

① Insertion sort on an already sorted array does best case work. It performs one comparison per element & no swap. $\rightarrow \Theta(n)$ comparisons & (0) swaps.

Shell sort (with shell's original sequence: gaps = $\frac{n}{2}, \frac{n}{4}, \dots$) runs a sequence of gapped insertion-sort passes, for an already sorted array each gapped pass finds that each gapped subarray is already sorted, so the gapped insertion operation do minimal work.

- Shell's early large gaps move elements distances in one pass; that reduces the no. of adjacent swaps later so if the array is almost sorted except for a few elements far from their final position shell moves them quickly, making later passes cheap.

② If the keys are multiples of 10 i.e., (10, 20, 30, ...) then $h(k) = k \bmod 10 = 0$ for all those keys.

This results in clustering, where all these keys are stored in the same bucket of the hash table. Instead of being distributed evenly, the keys are concentrated in a single location, leading to large no. of collision.

Due to this extreme clustering, finding a specific key requires searching through all the keys that have been clustered in that single bucket.

The access time to this becomes $\Theta(n)$ where $n = \text{no. of input keys}$.

3] \rightarrow #include <stdio.h>
 #include <stdlib.h>

```
Struct PolyNode {
    int coeff;
    int exp;
    Struct PolyNode * next;
}
Struct PolyNode * create (int c, int e) {
    Struct PolyNode * node = (Struct PolyNode *) malloc (sizeof
        Struct PolyNode));
    Node->coeff = c;
    Node->exp = e;
    Node->next = NULL;
    return node;
}
```

// Assume 2 polynomials are sorted in decreasing
 // exponent

```
Struct PolyNode * add Poly. (Struct PolyNode * p1,
    Struct PolyNode * p2) {
    Struct PolyNode dummy;
    Struct PolyNode * tail = & dummy;
    dummy.next = NULL;
    while (p1 != NULL && p2 != NULL) {
        if (p2->exp == p1->exp) {
```

```
            p1->coeff = p1->coeff + p2->coeff;
            tail = tail->next = p1;
            p1 = p1->next;
        } else if (p2->exp < p1->exp) {
```

```
int s = p1 -> coeff + p2 -> coeff;
```

```
if (s != 0) {
```

```
-tail -> next = create (s, p1 -> exp);
```

```
tail = tail -> next;
```

```
}
```

```
p1 = p1 -> next;
```

```
p2 = p2 -> next;
```

```
} else if (p1 -> exp > p2 -> exp) {
```

```
tail -> next = create (p1 -> coeff, p1 -> exp);
```

```
tail = tail -> next;
```

```
p1 = p1 -> next;
```

```
} else {
```

```
tail -> next = create (p2 -> coeff, p2 -> exp);
```

```
tail = tail -> next;
```

```
p2 = p2 -> next;
```

```
}}
```

```
while (p2 != NULL) {
```

```
tail -> next = create (p2 -> coeff, p2 -> exp);
```

```
tail = tail -> next;
```

```
p2 = p2 -> next;
```

```
}
```

```
return dummy.next;
```

```
}
```

4]- The diff. b/w Singly, Doubly & Circular linked list.

5] Property

Singly

Structure

node → next
or only

Doubly

prev & next

Circular

tail is connected
to head.

Insertion at
head

$O(1)$

$O(1)$

$O(1)$ if
head is known.

Insertion at
tail

$O(n)$

$O(1)$ if tail is
known otherwise
 $O(n)$

$O(1)$

Deletion at
head

$O(1)$

$O(1)$

$O(1)$

6] Traversal

Only forward
Traversal

forward &
backward

It iterates
continuously
if condition not
given.

Memory
overhead

1 pointer &
Data

2 pointers
& Data

Depend if singly or
Double.

Preferred
when

Low memory,
only forward
traversal, simple
stacks

frequent
deletion &
Bidirectional
traversal

Round Robin, Scheduling
Buffering.

Example
use cases

Implementing
adjacency list
in graph, stacks

Implement
LRU cache,
editor undo
Redo, deque

Implement
Circular queue
Circular linked

5] Reverse a singly linked list

Pseudo-code

prev = NULL

current = head

while (current != NULL) {

 next = current → next

 current → next ← prev

 prev = current

 current = next

}

head = prev.

C-Code

```
Struct Node * reverseList (Struct Node **head) {
    Struct Node * prev = NULL, * cur = * head;
    Struct Node * next = NULL;
    While (cur != NULL) {
        next = cur → next;
        cur → next = prev;
        prev = cur;
        cur = next;
    }
    return prev;
}
```

6] Quadratic Probing formula:

$h(k,i) = (h'(k) + i^2) \bmod m$ where $h'(k)$ is the initial hash & $i \geq 0$ is the probe number.

for prime-table size quadratic probing can guarantee to probe at least half of the slots before repeating.
 If the table is less than or equal to half full (load factor ≤ 0.5) quadratic probing guarantees that an empty slot will be found, as an empty slot is guaranteed to be visited within first $\frac{m}{2}$ probes.

Ex- If size $m = 11$.

$h(k,i) = (h(k) + i^2) \bmod 11$ the probe sequence starting at $h'(k) = 0$ would be $0, 1, 4, 9, 5, 3, 3, \dots$ (after 11th probe it starts repeating). This sequence only visits $0, 1, 3, 4, 5, 9$ which are only 6 not all 11.

$$7) m - 3 = 11 - 3 = 8 \quad (\text{Assuming base value} = 0).$$

$$\text{hash fn} \Rightarrow (2 + 3 \times k) \bmod 8$$

$$\text{for } 4_3 = (2 + 3(4_3)) \bmod 8 = 3$$

$$\text{for } 165 = (2 + 3(165)) \bmod 8 = 4$$

$$\text{for } 62 = (2 + 3(62)) \bmod 8 = 4$$

$$\text{for } 123 = (2 + 3(123)) \bmod 8 = 3.$$

By using linear probing (123) will go no 5 position.

for 142 value would be $(2+3(142)) \bmod 8 = 4$
using Linear Probing

142 will be inserted at 6 position.

8] $h(k) = ((9k^2) + 3k + 17) \bmod 23 \bmod 11$

Collision:

$$h_i(k) = (h(k) + i^2) \bmod 11.$$

a] index
 $h(21) = 1$
 $h(82) = 3$
 $h(93) = 9$
 $h(87) = 10$
 $h(54) = 8$
 $h(63) = 2$
 $h(72) = 4$

b) $h(99) = 8$
 $(8+1) \bmod 11 = 9$
 $(8+4) \bmod 11 = 1$
 $(8+9) \bmod 11 = 6$
99 will be placed at 6th position.

g] $h_1(k) = (5k^2 + 3k + 7) \bmod 17$

$$h_2(k) = 1 + (13k + 11) \bmod 16$$

after collision:

$$(h_1(k) + i h_2(k)) \bmod 17$$

$$h_1(25) = 11 \rightarrow \text{placed at } \underline{11}$$

$$h_2(25) = 7$$

$$h_1(47) = 7 \rightarrow \text{placed at } \underline{7}$$

$$h_2(47) = 9$$

$$h_1(47) = 7 \rightarrow \text{placed at } \underline{7}$$

$$h_2(47) = 9$$

$$h_1(89) = 14 \rightarrow \text{placed at } \underline{14}$$

$$h_2(89) = 7.$$

$$h_1(106) = 14, h_2(106) = 10$$

occupied

$$i=1 \Rightarrow (14+10 \equiv 124) \bmod 17$$

$\equiv 7$
occupied

$$i=2 \Rightarrow (14+20) \bmod 17 = 0$$

placed at 0

$$h_1(132) = 7 \rightarrow \text{occupied}$$

$$h_2(132) = 8$$

$$i=1 : (7+8) \bmod 17 = \underline{\underline{15}}$$

placed at 15

$$h_1(205) = 15 \text{ index } 15 \text{ occupied}$$

$$h_2(205) = 3$$

$$i=1 \Rightarrow (15+3) \bmod 17 = \underline{\underline{11}}$$

$$h_1(310) = 19 \rightarrow \text{occupied}$$

$$h_2(310) = 14$$

$$i=1 \Rightarrow (14+14) \bmod 17 = \underline{\underline{11}} \rightarrow \text{occupied}$$

$$i=2 \Rightarrow (11+28) \bmod 17 = \underline{\underline{8}}$$

0	106
1	205
2	
3	
4	
5	
6	
7	47
8	310
9	
10	
11	25
12	
13	
14	89
15	132
16	

b] Expected no. of probes of unsuccessful search

$$\Rightarrow \frac{1}{1-\alpha} = \frac{1}{1-7/17} \Rightarrow \frac{17}{10} = \underline{\underline{1.7}}$$

$$\left\{ \text{load factor } \alpha = \frac{7}{17} \right\}$$

10] #include <stdio.h>

#include <stdlib.h>

```
Struct node {  
    int data;  
    Struct node *next; };
```

```
Struct node * Create (int data) {  
    struct node * new = (struct node *) malloc (sizeof  
        (struct node));  
    new->data = data;  
    new->next = NULL;  
    return new; }
```

```
Void insert at begin (struct node ** head, int data) {  
    struct node * new = Create (data);  
    if (new == NULL) { printf ("Error in malloc");  
        return; }  
    if (*head == NULL) {  
        *head = new;  
        return; }  
    new->next = *head;  
    *head = new; }
```

```

Void print ( Struct node * head ) {
    Struct node * temp = head;
    While ( temp != NULL ) {
        printf ( " .d ", temp->data );
        temp = temp->next;
    }
}

int main () {
    Struct node * head = NULL;
    insertatbegin ( &head, 12 );
    insertatbegin ( &head, 13 );
    print ( head );
}

```

- b) If malloc fails on the 4th Node the first three allocation succeeded remain valid. Those 3 nodes continue to exist.

You can still add nodes to the list as the 4th node is not the head.

C-Code

11]

```
#include < stdio.h >
#include < stdlib.h >

struct node {
    int data ;
    struct node * next;
    struct node * prev;
}

struct node * create (int data) {
    struct node * new = (struct node *) malloc (sizeof (struct node));
    new -> data = data;
    new -> next = NULL;
    new -> prev = NULL;
    return new;
}

void insertatend (struct node ** head , int data) {
    struct node * new = create (data);
    if (*head == NULL) {
        *head = new;
        return;
    }
    struct node * temp = *head;
    while (temp -> next != NULL) temp = temp -> next;
    temp -> next = new;
    new -> prev = temp;
}

void print (struct node * head) {
    struct node * temp = head;
    while (temp) {
        printf ("%d", temp -> data);
        temp = temp -> next;
    }
}
```

```
struct Node * Merge ( struct Node * first , struct Node * second )
```

```
{ if (!first) return second;
```

```
if (!second) return first;
```

```
struct node * head = NULL;
```

```
struct node * tail = NULL;
```

```
if (first->data <= second->data) {
```

```
    head = tail = first;
```

```
    first = first->next; }
```

```
else { head = tail = second;
```

```
    second = second->next; }
```

```
while (first && second) {
```

```
    if (first->data <= second->data) {
```

```
        tail->next = first;
```

```
        first->prev = tail;
```

```
        tail = first;
```

```
        first = first->next; }
```

```
    else { tail->next = second;
```

```
        second->prev = tail;
```

```
        tail = second;
```

```
        second = second->next; }
```

```
}
```

```
    if (first) { tail->next = first;
```

```
        first->prev = tail;
```

```
} else if (second) { tail->next = second;
```

```
        second->prev = tail; }
```

```
} return head;
```

```

int main() {
    struct Node *list1 = NULL;
    struct Node *list2 = NULL;
    insertatend (&list1, 1);
    insertatend (&list1, 4);
    insertatend (&list1, 7);
    insertatend (&list2, 2);
    insertatend (&list2, 3);
    insertatend (&list2, 5);
    struct Node *merged = merge (list1, list2);
    print (merged);
}

```

13] a linked list is more suitable when size is highly dynamic & unpredictable as it supports dynamic growth without requiring large contiguous block of memory (using malloc).

Arrays are of fixed sizes. Dynamic resizing is difficult in array.

b) Random accessing is easier in array & it take $O(1)$. while in linked list it takes $O(n)$ where n is the no. of inputs.

Random Insertions & deletion is much easier in linked list
& takes $O(1)$ with just update of pointers.

While in Arrays Insertion & deletion takes shifting of
elements with $O(n)$ operations.

Therefore linked list is a better option for Data
Buffer System.