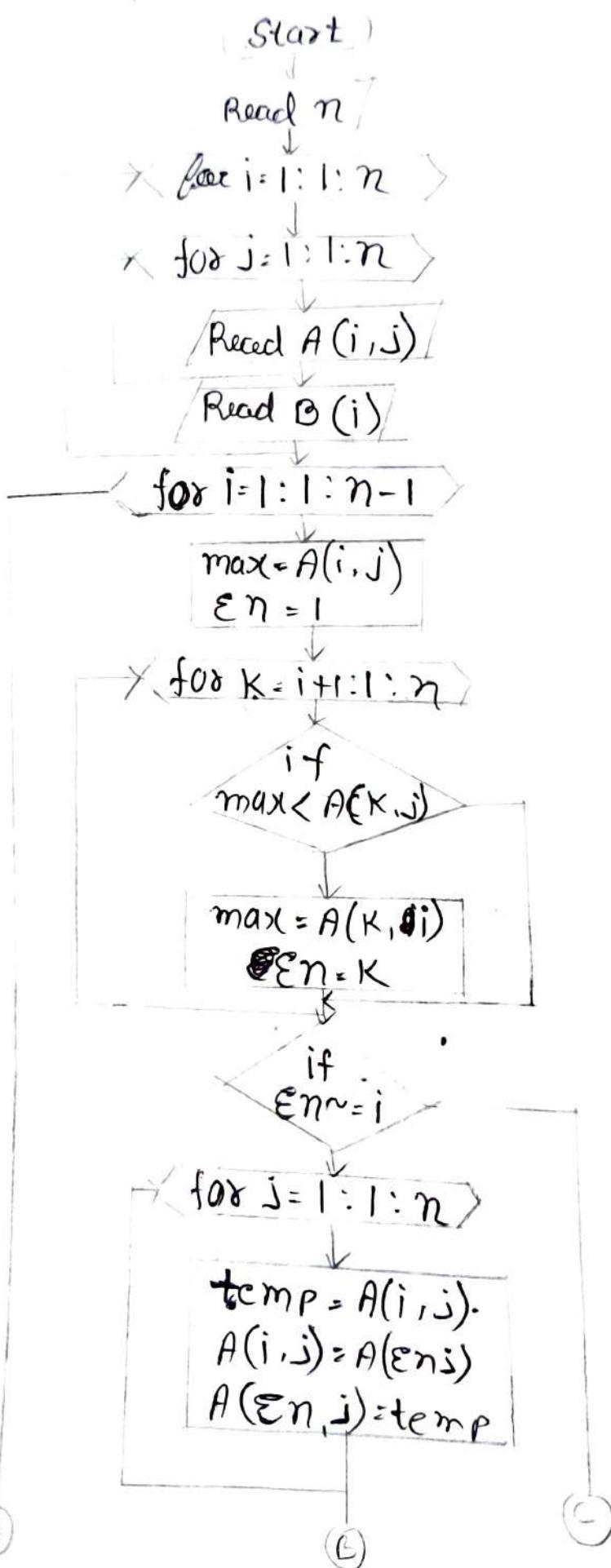
1st pivoting

$$\begin{bmatrix} 3 & 4 & 1 \\ 2 & 0 & 3 \\ 1 & 3 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 16 \\ 3 \\ 9 \end{bmatrix}$$

$$R_3 \rightarrow R_3 - \frac{R_2}{a_{22}} \times a_{32}$$

2nd Pivoting

Flowchart for Gauss Elimination Method



2nd Pruefung

$$\begin{bmatrix} 3 & 6 & 1 \\ 0 & 0 & 7/3 \\ 0 & 1 & 5/3 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 16 \\ 7/3 \\ 11/3 \end{bmatrix}$$

Equations

$$3x + 6y + z = 16$$

$$y + \frac{5}{3}z = \frac{11}{3}$$

$$\frac{7}{3}z = \frac{7}{3}$$

$$\therefore x = 1$$

$$y = 2$$

$$z = 1$$

$$\begin{aligned} \text{temp} &= B(i) \\ B(i) &= B(\epsilon n) \\ B(\epsilon n) &= \text{temp} \end{aligned}$$

~~for k = i+1:1:n~~

$$\text{mult} = \frac{A(k, i)}{A(i, i)}$$

~~for j = 1:1:n~~

$$A(k, j) = A(k, j) - \text{mult} * A(i, j)$$

$$B(k) = B(k) - \text{mult} * B(i)$$

~~for i = n:-1:1~~

$$\text{sum} = B(i)$$

~~for j = i+1:n~~

$$\text{sum} = \text{sum} - A(i, j) * x(j)$$

$$x(i) = \text{sum} / A(i, i)$$

~~for i = 1:1:n~~

~~print x(i)~~

(End)

14/2/24 10:09 AM E:\PCCOE\...\TYMEB228 GAUSS ELIMINATION.m 1 of 2

% Name : Sarthak Abhay PATIL
% Roll no. : TYMEB228
% Div. : B / B4

```
%INPUT
n = input('Enter the no. of the Equation= ');
for i=1:1:n
    for j=1:1:n
        a(i,j)= input('Enter the value of a(i,j)= ');
    end
    b(i)= input('Enter the value of b(i)= ');
end
for i=1:1:n-1
    max= abs(a(i,i));
    Rn=i;

    for k=i+1:1:n
        if max<abs(a(k,i))
            max= abs(a(k,i));
            Rn= k;
        end
    end
    if Rn~=i
        for j=1:1:n
            temp = a(i,j);
            a(i,j) = a(Rn,j);
            a(Rn,j)= temp;
        end
        temp = b(i);
        b(i) = b(Rn);
        b(Rn)= temp;
    end
end
Acc = input('Enter the value of Accuracy= ');
err = 1;
xold = zeros(n,1);
xnew = zeros(n,1);

while err>Acc
    for i=1:1:n
        xold(i)=xnew(i);
    end
    for i=1:1:n
        term = b(i);
        for j= 1:1:n
            if j~=i
                if j>i
                    term = term-a(i,j)*xold(j);
                else
                    term = term-a(i,j)*xnew(j);
                end
            end
        end
    end
    err = norm(xnew-xold);
end
```

```
    end
end
xnew[1] = xterm[1];
else abs(xnew - xold)
end

err = err();
for i=1:n
    if err(i) > 1e-10
        err(i)=0;
    else
        err(i)=1;
    end
end
err=err';

for i=1:n
    if err(i) == 1
        fprintf('Iteration %d is not successful\n',i);
    end
end

% Output
xnew
xold
t(1)
t(2)
t(3)
t(4)
t(5)
t(6)
t(7)
t(8)
t(9)
t(10)
t(11)
t(12)
t(13)
t(14)
t(15)
t(16)
t(17)
t(18)
t(19)
t(20)
```

2) Tri-diagonal matrix Algorithm Method:-

- solve the full tri-diagonal system & find temp T_1, T_2, T_3, T_4 in $^{\circ}\text{C}$

$$\begin{bmatrix} 2.04 & -1 & 0 & 0 \\ -1 & 2.04 & -1 & 0 \\ 0 & -1 & 2.04 & -1 \\ 0 & 0 & -1 & 2.04 \end{bmatrix} \begin{bmatrix} T_1 \\ T_2 \\ T_3 \\ T_4 \end{bmatrix} = \begin{bmatrix} 40.8 \\ 0.8 \\ 0.8 \\ 200.8 \end{bmatrix}$$

$$\rightarrow a = \begin{bmatrix} 0 \\ -1 \\ -1 \\ -1 \end{bmatrix} \quad b = \begin{bmatrix} 2.04 \\ 2.04 \\ 2.04 \\ 2.04 \end{bmatrix} \quad c = \begin{bmatrix} -1 \\ -1 \\ -1 \\ 0 \end{bmatrix} \quad d = \begin{bmatrix} 40.8 \\ 0.8 \\ 0.8 \\ 200.8 \end{bmatrix}$$

i: 2 : 1 : n

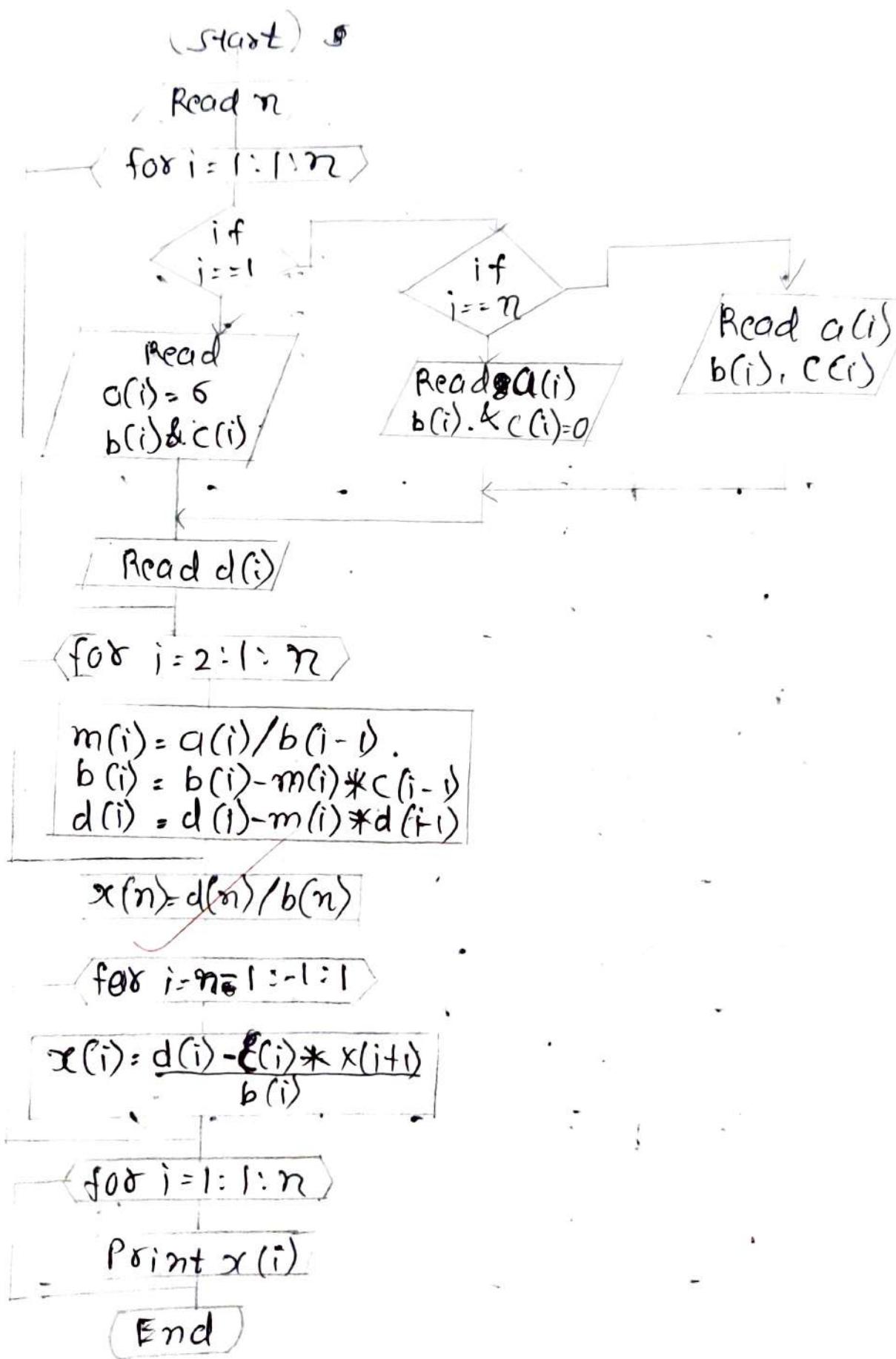
$$m(i) = \frac{a(i)}{b(i-1)} \quad m_2 = \frac{-1}{2.04}$$

$$b(i) = b(i) - m(i) \times c(i-1) \\ = -2.04 - \left(\frac{-1}{2.04}\right) \times (-1) = 1.549$$

$$d(i) = d(i) - m(i) \times d(i-1) \\ = 0.8 - \left(\frac{-1}{2.04}\right) \times 40.8 = 20.8$$

$$a = \begin{bmatrix} 0 \\ 0 \\ -1 \\ -1 \end{bmatrix} \quad b = \begin{bmatrix} 2.04 \\ 1.549 \\ 2.04 \\ 2.04 \end{bmatrix} \quad c = \begin{bmatrix} -1 \\ -1 \\ -1 \\ 0 \end{bmatrix} \quad d = \begin{bmatrix} 40.8 \\ 20.8 \\ 0.8 \\ 200.8 \end{bmatrix}$$

2) flowchart for TDMA



```
n=input('enter no of equations n=');  
for i=1:1:n  
    if i==1  
        a(i)=0;  
        b(i)=input('enter B matrix element=');  
        c(i)=input('enter C matrix element=')  
    else  
        if i==n  
            a(i)=input('enter A matrix element=');  
            b(i)=input('enter B matrix element=');  
            c(i)=0;  
        else  
            a(i)=input('enter A matrix element=');  
            b(i)=input('enter B matrix element=');  
            c(i)=input('enter C matrix element=');  
        end  
    end  
    d(i)=input('enter D matrix element=');  
end  
for i=2:1:n  
    m(i)=a(i)/b(i-1);  
    b(i)=b(i)-m(i)*c(i-1);  
    d(i)=d(i)-m(i)*d(i-1);  
end  
x(n)=d(n)/b(n)  
for i=n-1:-1:1  
    x(i)=(d(i)-c(i)*x(i+1))/b(i);  
end  
for i=1:1:n  
    fprintf('\nX(%d)=%f',i,x(i));  
end
```

v OUTPUT
v TDMA
v enter no of equations n=4
v enter B matrix element=2.04
v enter C matrix element=-1
v enter D matrix element=40.8
v enter A matrix element=-1
v enter B matrix element=1.04
v enter C matrix element=-1
v enter D matrix element=0.8
v enter A matrix element=-1
v enter B matrix element=0.04
v enter C matrix element=-1
v enter D matrix element=0.8
v enter A matrix element=-1

7/2/24 2:07 AMD:\TYMEB228\TDMA.m

```
% enter B matrix element=2.04
% enter D matrix element=200.8
%
x =
31.6887    23.8450    16.1550   159.4795
%
x(1)=65.969834
x(2)=93.778462
x(3)=124.538226
x(4)=159.479524>>
```

$$i = 3, m_3 = \frac{c(3)}{b(3-1)} = \frac{-1}{1.544}$$

b

$$b(3) = 2.04 - \left(\frac{-1}{1.544} \right) \times (-1) = 1.394$$

$$d(3) = 0.8 - \left(\frac{-1}{1.544} \right) \times 20.8 = 14.228$$

$a = [0]$	$b = [2.04]$	$c = [-1]$	$d = [0.8]$
$[0]$	$[1.544]$	$[-1]$	$[20.8]$
$[0]$	$[1.394]$	$[-1]$	$[14.228]$
$[-1]$	$[2.04]$	$[0]$	$[200.8]$

$$i = 4, m_4 = \frac{c(4)}{b(4-1)} = \frac{-1}{1.394}$$

$$b(4) = 2.04 - \left(\frac{-1}{1.394} \right) \times (-1) = 1.322$$

$$d(4) = 200.8 - \left(\frac{-1}{1.394} \right) \times 14.228 = 211.006$$

$a = [0]$	$b = [2.04]$	$c = [-1]$	$d = [0.8]$
$[0]$	$[1.544]$	$[-1]$	$[20.8]$
$[0]$	$[1.394]$	$[-1]$	$[14.228]$
$[0]$	$[1.322]$	$[0]$	$[211.006]$

$$\gamma(n) = \frac{d(n)}{b(n)}$$

$$T_4 = \gamma(4) = \frac{d(4)}{b(4)} = \frac{211.006}{1.322}$$

$$T_4 = 159.611^\circ\text{C}$$

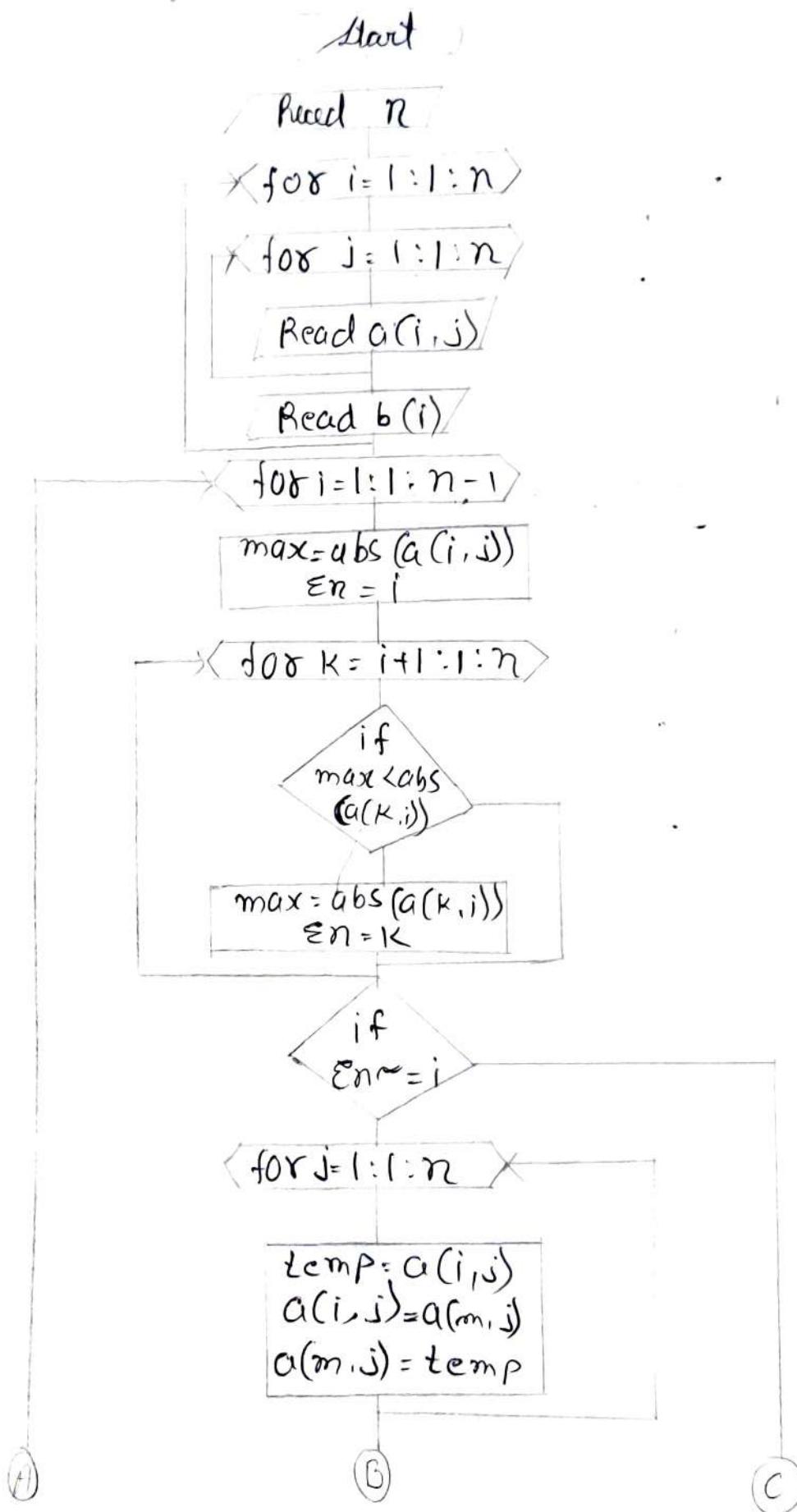
$$T(i) = \frac{d(i) - c(i) \times T(i+1)}{b(i)}$$

$$T(3) = 124.70^\circ\text{C}$$

$$T(2) = 93.77^\circ\text{C}$$

$$T(1) = 63.96^\circ\text{C}$$

3) Flowchart for Gauss Seidel Method



3) Gauss Seidel Method :-

- solve the foll upto 0.001 accuracy

$$x_1 + 2x_2 + 9x_3 = -23$$

$$2x_1 - 7x_2 - 20x_3 = -57$$

$$20x_1 + 2x_2 + 6x_3 = 28$$

→ Bounding

$$20x_1 + 2x_2 + 6x_3 < 28 \quad \text{--- (1)}$$

$$x_1 + 20x_2 + 9x_3 = -23 \quad \text{--- (2)}$$

$$2x_1 - 7x_2 - 20x_3 < -51 \quad \text{--- (3)}$$

- from eqn (1) (2) (3)

$$x_1 = \frac{1}{20} (28 - 2x_2 - 6x_3)$$

$$x_2 = \frac{1}{20} (-23 - x_1 - 9x_3)$$

$$x_3 = \frac{1}{20} (-57 - 2x_1 + 7x_2)$$

Iteration (1)

assume $x_1 = 0, x_2 = 0, x_3 = 0$

$$\therefore x_1 = \frac{1}{20} (28 - 2(0) - 6(0)) = 1.4$$

$$x_2 = -1.22$$

$$x_3 = 3.417$$

B

$\text{temp} = b(i)$
 $b(i) = b(\epsilon^n)$
 $b(\epsilon^n) = \text{temp}$

Read(acc, ϵ^n)

$err = 1$

while $err > acc$

for $i = 1 : 1 : n$

$x_{old}(i) = x_{new}(i)$

for $i = 1 : 1 : n$

$term = b(i)$

for $j = 1 : 1 : n$

if
 $j \neq i$

if
 $j < i$

$term = term - a(i,j) * x_{old}(j)$

$term = term - a(i,j) * x_{new}(j)$

$x_{new}(i) = term / A(i,i)$

$e(i) = \text{abs}(x_{new}(i) - x_{old}(i))$

①

$$|x_1^{\text{new}} - x_1^{\text{old}}| = 1.4 > 0.001$$

$$|x_2^{\text{new}} - x_2^{\text{old}}| = 1.22 > 0.001$$

$$|x_3^{\text{new}} - x_3^{\text{old}}| = 3.917 > 0.001$$

→ doesn't match with accuracy

then go for next iteration

Iteration	x_1	x_2	x_3
1	0	0	0
2	1.4	-1.22	3.917
3	0.346	-2.7125	3.849
4	0.6165	-2.9079	3.919
5	0.5144	-2.9394	3.930
6	0.5148	-2.9443	3.9320
7	0.51483	-2.9451	3.9322

(1)

(2)

$\text{err} = e(i)$

$\leftarrow \text{for } i = 2 : 1 : n \rightarrow$

if
 $\text{err} < e(i)$

$\text{err} = e(i)$

$\leftarrow \text{for } i = 1 : 1 : n \rightarrow$

$\text{Point } x_{\text{new}}(i)$

(end)



```
n=input('enter number or equation');
for i=1:1:n
    for j=1:1:n
        a(i,j)=input('Enter matrix A elements=');
    end
    b(i)=input('Enter matrix B elements=');
end
for i=1:1:n-1
max = abs(a(i,i));
rn = i;
for k = i+1:1:n
    if max<abs(a(k,i));
        max = abs(a(k,i));
        rn=k;
    end
    if rn == i;
        for j=1:1:n
            temp=a(i,j);
            a(i,j)=a(rn,j);
            a(rn,j)=temp;
        end;
        temp = b(i);
        b(i)=b(rn);
        b(rn)=temp;
    end
end
end
acc = input('Enter accuracy = ');
err=1
xold=zeros(n,1);
xnew=zeros(n,1);
while err>acc
    for i=1:1:n
        xold(i)=xnew(i);
    end
    for i=1:1:n
        term=b(i);
        for j = 1:1:n
            if j~=i
                if j<i
                    term=term-a(i,j)*xold(j);
                else
                    term=term-a(i,j)*xnew(j);
                end
            end
            xnew(i)=((term)/a(i,j));
            e(i)=abs(xold(i)-xnew(i));
            fprintf('\nx(%d)=%f',i,xnew(i));
        end
        err= e(1)
```

```
for i=2:l:n
    if err<e(i)
        err=e(i);
    end
end
fprintf('\n');
enter number of equation3
Enter matrix A elements=1
Enter matrix A elements=2
Enter matrix A elements=20
Enter matrix B elements=20
Enter matrix A elements=-7
Enter matrix A elements=2
Enter matrix A elements=9
Enter matrix B elements=-20
Enter matrix A elements=6
Enter matrix A elements=-23
Enter matrix A elements=-57
Enter matrix B elements=28
Enter accuracy = 0.001
err =
1
x(1)=1.000000 x(2)=-1.444444 x(3)=0.196881
err =
1
x(1)=0.947563 x(2)=-1.682110 x(3)=0.287261
err =
0.0524
x(1)=0.880950 x(2)=-1.824301 x(3)=0.337625
err =
0.0666
x(1)=0.844805 x(2)=-1.902776 x(3)=0.365486
err =
0.0361
x(1)=-0.824792 x(2)=-1.946203 x(3)=0.380902
err =
0.0200
x(1)=0.813718 x(2)=-1.970232 x(3)=0.389433
err =
0.0111
x(1)=0.807091 x(2)=-1.983529 x(3)=0.394153
err =
0.0041
x(1)=0.804200 x(2)=-1.990886 x(3)=0.396765
err =
0.0034
x(1)=0.802324 x(2)=-1.994957 x(3)=0.398210
err =
0.0019
x(1)=0.801286 x(2)=-1.997506 x(3)=0.399009
```

Assignment no 04

Numerical Integration:-

- Numerical integration is the method to estimate the area under a curve when it is hard to find the exact answer.
- It divides the curve into small parts & approximate the area of each part . Then add them up for overall estimate.

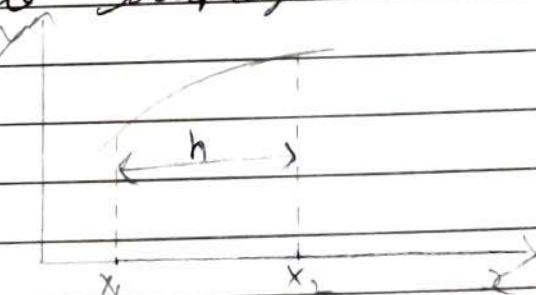
i) Trapezoidal method

- it is simple but less accurate compared to other methods
- Approximates the integral by dividing the area under curve into trapezoid.

$h = \text{step size}$

$$A = h/2 [Y_1 + Y_n]$$

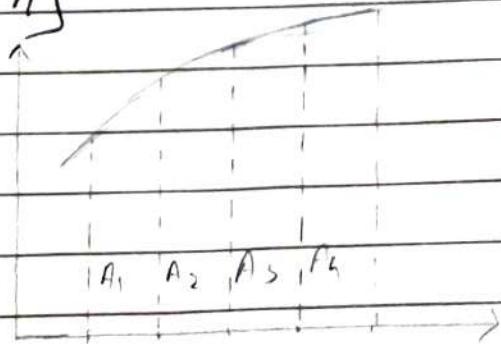
- here $Y = f(x)$



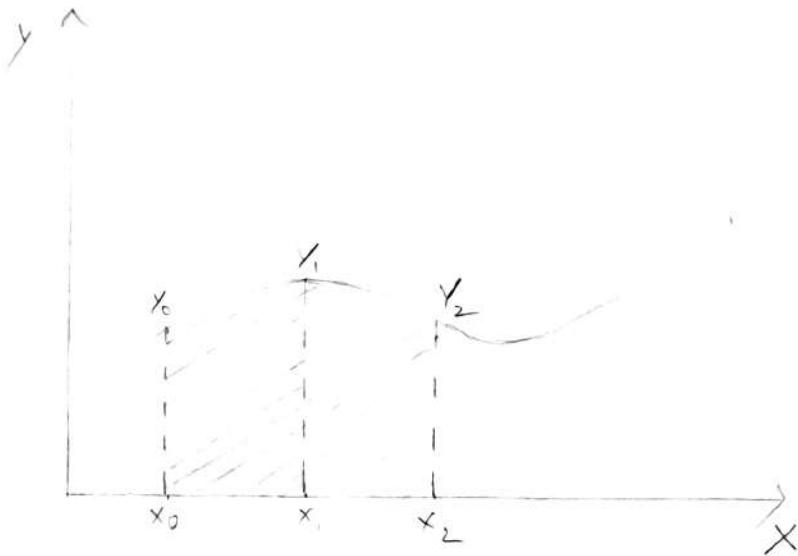
When there are multiple areas then:-

$$I: A_1 + A_2 + A_3 + A_4 + \dots + A_n$$

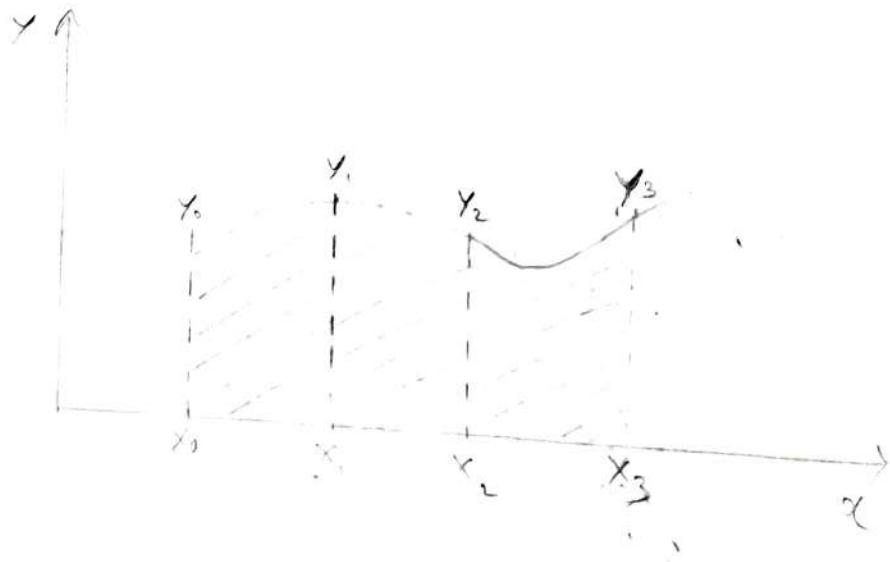
$$I: h \left[Y_1 + 2Y_2 + 2Y_3 + 2Y_4 + \dots + Y_n \right]$$



2) Simpson's $\frac{1}{3}$ rd rule



3) Simpson's $\frac{3}{8}$ th rule



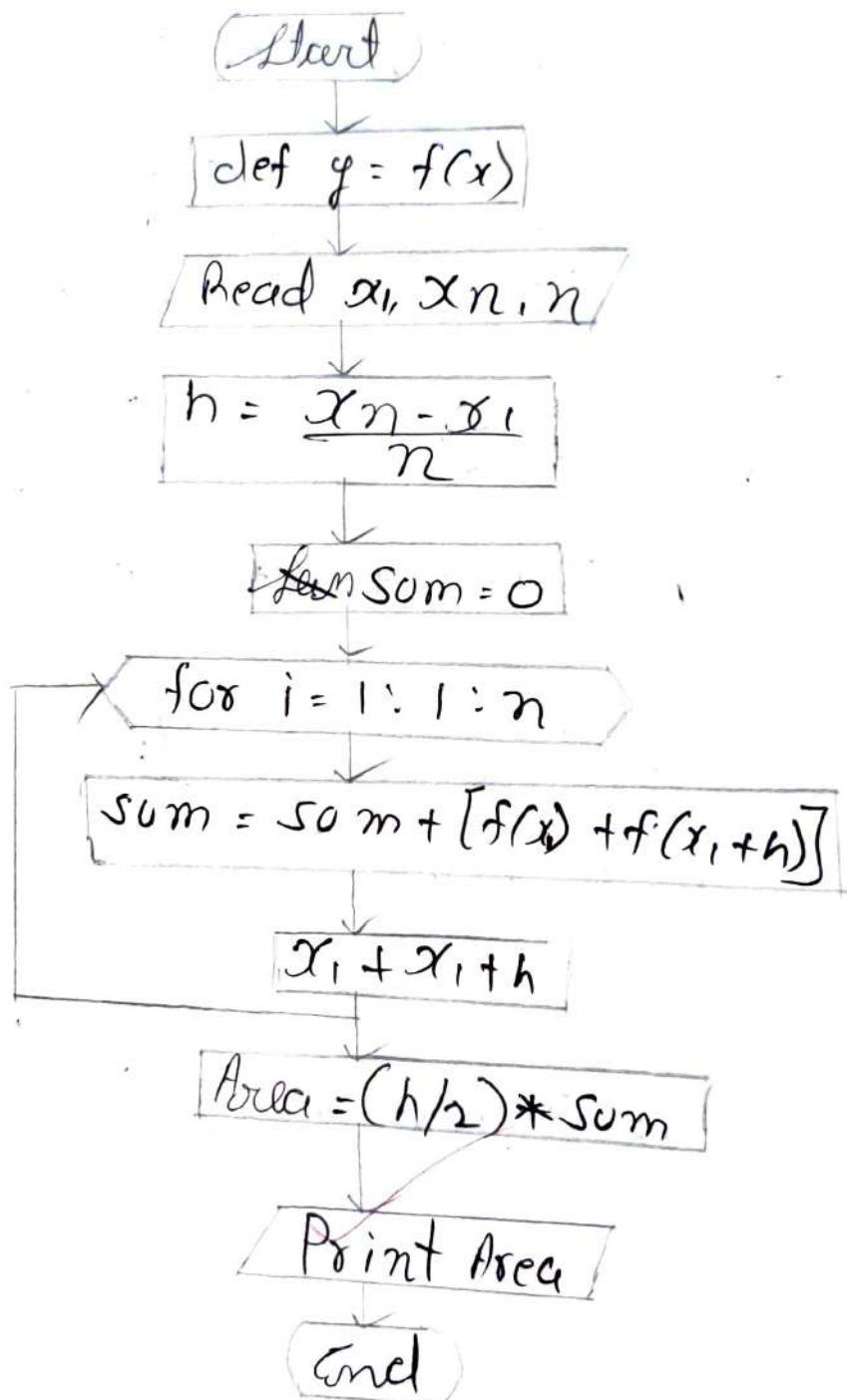
27 Simpson's $\frac{1}{3}$ rd rule method:

- Simpson's $\frac{1}{3}$ rd rule uses quadratic interpolations to approximate the integral this more accurate than the trapezoidal rule & require fewer function evaluations.
- A polynomial of second order or that different of order higher than second.
- here $A = \frac{h}{3} [Y_1 + 4Y_2 + 2Y_3 + 4Y_4 + Y_n]$

37 Simpson's $\frac{3}{8}$ th rule method:

- Simpson's $\frac{3}{8}$ th rule is similar to Simpson's $\frac{1}{3}$ rd rule but uses cubic interpolation.
- it provide even higher accuracy but require more function evaluation.
- here $A = \frac{3h}{8} [Y_0 + 3Y_1 + 3Y_2 + Y_3]$

#1 Flowchart for Trapezoidal Rule.



```
% Name : sarthak PATIL
% Roll no. : TYMEB228
% Batch : B4
f = inline('3*(0.4+0.004*T)');
x1 = input('Enter the value of x1 = ');
xn = input('Enter the value of xn = ');
n = input('Enter the value of n = ');

h = (xn-x1)/n;
Area = 0;
for i=1:1:n
    Area = Area+(f(x1)+f(x1+h));
    x1 = (x1+h);
end
Area = (h/2)*Area;
fprintf('The value Area is =%f',Area)

%OUTPUT
Enter the value of x1 = 25
Enter the value of xn = 125
Enter the value of n = 4
The value Area is =210.000000>
```



Q) During a certain process the specific heat capacity of system is given by $C = [0.4 + 0.004T]$. Find the heat transferred when temp changes from 25°C to 125°C . the mass of gas is 3kg . take $n = 4$ & solve by :-
 1) trapezoidal method
 2) Simpson's $\frac{1}{3}$ rd rule
 3) Simpson's $\frac{3}{8}$ th rule

→ Given data:- $T_1 = 25^\circ\text{C}$ $6 \Rightarrow$

$$T_n = 125^\circ\text{C}$$

$$C = [0.4 + 0.004T] \text{ kJ/kg}^\circ\text{C}$$

$$m = 3\text{kg}$$

We know, T_n

$$\therefore Q = \int_{T_1}^{T_n} m(C_p dT)$$

$$\therefore Q = \int_{25}^{125} 3 \times [0.4 + 0.004T] dT$$

$$y = f(T) = 3[0.4 + 0.004T]$$

$$T_1 = 25^\circ\text{C}$$

$$T_2 = T_1 + h = 50^\circ\text{C} \quad h = \frac{T_n - T_1}{n}$$

$$T_3 = 75^\circ\text{C}$$

$$T_4 = 100^\circ\text{C}$$

$$T_n = 125^\circ\text{C}$$

$$= \frac{125 - 25}{4} = 25$$

$$Y_1 = f(T_1) = 3(0.4 + 0.004 \times 25) = 1.50$$

$$Y_2 = 1.80$$

$$Y_3 = 2.10$$

$$Y_4 = 2.40$$

$$Y_n = 2.70$$

flowchart for Simpson's rule

(Start)

def $y = f(x)$

Area, x_n, n

$$h = \frac{x_n - x_1}{n}$$

$$\text{Sum} = 0$$

for $i = 1 : 2 : n$

$$\text{Sum} = \text{Sum} + [f(x_1) + 4 * f(x_1 + h) + f(x_1 + 2h)]$$

$$x_1 = x_1 + 2h$$

$$\text{Area} = (h/3) * \text{Sum}$$

Print Area

End.

```
% Name :sarthak PATIL
% Roll no. : TYMEB228
f = inline('3*(0.4+0.004*T)');
x1 = input('Enter the value of x1 = ');
xn = input('Enter the value of xn = ');
n = input('Enter the value of n = ');

h = (xn-x1)/n;
Area = 0;
for i=1:2:n
    Area = Area+(f(x1)+ 4*f(x1+h)+ f(x1+2*h));
    x1 = (x1+2*h);
end
Area = (h/3)*Area;
fprintf('The value Area is =%f',Area )

%OUTPUT
Enter the value of x1 = 25
Enter the value of xn = 125
Enter the value of n = 4
The value Area is =210.000000
```



- By Trapezoidal rule

$$A = I - \alpha = h \left[\frac{Y_1 + 2Y_2 + 2Y_3 + 2Y_4 + Y_n}{2} \right]$$

$$= \frac{25}{2} [1.5 + (2 \times 1.8) + (2 \times 2.10) + 2(2.40) + 2.7]$$

$$= 210$$

- By Simpson's $\frac{1}{3}$ rd Rule

$$A = I - \alpha = \frac{h}{3} [Y_1 + 4Y_2 + 2Y_3 + 4Y_4 + Y_n]$$

$$= \frac{25}{3} [1.5 + 4(1.8) + 2(2.1) + 4(2.4) + 2.7]$$

$$= 210$$

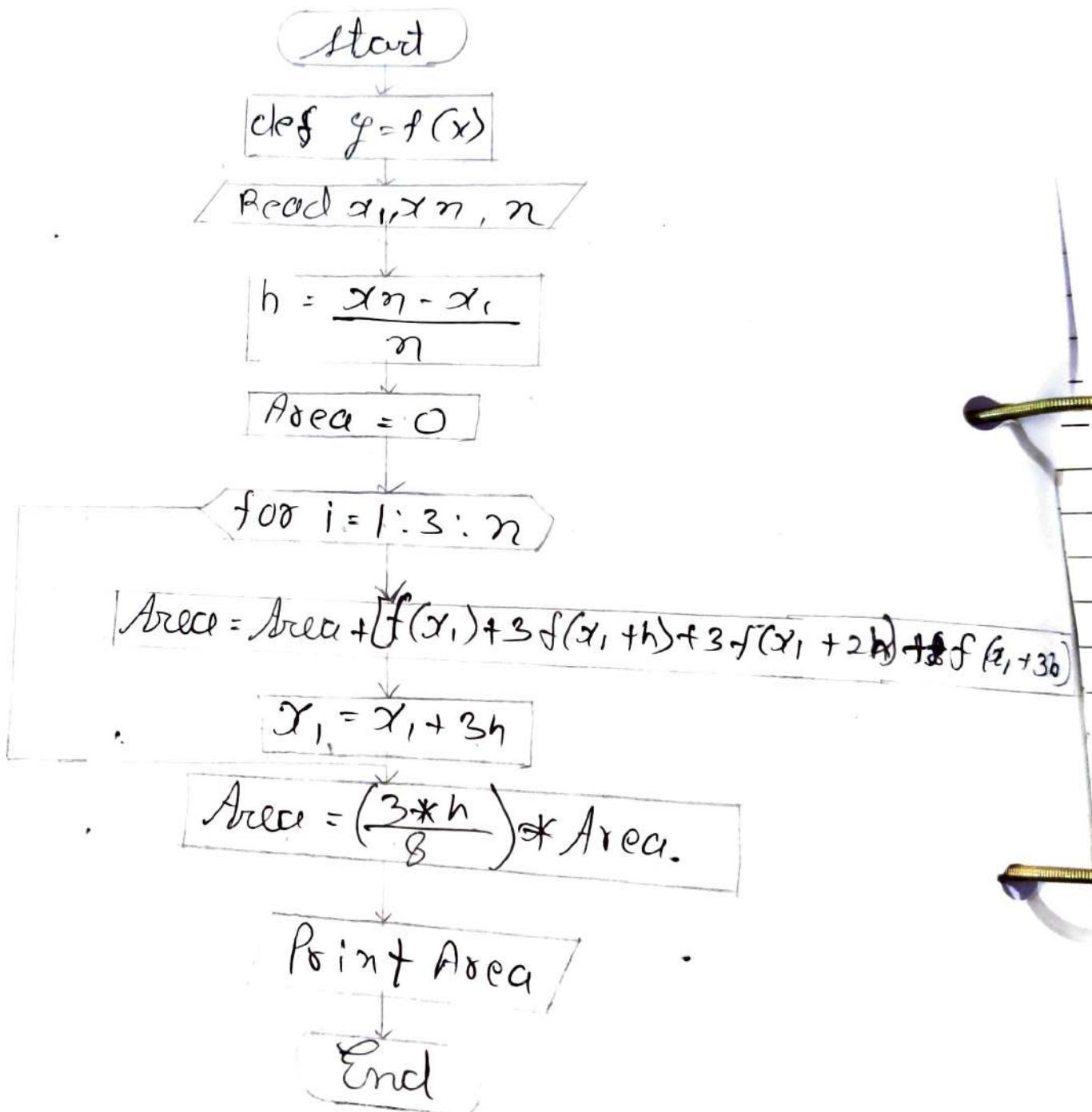
- By Simpson's $\frac{3}{8}$ th rule

$$A = I - \alpha = \frac{3h}{8} [(Y_1 + Y_n) + 3(Y_2 + Y_3) + 2(Y_4)]$$

$$= \frac{3 \times 25}{8} [(1.5 + 2.7) + 3(1.8 + 2.1) + 2(2.4)]$$

$$= 210$$

Flowchart for Simpson 3/8th rule.



```
Name = sarthak Patil
Roll no = TYMER228
Batch -B4
f = inline('3*(0.4+0.004*T)');
x1 = input('Enter the value of x1 = ');
xn = input('Enter the value of xn = ');
n = input('Enter the value of n = ');

h = (xn-x1)/n;
Area = 0;
for i=1:3:n
    Area = Area+(f(x1)+ 3*f(x1+h)+ 3*f(x1+2*h)+ f(x1+3*h));
    x1 = (x1+3*h);
end
Area = (3*h/8)*Area;
fprintf('The value Area is =%f',Area )

simpsonrule3by8
Enter the value of x1 = 25
Enter the value of xn = 125
Enter the value of n = 6
The value Area is =210.000000>>
```

Assignment no 5

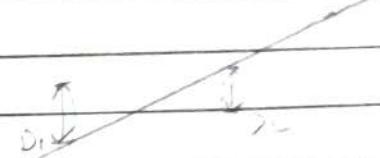
* Least Square Method

1) Straight Line

$$y = mx + c$$

$$a \sum x^2 + b \sum x = \sum xy$$

$$a \sum x + nb = \sum y$$



2) The result of measured electrical resistance (R) of copper wire at various temperature are

Temp	19	25	30	36	40	45	50
Resistance	76	77	79	80	82	83	85

if resistance is related to temp by relation

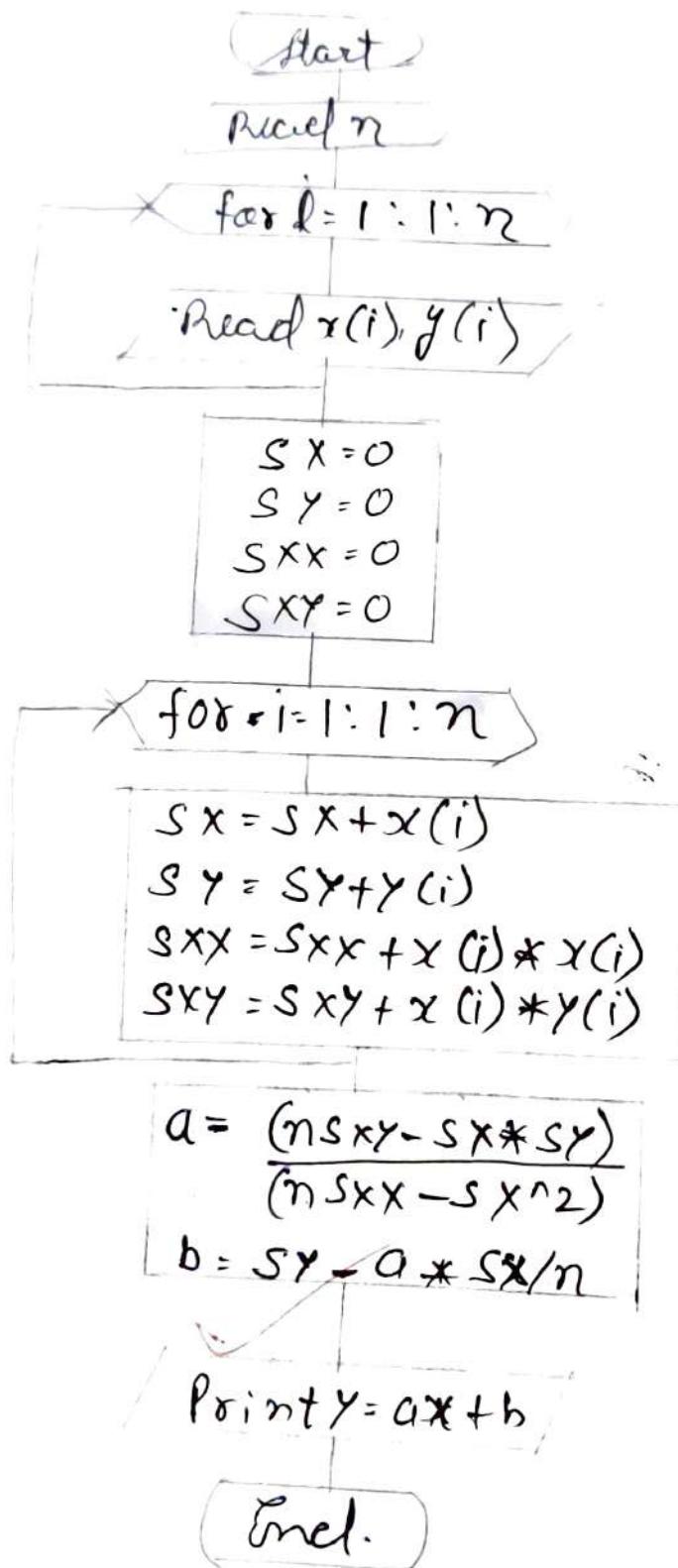
$R = aT + b$ find the value of a & b

$$\rightarrow n = 7 \quad a \sum x^2 + b \sum x = \sum xy$$

$$\sum D^2 = nm \quad a \sum x + nb = \sum y$$

$\sum T$	$\sum R$	$\sum T^2$	$\sum TR$
19	76	361	1999
25	77	625	1925
30	79	900	2370
36	80	1290	2880
40	82	1600	2380
45	83	2025	3735
50	85	2500	4250
245	562	9307	19889

Flowchart for 1st straight line.

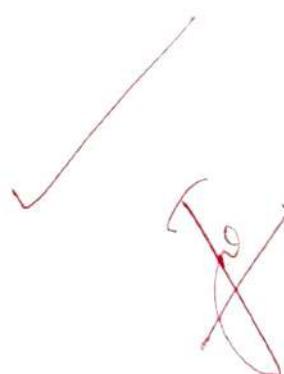


```
n = input ('Enter the Number Of intervals');
for i= 1:1:n
x(i)= input ('Enter the x value .');
y(i)= input ('Enter the y value .');
end
sx=0;
sy=0;
sxx=0;
sxy=0;
for i= 1:1:n
sx=sx+x(i);
sy=sy+y(i);
sxx=sxx+x(i)*x(i);
sxy=sxy+x(i)*y(i);
end
a=(n*sxy-sx*sy)/(n*sxx-sx*sx);
b=(sy-a*sx)/n;
fprintf('y=%fx+%f',a,b);
```

%OUTPUT

```
%Enter the Number Of intervals :7
%Enter the x value :19
%Enter the y value :76
%Enter the x value :25
%Enter the y value :77
%Enter the x value :30
%Enter the y value :79
%Enter the x value :36
%Enter the y value :80
%Enter the x value :40
%Enter the y value :82
%Enter the x value :45
%Enter the y value :83
%Enter the x value :50
%Enter the y value :85
```

y = 0.292350x+70.053474>>



Wing equation

$$a \varepsilon x^2 + b \varepsilon x = \varepsilon xy$$

$$a \varepsilon x + nb = \varepsilon y$$

$$(a \times 9307) + (b \times 245) = 19884$$

$$(a \times 245) + (b \times 7) = 562$$

by solving the above equation

$$a = 0.2923$$

$$b = 70.05$$

$$\therefore y = ax + b$$

$$\therefore y = 0.2923x + 70.05$$

2) Quadratic Equation

It is used in fitting quadratic equation to data points in curve fitting.

To fit a quadratic equation $y = ax^2 + bx + c$ to a set of data points, you would minimize the sum of the square of the diff between the observed & predicted value of y for each data point.

$$a \sum x^4 + b \sum x^3 + c \sum x^2 = \sum y^2$$

$$a \sum x^3 + b \sum x^2 + c \sum x = \sum xy$$

$$c \sum x^2 + b \sum x + n c = \sum y$$

2. Find the value for $y = ax^2 + bx + c$ for given data using quadratic equation method of least square technique

x	1	2	3	4	5	6	7
y	-5	-2	5	16	31	50	73

$$n = 7$$

$$\sum D = \min$$

x	y	x^4	x^3	x^2	$x^2 y$	xy
1	-5	1	1	1	-5	-5
2	-2	16	8	4	-8	-4
3	5	81	27	9	45	15
4	16	256	64	16	256	64
5	31	625	125	25	775	155
6	50	1296	216	36	1800	300
7	73	2401	343	49	3577	511
28	168	3676	784	196	6496	1036

to find a, b, c

$$(a \times 9675) + b(784) + c(140) = 6550$$

$$(a \times 784) + (b \times 140) + (c \times 28) = 1036$$

$$(a \times 140) + (b \times 28) + c(7 \times 4) = 168$$

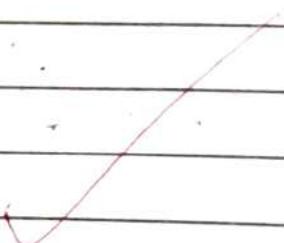
$$\therefore a = 2$$

$$b = -3$$

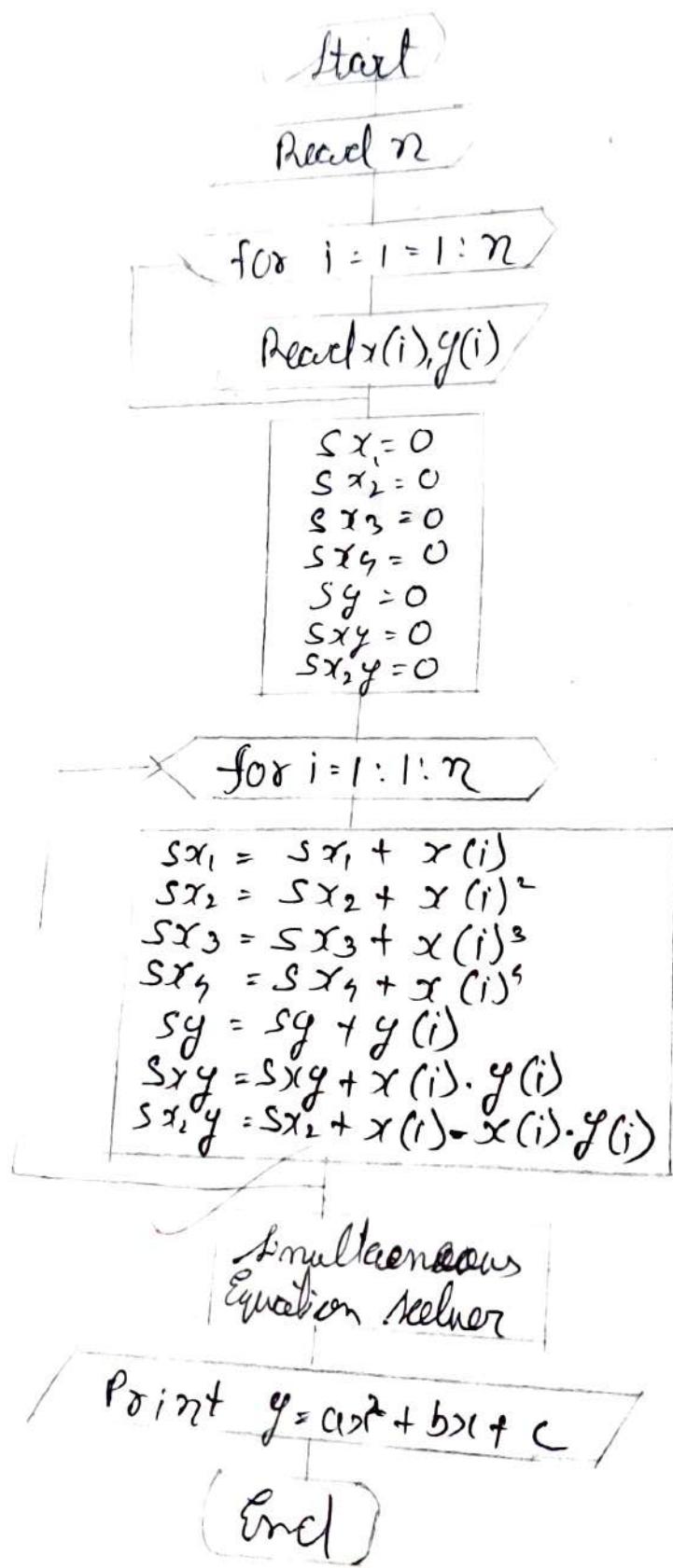
$$c = -4$$

$$\therefore y = ax^2 + bx + c$$

$$\therefore y = 2x^2 - 3x - 4$$



Flowchart for 1st quadratic equation:



21/2/24 10:10 AM C:\Users\PCCOE\Desktop\Degree Curve 2nd.m 1 of 2

```
% Sittikar Abhay Patil
% TYMEB208
% B4
n = input('Enter the value of n = ');
for i=1:1:n
    x(i)= input('Enter the value of x = ');
    y(i)= input('Enter the value of y = ');
end
Sx = 0;
Sx2 = 0;
Sx3 = 0;
Sx4 = 0;
Sy = 0;
Sxy = 0;
Sx2y = 0;
for i = 1:1:n
    Sx = Sx + x(i);
    Sx2 = Sx2 + x(i)*x(i);
    Sx3 = Sx3 + x(i)^3;
    Sx4 = Sx4 + x(i)^4;
    Sy = Sy + y(i);
    Sxy = Sxy + x(i)*y(i);
    Sx2y = Sx2y + x(i)*x(i)*y(i);
end
A = [Sx4 Sx3 Sx2; Sx3 Sx2 Sx; Sx2 Sx n];
B = [Sx2y; Sxy; Sy];

x = linsolve(A,B);
a = x(1);
b = x(2);
c = x(3);
fprintf('y = (%f)*x^2 + (%f)*x + %f',a,b,c)

%OUTPUT
Enter the value of n = 7
Enter the value of x = 1
Enter the value of y = -5
Enter the value of x = 2
Enter the value of y = -2
Enter the value of x = 3
Enter the value of y = 5
Enter the value of x = 4
Enter the value of y = 16
Enter the value of x = 5
Enter the value of y = 31
Enter the value of x = 6
Enter the value of y = 50
Enter the value of x = 7
Enter the value of y = 73
y = (2.000000)*x^2 + (-3.000000)*x + -4.000000>>
```

3)

Power curve equation

$$a) y = ax^b$$

$$b) y = ab^x$$

$$c) y = xy^b$$

$$d) y = ax^b$$

$$b) y = ab^x$$

$$\log y = \log a + b \log x$$

$$Y = \log y$$

$$A = b$$

$$B = \log a$$

$$X = \log x$$

$$\log y = \log a + x \log b$$

$$Y = \log y$$

$$A = \log b$$

$$X = x$$

$$B = \log a$$

$$A \varepsilon x^2 + B \varepsilon x = \cancel{\varepsilon XY}$$

$$A \varepsilon x + nB = \cancel{\varepsilon X} \varepsilon Y$$

$$A \varepsilon x^2 + B \varepsilon x = \varepsilon XY$$

$$A \varepsilon x + nB = \varepsilon Y$$

$$A = b, a = e^B$$

$$a = e^B, b = e^A$$

$$c) a = xy^b$$

$$\log a = \log x + b \log y$$

$$\log a = \frac{1}{b} \log x - \frac{1}{b} \log y$$

$$\therefore Y = \log y$$

$$X = \log x$$

$$A = -\frac{1}{b}$$

$$B = \frac{1}{b}$$

$$A \varepsilon x^2 + B \varepsilon x = \varepsilon xy$$

$$A \varepsilon x + nB = \varepsilon y$$

$$a = e^b \quad b = A$$

Q) Equation of best fitted curve $y = ax^b$ using least sq criteria for the set of point given below a & b value.

x	0.5	1.5	2	2.5	3
y	0.7425	3.8578	5.9397	8.301	10.912

$$\rightarrow y = a x^b$$

$$\log y = \log a + b \log x$$

$$A \varepsilon x^2 + B \varepsilon x = \varepsilon xy$$

$$A \varepsilon x + nB = \varepsilon y$$

$x = \log x$	$y = \log y$	x^2	xy
-0.693	-0.2977	0.4802	0.2063
0.405	1.3500	0.1640	0.5467
0.693	1.7815	0.4802	1.2346
0.916	2.1163	0.8306	1.4385
1.0986	2.3893	1.2069	2.6255
2.4196	7.3395	3.1707	6.5505

$$(A \times 3.1707) + B(2.9196) = 6.5509$$

$$(A \times 2.9196) + (5 \times B) = 7.3395$$

$$A = 1.599$$

$$B = 0.7421$$

$$A = b = 1.599$$

$$A = e^B$$

$$= e^{0.7421} = 2.10034$$

$$\therefore y = A x^b$$

$$y = 2.10034 x^{1.599}$$

flowchart for power eqn $y = ax^b$

Start

read n

for $i = 1:1:n$

read $x(i)$ $y(i)$

$$x(i) = \log x(i)$$

$$y(i) = \log y(i)$$

$$Sx = 0$$

$$Sy = 0$$

$$Sxx = 0$$

$$Sxy = 0$$

for $i = 1:1:n$

$$Sx = Sx + x(i)$$

$$Sy = Sy + y(i)$$

$$Sxx = Sxx + x(i)^2$$

$$Sxy = Sxy + x(i)y(i)$$

$$A = \frac{n Sxy - SxSy}{n Sxx - (Sx)^2}$$

$$B = \frac{Sy - ASx}{n}$$

$$a = \exp(B)$$

$$b = A$$

Point $y = ax^b$

End

```
n = input ('Enter the Number Of intervals :');
for i= 1:1:n
    x(i)= input ('Enter the x value :');
    y(i)= input ('Enter the y value :');
    x(i)=log(x(i));
    y(i)=log(y(i));
end
sx=0;
sy=0;
sxx=0;
sxy=0;
for i= 1:1:n
    sx=sx+x(i);
    sy=sy+y(i);
    sxx=sxx+x(i)*x(i);
    sxy=sxy+x(i)*y(i);
end
A=(n*sxy-sx*sy)/(n*sxx-sx*sx);
B= (sy-A*sx)/n;
a=exp(B);
b=A;
fprintf('\n the values are constant A=%f and B=%f', A,B);
fprintf('\n the equation of power curve is y=%2.4f x^%2.4fx' ,a,b);

%OUTPUT
%Enter the Number Of intervals :5
%Enter the x value :0.5
%Enter the y value :0.7425
%Enter the x value :1.5
%Enter the y value :3.8578
%Enter the x value :2
%Enter the y value :5.9397
%Enter the x value :2.5
%Enter the y value :8.301
%Enter the x value :3
%Enter the y value :10.912

%the values are constant A=1.499974 and B=0.741954
%the equation of power curve is y=2.1000 x^1.5000x>>
```



Q) Exponential Curve

$$y = A \cdot e^{bx}$$

$$\log y = \log A + bx$$

$$y = \log y$$

$$A = b$$

$$X = x$$

$$B = \log A$$

$$A \varepsilon y^2 + B \varepsilon x = \varepsilon xy$$

$$A \varepsilon x + n \cdot B = \varepsilon y$$

$$a = e^b \quad b = A$$

Q) Equation of best fitting curve $y = a \cdot e^{bx}$
find a & b

x	y	x^2	xy
2	25	4	50
4	38	16	152
6	56	36	336
8	84	64	672
20	15.3112	400	1062.24

$$A(120) + B(30) = 80 \cdot 5822$$

$$A(80) + B(3) = 15 \cdot 3112$$

$$\therefore A = 0.20131$$

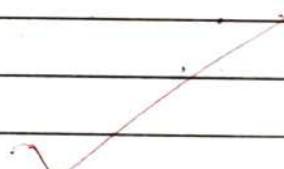
$$B = 2.82125$$

$$b = A = 0.20131$$

$$a = e^B = 16.797$$

$$g = a \cdot e^{bx}$$

$$g = 16.79 \cdot e^{0.20131 \cdot x}$$



Flowchart for exponential curve.

Start

Reactn

for i=1:n

React x(i) y(i)

$$y(i) = \log y(i)$$

$$x(i) = x(i)$$

$$\sum x = 0 \quad \sum x^2 = 0$$

$$\sum y = 0 \quad \sum xy = 0$$

for i=1..1:n

$$\sum x = \sum x + x(i)$$

$$\sum y = \sum y + y(i)$$

$$\sum x^2 = \sum x^2 + x(i)^2$$

$$\sum xy = \sum xy + x(i)y(i)$$

$$A = \frac{n \sum xy - \sum x \sum y}{n \sum x^2 - \sum x^2}$$

$$B = \frac{\sum y - Ax}{n}$$

$$a = e^{xp(B)}$$

$$b = A$$

Print $a \cdot e^{xb}$

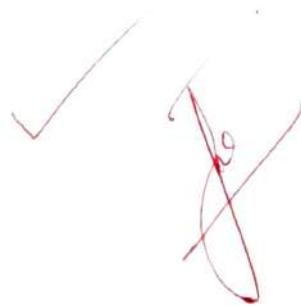
End.

```
n = input ('Enter the Number Of intervals :');
for i= 1:1:n
    x(i)= input ('Enter the x value :');
    y(i)= input ('Enter the y value :');
    y(i)=log(y(i));
    x(i)=x(i);
end
sx=0;
sy=0;
sxx=0;
sxy=0;
for i= 1:1:n
    sx=sx+x(i);
    sy=sy+y(i);
    sxx=sxx+x(i)*x(i);
    sxy=sxy+x(i)*y(i);
end
A=(n*sxy-sx*sy)/(n*sxx-sx*sx);
B= (sy-A*sx)/n;
a=exp(B);
b=A;
fprintf('\n the values are constant A=%f and B=%f', A,B);
fprintf('\n the equation of expomemtial curve is y=%2.4fe^%2.4fx' ,a,b);
```

%OUTPUT

```
%Enter the Number Of intervals :4
%Enter the x value :2
%Enter the y value :25
%Enter the x value :4
%Enter the y value :38
%Enter the x value :6
%Enter the y value :56
%Enter the x value :8
%Enter the y value :84
```

```
%the values are constant A=0.201179 and B=2.822261
%the equation of exponential curve is y=16.8148e^0.2012x>>
```



Assignment no 6

* Lagrange Interpolation

Lagrange interpolation is method for finding a polynomial that takes on specific value at certain points. It is used in numerical analysis to find the lowest degree polynomial that interpolates a given set of data.

The Lagrange interpolation theorem can be used to create a polynomial that passes over a group of point & take certain value randomly.

$$x_g = \sum_{i=1}^n x_i \prod_{j=1}^{i-1} \left(\frac{y_g - y_j}{x_i - x_j} \right) \quad i \neq j$$

$$y_g = \sum_{i=1}^n y_i \prod_{j=1}^{i-1} \left(\frac{x_g - x_j}{x_i - x_j} \right) \quad i \neq j$$

$$f_y = f(x_g)$$

$$f_x = f(y_g)$$

- a) Using Lagrange method of interpolation determine y for $x = 1.1$

x	1	1.2	1.3	1.5
y	1	1.09	1.15	1.22

$$\Rightarrow \frac{xy}{y^2} = 1 - \frac{y}{x} \quad \text{if } y \neq 0 \quad \text{it is}$$

for $n=4$

$$yy = y_1 \left(\frac{x_2 - x_1}{x_1 - x_2} \right) \left(\frac{x_3 - x_1}{x_1 - x_3} \right) \left(\frac{x_4 - x_1}{x_1 - x_4} \right) + y_2 \left(\frac{x_3 - x_2}{x_2 - x_3} \right)$$

$$\left(\frac{x_4 - x_2}{x_2 - x_4} \right) + y_3 \left(\frac{x_4 - x_3}{x_3 - x_4} \right) \left(\frac{x_1 - x_3}{x_3 - x_1} \right) \left(\frac{x_2 - x_3}{x_3 - x_2} \right)$$

$$+ y_4 \left(\frac{x_1 - x_4}{x_4 - x_1} \right) \left(\frac{x_2 - x_4}{x_4 - x_2} \right) \left(\frac{x_3 - x_4}{x_4 - x_3} \right)$$

$$yy = 1 \left(\frac{1.1 - 1.2}{1 - 1.2} \right) \left(\frac{1.1 - 1.3}{1 - 1.3} \right) \left(\frac{1.1 - 1.5}{1 - 1.5} \right)$$

$$+ 1.09 \left(\frac{1.1 - 1}{1.2 - 0.1} \right) \left(\frac{1.1 - 1.3}{1.2 - 1.3} \right) \left(\frac{1.1 - 1.5}{1.2 - 1.5} \right)$$

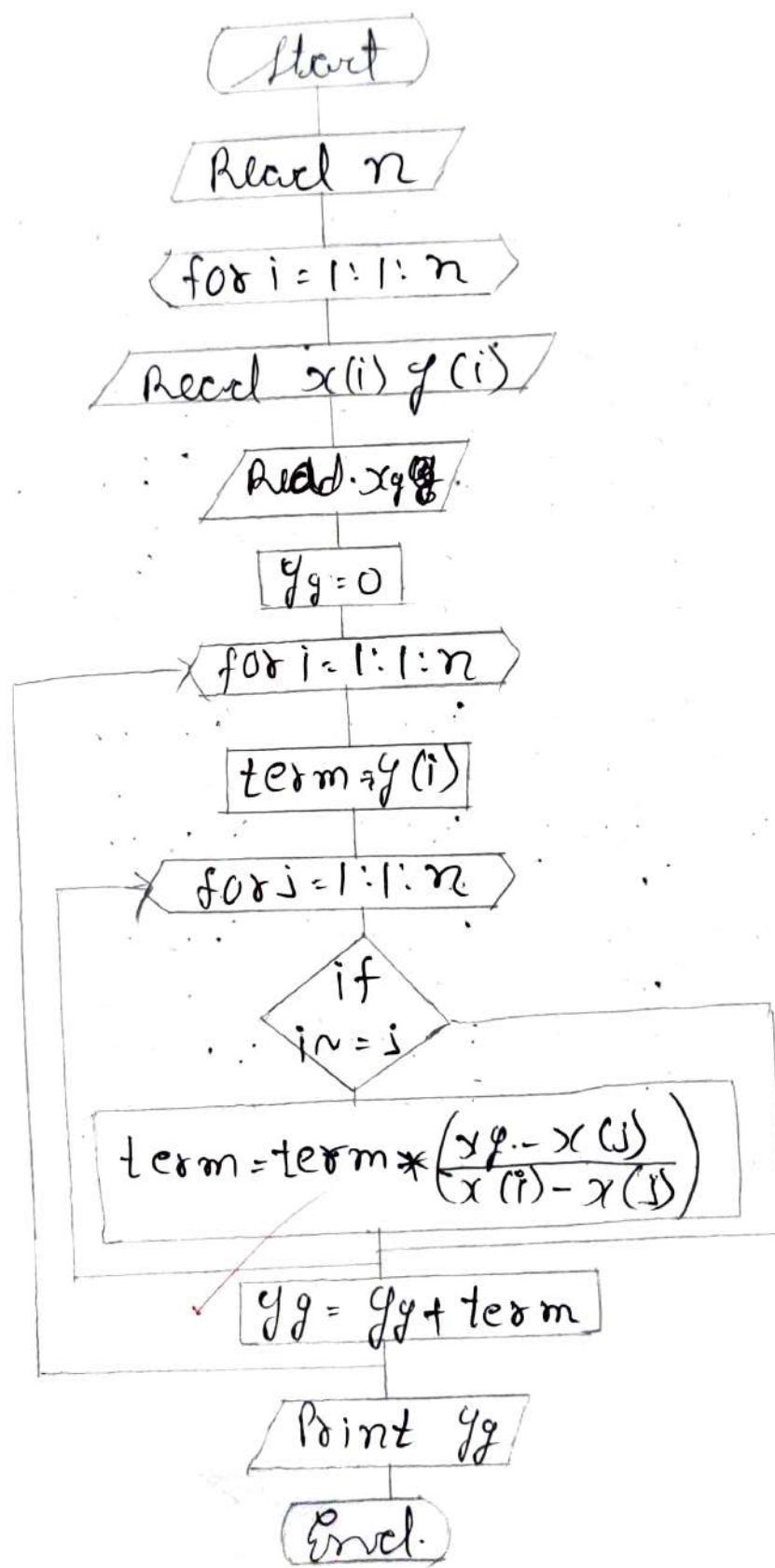
$$+ 1.15 \left(\frac{1.1 - 1}{1.3 - 1} \right) \left(\frac{1.1 - 1.2}{1.3 - 1.2} \right) \left(\frac{1.1 - 1.5}{1.3 - 1.5} \right)$$

$$+ 1.22 \left(\frac{1.1 - 1}{1.5 - 1} \right) \left(\frac{1.1 - 1.2}{1.5 - 1.2} \right) \left(\frac{1.1 - 1.3}{1.5 - 1.3} \right)$$

$$yy = 0.262 + 1.553 + 0.0813 = 0.76$$

$$= 1.0913$$

Flowchart for Lagrange Interpolation



14/3/24 11:57 AM D:\TYMEB207\lagrange_interpolation.m 1 of 1

```
n = input('Enter the value of n =');
for i=1:1:n
    x(i) = input('enter value of x');
    y(i) = input('enter value of y');
end
Xg=input('enter Xg');
Yg=0;
for i =1:1:n
    term=y(i);
    for j=1:1:n
        if j~=i
            term=term*(Xg-x(j))/(x(i)-x(j));
        end
    end
    Yg=Yg+term
end
fprintf('interpolating value Yg =%f',Yg);
```

OUTPUT :

Enter the value of n =4

enter value of x1

enter value of y1

enter value of x1.2

enter value of y1.09

enter value of x1.3

enter value of y1.14

enter value of x1.5

enter value of y1.22

enter Xg1.1

Yg = 0.2667

Yg = 1.7200

Yg = 0.9600

Yg = 1.0413

interpolating value Yg =1.041333>>

✓
✗

* Newton Forward interpolation:-

It is a numerical method that estimates value of ~~pred~~ function between given data points. It is named after Sir Isaac Newton, who contributed to calculus & interpolation is technique of estimating the value of the independent variable

Newton forward interpolation used when step size is same.

$$y_g = y_1 \frac{(x_g - x_1)}{h} \Delta_i + \frac{(x_g - x_1)(x_g - x_2)}{2! h^2} \Delta_i^2 + \frac{(x_g - x_1)(x_g - x_2)(x_g - x_3)}{3! h^3} \Delta_i^3 + \dots$$

$$x_g + ih \quad \Delta_i = \frac{x_g - x_1}{h}$$

- Q) A experiment is performed to study the failure of steel Bar. The applied stress at time to fracture are recorded as follows. Estimate the probable time to generate fracture where a stress of 15 MPa is applied.

$T(\text{mpg})$	$T(\text{sec})$	Δ^1	Δ^2	Δ^3	Δ^4	Δ^5	Δ^6	Δ^7
5	30	-5	2	-3	1	10	-28	94
10	35	-3	-1	-2	11	-28	56	
15	32	-4	-3	9	-17	28		
20	28	-7	6	-8	11			
25	21	-1	-2	3				
30	20	-3	1					
35	17	-2						
40	17							

$$xy = 13$$

$$h = 5$$

$$q = \frac{xy - x_1}{h} = \frac{13 \cdot 5}{5} = 1.5$$

$$\begin{aligned}
 y_g &= q_1 + q \Delta_1^1 + \frac{q(q-1)}{2!} \Delta_1^2 + \frac{q(q-1)(q-2)}{3!} \Delta_1^3 + \\
 &\quad \cancel{q(q-1)(q-2)(q-3) \Delta_1^4} + \cancel{q(q-1)(q-2)(q-3)(q-4) \Delta_1^5} + \\
 &\quad \cancel{q(q-1)(q-2)(q-3)(q-4)(q-5) \Delta_1^6} + \\
 &\quad \cancel{q(q-1)(q-2)(q-3)(q-4)(q-5)(q-6) \Delta_1^7} \\
 &= 32.3755
 \end{aligned}$$

Flowchart for Newton forward interpolation.

(Start)

Read n, x_g

for $i = 1 : 1 : n$

Read $x(i), y(i)$

$$h = x(2) - x(1)$$

for $j = 1 : 1 : n-1$

for $i = 1 : 1 : n-1$

if
 $j == 1$

$$nf(i,j) = nf(i+1,j-1) - nf(i,j-1)$$

$$nf(i,j) = y(i+j) - y(i)$$

$$y_g = y(i)$$

for $j = 1 : 1 : n-1$

$$\text{term} = nf(1,j)$$

$$a = (x_g - x(f)) / n$$

for $k = 1 : 1 : j$

$$\text{term} = \frac{y}{k} \text{term}$$

(C) (B)

(A)

$$a = a - 1$$

$$y_g = y_g + \text{term}$$

Print y_g

(End)

```
% Name- sarthak patil
% Roll no -228
n=input('Enter the number of equation=');
for i=1:1:n
    x(i)=input('Enter the value of x=');
    y(i)=input('Enter the value of y=');
end
xg=input('Enter the value of xg=');
h=x(2)-x(1);
for j=1:1:n-1
    for i=1:1:n-j
        if j==1
            nf(i,j)=y(i+1)-y(i);
        else
            nf(i,j)=nf(i+1,j-1)-nf(i,j-1);
        end
    end
end
yg=y(i);
for j=1:1:n-1
    term=nf(1,j);
    u=(xg-x(1))/h;
    for k=1:1:j
        term=term*u/k;
        u=u-1;
    end
    yg=yg+term;
end
fprintf('x(%d)=%f',yg);
```

- OUTPUT:-
newton_forward_difference
Enter the number of equation=8
Enter the value of x=2
Enter the value of y=19
Enter the value of x=3
Enter the value of y=48
Enter the value of x=4
Enter the value of y=99
Enter the value of x=5
Enter the value of y=178
Enter the value of x=6
Enter the value of y=291
Enter the value of x=7
Enter the value of y=444
Enter the value of x=8
Enter the value of y=647
Enter the value of x=9
Enter the value of y=894
Enter the value of x=10
Enter the value of y=1141



Assignment no 7

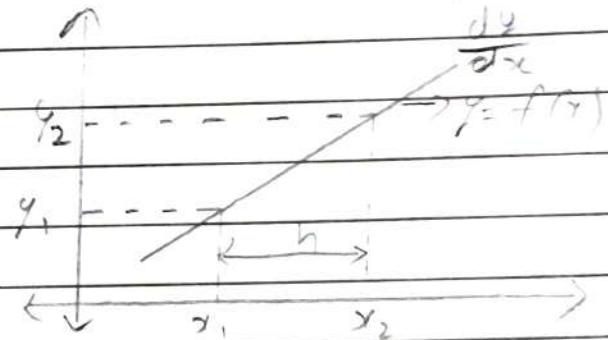
Ordinary differential equation

1) Euler's Method :- it is a numerical technique for approximating solution to first order differential equation, it a first order method which means that the local error is proportional to square of the step size & the global error is proportional to the step size.

The method is based on the idea of approximating a curve using tangent line. The tangent line to a curve at a point is the line that touches the curve at that point & has the same slope as curve at that point

$$\frac{dy}{dx} = \frac{y_2 - y_1}{x_2 - x_1}$$

$$y_n = y_{n-1} + h f(x_{n-1}, y_{n-1})$$



2) Given $\frac{dy}{dx} = x^2/y^2 + 1$ with initial condition $y=0$ when $x=0$ obtain y for $x=1$, taking step size (h) as 0.25.

$$\rightarrow \frac{dy}{dx} = \frac{x^2}{y^2 + 1}$$

$$x_1 = 0$$

$$x_2 = x_1 + h = 0.25$$

$$x_3 = 0.5$$

$$x_4 = 0.75$$

$$x_5 = 1$$

$$y_1 = 0$$

$$y_2 = 0 \times 0.25 + 0 = 0$$

$$y_3 = 0 + 0.25 \times 0.625 = 0.015625$$

$$y_4 = 0.015625 + 0.25 \times 0.75 = 0.0781$$

$$y_5 = 0.0781 + 0.25 \times 1 = 0.2179$$

Flowchart for Euler's method.

Start

Def $f(x, y)$

Read x_1, y_1, x_n, h

\rightarrow while $x_i < x_n$

$y_{i+1} = y_i + h * f(x_i, y_i)$

$x_{i+1} = x_i + h$

Print x_i, y_i

End

```
f=inline('sqrt(x+y)');
x1=input ('Enter the given value of x :');
y1=input ('Enter the given value of y :');
xn=input ('Enter value of x for which y to be found :');
h=input ('Enter increment in x :');
acc=input('Enter the accuracy:');
while x1<xn
    yp=y1+h*f(x1,y1);
    x2=x1+h;
    yc=y1+(h/2)*(f(x1,y1)+f(x2,yp));
    while abs(yc-yp)>acc
        yp=yc;
        yc=y1+(h/2)*(f(x1,y1)+f(x2,yp));
    end
    x1=x1+h;
    y1=yc;
end
fprintf('\n x=%f,y=%f', x1, y1);
```

OUTPUT

```
modifiedeuler
Enter the given value of x :1
Enter the given value of y :2.2
Enter value of x for which y to be found :1.2
Enter increment in x :0.1
Enter the accuracy=0.001
x=1.200000,y=2.573186>>
```

X
✓

2)

Runge Kutta Method (2nd order) (4th order)

It is numerical method for solving initial value problem of differential equation it can be used to construct high order accurate numerical method without needing high order derivatives of func.

RK 2

$$x_2 = x_1 + h$$

$$k_1 = h f(x_1, y_1)$$

$$k_2 = h f(x_1 + h, y_1 + k_1)$$

$$k = \frac{k_1 + k_2}{2}$$

$$y_2 = y_1 + k$$

RK 4

$$x_2 = x_1 + h$$

$$k_1 = h f(x_1, y_1)$$

$$k_2 = h f(x_1 + h/2, y_1 + k_1/2)$$

$$k_3 = h f(x_1 + h/2, y_1 + k_2/2)$$

$$k_4 = h f(x_1 + h, y_1 + k_3)$$

$$k = \frac{k_1 + 2k_2 + 2k_3 + k_4}{6}$$

$$y_2 = y_1 + k$$

Q) Given DE: $\frac{dy}{dx} = \frac{x^2}{y^2} \cdot \frac{dy}{dx} = \frac{x^2}{y^2 + x^2}$ with initial condition $y=0$, when $x=0$, obtain y for $x=1$. (Step n=300)

$$\rightarrow \frac{dy}{dx} = f(x, y) = \frac{x^2}{y^2 + 1}$$

$$x_1 = 0$$

$$x_n = 1$$

$$n = 4$$

$$y_1 = 0$$

$$h = 0.25$$

By RK₂

at $x_1 - \gamma_1 + h = 0.25$

$$K_1 = hf(x_1, y_1) \\ = 0.25 \left(\frac{0^2}{0+1} \right)$$

$$= 0$$

$$K_2 = hf(x_1 + h, y_1 + K_1)$$

$$= 0.25 \left(0.25, 0 \right)$$

$$= 0.0156$$

$$K = \frac{K_1 + K_2}{2} = \frac{0 + 0.0156}{2} = 7.8 \times 10^{-3}$$

$$y = y_1 + K = 7.8 \times 10^{-3}$$

at $x_3 = x_2 + h = 0.5$

$$K_1 = 0.25 \left(\frac{0.25^2}{(7.8 \times 10^{-3})^2 + 1} \right)$$

$$= 0.0156$$

$$K_2 = 0.25 \left(\frac{0.5^2}{(7.8 \times 10^{-3})^2 + 1} \right)$$

$$= 0.0625$$

$$K = \frac{0.0156 + 0.0625}{2} = 0.0391$$

$$y_3 = y_2 + K = (7.8 \times 10^{-3}) + (0.0391)$$

$$= 0.0469$$

at $x_4 = x_3 + h = 0.75$

$$K_1 = 0.25 \left(\frac{0.5^2}{(0.0469)^2 + 1} \right)$$

$$K_2 = 0.25 \left(\frac{0.75^2}{(0.0469)^2 + 1} \right)$$

$$K = \frac{0.0625 + 0.1389}{2} = 0.1007$$

$$y_4 = y_3 + K = 0.0469 + 0.1007 = 0.1479$$

$$at \quad x_5 = y_4 + h = 1$$

$$K_1 = hf(y_4, y_4) \\ = 0.25 \left(\frac{0.75^2}{0.1979^2 + 1} \right)$$

$$K_2 = 0.25 \left(\frac{1^2}{0.2855^2 + 1} \right)$$

$$K_1 = 0.1376 \quad K_2 = 0.2312$$

$$K = \frac{0.1376 + 0.2312}{2} = 0.1844$$

$$y_5 = y_4 + K \\ = 0.1979 + 0.1844 \\ = 0.3323$$

$$\therefore x = 1 \quad y = 0.3323$$

Flowchart:
Runge kutta method (RK-4)

Start

$$f_{ref} \cdot 2 = f(x, y)$$

Recall x_1, y_1, x_n, h

while $x_1 < x_n$

$$k_1 = h * f(x_1, y_1)$$

$$k_2 = h * f(x_1 + h, y_1 + k_1)$$

$$k_3 = \frac{k_1 + k_2}{2}$$

$$y_1 = y_1 + k_3$$

$$x_1 = x_1 + h$$

$$\text{Point} = x_1, y_1$$

End

21/3/24 11:57 AM D:\TYMEB207\Rk2method.m

```
z=inline('sqrt(x+y)');
x1=input ('Enter the given value of x : ');
y1=input ('Enter the given value of y : ');
xn=input ('Enter value of x for which y to be found : ');
h=input ('Enter increment in x : ');
while x1<xn
    k1=h*f(x1,y1);
    k2=h*f(x1+h,y1+k1);
    k=(k1+k2)/2;
    y1=y1+k;
    x1=x1+h;
end
fprintf('x1=%f,y1=%f',x1,y1)
OUTPUT
Enter the given value of x : 1
Enter the given value of y : 2.2
Enter value of x for which y to be found : 1.2
Enter increment in x : 0.1
x1=1.200000,y1=2.200000>>
```



Q) Apply Runge Kutta method to find an approximate value of $y=0.2$ given $\frac{dy}{dx} = x+y$ & $y=1$ when $x=0$ take $h=0.2$

\rightarrow

$$\frac{dy}{dx} = f(x, y) = x+y$$

$$x_1 = 0$$

$$y_1 = 0$$

$$x_n = 0.2$$

$$h = 0.2$$

$$n = 1$$

$$\text{at } x_2 = x_1 + h = 0.2$$

$$k_1 = 0.2 (0+0) \\ = 0.2$$

$$k_2 = 0.2 (0.1+1.1) \\ = 0.24$$

$$k_3 = 0.2 (0.1+1.12) \\ = 0.244$$

$$k_4 = 0.2 (0.2+1.244) \\ = 0.2888$$

$$K = \frac{k_1 + (k_2 + k_3)}{6}$$

$$= \frac{0.2 + 2 \times 0.24 + 2 \times 0.244 + 0.2888}{6} \\ = 0.2428$$

$$y_2 = y_1 + K = 1 + 0.2428 = 1.2428$$

$$\therefore x = 0.2, y = 1.2428$$

Range Kutta method (RK-4)

Start)

$$\boxed{\text{Def } x = f(y_1, y)}$$

Read x_1, y_1, x_n, h

$\rightarrow \leftarrow \text{while } x_1 < x_n$

$$K_1 = h * f(x_1, y_1)$$

$$K_2 = h * f\left(x_1 + \frac{h}{2}, y_1 + \frac{K_1}{2}\right)$$

$$K_3 = h * f\left(x_1 + \frac{h}{2}, y_1 + \frac{K_2}{2}\right)$$

$$K_4 = h * f(x_1 + h, y_1 + K_3)$$

$$K = \frac{1}{6}(K_1 + 2K_2 + 2K_3 + K_4)$$

$$y_1 = y_1 + K$$

$$\boxed{x_1 = x_1 + h}$$

~~Print~~ x_1, y_1

End.

```
z=inline('sqrt(x+y)');
x1=input ('Enter the given value of x : ');
y1=input ('Enter the given value of y : ');
xn=input ('Enter value of x for which y to be found : ');
h=input ('Enter increment in x : ');
while x1<xn
    k1=h*f(x1,y1);
    k2=h*f(x1+h/2,y1+(k1)/2);
    k3=h*f(x1+h/2,y1+(k2)/2);
    k4=h*f(x1+h,y1+k3);
    k=(1/6)*(k1+2*k2+2*k3+k4);
    y1=y1+k;
    x1=x1+h;
end
fprintf('\n x1=%f,y1=%f',x1,y1)
OUTPUT
Enter the given value of x : 1
Enter the given value of y : 2.2
Enter value of x for which y to be found : 1.2
Enter increment in x : 0.1
```

x1=1.200000,y1=2.573206

X

3) Simultaneous equation

$$\frac{dy}{dx} = f(x, y, z) \quad \frac{dz}{dx} = g(x, y, z)$$

$$\frac{d^2y}{dx^2} = \frac{d}{dx} \left(\frac{dy}{dx} \right) \Rightarrow \frac{d^2z}{dx^2}$$

R K - 2

$$ky_1 = hf(x, y, z)$$

$$ky_2 = hf(x + h, y_1 + ky_1, z + kz_1)$$

$$ky = \underbrace{ky_1 + ky_2}_2$$

$$y_n = y_{n-1} + ky$$

$$kz_1 = hg(x, y_1, z_1)$$

$$kz_2 = hg(x + h, y_1 + ky_1, z_1 + kz_1)$$

$$kz = \underbrace{kz_1 + kz_2}_2$$

$$z_n = z_{n-1} + kz$$

Q) solve the following simultaneous eqns $y = y_2$ & $z = z(y)$
 given that
 the value of $y(0,1)$ & $z(0,2)$ given that
 $y(0,0) = 1$ & $z(0,0) = 1$

$$\rightarrow y' = \frac{dy}{dx} = y_2 = f(x, y, z)$$

$$z' = \frac{dz}{dx} = zg(x, y, z)$$

$$h = 0.2 - 0.1 = 0.1$$

at $x_2 = x_1 + h = 0.1$

$$\begin{aligned} KY_1 &= hf(x_1, y_1, z_1) \cdot K_{2,1} = hg(x_1, y_1, z_1) \\ &= 0.1(1 \times 1) & K_{2,1} &= 0.1(0 \times 1) \\ &= 0.1 & &= 0 \end{aligned}$$

$$\begin{aligned} KY_2 &= hf(x_1 + h, y_1 + KY_1, z_1 + K_{2,1}) \\ &= 0.1(0.1 \times 1, 1.1, 1) \\ &= 0.11 \end{aligned}$$

$$\begin{aligned} K_{2,2} &= hg(x_1 + h, y_1 + KY_1, z_1 + K_{2,1}) \\ &= 0.1(0.1 \times 1) \\ &= 0.011 \end{aligned}$$

$$\begin{aligned} KY &= \frac{KY_1 + KY_2}{2} \\ &= \frac{0.1 + 0.11}{2} \\ &= 0.105 \end{aligned}$$

$$\begin{aligned} K_2 &= \frac{K_{2,1} + K_{2,2}}{2} \\ &= \frac{0 + 0.011}{2} \\ &= 0.0055 \end{aligned}$$

$$\begin{aligned} Y_n &= Y_{n-1} + KY \\ &= 1 + 0.105 \\ &= 1.105 \end{aligned}$$

~~$$\begin{aligned} Z_n &= Z_{n-1} + K_2 \\ &= 1 + 0.0055 \\ &= 1.0055 \end{aligned}$$~~

at $x_3 = x_2 + h = 0.2$

$$\begin{aligned} KY_1 &= hf(x_2, y_2, z_2) \\ &= 0.1(0.105 \times 1.0055) \\ &= 0.1111 \end{aligned}$$

$$\begin{aligned} K_{2,1} &= hg(x_2, y_2, z_2) \\ &= 0.1(0.1 \times 1.105) \\ &= 0.0111 \end{aligned}$$

$$k_2 = hf(x_1 + h, y_1 + k_1, z_1 + k_2) \\ = 0.1 (1.2161 \times 1.066) \\ = 0.1236$$

$$k_2 = hf(x_2 + h, y_2 + k_2, z_2 + k_{21}) \\ = 0.1 (0.2 \times 1.2161) \\ = 0.243$$

$$k_y = \frac{k_1 + k_2}{2} \\ = \frac{0.111 + 0.1236}{2} \\ = 0.11735$$

$$k_z = \frac{k_{21} + k_{22}}{2} \\ = \frac{0.0111 + 0.0243}{2} \\ = 0.0177$$

$$y_3 = y_2 + k_y \\ = 1.105 + 0.11735 \\ = 1.2224$$

$$z_4 = z_2 + k_z \\ = 1.0055 + 0.0177 \\ = 1.0232$$

Hancock for simultaneous RK2

Heort

$$\text{Def } f(x, y, z)$$

$$g(x, y, z)$$

Read x_1, y_1 on x_n

while $x_i < x_n$

$$k_y_1 = h * f(x_1, y_1, z_1)$$

$$k_y_2 = h * f(x_1 + h, y_1 + k_{y_1} / 2, z_1 + k_{z_1})$$

$$k_{z_1} = h * g(x_1, y_1, z_1)$$

$$k_{z_2} = h * g(x_1 + h, y_1 + k_{y_1}, z_1 + k_{z_1})$$

$$k_y = (k_y_1 + k_y_2) / 2$$

$$k_z = (k_{z_1} + k_{z_2}) / 2$$

$$y_1 = y_1 + k_y$$

$$z_1 = z_1 + k_z$$

$$x_1 = x_1 + h$$

Point x_1, y_1, z_1

End

```
%NAME: Sarthak Abhay Patil  
%DIV:B  
*BATCH:B-4  
* SimultaneousRK2Method  
  
function sim_rk1_methjod()  
x1=input('Enter the value of x1:');  
y1=input('Enter the value of y1:');  
z1=input('Enter the value of z1:');  
h=input('Enter stepsize h:');  
xn=input('Enter xn value:');  
while x1<xn  
    kyl=h*f(x1,y1,z1);  
    kz1=h*g(x1,y1,z1);  
    ky2=h*f(x1+h,y1+kyl,z1+kz1);  
    kz2=h*g(x1+h,y1+ky1,z1+kz1);  
    ky=(ky1+ky2)/2;  
    kz=(kz1+kz2)/2;  
    y1=y1+ky;  
    z1=z1+kz;  
    x1=x1+h;  
    fprintf('\nxf = %f',x1,y1,z1);  
end  
fprintf('\nat xn=%f, yn=%f',x1,y1,z1);  
end  
function s=f(x,y,z)  
s=y*z;  
end  
function w=g(x,y,z)  
w=x*y  
end
```

```
% OUTPUT  
% Enter the value of x1:0  
% Enter the value of y1:1  
% Enter the value of z1:1  
% Enter stepsize h:0.1  
% Enter xn value:0.2  
%  
% w =  
% 0  
%  
% w =  
% 0.1100  
%  
% 0.10000 1.10500 1.11000  
% w =
```

✓
X 9

Assignment no 08

Laplace equation

$$A \frac{\partial^2 u}{\partial x^2} + B \frac{\partial^2 u}{\partial x \partial y} + C \frac{\partial^2 u}{\partial y^2} + D \frac{\partial u}{\partial x} + E \frac{\partial u}{\partial y} + F = 0$$

$S < 0$ Elliptical equation

$$\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$$

$$\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = f(x, y)$$

$S = 0$ Parabolic equation

Schmidt equation

$$\frac{a \partial^2 u}{\partial x^2} = \frac{\partial u}{\partial y}$$

$S > 0$ Hyperbolic equation

Curve equation

$$\frac{\partial^2 u}{\partial x^2} = \frac{a \partial^2 u}{\partial y^2}$$

$$\frac{\partial^2 u}{\partial x^2} = \frac{u(i+1, j) - 2u(i, j) + u(i-1, j)}{h^2}$$

$$\frac{\partial^2 u}{\partial y^2} = \frac{u(i, i+1) - 2u(i, j) + u(i, j-1)}{k^2}$$

$$h = k$$

$$u(i, j) = u(i+1, j) + u(i-1, j) + u(i, j+1) \\ + u(i, j-1)$$

$$G(i,j) = \frac{1}{4} [G(i+1), j] + G(i-1, j) + G(i, j+1) + G(i, j-1)$$

$$Q \frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} = 0 \quad \text{Solve the Laplace eqn with given cond. Find } T_1, T_2, T_3 \text{ & } T_4.$$

$$\rightarrow g(i, j) = \frac{1}{4} [g(i+1, j) + g(i-1, j) + g(i, j+1) + g(i, j-1)]$$

$$T_1 = \frac{1}{3} [40 + T_2 + 60 + 74]$$

$$= \frac{1}{3} \{100 + T_2 + T_4\} \dots \textcircled{1}$$

$$T_2 = \frac{1}{4} [T_1 + 50 + 60 + T_3]$$

$$= \frac{1}{3} [110 + T_1 + T_3] \dots \dots \dots (2)$$

$$T_3 = \frac{1}{3} [60 + T_4 + T_2 + 20]$$

$$= \frac{1}{4} [60 + T_4 + T_2] \dots \text{--- } (3)$$

$$T_4 = \frac{1}{3} [30 + T_3 + T_1] \quad \dots \quad (7)$$

Congressional
acc = 0.01

$$T_1 = T_2 = T_3 = T_4 = 0$$

$$T_1 = 25$$

$$T_2 = 33.75$$

$$T_3 = 33.4375$$

$$T_4 = 19.6093$$

by substituting value $T_1 = T_2 = T_3 = T_4 = 0$ in ①

i+j	T_1	T_2	T_3	T_4
1	0	0	0	0
2	25	33.75	23.437	19.609
3	33.339	31.644	30.325	23.4164
4	41.277	45.500	32.204	25.8704
5	32.817	46.255	33.0314	26.4623
6	43.1744	46.5527	33.2537	26.6082
7	43.2902	46.6359	33.3110	26.6503
8	43.3219	46.6581	33.3271	26.66201

Fließchart Laplace

(Start)

Read n, h

for i = 1 : 1 : n

if
j == 1 ||
j == n

for j = 1 : 1 : n

Read a(i,j)

Read i, r

for k = 1 : 1 : i, r

for i = 2 : 1 : n - 1

for j = 2 : 1 : n - 1

$$a(i,j) = \frac{1}{h} [a(i+1,j) + a(i-1,j) + a(i,j+1) + a(i,j-1)]$$

for i = 2 : 1 : n - 1

for j = 2 : 1 : n - 1

Print a(i,j)

End

for j = 1 : 1 : n

if
j == 1 ||
j == n

$$c(i,j) = 0$$

Read u(i,j)

```
n=input("enter the value of n");
%h=input("Enter the value of h:");
for i=1:1:n
    if i==1||i==n
        for j=1:1:n
            u(i,j)=input("Enter the value of u(i,j)=");
        end
    else
        for j=1:1:n
            if j==1||j==n
                u(i,j)=input("Enter the value of u(i,j)");
            else
                u(i,j)=0;
            end
        end
    end
end
itr=input("Enter the number of iterations=");
for k=1:1:itr
    for i=2:1:n-1
        for j=2:1:n-1
            u(i,j)=(1/4)*(u(i+1,j)+u(i-1,j)+u(i,j+1)+u(i,j-1));
        end
    end
    for i=2:1:n-1
        for j=2:1:n-1
            fprintf("%f\n",u(i,j));
        end
    end
end
```

```
%output
Laplace
enter the value of n4
Enter the value of u(i,j)=60
Enter the value of u(i,j)=40
Enter the value of u(i,j)=20
Enter the value of u(i,j)=0
Enter the value of u(i,j)60
Enter the value of u(i,j)10
Enter the value of u(i,j)60
Enter the value of u(i,j)20
Enter the value of u(i,j)=60
Enter the value of u(i,j)=50
Enter the value of u(i,j)=40
Enter the value of u(i,j)=30
Enter the number of iterations=15
43.333333
26.666667
```

X

ASSIGNMENT No. 9

Title : Matlab Solver for all Numerical Methods

1. Roots of Equation

```
>> f = inline('x^2 + 10*x -3100')
```

f =

Inline function:

$$f(x) = x^2 + 10*x - 3100$$

```
>> root = fzero(f,0)
```

root =

50.9017

2. Numerical Integration

```
>> f = inline('3*(0.4+0.004*T)')
```

f =

Inline function:

$$f(T) = 3*(0.4+0.004*T)$$

```
>> I = quad(f,25,125)
```

I =

210

3. Simultaneous Equation

>> A = [2 4 3; 3 6 1; 1 3 2]

A =

$$\begin{matrix} 2 & 4 & 3 \\ 3 & 6 & 1 \\ 1 & 3 & 2 \end{matrix}$$

>> B = [13; 16; 9]

B =

$$\begin{matrix} 13 \\ 16 \\ 9 \end{matrix}$$

>> X = linsolve(A,B)

X =

$$\begin{matrix} \underline{1.0000} \\ \underline{2.0000} \\ \underline{1.0000} \end{matrix}$$

4. Curve Fitting

a) Straight line

```
>> X = [19 25 30 36 40 45 50]
```

X =

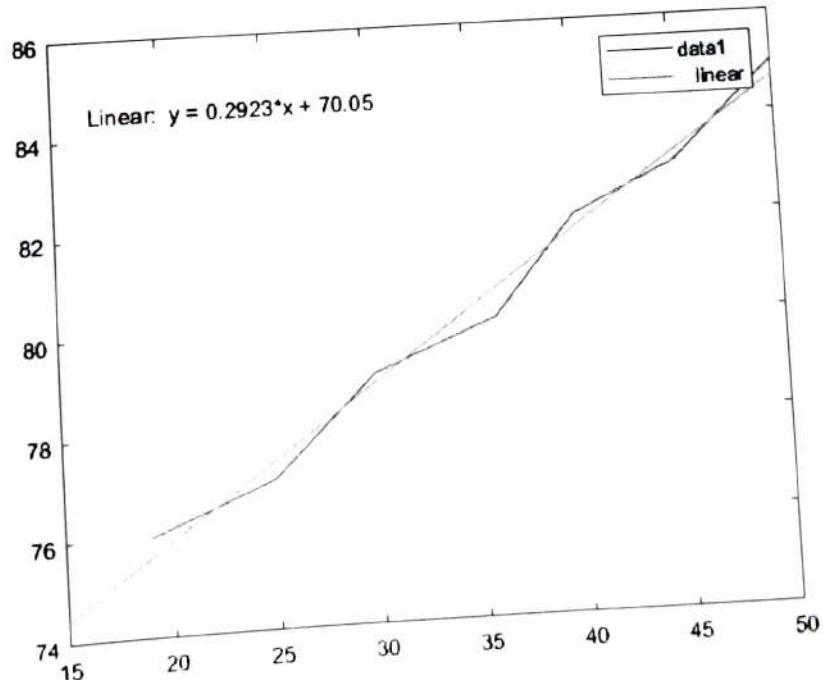
19 25 30 36 40 45 50

```
>> Y = [76 77 79 80 82 83 85]
```

Y =

76 77 79 80 82 83 85

```
>> plot(X,Y)
```



(Answer : Linear: $y = 0.2923 \cdot x + 70.05$)

5. Interpolation

>> X = [-12 10 38]

X =

-12 10 38

>> Y = [50.1 10 4.9]

Y =

50.1000 10.0000 4.9000

>> Xg = interp1(Y,X,16,"spline")

Xg =

-15.6600

6. Ordinary Diff. Equation

```
>> f = inline('(x^2)/(y^2 + 1)')
```

f =

Inline function:

$$f(x,y) = (x^2)/(y^2 + 1)$$

```
>> [Xn Yn] = ode23(f,[0,1],0)
```

Xn =

0	0
0.0250	0.0000
0.0500	0.0000
0.0731	0.0001
0.0962	0.0003
0.1192	0.0006
0.1423	0.0010
0.1654	0.0015
0.1918	0.0024
0.2225	0.0037
0.2581	0.0057
0.2995	0.0090
0.3474	0.0140
0.4030	0.0218
0.4677	0.0341
0.5431	0.0533
0.6315	0.0838
0.7315	0.1298
0.8315	0.1894
0.9315	0.2634
1.0000	0.3222

Yn =

✓ ✓ ✓