## Final.R

#### sarthakmehta

2022-12-06

```
# Final
library(readr)
## Warning: package 'readr' was built under R version 4.1.2
library(fpp)
## Loading required package: forecast
## Warning: package 'forecast' was built under R version 4.1.2
## Registered S3 method overwritten by 'quantmod':
##
    method
     as.zoo.data.frame zoo
## Loading required package: fma
## Loading required package: expsmooth
## Loading required package: lmtest
## Warning: package 'lmtest' was built under R version 4.1.2
## Loading required package: zoo
## Warning: package 'zoo' was built under R version 4.1.2
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
       as.Date, as.Date.numeric
## Loading required package: tseries
## Warning: package 'tseries' was built under R version 4.1.2
```

```
library(fpp2)
## -- Attaching packages ------ fpp2 2.4 --
## v ggplot2 3.3.5
##
##
## Attaching package: 'fpp2'
## The following objects are masked from 'package:fpp':
##
##
      ausair, ausbeer, austa, austourists, debitcards, departures,
      elecequip, euretail, guinearice, oil, sunspotarea, usmelec
##
IPG3113N <- read csv("/Users/sarthakmehta/Desktop/IPG3113N.csv")</pre>
## Rows: 121 Columns: 2
## -- Column specification -------
## Delimiter: ","
## dbl (1): IPG3113N
## date (1): DATE
##
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.
candy_ts <- ts(IPG3113N$IPG3113N,frequency = 12,start=c(2012,10))</pre>
#Plot and Inference
candy_ts
##
            .Jan
                    Feb
                             Mar
                                     Apr
                                              May
                                                      Jun
                                                               Jul
                                                                       Aug
## 2012
## 2013 92.8393 88.4378 88.9572 82.6418 79.6009 79.7216 80.3623 87.3990
## 2014 91.8045 91.3464 88.8527
                                 81.7442 77.6292 78.3359 77.0192 85.4452
## 2015 93.6676 92.4733 90.2388 85.5111 81.8907 85.4442 87.4143 99.0757
## 2016 97.1509 97.9475 98.4111
                                 95.0657 93.3682 93.8015
                                                           94.3271 96.2487
## 2017 100.4828 103.5407 95.2095
                                 96.9654 91.2276 92.9268 90.3917 100.6988
## 2018 99.9651 101.7932 97.6257
                                 97.1776 93.2973 90.7030
                                                           90.7825 96.9555
## 2019 102.3790 103.2079 102.5133
                                 96.6862 93.2061 93.6885
                                                           91.3219 99.4256
## 2020 100.1032 102.5297 96.9412
                                 82.4777
                                          84.4155
                                                  87.5411
                                                           91.2016 100.3417
## 2021 110.1841 101.7558 102.2030 94.1243 94.0966 94.4684 92.0391 98.7301
## 2022 113.1828 111.8384 110.4263 111.0788 103.3188 105.4497 104.2348 105.6166
##
            Sep
                    Oct
                             Nov
                                     Dec
## 2012
                99.8541 100.7874 100.7643
## 2013 92.0523 102.5585 106.4783 108.0668
## 2014 92.7103 103.4097 110.9082 109.9962
## 2015 99.8525 110.3226 109.3626 106.4516
```

```
## 2016 101.3271 111.2323 108.1348 107.5859

## 2017 106.6639 106.8689 105.1628 109.8611

## 2018 105.8597 105.4468 106.0408 111.4674

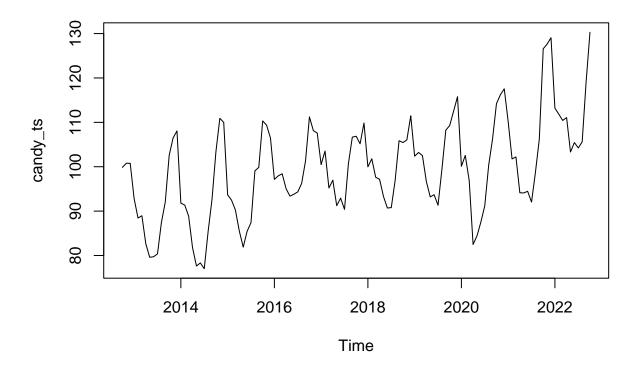
## 2019 108.2320 109.2961 112.5268 115.7811

## 2020 106.3095 114.2083 116.2062 117.5581

## 2021 106.2289 126.5753 127.6255 129.0640

## 2022 119.0161 130.2894
```

```
plot(candy_ts) #plotting the candy_ts data
```



#Observation: Through the graph we can that the monthly production of candies in the US has been pretty #can see a clear pattern to it. And there are sharp declines and rises throughout the data, so to cut o #would not be correct. Hence would be going on with the full data set provided.

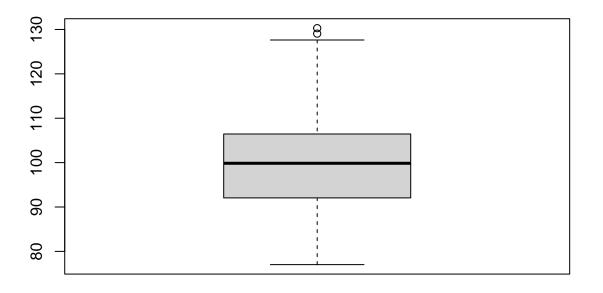
```
#Central Tendency
min(candy_ts)
```

## [1] 77.0192

```
# [1] 77.0192
max(candy_ts)
```

## [1] 130.2894

```
# [1] 130.2894
mean(candy_ts)
## [1] 99.44454
# [1] 99.44454
median(candy_ts)
## [1] 99.8525
# [1] 99.8525
quantile(candy_ts)
##
        0%
                25%
                         50%
                                  75%
                                          100%
## 77.0192 92.0523 99.8525 106.4516 130.2894
# 25%
           75%
# 92.0523 106.4516
boxplot((candy_ts))
```



#Summary: Well the summaries show us that the amongst the median values calculated min value of candy p #period of 2012 to 2022 was 77.0192 and the max value was 130.2894. Furthermore, the mean value was 99. #the median value was 99.8525. The 1st quartile was 92.0523 and the 3rd quartile was 106.4516. The box #that the there are 2 outliers, and the minimum value is a bit more closer to the 1st quartile than the #the 3rd quatile, and the median is approximate in between the 1st and 3rd quartile. But when we look cl #median we can see that as mean is a bit lower than the median (2nd quartile line) hence would me that

```
#Decomposition
stl_decomp <- stl(candy_ts,s.window =12)</pre>
stl_decomp
   Call:
   stl(x = candy_ts, s.window = 12)
##
## Components
##
               seasonal
                            trend
                                      remainder
## Oct 2012 10.5991242
                         88.76885
                                    0.486128404
## Nov 2012 11.9082450
                         88.94684
                                   -0.067689965
## Dec 2012 12.4396616
                         89.12484
                                   -0.800204106
## Jan 2013
                         89.30284
              0.9586825
                                    2.577777391
## Feb 2013
              0.5607168
                         89.50068
                                   -1.623601801
## Mar 2013
            -2.0268681
                         89.69853
                                    1.285538278
## Apr 2013
            -6.6117581
                         89.89637
                                   -0.642816560
## May 2013 -10.0729539
                         90.10035
                                   -0.426498736
## Jun 2013
            -9.3367546
                         90.30433
                                   -1.245976113
## Jul 2013
            -9.5950782
                         90.50831
                                   -0.550930554
                                   -1.156182465
## Aug 2013
            -2.0496520
                         90.60483
## Sep 2013
              3.3932326
                         90.70136
                                   -2.042292762
## Oct 2013
            10.5381605
                         90.79789
                                    1.222453628
## Nov 2013
            11.7366414
                         90.68594
                                    4.055718666
## Dec 2013
            12.3879538
                         90.57399
                                    5.104852222
## Jan 2014
              0.9628192
                         90.46205
                                    0.379632771
## Feb 2014
              0.6389851
                         90.41520
                                    0.292219599
## Mar 2014
            -2.0111343
                         90.36834
                                    0.495491725
## Apr 2014
            -6.6100457
                         90.32149
                                   -1.967244165
                         90.46147
## May 2014 -10.0306151
                                   -2.801659713
## Jun 2014
            -9.3114433
                         90.60146
                                   -2.954116492
## Jul 2014
            -9.5920828
                         90.74144
                                   -4.130162024
## Aug 2014
            -2.0542340
                         90.98619
                                   -3.486757861
## Sep 2014
              3.4924209
                         91.23094
                                   -2.013059763
## Oct 2014
            10.4813530
                         91.47569
                                    1.452661089
## Nov 2014
            11.5692114
                         91.99909
                                    7.339900617
## Dec 2014
            12.3404369
                         92.52249
                                    5.133272951
## Jan 2015
              0.9713533
                         93.04589
                                   -0.349645527
## Feb 2015
              0.7218572
                         93.63809
                                   -1.886647844
## Mar 2015
            -1.9905303
                         94.23029
                                   -2.000958834
## Apr 2015
             -6.6031967
                         94.82249
                                   -2.708190937
## May 2015
                         95.09530
            -9.9830309
                                   -3.221568015
## Jun 2015
            -9.2807779
                         95.36811
                                   -0.643132352
```

## Jul 2015

-9.5840192

## Aug 2015 -2.0540339

95.64092

96.13102

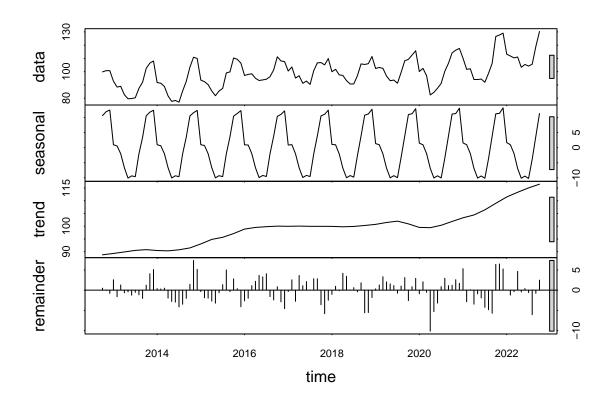
1.357397749

4.998711111

```
3.5954289
## Sep 2015
                                    -0.364053081
                          96.62112
## Oct 2015
             10.4285374
                          97.11123
                                     2.782837102
             11.3025047
## Nov 2015
                          97.69738
                                     0.362714208
## Dec 2015
             12.2706801
                          98.28354
                                    -4.102616766
              0.9304921
## Jan 2016
                          98.86969
                                    -2.649284402
## Feb 2016
              0.8764821
                          99.08581
                                    -2.014796319
## Mar 2016
             -1.9993279
                          99.30194
                                     1.108491712
             -6.6292411
## Apr 2016
                          99.51806
                                     2.176882941
## May 2016
             -9.9089575
                          99.61689
                                     3.660265343
## Jun 2016
             -9.2001789
                          99.71573
                                     3.285952692
## Jul 2016
             -9.5406504
                          99.81456
                                     4.053190219
## Aug 2016
             -2.0359966
                          99.88701
                                    -1.602309051
## Sep 2016
              3.7863623
                         99.95945
                                    -2.418713451
## Oct 2016
                                     0.845282712
             10.3551207 100.03190
## Nov 2016
             11.0123956 100.00919
                                    -2.886783341
## Dec 2016
             12.1747194
                          99.98648
                                    -4.575298361
## Jan 2017
              0.8589920
                         99.96377
                                    -0.339962196
## Feb 2017
              0.9960331
                         99.98942
                                     2.555249318
## Mar 2017
             -2.0487293 100.01507
                                    -2.756835789
## Apr 2017
             -6.7014192 100.04071
                                     3.626106613
## May 2017
             -9.8860464 100.01204
                                     1.101609349
## Jun 2017
                          99.98336
             -9.1757707
                                     2.119209238
## Jul 2017
             -9.5560123
                          99.95469
                                    -0.006973671
## Aug 2017
             -2.0792298
                          99.95389
                                     2.824143474
## Sep 2017
              3.9180669
                          99.95309
                                     2.792746411
## Oct 2017
             10.5189014
                          99.95229
                                    -3.602288426
## Nov 2017
             11.0420904
                         99.94582
                                    -5.825108760
## Dec 2017
             12.4069792
                         99.93935
                                    -2.485228857
              1.0703083
## Jan 2018
                          99.93288
                                    -1.038089254
## Feb 2018
              0.9505060
                          99.87849
                                     0.964202807
## Mar 2018
             -2.0618904
                          99.82410
                                    -0.136510979
## Apr 2018
             -6.7759368
                          99.76971
                                     4.183825153
## May 2018
             -9.9575216
                          99.81734
                                     3.437481672
## Jun 2018
             -9.2362093
                          99.86497
                                     0.074241035
## Jul 2018
             -9.7580459
                          99.91260
                                     0.627949363
## Aug 2018
             -2.6602766 100.03749
                                    -0.421708467
## Sep 2018
              3.8733267 100.16237
                                     1.823999816
## Oct 2018
             10.7524738 100.28726
                                    -5.592935852
## Nov 2018
             11.1397392 100.43136
                                    -5.530297287
## Dec 2018
             12.7053552 100.57545
                                    -1.813409278
## Jan 2019
              1.3426650 100.71955
                                     0.316784921
## Feb 2019
              0.9609437 100.96702
                                     1.279936357
## Mar 2019
             -2.0251972 101.21449
                                     3.324007384
## Apr 2019
             -6.8067104 101.46196
                                     2.030950738
## May 2019
             -9.9908230 101.63893
                                     1.557993363
## Jun 2019
             -9.2640441 101.81590
                                     1.136644525
## Jul 2019
             -9.9317231 101.99287
                                    -0.739246400
## Aug 2019
             -3.2172141 101.63460
                                     1.008214976
## Sep 2019
              3.8494705 101.27633
                                     3.106200634
## Oct 2019
             10.9518486 100.91806
                                    -2.573807143
## Nov 2019
             11.2186645 100.45449
                                     0.853641995
## Dec 2019
             12.8851579
                         99.99093
                                     2.905013508
## Jan 2020
              1.4674880
                         99.52736
                                    -0.891651539
## Feb 2020
              0.9667147
                         99.49509
                                     2.067894875
```

```
## Mar 2020 -1.9830794 99.46282
                                  -0.538537889
## Apr 2020 -6.8148633 99.43054 -10.137980898
## May 2020 -10.0329043 99.74307
                                   -5.294666481
## Jun 2020 -9.3135889 100.05560
                                   -3.200908472
## Jul 2020 -10.0346542 100.36812
                                   0.868130191
## Aug 2020 -3.4609873 100.86804
                                    2.934642849
## Sep 2020
              3.8269911 101.36796
                                    1.114543976
## Oct 2020 11.1280938 101.86789
                                    1.212320792
## Nov 2020 11.2760261 102.34620
                                    2.583971116
## Dec 2020 13.0449631 102.82452
                                    1.688616745
## Jan 2021
             1.5755494 103.30284
                                    5.305713092
## Feb 2021
             0.9589601 103.67269
                                  -2.875850112
                                   0.110818098
## Mar 2021
            -1.9503607 104.04254
## Apr 2021 -6.8282886 104.41240
                                  -3.459806511
## May 2021 -10.0761009 105.08146
                                  -0.908754977
## Jun 2021 -9.3600919 105.75052
                                   -1.922024797
## Jul 2021 -10.1312918 106.41958
                                  -4.249185771
## Aug 2021
            -3.6952153 107.27536
                                  -4.850048264
## Sep 2021
              3.8158456 108.13115
                                  -5.718095113
## Oct 2021
            11.2130846 108.98694
                                   6.375279931
## Nov 2021 11.3363315 109.81832
                                   6.470852045
## Dec 2021 13.1803233 110.64970
                                    5.233979330
              1.6748211 111.48108
## Jan 2022
                                   0.026900529
## Feb 2022
             0.9604557 112.09593
                                  -1.217984182
## Mar 2022 -1.9154152 112.71078
                                  -0.369063354
## Apr 2022 -6.8967372 113.32563
                                   4.649908547
## May 2022 -10.1274938 113.89493
                                  -0.448631708
## Jun 2022 -9.4097104 114.46422
                                   0.395188008
## Jul 2022 -10.2055011 115.03352
                                  -0.593218213
## Aug 2022 -3.8402816 115.52604
                                  -6.069163191
## Sep 2022
              3.7907091 116.01857
                                   -0.793179360
## Oct 2022 11.2961746 116.51110
                                    2.482129583
```

plot(stl\_decomp) #Decomposition Plot



#Yes the time series is seasonal, and it is additive seasonal not multiplicative as the magnitude is co #the month of October - December had pretty high seasonal values and later we also see that this trend #months of October - December have really high seasonal values. I believe the reason for it is that aro #we have the holidays season meaning thanksgiving, Christmas and new years so naturally the consumers w #candies to celebrate the holidays. As for the rest of the years as expected the seasonal values are ne #is like the holiday season and the production during those months is really high therefore in the mont #seasonal values tend to become very low or even negative.

#### seasadj(stl\_decomp)

##		Jan	Feb	Mar	Apr	May	Jun	Jul
##	2012							
##	2013	91.88062	87.87708	90.98407	89.25356	89.67385	89.05835	89.95738
##	2014	90.84168	90.70741	90.86383	88.35425	87.65982	87.64734	86.61128
##	2015	92.69625	91.75144	92.22933	92.11430	91.87373	94.72498	96.99832
##	2016	96.22041	97.07102	100.41043	101.69494	103.27716	103.00168	103.86775
##	2017	99.62381	102.54467	97.25823	103.66682	101.11365	102.10257	99.94771
##	2018	98.89479	100.84269	99.68759	103.95354	103.25482	99.93921	100.54055
##	2019	101.03634	102.24696	104.53850	103.49291	103.19692	102.95254	101.25362
##	2020	98.63571	101.56299	98.92428	89.29256	94.44840	96.85469	101.23625
##	2021	108.60855	100.79684	104.15336	100.95259	104.17270	103.82849	102.17039
##	2022	111.50798	110.87794	112.34172	117.97554	113.44629	114.85941	114.44030
##		Aug	Sep	Oct	Nov	Dec		
##	2012			89.25498	88.87915	88.32464		
##	2013	89.44865	88.65907	92.02034	94.74166	95.67885		
##	2014	87.49943	89.21788	92.92835	99.33899	97.65576		

```
## 2015 101.12973 96.25707 99.89406 98.06010 94.18092

## 2016 98.28470 97.54074 100.87718 97.12240 95.41118

## 2017 102.77803 102.74583 96.35000 94.12071 97.45412

## 2018 99.61578 101.98637 94.69433 94.90106 98.76204

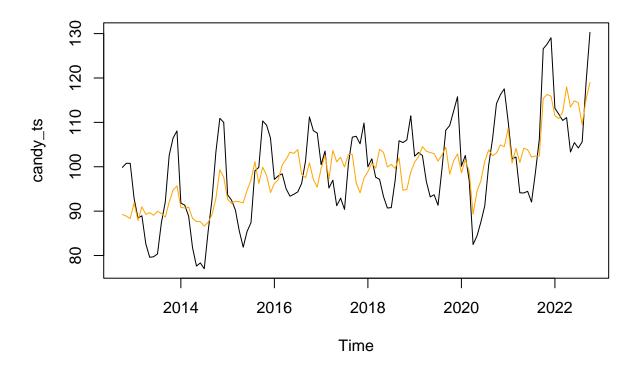
## 2019 102.64281 104.38253 98.34425 101.30814 102.89594

## 2020 103.80269 102.48251 103.08021 104.93017 104.51314

## 2021 102.42532 102.41305 115.36222 116.28917 115.88368

## 2022 109.45688 115.22539 118.99323
```

```
plot(candy_ts)
lines(seasadj(stl_decomp), col="Orange")
```

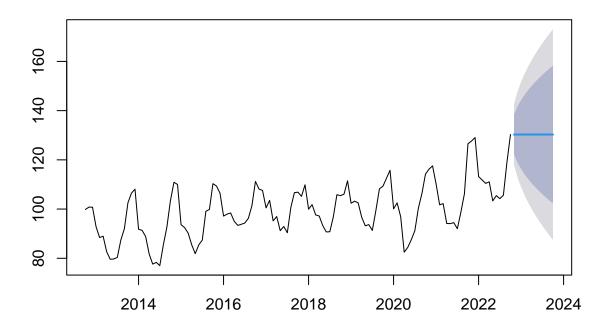


#After taking out the seasonal component the graph still looks the same in the overall direction and tr #shrunk dramatically this means that the magnitude of values in the timeseries is affected but the seas #seasonality has big fluctuations to the values of the timeseries.

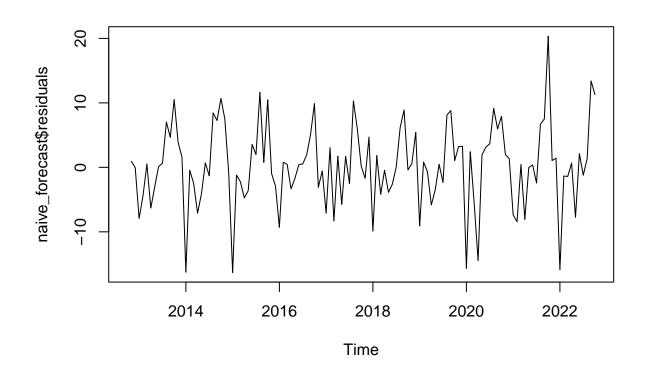
#### #Naive

naive\_forecast <- naive(candy\_ts,12) #give me the forecast for the next 12 months using Naive forecast
plot(naive\_forecast)</pre>

## **Forecasts from Naive method**



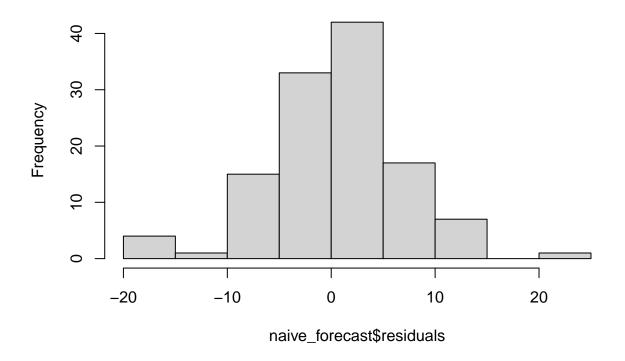
```
attributes(naive_forecast)
## $names
##
   [1] "method"
                    "model"
                                 "lambda"
                                             "x"
                                                          "fitted"
                                                                      "residuals"
   [7] "series"
                    "mean"
                                 "level"
                                             "lower"
                                                          "upper"
##
## $class
## [1] "forecast"
#$names
#[1] "method"
                 "model"
                              "lambda"
                                          "x"
                                                       "fitted"
                                                                   "residuals" "series"
                                                                                            "mean"
#[11] "upper"
#$class
#[1] "forecast"
plot(naive_forecast$residuals) #the residual plot shows 6 anomalies(not within range from what I can se
```



 $\verb|hist(naive_forecast$residuals)| \textit{\#shows a pretty decent normal distribution}|\\$ 

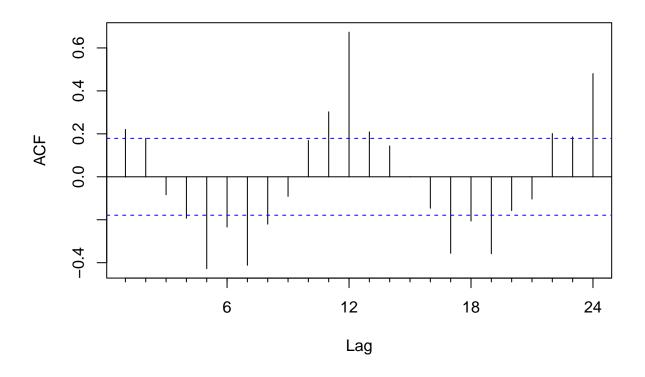
#start of year 2014 where there is a sharp decline in production same goes for the start of year 2015,2 #beginning months of year 2022 and the 6th one being the sharp increase in the production just at the e

# Histogram of naive\_forecast\$residuals



Acf(naive\_forecast\$residuals) #shows most values are out of the threshold region meaning they are depen

# Series naive\_forecast\$residuals

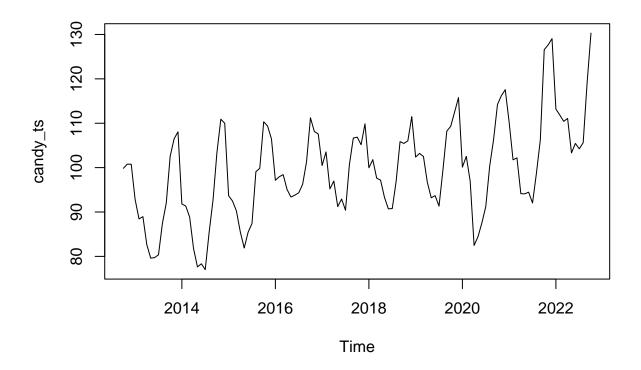


```
#values (correaltion present).
accuracy(naive_forecast)
```

## Training set 0.2536275 6.305638 4.625101 0.02809525 4.635846 1.05288 0.2207691

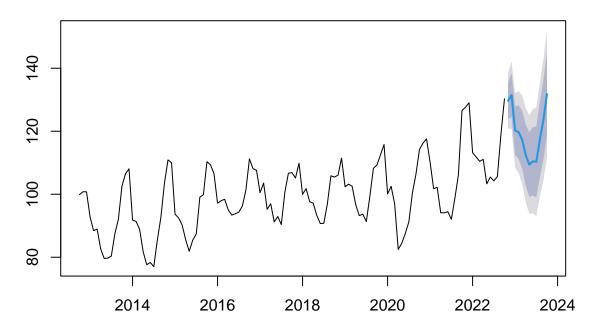
# ME RMSE MAE MPE MAPE MASE ACF1
#Training set 0.2536275 6.305638 4.625101 0.02809525 4.635846 1.05288 0.2207691

ets\_forecast <- ets(candy\_ts)
plot(candy\_ts)



forecast\_ets <- forecast(ets\_forecast, h=12) #forecasting for the next 12 months plot(forecast\_ets)

## Forecasts from ETS(M,A,A)



#### forecast\_ets

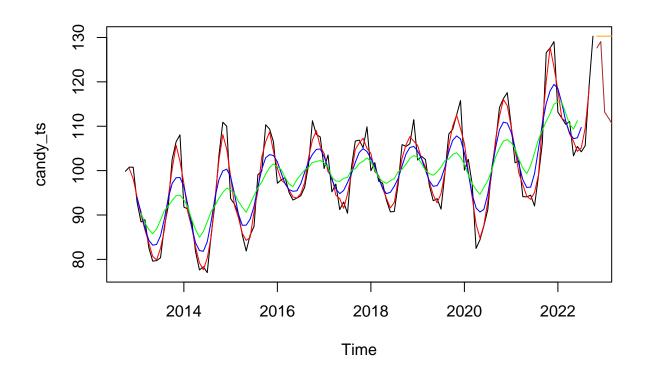
#Jun 2023

```
Point Forecast
##
                              Lo 80
                                       Hi 80
                                                 Lo 95
                                                          Hi 95
## Nov 2022
                 129.6266 123.89521 135.3579 120.86121 138.3919
## Dec 2022
                 131.4585 124.44955 138.4674 120.73925 142.1777
## Jan 2023
                 120.2379 112.53103 127.9448 108.45126 132.0245
## Feb 2023
                 119.7004 111.19327 128.2074 106.68990 132.7108
## Mar 2023
                 117.3170 108.13076 126.5032 103.26787 131.3661
## Apr 2023
                 112.4141 102.67755 122.1506
                                             97.52333 127.3049
## May 2023
                 109.4166
                          99.16483 119.6684 93.73787 125.0953
## Jun 2023
                 110.4319
                           99.63670 121.2271
                                              93.92206 126.9418
## Jul 2023
                 110.2762 98.97651 121.5760 92.99479 127.5577
## Aug 2023
                 117.4103 105.49177 129.3289 99.18246 135.6382
## Sep 2023
                 123.6545 111.09743 136.2116 104.45011 142.8589
## Oct 2023
                 131.8069 118.54708 145.0667 111.52776 152.0860
#
        Point Forecast
                          Lo 80 Hi 80 Lo 95
#Nov 2022
                129.6266 123.89521 135.3579 120.86121 138.3919
#Dec 2022
                131.4585 124.44955 138.4674 120.73925 142.1777
#Jan 2023
               120.2379 112.53103 127.9448 108.45126 132.0245
               119.7004 111.19327 128.2074 106.68990 132.7108
#Feb 2023
#Mar 2023
                117.3170 108.13076 126.5032 103.26787 131.3661
#Apr 2023
               112.4141 102.67755 122.1506 97.52333 127.3049
#May 2023
               109.4166 99.16483 119.6684 93.73787 125.0953
```

110.4319 99.63670 121.2271 93.92206 126.9418

#### ## [1] 10.95792

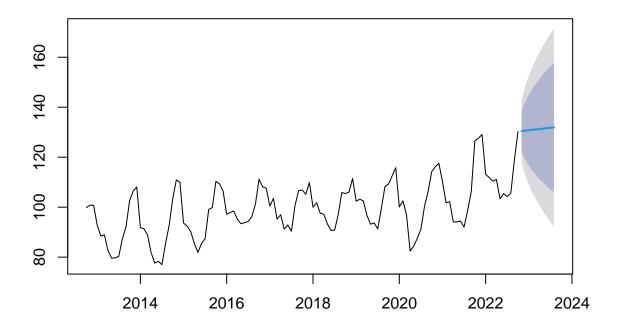
```
#[1] 10.95792
#RSME is 6.305638 on average forecast values were 6.305638 away from the actual
#MPE is 2.8% percenatge of error is around 2.8%
#Simple Moving Average
plot(candy_ts)
MA3_forecast <- ma(candy_ts,order=3) #taking into account the 5 most recent values
MA6_forecast <- ma(candy_ts,order=6) #taking into account the 9 most recent values
MA9_forecast <- ma(candy_ts,order=9) #taking into account the 9 most recent values
rwf_forecast <- rwf(candy_ts,12)</pre>
snaive_forecast <- snaive(candy_ts, 12)</pre>
plot(candy_ts)
lines(rwf forecast$mean,col="Orange")
lines(snaive_forecast$mean,col="brown") #works best for my time series: snaive method
lines(MA3_forecast,col="Red")
lines(MA6_forecast,col="Blue")
lines(MA9_forecast,col="Green")
```



#as the order goes up the line comes up shorter and shorter from the end, and from the start as well, t #smaller. And also as the order goes up the trend is somewhat followed but the magnitude shrinks in size

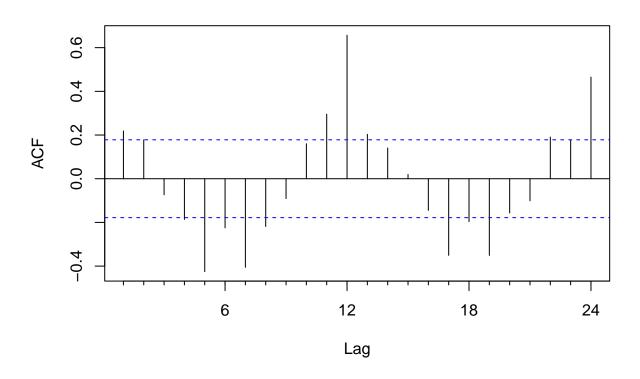
```
#Simple Smoothing
SSE_Simple <- holt(candy_ts,gamma=FALSE)</pre>
attributes(SSE_Simple)
## $names
    [1] "model"
                     "mean"
                                  "level"
                                                            "upper"
                                                                        "lower"
##
    [7] "fitted"
                     "method"
                                  "series"
                                               "residuals"
##
## $class
## [1] "forecast"
plot(SSE_Simple)
```

## Forecasts from Holt's method



```
attributes(SSE_Simple)
## $names
   [1] "model"
                     "mean"
                                 "level"
                                             "x"
                                                          "upper"
                                                                       "lower"
   [7] "fitted"
                    "method"
##
                                 "series"
                                             "residuals"
## $class
## [1] "forecast"
#$names
#[1] "model"
                  "mean"
                              "level"
                                           "x"
                                                       "upper"
                                                                    "lower"
                                                                                "fitted"
                                                                                             "method"
#$class
#[1] "forecast"
Acf(SSE_Simple$residuals)
```

# Series SSE\_Simple\$residuals



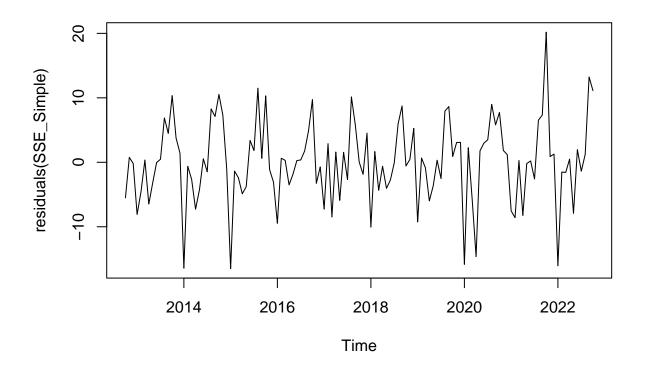
```
Box.test(residuals(SSE_Simple), lag=12, type="Ljung")
```

```
##
## Box-Ljung test
##
## data: residuals(SSE_Simple)
## X-squared = 147.8, df = 12, p-value < 2.2e-16</pre>
```

```
#data: residuals(auto_fit)
#X-squared = 13.084, df = 12, p-value < 2.2e-16

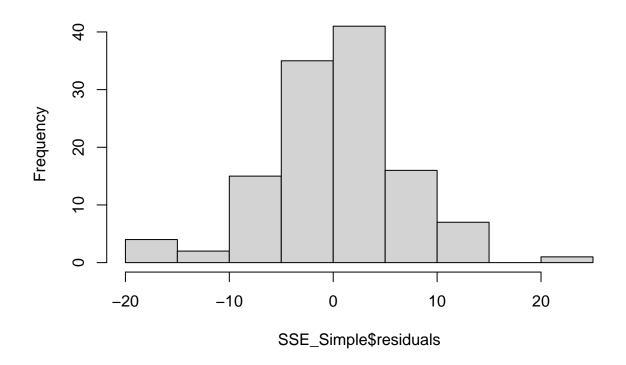
#As we can see from the Ljung box statistic that the p-values are < 2.2e-16 which makes them significan
#hypothesis which means that the residual values are dependent

plot.ts(residuals(SSE_Simple))</pre>
```



hist(SSE\_Simple\$residuals) #normal distribution

# **Histogram of SSE\_Simple\$residuals**



#### accuracy(SSE\_Simple)

## ME RMSE MAE MPE MAPE MASE ACF1
## Training set 0.04457017 6.29552 4.615979 -0.1819999 4.631386 1.050803 0.2185404

# ME RMSE MAE MPE MAPE MASE ACF1
#Training set 0.04457017 6.29552 4.615979 -0.1819999 4.631386 1.050803 0.2185404

SSE\_Simple\$mse

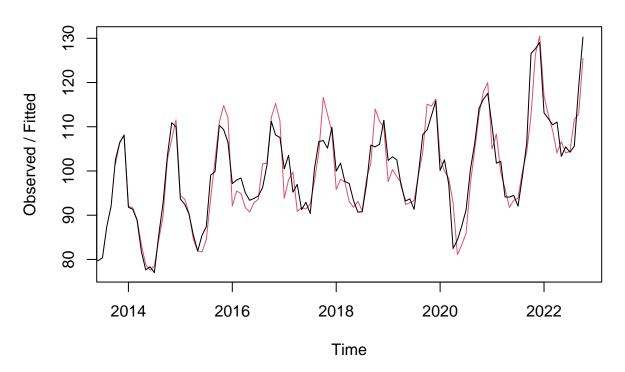
#### ## NULL

#[1] NULL
#RSME is 6.29552 on average forecast values were 6.29552 away from the actual
#MPE is 18% percenatge of error is around 18%

#Holt Winters

HW\_forecast <- HoltWinters(candy\_ts)
plot(HW\_forecast)</pre>

# **Holt-Winters filtering**

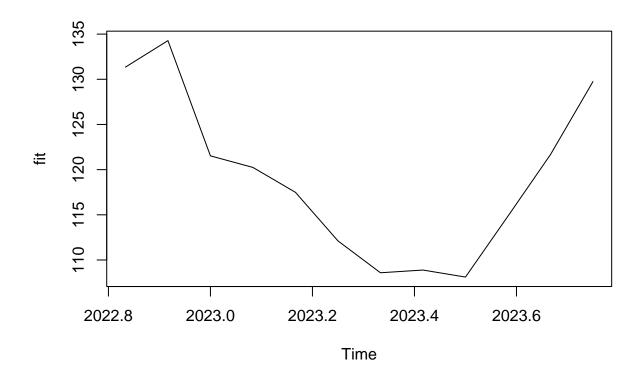


#### HW\_forecast

```
## Holt-Winters exponential smoothing with trend and additive seasonal component.
## Call:
## HoltWinters(x = candy_ts)
##
## Smoothing parameters:
    alpha: 0.7137653
##
    beta: 0
##
    gamma: 0.3677262
##
## Coefficients:
##
               [,1]
       118.58175151
## a
## b
         0.02735169
##
        12.73645821
  s1
   s2
        15.64347958
##
         2.86140879
##
   s3
##
         1.55347367
   s4
##
  s5
        -1.22825112
## s6
        -6.63034922
## s7
       -10.18821076
        -9.91381693
## s8
## s9
       -10.71852359
       -3.99912312
## s10
```

```
## s11 2.78200916
## s12 10.83734441
```

```
HWForecast <- predict(HW_forecast, 12)
plot(HWForecast)</pre>
```



#### ${\tt HWForecast}$

```
##
             Jan
                      Feb
                                Mar
                                         Apr
                                                  May
                                                            Jun
                                                                     Jul
                                                                              Aug
## 2022
## 2023 121.5252 120.2446 117.4903 112.1155 108.5850 108.8867 108.1094 114.8561
             Sep
                                Nov
## 2022
                           131.3456 134.2799
## 2023 121.6646 129.7473
```

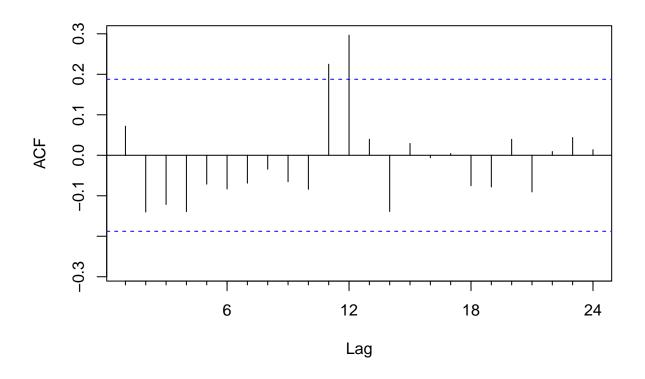
HW\_forecast #Alpha = 0.7137653 (the newest values does not have maximum weight but has relatively more

```
## Holt-Winters exponential smoothing with trend and additive seasonal component.
##
## Call:
## HoltWinters(x = candy_ts)
##
## Smoothing parameters:
## alpha: 0.7137653
```

```
## beta: 0
##
   gamma: 0.3677262
##
## Coefficients:
##
               [,1]
## a
       118.58175151
## b
        0.02735169
        12.73645821
## s1
## s2
        15.64347958
## s3
        2.86140879
## s4
        1.55347367
        -1.22825112
## s5
       -6.63034922
## s6
## s7 -10.18821076
## s8
       -9.91381693
## s9 -10.71852359
## s10 -3.99912312
## s11
         2.78200916
## s12 10.83734441
#beta : O (this is the coefficient of trend smoothing in HW)
#gamma: 0.3677262 (seasonal model)
ets_forecast #sigma: 0.0345 (standard dev. of residuals)
## ETS(M,A,A)
##
## Call:
## ets(y = candy_ts)
##
##
    Smoothing parameters:
##
       alpha = 0.6829
##
       beta = 1e-04
##
       gamma = 1e-04
##
##
    Initial states:
##
       1 = 90.6178
##
       b = 0.2533
##
       s = 3.0373 - 2.9535 - 9.8347 - 9.4264 - 10.1889 - 6.9389
##
              -1.7831 0.8532 1.6436 13.117 11.537 10.9375
##
##
     sigma: 0.0345
##
##
        AIC
                AICc
                          BIC
## 894.2047 900.1464 941.7331
#Initial states: 1 = 90.6178
#b = 0.2533
# AIC
          AICc
                    BIC
#894.2047 900.1464 941.7331
attributes(HW_forecast)
```

```
## $names
## [1] "fitted"
                 "x"
                                     "alpha"
                                                    "beta"
                                                                    "gamma"
## [6] "coefficients" "seasonal"
                                     "SSE"
                                                    "call"
##
## $class
## [1] "HoltWinters"
#$names
                  "x"
#[1] "fitted"
                                   "alpha"
                                                  "beta"
                                                                                 "coefficients" "seasona
                                                                  "gamma"
#[9] "call"
#$class
#[1] "HoltWinters"
attributes(HWForecast)
## $dim
## [1] 12 1
##
## $dimnames
## $dimnames[[1]]
## NULL
##
## $dimnames[[2]]
## [1] "fit"
##
##
## $tsp
## [1] 2022.833 2023.750 12.000
## $class
## [1] "ts"
#$dim
#[1] 12 1
#$dimnames
#$dimnames[[1]]
#NULL
#$dimnames[[2]]
#[1] "fit"
#$tsp
#[1] 2022.833 2023.750 12.000
#$class
#[1] "ts"
HWFResiduals <-residuals(HW_forecast)</pre>
Acf(HWFResiduals) #most values seem to be in the threshold region meaning apart from the 2 values outsi
```

### Series HWFResiduals



#values are dependent on the last value

```
Box.test(HWFResiduals, lag=12, type="Ljung")

##

## Box-Ljung test

##

## data: HWFResiduals

## X-squared = 27.423, df = 12, p-value = 0.006713

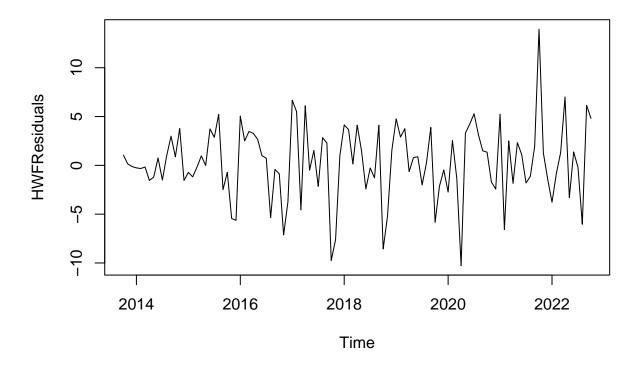
#Box-Ljung test

#data: HWFResiduals

#X-squared = 27.423, df = 12, p-value = 0.006713

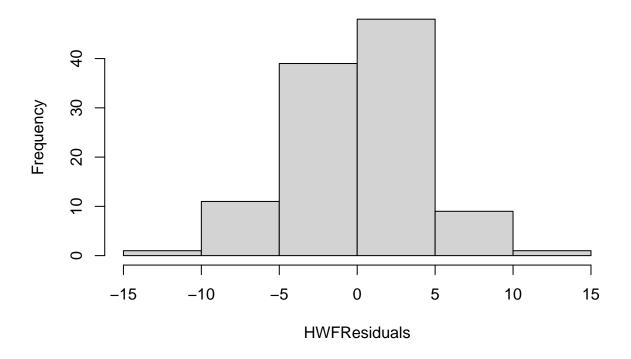
#As we can see from the Ljung box statistic that the p-values are 0.006713 which makes them significant 
#hypothesis which means that the residual values are dependent.

plot.ts(HWFResiduals)
```



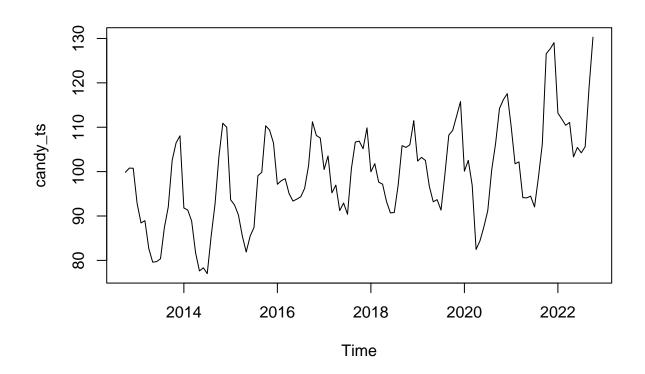
hist(HWFResiduals) #normal distribution

# **Histogram of HWFResiduals**



#ARIMA or  $Box ext{-}Jenkins$ 

plot(candy\_ts)



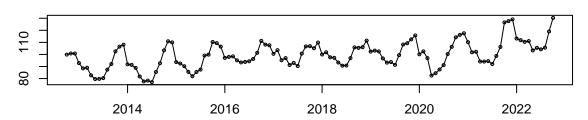
ndiffs(candy\_ts) #as the ndiffs function gives out the value 1 it means that the model is not stationar

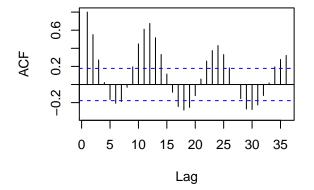
### ## [1] 1

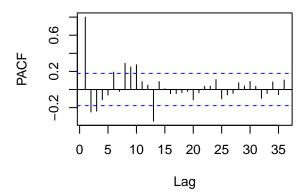
 $\hbox{\it\#that we need 1 difference to get the stationary value.}\\ \hbox{\it\#Seasonality is not needed for this.}$ 

tsdisplay(candy\_ts)

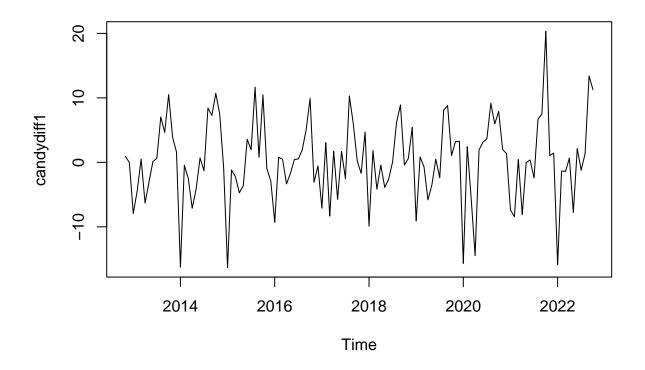






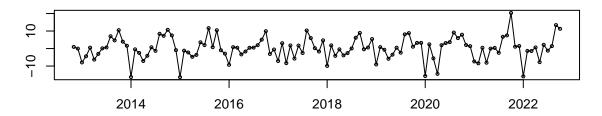


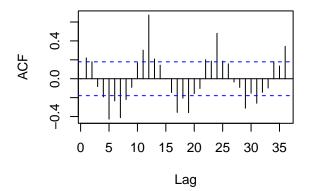
candydiff1 <- diff(candy\_ts, differences=1)
plot(candydiff1)</pre>

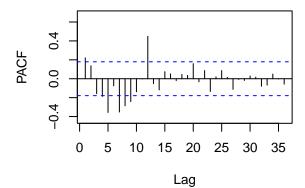


tsdisplay(candydiff1)

### candydiff1







auto\_fit <- auto.arima(candy\_ts, trace=TRUE, stepwise = FALSE)</pre>

```
##
    ARIMA(0,0,0)(0,1,0)[12]
                                                 : 695.7015
                                                 : 670.7642
##
    ARIMA(0,0,0)(0,1,0)[12] with drift
##
    ARIMA(0,0,0)(0,1,1)[12]
                                                  695.999
##
    ARIMA(0,0,0)(0,1,1)[12] with drift
                                                 : Inf
##
    ARIMA(0,0,0)(0,1,2)[12]
                                                 : 696.3967
##
                                                 : Inf
    ARIMA(0,0,0)(0,1,2)[12] with drift
##
    ARIMA(0,0,0)(1,1,0)[12]
                                                 : 696.3465
                                                 : 672.2067
##
    ARIMA(0,0,0)(1,1,0)[12] with drift
    ARIMA(0,0,0)(1,1,1)[12]
                                                 : Inf
    ARIMA(0,0,0)(1,1,1)[12] with drift
                                                   Inf
##
##
    ARIMA(0,0,0)(1,1,2)[12]
                                                 : Inf
##
                                                 : Inf
    ARIMA(0,0,0)(1,1,2)[12] with drift
##
    ARIMA(0,0,0)(2,1,0)[12]
                                                 : 697.5285
                                                 : 666.0752
##
    ARIMA(0,0,0)(2,1,0)[12] with drift
##
    ARIMA(0,0,0)(2,1,1)[12]
                                                 : Inf
                                                 : Inf
##
    ARIMA(0,0,0)(2,1,1)[12] with drift
   ARIMA(0,0,0)(2,1,2)[12]
                                                 : Inf
##
##
    ARIMA(0,0,0)(2,1,2)[12] with drift
                                                   Inf
##
    ARIMA(0,0,1)(0,1,0)[12]
                                                 : 654.6188
##
    ARIMA(0,0,1)(0,1,0)[12] with drift
                                                 : 639.2968
##
    ARIMA(0,0,1)(0,1,1)[12]
                                                 : 656.1893
    ARIMA(0,0,1)(0,1,1)[12] with drift
                                                 : Inf
```

```
ARIMA(0,0,1)(0,1,2)[12]
                                                : 657.6255
   ARIMA(0,0,1)(0,1,2)[12] with drift
##
                                                : Inf
                                                : 656.284
   ARIMA(0,0,1)(1,1,0)[12]
## ARIMA(0,0,1)(1,1,0)[12] with drift
                                                : 637.5419
##
   ARIMA(0,0,1)(1,1,1)[12]
                                                : 657.9208
##
   ARIMA(0,0,1)(1,1,1)[12] with drift
                                                : Inf
  ARIMA(0,0,1)(1,1,2)[12]
                                                : 659.7173
##
   ARIMA(0,0,1)(1,1,2)[12] with drift
                                                : Inf
##
   ARIMA(0,0,1)(2,1,0)[12]
                                                : 657.8574
##
   ARIMA(0,0,1)(2,1,0)[12] with drift
                                                : 634.4358
   ARIMA(0,0,1)(2,1,1)[12]
                                                : 659.7902
##
   ARIMA(0,0,1)(2,1,1)[12] with drift
                                                : Inf
                                                : Inf
##
   ARIMA(0,0,1)(2,1,2)[12]
##
   ARIMA(0,0,1)(2,1,2)[12] with drift
                                                : Inf
                                                : 636.3448
##
   ARIMA(0,0,2)(0,1,0)[12]
##
   ARIMA(0,0,2)(0,1,0)[12] with drift
                                                : 626.0602
                                                : 637.898
##
   ARIMA(0,0,2)(0,1,1)[12]
##
   ARIMA(0,0,2)(0,1,1)[12] with drift
                                                : Inf
                                                : 636.7653
##
   ARIMA(0,0,2)(0,1,2)[12]
   ARIMA(0,0,2)(0,1,2)[12] with drift
                                                : Inf
##
   ARIMA(0,0,2)(1,1,0)[12]
                                                : 638.0881
                                                : 625.6669
  ARIMA(0,0,2)(1,1,0)[12] with drift
                                                : 638.334
##
  ARIMA(0,0,2)(1,1,1)[12]
                                                : Inf
   ARIMA(0,0,2)(1,1,1)[12] with drift
##
                                                : 638.992
##
   ARIMA(0,0,2)(1,1,2)[12]
   ARIMA(0,0,2)(1,1,2)[12] with drift
                                                : Inf
##
                                                : 637.8508
   ARIMA(0,0,2)(2,1,0)[12]
##
   ARIMA(0,0,2)(2,1,0)[12] with drift
                                                : 621.3809
##
                                                : 638.4469
   ARIMA(0,0,2)(2,1,1)[12]
   ARIMA(0,0,2)(2,1,1)[12] with drift
                                                : Inf
##
   ARIMA(0,0,3)(0,1,0)[12]
                                                : 629.9275
##
   ARIMA(0,0,3)(0,1,0)[12] with drift
                                                : 622.7562
##
   ARIMA(0,0,3)(0,1,1)[12]
                                                : 629.7434
                                                : Inf
##
   ARIMA(0,0,3)(0,1,1)[12] with drift
                                                : 629.0504
##
   ARIMA(0,0,3)(0,1,2)[12]
##
   ARIMA(0,0,3)(0,1,2)[12] with drift
                                                : Inf
   ARIMA(0,0,3)(1,1,0)[12]
                                                : 630.4963
                                                : 620.9963
##
   ARIMA(0,0,3)(1,1,0)[12] with drift
                                                : 629.6219
##
   ARIMA(0,0,3)(1,1,1)[12]
                                                : Inf
##
   ARIMA(0,0,3)(1,1,1)[12] with drift
                                                : 630.7565
  ARIMA(0,0,3)(2,1,0)[12]
##
   ARIMA(0,0,3)(2,1,0)[12] with drift
                                                : 618.3351
##
   ARIMA(0,0,4)(0,1,0)[12]
                                                : 629.5131
##
                                                : 623.8854
   ARIMA(0,0,4)(0,1,0)[12] with drift
   ARIMA(0,0,4)(0,1,1)[12]
                                                : 628.2313
                                                : Inf
##
   ARIMA(0,0,4)(0,1,1)[12] with drift
##
   ARIMA(0,0,4)(1,1,0)[12]
                                                : 629.5068
##
   ARIMA(0,0,4)(1,1,0)[12] with drift
                                                : 621.9546
  ARIMA(0,0,5)(0,1,0)[12]
                                                : 630.6005
##
   ARIMA(0,0,5)(0,1,0)[12] with drift
                                                : 625.8286
                                                : 622.9559
##
   ARIMA(1,0,0)(0,1,0)[12]
## ARIMA(1,0,0)(0,1,0)[12] with drift
                                                : 619.2546
## ARIMA(1,0,0)(0,1,1)[12]
                                                : 616.096
   ARIMA(1,0,0)(0,1,1)[12] with drift
                                                : Inf
```

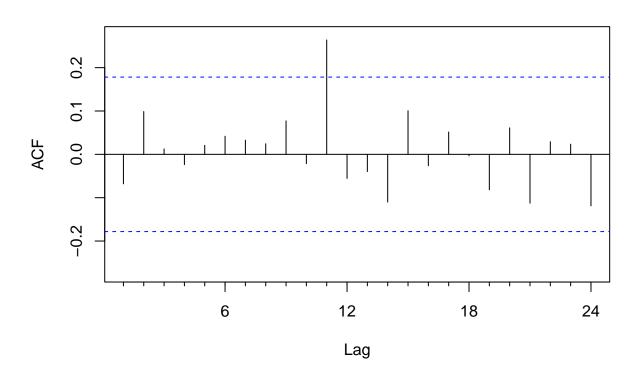
```
ARIMA(1,0,0)(0,1,2)[12]
                                               : Inf
   ARIMA(1,0,0)(0,1,2)[12] with drift
##
                                               : Inf
## ARIMA(1,0,0)(1,1,0)[12]
                                               : 620.045
## ARIMA(1,0,0)(1,1,0)[12] with drift
                                               : 615.4554
   ARIMA(1,0,0)(1,1,1)[12]
##
                                               : Inf
## ARIMA(1,0,0)(1,1,1)[12] with drift
                                               : Inf
## ARIMA(1,0,0)(1,1,2)[12]
                                               : Inf
## ARIMA(1,0,0)(1,1,2)[12] with drift
                                               : Inf
##
   ARIMA(1,0,0)(2,1,0)[12]
                                               : 619.4956
                                               : 613.3055
##
   ARIMA(1,0,0)(2,1,0)[12] with drift
  ARIMA(1,0,0)(2,1,1)[12]
                                               : Inf
##
   ARIMA(1,0,0)(2,1,1)[12] with drift
                                               : Inf
                                               : Inf
##
   ARIMA(1,0,0)(2,1,2)[12]
##
   ARIMA(1,0,0)(2,1,2)[12] with drift
                                               : Inf
                                               : 621.839
  ARIMA(1,0,1)(0,1,0)[12]
##
   ARIMA(1,0,1)(0,1,0)[12] with drift
                                               : 619.5991
                                               : 615.267
##
   ARIMA(1,0,1)(0,1,1)[12]
  ARIMA(1,0,1)(0,1,1)[12] with drift
                                               : Inf
## ARIMA(1,0,1)(0,1,2)[12]
                                               : Inf
   ARIMA(1,0,1)(0,1,2)[12] with drift
                                               : Inf
##
   ARIMA(1,0,1)(1,1,0)[12]
                                               : 618.9704
## ARIMA(1,0,1)(1,1,0)[12] with drift
                                               : 616.1254
                                               : Inf
## ARIMA(1,0,1)(1,1,1)[12]
   ARIMA(1,0,1)(1,1,1)[12] with drift
                                               : Inf
##
## ARIMA(1,0,1)(1,1,2)[12]
                                               : Inf
  ARIMA(1,0,1)(1,1,2)[12] with drift
                                               : Inf
##
                                               : 618.2582
   ARIMA(1,0,1)(2,1,0)[12]
##
   ARIMA(1,0,1)(2,1,0)[12] with drift
                                               : 614.2405
                                               : Inf
  ARIMA(1,0,1)(2,1,1)[12]
## ARIMA(1,0,1)(2,1,1)[12] with drift
                                               : Inf
##
   ARIMA(1,0,2)(0,1,0)[12]
                                               : 623.7407
##
   ARIMA(1,0,2)(0,1,0)[12] with drift
                                               : 620.8486
##
   ARIMA(1,0,2)(0,1,1)[12]
                                               : Inf
##
  ARIMA(1,0,2)(0,1,1)[12] with drift
                                               : Inf
   ARIMA(1,0,2)(0,1,2)[12]
                                               : Inf
                                               : Inf
## ARIMA(1,0,2)(0,1,2)[12] with drift
## ARIMA(1,0,2)(1,1,0)[12]
                                               : 621.1253
## ARIMA(1,0,2)(1,1,0)[12] with drift
                                               : 618.2083
                                               : Inf
##
   ARIMA(1,0,2)(1,1,1)[12]
                                               : Inf
## ARIMA(1,0,2)(1,1,1)[12] with drift
                                               : 620.3847
## ARIMA(1,0,2)(2,1,0)[12]
## ARIMA(1,0,2)(2,1,0)[12] with drift
                                               : 616.1228
##
   ARIMA(1,0,3)(0,1,0)[12]
                                               : 624.0376
##
                                               : 622.9934
  ARIMA(1,0,3)(0,1,0)[12] with drift
## ARIMA(1,0,3)(0,1,1)[12]
                                               : Inf
                                               : Inf
## ARIMA(1,0,3)(0,1,1)[12] with drift
##
   ARIMA(1,0,3)(1,1,0)[12]
                                               : 621.5939
##
  ARIMA(1,0,3)(1,1,0)[12] with drift
                                               : 620.4402
  ARIMA(1,0,4)(0,1,0)[12]
                                               : 625.2055
##
   ARIMA(1,0,4)(0,1,0)[12] with drift
                                               : 624.5141
                                               : 621.502
## ARIMA(2,0,0)(0,1,0)[12]
## ARIMA(2,0,0)(0,1,0)[12] with drift
                                               : 619.1749
## ARIMA(2,0,0)(0,1,1)[12]
                                               : 615.6749
## ARIMA(2,0,0)(0,1,1)[12] with drift
                                               : Inf
```

```
ARIMA(2,0,0)(0,1,2)[12]
                                               : Inf
   ARIMA(2,0,0)(0,1,2)[12] with drift
##
                                               : Inf
## ARIMA(2,0,0)(1,1,0)[12]
                                               : 619.0898
## ARIMA(2,0,0)(1,1,0)[12] with drift
                                               : 616.0103
   ARIMA(2,0,0)(1,1,1)[12]
##
                                               : Inf
## ARIMA(2,0,0)(1,1,1)[12] with drift
                                               : Inf
## ARIMA(2,0,0)(1,1,2)[12]
                                               : Inf
## ARIMA(2,0,0)(1,1,2)[12] with drift
                                               : Inf
##
   ARIMA(2,0,0)(2,1,0)[12]
                                               : 618.3519
                                               : 614.0563
##
   ARIMA(2,0,0)(2,1,0)[12] with drift
  ARIMA(2,0,0)(2,1,1)[12]
                                               : Inf
                                               : Inf
##
   ARIMA(2,0,0)(2,1,1)[12] with drift
                                               : 623.5522
##
   ARIMA(2,0,1)(0,1,0)[12]
   ARIMA(2,0,1)(0,1,0)[12] with drift
                                               : 621.0785
                                               : Inf
   ARIMA(2,0,1)(0,1,1)[12]
##
   ARIMA(2,0,1)(0,1,1)[12] with drift
                                               : Inf
                                               : Inf
##
   ARIMA(2,0,1)(0,1,2)[12]
  ARIMA(2,0,1)(0,1,2)[12] with drift
                                               : Inf
##
  ARIMA(2,0,1)(1,1,0)[12]
                                               : 619.2936
   ARIMA(2,0,1)(1,1,0)[12] with drift
                                               : 618.2342
##
   ARIMA(2,0,1)(1,1,1)[12]
                                               : Inf
## ARIMA(2,0,1)(1,1,1)[12] with drift
                                               : Inf
                                               : 617.3422
## ARIMA(2,0,1)(2,1,0)[12]
   ARIMA(2,0,1)(2,1,0)[12] with drift
##
                                               : Inf
## ARIMA(2,0,2)(0,1,0)[12]
                                               : 625.7487
  ARIMA(2,0,2)(0,1,0)[12] with drift
                                               : 623.077
##
                                               : Inf
   ARIMA(2,0,2)(0,1,1)[12]
##
   ARIMA(2,0,2)(0,1,1)[12] with drift
                                               : Inf
                                               : 621.2392
  ARIMA(2,0,2)(1,1,0)[12]
  ARIMA(2,0,2)(1,1,0)[12] with drift
                                               : 620.4897
##
   ARIMA(2,0,3)(0,1,0)[12]
                                               : 625.4338
##
   ARIMA(2,0,3)(0,1,0)[12] with drift
                                               : 624.7418
##
   ARIMA(3,0,0)(0,1,0)[12]
                                               : 623.565
                                               : 620.9597
##
  ARIMA(3,0,0)(0,1,0)[12] with drift
   ARIMA(3,0,0)(0,1,1)[12]
                                               : 617.5374
##
   ARIMA(3,0,0)(0,1,1)[12] with drift
                                               : Inf
  ARIMA(3,0,0)(0,1,2)[12]
                                               : Inf
##
                                               : Inf
  ARIMA(3,0,0)(0,1,2)[12] with drift
                                               : 621.2407
##
   ARIMA(3,0,0)(1,1,0)[12]
                                               : 618.2282
## ARIMA(3,0,0)(1,1,0)[12] with drift
  ARIMA(3,0,0)(1,1,1)[12]
                                               : Inf
##
                                               : Inf
  ARIMA(3,0,0)(1,1,1)[12] with drift
##
   ARIMA(3,0,0)(2,1,0)[12]
                                               : Inf
##
                                               : 616.1571
   ARIMA(3,0,0)(2,1,0)[12] with drift
  ARIMA(3,0,1)(0,1,0)[12]
                                               : Inf
                                               : Inf
##
   ARIMA(3,0,1)(0,1,0)[12] with drift
##
   ARIMA(3,0,1)(0,1,1)[12]
                                               : Inf
                                               : Inf
##
  ARIMA(3,0,1)(0,1,1)[12] with drift
  ARIMA(3,0,1)(1,1,0)[12]
                                               : Inf
##
   ARIMA(3,0,1)(1,1,0)[12] with drift
                                               : 620.2729
                                               : Inf
## ARIMA(3,0,2)(0,1,0)[12]
## ARIMA(3,0,2)(0,1,0)[12] with drift
                                               : Inf
## ARIMA(4,0,0)(0,1,0)[12]
                                               : 625.6611
## ARIMA(4,0,0)(0,1,0)[12] with drift
                                               : 623.1987
```

```
## ARIMA(4,0,0)(0,1,1)[12]
                                            : 619.4666
                                           : Inf
## ARIMA(4,0,0)(0,1,1)[12] with drift
## ARIMA(4,0,0)(1,1,0)[12]
                                            : 623.4068
## ARIMA(4,0,0)(1,1,0)[12] with drift
                                            : 620.4931
## ARIMA(4,0,1)(0,1,0)[12]
                                            : Inf
## ARIMA(4,0,1)(0,1,0)[12] with drift
                                           : Inf
## ARIMA(5,0,0)(0,1,0)[12]
                                            : 626.6308
## ARIMA(5,0,0)(0,1,0)[12] with drift
                                          : 624.8284
##
##
##
## Best model: ARIMA(1,0,0)(2,1,0)[12] with drift
# Best model: ARIMA(1,0,0)(2,1,0)[12] with drift
auto_fit
## Series: candy_ts
## ARIMA(1,0,0)(2,1,0)[12] with drift
## Coefficients:
          ar1
                 sar1
                           sar2
                                  drift
##
        0.6441 -0.3042 -0.2351 0.2083
## s.e. 0.0742 0.1040 0.1099 0.0579
## sigma^2 = 14.95: log likelihood = -301.36
## AIC=612.72 AICc=613.31 BIC=626.18
# Series: candy ts
#ARIMA(1,0,0)(2,1,0)[12] with drift
#Coefficients:
      ar1
               sar1
                       sar2 drift
      0.6441 -0.3042 -0.2351 0.2083
#s.e. 0.0742 0.1040 0.1099 0.0579
\#sigma^2 = 14.95: log\ likelihood = -301.36
#AIC=612.72 AICc=613.31 BIC=626.18
attributes(auto_fit)
## $names
## [1] "coef"
                   "sigma2"
                               "var.coef" "mask"
                                                      "loglik"
                                                                 "aic"
                   "residuals" "call"
## [7] "arma"
                                          "series"
                                                      "code"
                                                                 "n.cond"
## [13] "nobs"
                   "model"
                               "xreg"
                                          "bic"
                                                      "aicc"
                                                                 "x"
## [19] "fitted"
##
## $class
## [1] "forecast_ARIMA" "ARIMA"
                                       "Arima"
```

```
#$names
#[1] "coef"
                  "siqma2"
                                            "mask"
                                                         "loglik"
                                                                                               "residuals" "c
                               "var.coef"
                                                                                  "arma"
#[11] "code"
                                "nobs"
                                                                      "bic"
                                                                                                "x"
                   "n.cond"
                                             "model"
                                                         "xreg"
                                                                                   "aicc"
#$class
#[1] "forecast_ARIMA" "ARIMA"
                                          "Arima"
Acf(auto_fit$residuals)
```

## Series auto\_fit\$residuals



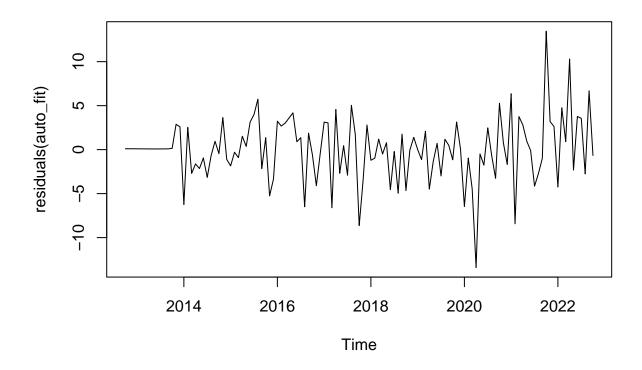
```
Box.test(residuals(auto_fit), lag=12, type="Ljung")

##
## Box-Ljung test
##
## data: residuals(auto_fit)
## X-squared = 13.084, df = 12, p-value = 0.363

#data: residuals(auto_fit)
#X-squared = 13.084, df = 12, p-value = 0.363

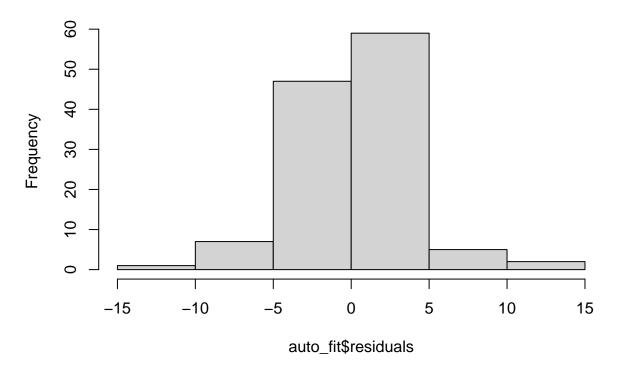
#As we can see from the Ljung box statistic that the p-values are 0.363 which makes them non-significan #hypothesis which means that the residual values are independent

plot.ts(residuals(auto_fit))
```



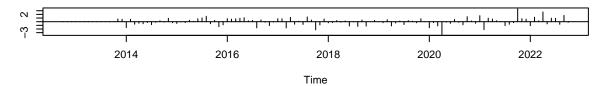
hist(auto\_fit\$residuals) #normal distribution

# Histogram of auto\_fit\$residuals

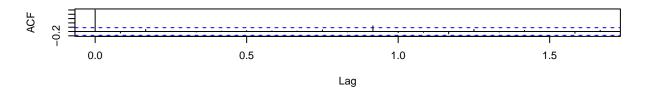


tsdiag(auto\_fit) #ACF test shows no relative significance amongst residuals as well same as the p-value

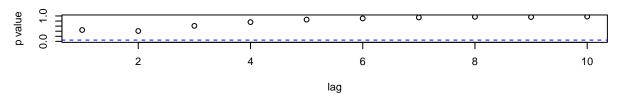
#### **Standardized Residuals**



#### **ACF of Residuals**



### p values for Ljung-Box statistic



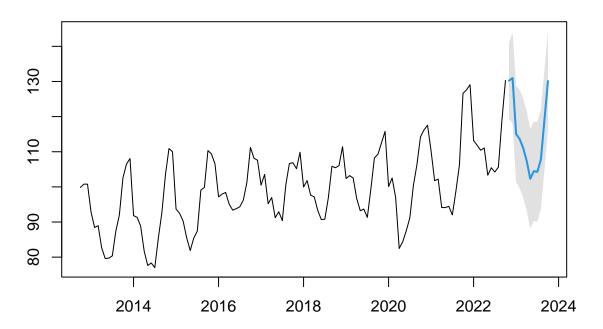
#### accuracy(auto\_fit)

## Training set -0.004444951 3.602064 2.583457 -0.1100037 2.571757 0.5881103 ## Training set -0.06809078

# ME RMSE MAE MPE MAPE MASE ACF1
#Training set -0.004444951 3.602064 2.583457 -0.1100037 2.571757 0.5881103 -0.06809078

ARIMAF12 <- plot(forecast(auto\_fit,h=12,level=c(99.5)))

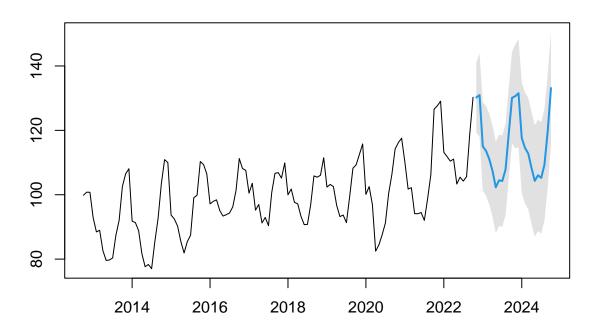
# Forecasts from ARIMA(1,0,0)(2,1,0)[12] with drift



#### ARIMAF12

```
## $mean
##
                                Mar
                                         Apr
                                                   May
                                                            Jun
                                                                      Jul
                                                                               Aug
## 2023 115.0259 113.6240 111.0655 107.3725 102.3049 104.4700 104.2670 107.8069
##
                                Nov
                                         Dec
                           130.2152 130.9781
  2023 119.0309 130.1239
##
##
## $lower
##
                                                                             Jul
              Jan
                         Feb
                                   Mar
                                              Apr
                                                        May
                                                                  Jun
## 2022
                   99.64659
## 2023 101.35264
                              96.96380
                                        93.21964
                                                  88.13085 90.28708 90.08048
##
              Aug
                         Sep
                                   Oct
                                              Nov
## 2022
                                       119.36102 118.06743
## 2023 93.61892 104.84220 115.93496
##
## $upper
##
             Jan
                      Feb
                                Mar
                                         Apr
                                                   May
                                                            Jun
                                                                     Jul
                                                                               Aug
## 2022
## 2023 128.6992 127.6015 125.1672 121.5254 116.4790 118.6528 118.4535 121.9950
             Sep
                                Nov
                           141.0694 143.8888
## 2022
## 2023 133.2195 144.3128
```

# Forecasts from ARIMA(1,0,0)(2,1,0)[12] with drift



#### ARIMAF24

```
## $mean
##
             Jan
                      Feb
                                Mar
                                                            Jun
                                                                     Jul
                                         Apr
                                                  May
                                                                               Aug
## 2022
## 2023 115.0259 113.6240 111.0655 107.3725 102.3049 104.4700 104.2670 107.8069
  2024 117.6141 114.5620 112.7877 108.3628 104.2936 106.0342 105.2377 109.3693
##
             Sep
                      Oct
                                Nov
                           130.2152 130.9781
## 2022
## 2023 119.0309 130.1239 130.6058 131.5482
## 2024 119.8675 133.1484
##
## $lower
##
              Jan
                         Feb
                                   Mar
                                             Apr
                                                        May
                                                                  Jun
                                                                             Jul
## 2022
## 2023 101.35264
                   99.64659
                              96.96380
                                        93.21964
                                                  88.13085
                                                             90.28708
                                                                       90.08048
## 2024 100.49160
                   97.31920
                              95.49535
                                        91.04988
                                                  86.97211
                                                             88.70925 87.91127
              Aug
##
                         Sep
                                   Oct
                                             Nov
                                                        Dec
## 2022
                                       119.36102 118.06743
## 2023 93.61892 104.84220 115.93496 114.50585 114.71910
## 2024 92.04224 102.54024 115.82103
##
## $upper
```

```
##
                 Feb
                               Mar
                                        Apr
                                                 May
                                                                    Jul
                                                                             Aug
## 2022
## 2023 128.6992 127.6015 125.1672 121.5254 116.4790 118.6528 118.4535 121.9950
## 2024 134.7366 131.8047 130.0801 125.6757 121.6150 123.3592 122.5642 126.6963
             Sep
                      Oct
                               Nov
                                        Dec
## 2022
                          141.0694 143.8888
## 2023 133.2195 144.3128 146.7058 148.3774
## 2024 137.1948 150.4758
auto_fit$mse
## NULL
#[1] NULL
#RSME is 3.602064 on average forecast values were 3.602064 away from the actual
#MPE is 11% percenatge of error is around 11%
#accuracy summary
accuracy(ets_forecast)
                                RMSE
                                          MAE
                                                     MPE
                                                             MAPE
                                                                       MASE
##
                         ME
## Training set -0.03996037 3.310275 2.498396 -0.1249896 2.482994 0.5687464
## Training set 0.07788466
accuracy(naive forecast)
                              RMSE
                                                   MPE
##
                       ME
                                        MAE
                                                           MAPE
                                                                    MASE
                                                                              ACF1
## Training set 0.2536275 6.305638 4.625101 0.02809525 4.635846 1.05288 0.2207691
accuracy(rwf_forecast)
                       ME
                              RMSE
                                        MAE
                                                   MPE
                                                           MAPE
                                                                    MASE
                                                                              ACF1
##
## Training set 0.2536275 6.305638 4.625101 0.02809525 4.635846 1.05288 0.2207691
accuracy(snaive_forecast)
##
                      ME
                             RMSE
                                       MAE
                                                MPE
                                                        MAPE MASE
                                                                        ACF1
## Training set 2.731406 5.829941 4.392811 2.525765 4.342721
accuracy(SSE_Simple)
                        ME
                              RMSE
                                        MAE
                                                   MPE
                                                           MAPE
                                                                    MASE
## Training set 0.04457017 6.29552 4.615979 -0.1819999 4.631386 1.050803 0.2185404
```

```
accuracy(auto_fit)
##
                          ME
                                 RMSE
                                           MAE
                                                      MPE
                                                               MAPE
                                                                         MASE
## Training set -0.004444951 3.602064 2.583457 -0.1100037 2.571757 0.5881103
## Training set -0.06809078
#I would choose ets_forecast as it has the lowest MAPE. I chose MAPE because the units are in Percent,
#when observations are large numbers and also It can be used to compare same or different techniques as
#Best MAPE Forecast
accuracy(ets_forecast)
                                RMSE
                                                     MPE
                                                             MAPE
                                                                        MASE
##
                         ME
                                          MAE
## Training set -0.03996037 3.310275 2.498396 -0.1249896 2.482994 0.5687464
## Training set 0.07788466
#worst MAPE Forecast
accuracy(naive_forecast)
                       ME
                              RMSE
                                        MAE
                                                   MPE
                                                           MAPE
                                                                    MASE
                                                                              ACF1
## Training set 0.2536275 6.305638 4.625101 0.02809525 4.635846 1.05288 0.2207691
```

#conclusion

#based on my analysis the value of time series will be cyclical as it has been so far in 1 and 2 both y