

## Assignment - 03.

1) Recursion is a better technique for solving the Tower of Hanoi problem because the problem itself is defined recursively. Each step involves solving a smaller instance of the same problem, which makes the recursive approach simple, natural and easy to understand. This, iterative method is more complex and harder to implement, while recursion directly represents the logical structure of the solutions.

Hence, recursion is preferred over iteration for the Tower of Hanoi problem.

2) Datatype using Stack:

```
#include <iostream>
#include <stack>
using namespace std;
```

```
int main()
{
    stack<char> s; // LIFO principle
    string input = "ABCD EF";
    for (char ch : input)
        s.push(ch);
    cout << "Reversed Order: ";
    while (!s.empty())
        cout << s.top();
    return 0;
}
```

Output  $\rightarrow$  Reversed order = FEDCBA

Ques-3

- Application of Stack in:
  - Expression evaluation and conversion (e.g. infix to postfix)
  - Function call management, using call stack in recursion

Ques-4

- Application of Queue in:
  - Job scheduling or Process management in operation system
  - Data transfer in networking (e.g. buffering message queues)

Representation of Stack using Linked List

- All stacks can be represented using a singly linked list where -
- Each node contains data & the head of the next node.
- The top of the stack points to the head of the linked list.
- Push operation - Insert a new node at the begining (head) of the list.
- Pop operation - Delete the node from the begining (head).

Ques-4

Given expression:  $\rightarrow 1142 \times 13 + 1567$

$$1142 = 7$$

$$+ 15 = 6$$

$$\times 36 = 18$$

$$1186 = 3$$

$$+ 73 = 10$$

$$- 107 = 3$$

$$\text{Ans} = 3 \text{ is answer}$$

5) To delete an element from the middle of a stack when only push and pop operations are allowed we use an auxiliary stack first, we pop elements from the original stack and push them into the auxiliary stack until we reach the middle element. Then we pop all elements from the auxiliary stack and push them back into the original stack to restore the order.

Algorithm -

Find middle position =  $\text{size}/2$

Pop & push first half elements into auxiliary stack

Pop off middle element

Push back all elements from auxiliary stack to original stack

Time complexity =  $O(n)$  where  $n$  is size

Space complexity  $= O(n)$  in worst case

6)

Given Infix expression -

$A \wedge B + C(D+E)/F - G$

Step 1 Insert all the missing operators for clarity -

$A \wedge B + C * (D+E) / F - G$

Step 2 Apply stack method (operator precedence :  $\wedge > +, 1 > +, -$ )

	Symbol	Stack	Output
1	A	AB	AB
2	B	AB^	AB^
3	C	AB^C	AB^C
4	D	AB^CD	AB^CD
5	E	AB^CD^	AB^CD^
6	F	AB^CD^E	AB^CD^E
7	G	AB^CD^EF	AB^CD^EF

## 7 Head Recursion

In head recursion, the function calls itself before performing any operation. All statement are executed after the recursive call returns.

## Tail Recursion

In tail recursion, the function calls itself after performing all operations.

No work is left after the recursive call.

Program for fibonacci series

\* includes <iostream>

using namespace std;

int fibonacci (int n) {

if (n<=1) {

return n;

}, return fibonacci(n-1) + fibonacci(n-2);

}

int main () {

int n;

cout << "Enter number of terms" ;

cin >> n;

Count << "Fibonacci series" ;

for (int i=0; i<n; i++)

cout << fibonacci(i) ;

} // (1) Create a queue

}

Output - 0112358

### 8) Circular Queue

A circular queue is a type of queue in which the last position is interconnected back to the first position to form a circle.

It helps in efficient use of memory because unlike normal queue, the empty spaces left after deletions can be reused.

In a normal queue, once the rear reaches the end, no new elements can be inserted even if there is space at the beginning.

But in a circular queue the rear can move back to the front and use the

free space again. Hence, it utilizes memory better than a normal queue.

### Algorithm for Circular Queue

#### Insertion -

- ① If  $(front + 1) == 0$  &  $(rear == size - 1)$  or  $(front == rear)$   
Queue is full
- ② Else if  $(front == -1)$   
 $front = 0$  and  $rear = 0$
- ③ Else if  $(rear == size - 1)$   
 $rear = 0$  and  $front = size - 1$
- ④ Else  $(front + 1) == rear)$  (i)  
 $rear = rear + 1$  and (ii)
- ⑤ Insert the element at queue[rear]

#### Deletion

- ① If  $(front == -1)$   
Queue is empty
- ② If  $[front] \neq \text{int} \neq \text{int}$
- ③ If  $(front == rear)$  (i) both deleted  
 $front = -1$  and  $rear = -1$   
 $rear = front + 1$  and (ii) add one to front
- ④ Else if  $(front == size - 1)$  (i) both deleted  
 $front = 0$  and  $rear = 0$ , after that  
 $front = front + 1$  and (ii) add one to front
- ⑤ Else  $value = \text{queue}[front]$ , swap front with  $front + 1$
- ⑥ Display deleted item

9)

Rewrite  $(A+B)(D+E)+F-G$

Parenthesis to show order

$$((A+B)*(D+E))+F-G$$

Convert sub-expressions to prefix

$$D+E \rightarrow +DE$$

$$B*(D+E) \rightarrow *BD+E$$

$$A+*(B*(D+E)) \rightarrow +A*B+DE$$

$$(+A+B*(D+E)+F-G) \rightarrow +A+B+DE+$$

$$\text{Final} - (+A*B+DE) + A*B+DEF-G$$

4)

Given expression :  $- * X Y * W Z - M N$

$$-M N \rightarrow (M-N)$$

$$*WZ \rightarrow (W*Z)$$

$$-*XY(*WZ-MN) \rightarrow ((X*Y).-.(W*Z))$$

$$(- * X Y * W Z - M N) \rightarrow ((X*Y).-.(W*Z)) / (M-N)$$

12)

A number is said to be a Palindrome if it remains the same when its digits are reversed. For eg. 121, 1331, 4554, are palindromes.

Using a stack we can check this by pushing digits on and then popping them in reverse order.

Algorithm (using stack)

Stack (pointer)  $\rightarrow$  Prefix notation  $\rightarrow$  Postfix

Read the number  $n$  from user

Copy  $n$  into a temporary variable,  $num$   
 Initialize an empty stack  
 While  $num > 0$  :  
     Push  $num \mod 10$  onto the stack  
      $num = num / 10$   
     Set  $rev = 0$  and  $pos = 1$   
 while stack is not empty  
     Pop top element (and calculate it + to  $rev = rev * 10 + pos * it$ )  
      $pos++$   
     If  $rev == n$   
         Print "Number is Palindrome"  
     else  
         Print "Number is not Palindrome"

Due-13

Merge Sort is based on divide-and-conquer technique. In this technique, a problem is divided into smaller sub-problems. Each sub-problem is solved individually and then result are combined to get the final solution.

Algorithm is as follows:

If  $low < high$  then,  
      $mid := (low + high) / 2$ .  
     Merge-Sort (arr, low, mid).  
     Merge-Sort (arr, mid, high).  
     Merge-Sort (arr, low, mid, high).  
 end if

Time complexity  $\rightarrow O(n \log n)$   
 Space complexity  $\rightarrow O(n)$

14)

Array  $\rightarrow [11, 2, 45, 33, 15, 21, 10, 5]$

### Algorithm

(Merge Sort (arr, low, high))

If  $low < high$  then

$$\text{mid} = (\text{low} + \text{high}) / 2$$

Merge . sort ( arr, low, mid )

Merge . sort ( arr, mid + 1, high )

Merge ( arr, low, mid, high )

end if

Merge ( arr, low, mid, high )

Copy left half and right half into two temporary array

Compare elements of both halves

Copy smaller element into main array

Repeat until you get sorted array

### Step by Step Sorting

Divide :  $[11, 2, 45, 33, 15, 21, 10, 5]$

$\rightarrow [11, 2, 45, 33] \& [15, 21, 10, 5]$

### further divide

$[11, 2], [45, 33], [15, 21], [10, 5]$

Sort each :

$[11, 2] \rightarrow [2, 11]$

$[45, 33] \rightarrow [33, 45]$

$[15, 21] \rightarrow [15, 21]$

$[10, 5] \rightarrow [5, 10]$

### Merge

$[2, 11, 33, 45] \& [3, 10, 15, 21]$

$[2, 3, 5, 10, 11, 15, 21, 33, 45]$