

~~18C~~ WITH GRAPH PAPER

केन्द्रीय माध्यमिक शिक्षा बोर्ड, दिल्ली  
सैकंडरी स्कूल परीक्षा (कक्षा दसवीं)  
परीक्षार्थी प्रवेश-पत्र के अनुसार भरें

विषय Subject : Mathematics Basic

विषय कोड Subject Code : 241

परीक्षा का दिन एवं तिथि

Day & Date of the Examination : Thursday, 12/03/2020

उत्तर देने का माध्यम

Medium of answering the paper : English

प्रश्न पत्र के ऊपर लिखे

कोड को दर्शाएँ :

Write code No. as written on  
the top of the question paper :

Code Number  
430/4/1

Set Number  
 ① ② ③ ④

अतिरिक्त उत्तर-पुस्तिका (ओ) की संख्या

No. of supplementary answer-book(s) used

Nil

बैचमार्क विकलांग व्यक्ति : हाँ / नहीं

Person with Benchmark Disabilities : Yes / No

No

विकलांगता का कोड (प्रवेश पत्र के अनुसार)

Code of Disability (As per the admit card)

No

कथा लेखन - लिपिक उपलब्ध करवाया गया : हाँ / नहीं

Whether writer provided : Yes / No

No

यदि दृष्टिहीन हैं तो उपयोग में लाए गये

सोफ्टवेयर का नाम :

If Visually challenged, name of software used :

No

\*एक खाने में एक अक्षर लिखें। नाम के प्रथम भाग के बीच एक खाना रिक्त छोड़ दें। यदि परीक्षार्थी का नाम 24 अक्षरों से अधिक है, तो केवल नाम के प्रथम 24 अक्षर ही लिखें।

Each letter be written in one box and one box be left blank between each part of the name. In case Candidate's Name exceeds 24 letters, write first 24 letters.

वार्तालय उपयोग के लिए

Space for office use

16

Rough

$$\begin{array}{r} 2 \\ \times 156,78 \\ \hline 2 \\ 2 \\ \hline 39 \end{array}$$

$$\sqrt{(5+1)^2 + (-2+3)^2}$$

$$\sqrt{36+1}$$

$$\sqrt{37}$$

$$\begin{array}{r} 2 \\ \times 186,78 \\ \hline 2 \\ 2 \\ \hline 39,39 \end{array}$$

$$\sqrt{b^2 - 4ac} = \sqrt{13,13}$$

$$\begin{array}{r} \sqrt{16-24} \\ \hline \sqrt{39} \\ \times 4 \\ \hline 13,13 \end{array}$$

$$D = b^2 - 4ac = 156$$

$$= 16-24$$

$$= -8$$

$$\sqrt{(5+1)^2 + (-2+3)^2}$$

$$\begin{array}{r} 1 - \text{odd} \\ 2 \\ 3 - \text{odd} \\ 4 \\ 5 - \text{odd} \\ 6 \end{array}$$

$$36+1$$

$$= 37$$

$$5 - \text{odd}$$

$$16-24$$

$$-8$$

SECTION-AAns. 1.

$$(A) 156$$

Ans. 2.

$$(D) 16 : 81$$

Ans. 3.

$$(B) \sqrt{37} \text{ units}$$

Ans. 4. (Choice-I)

$$(A) -8$$

Ans. 5.

$$(C) 1$$

Ans. 6.

$$(B) \frac{1}{2}$$

Ans

$$\frac{3}{2} = \frac{2}{6}$$

$$k = 2.$$

$$\begin{aligned} a &= 47 \\ d &= -3 \end{aligned}$$

$$\begin{aligned} a_2 &= a + d \\ &= 47 - 3 \\ &= 44 \\ m_1 &= 1, m_2 \\ -3 &-3 \\ \hline 2 & \end{aligned}$$

$$\begin{aligned} -3 &-3, 3- \\ 2 & \\ \hline -6 &, 0 \\ \hline 2 & \end{aligned}$$

$$\begin{aligned} \frac{-8}{2} & \\ -3 &-3, 1-3 \\ \hline -6 &2-3, 0- \end{aligned}$$

A = 1011011011

Ans. 7.  
✓ (D) -2

Ans. 8.  
✓ (D) 45°

Ans. 9.  
✓ (C) 44

Ans. 10.  
✓ (C) 4πr² (A) 3πr²

Ans. 11.  
 $D = 0$  (discriminant is zero)  
or  $b^2 - 4ac = 0$  {Here  $a = 1$ }  
 $b^2 = 4c$

Ans. 12. (-3, 0)

Ans. 13°  
equal.

$$l = m + 1 = 10$$

$$d = m + 1^2 = 10$$

$$d = \frac{1}{2}g \quad g = 20$$

58,50

55

6  
715  
6  
25  
23  
16

Ans. 14°

58

Ans. 15°

$$\alpha + \beta = -\frac{b}{a} = \frac{0}{1} = 0$$

Ans. 16°

$$a_{26} = ? \quad n = 26, a = 7, d = a_2 - a_1 = 4 - 7 = -3$$

$$a_n = a + (n-1)d$$

$$a_{26} = 7 + (26-1)(-3)$$

$$\frac{a}{26} = 7 + \frac{a}{26} =$$

$$a_{26} = 7 - 75$$

$$\boxed{a_{26} = -68}$$

$$\checkmark m_1 = 1, m_2 = 2$$

$$x_1 = 2, x_2 = 5$$

$$y_1 = 3, y_2 = -6$$

Let the point be P and its coordinates be  $(x, y)$

$$(x, y) = \left( \frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2} \right)$$

$$(x, y) = \left( \frac{1(5) + 2(2)}{1+2}, \frac{1(-6) + 2(3)}{1+2} \right)$$

$$(x, y) = \left( \frac{5+4}{3}, \frac{-6+6}{3} \right)$$

$$(x, y) = \left( \frac{9}{3}, \frac{0}{3} \right)$$

$$(x, y) = (3, 0)$$

Since the point is on x-axis, therefore the point on y-axis will be '0'.

Ans. 18° (Choice - II)

$$\begin{aligned}
 & \sin 42^\circ - \cos 48^\circ \quad \checkmark \\
 &= \sin 42^\circ - \sin(90^\circ - 48^\circ) \quad \{ \because \cos \theta = \sin(90^\circ - \theta) \} \\
 &= \sin 42^\circ - \sin 42^\circ \\
 &= [0]
 \end{aligned}$$

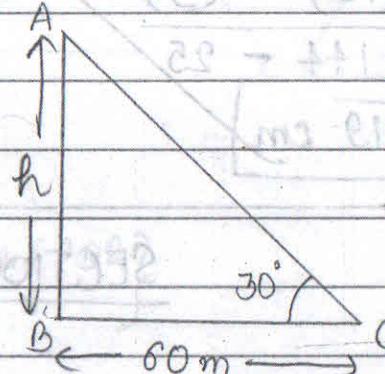
Ans. 19°

Let the height of the tower be  $h$ -m

In  $\triangle ABC$

$\angle ABC = 90^\circ$  (Tower stands vertical on the ground)

$$\therefore \tan 30^\circ = \frac{AB}{BC}$$



$$\frac{1}{\sqrt{3}} = \frac{h}{60}$$

$$h = \frac{60}{\sqrt{3}} \Rightarrow h = \frac{20\sqrt{3}}{\sqrt{3}} \Rightarrow h = 20\sqrt{3} \text{ m}$$

Ques. 20.

In  $\triangle OQP$

$\angle OQP = 90^\circ$  (radius is  $\perp$  to tangent)

By Pythagoras theorem,

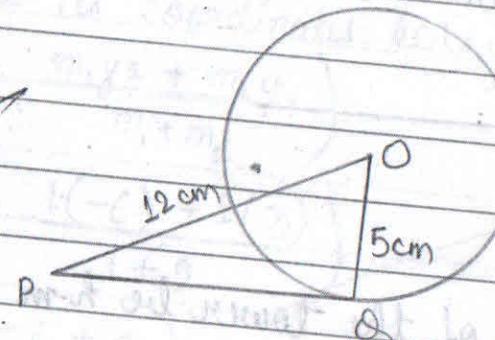
$$OP^2 = OQ^2 + PQ^2$$

$$PQ^2 = OP^2 - OQ^2$$

$$PQ^2 = (12)^2 - (5)^2$$

$$PQ = \sqrt{144 - 25}$$

$$PQ = \sqrt{119} \text{ cm}$$



(II-minut)

प्रत्यय  
25  
119

119  
 $\frac{13}{17}$

119

114  
82  
88  
32

8  
14  
632

54  
08  
19

112

896  
22  
196

120  
32  
56

04  
98  
8

## SECTION - B

Ques. 21.

Cylinder

$$h = 32 \text{ cm}$$

$$\pi = \frac{22}{7}$$

$$r = 14 \text{ cm}$$

Volume of sand = Vol. of cylinder

$$= \pi r^2 h$$

P.T.O.

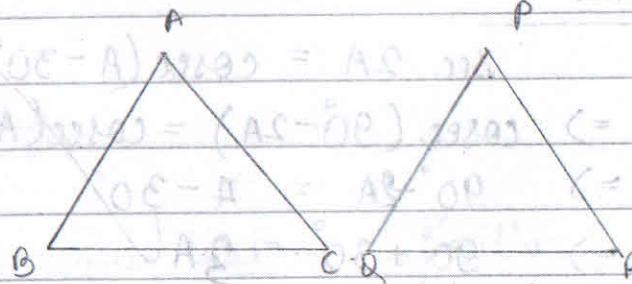
$$\begin{aligned}
 &= \left( 22 \times \frac{1}{4} \times 14 \times 32 \right) \text{ cm}^3 \\
 &= 19712 \text{ cm}^3
 \end{aligned}$$

Ans. 22° (Choice II)

Given

$$\triangle ABC \sim \triangle PQR$$

$$\text{ar}(ABC) = \text{ar}(PQR)$$



To prove:  $\triangle ABC \cong \triangle PQR$

Proof:

$$\frac{\text{ar}(ABC)}{\text{ar}(PQR)} = 1 \quad \left\{ \therefore \text{ar}(ABC) = \text{ar}(PQR) \right\}$$

$$\frac{\text{ar}(ABC)}{\text{ar}(PQR)} = \left( \frac{AB}{PQ} \right)^2$$

$\left. \begin{array}{l} \text{S. : the ratio of areas of two similar } \\ \Delta \text{ is equal to the } \frac{\text{square of}}{\text{ratio of their sides}} \end{array} \right\}$

$$\frac{AB}{PQ} = 1^2$$

$$AB = PQ \quad \text{--- 1.}$$

$$\text{Similarly } \frac{BC}{QR} = 1^2 \Rightarrow BC = QR \quad \text{--- 2.}, \quad \frac{AC}{PR} = 1^2 \Rightarrow AC = PR \quad \text{--- 3.}$$

From (1), (2) and (3)  
 $\triangle ABC \cong \triangle PQR$  (SSS congruency)  
 $\therefore$  Proved

Ans. 23.

$$\begin{aligned}
 \sec 2A &= \operatorname{cosec}(A - 30^\circ) \\
 \Rightarrow \operatorname{cosec}(90^\circ - 2A) &= \operatorname{cosec}(A - 30^\circ) \quad \left\{ \because \sec \theta = \operatorname{cosec}(90^\circ - \theta) \right\} \\
 \Rightarrow 90^\circ - 2A &= A - 30^\circ \\
 \Rightarrow 90^\circ + 30^\circ &= 3A \\
 \Rightarrow 120^\circ &= 3A \\
 \Rightarrow A = 60^\circ &\Rightarrow A = \frac{120^\circ}{3} = 40^\circ
 \end{aligned}$$

Ans. 24.

Let  $a$  be any positive integer. Let it be divided by 2 giving ' $q$ ' as quotient, ' $r$ ' as remainder.

$$a = 2q + r$$

According to Euclid's division algorithm.

$$0 \leq r < b \Rightarrow 0 \leq r < 2$$

$r$  can either be 0 or 1

When -  $r = 0$

$$a = 2q + 0 \Rightarrow a = 2q \text{ (Here } a \text{ is even)} - \textcircled{1}$$

When  $r = 1$

$$a = 2q + 1 \text{ (Here } a \text{ is odd)} - \textcircled{2}$$

Thus, from  $\textcircled{1}$  and  $\textcircled{2}$  it can be said that every even positive integer is of the form  $2q$  and every positive odd integer is of the form  $2q+1$ .

Ans. 250 (Choice - II)

$$d = 5, n = 10, S_{10} = 75$$

$$a = ?$$

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

1.	I.I
011	31-2
010	35-31
005	25-23
005	24-25

$$S_{10} = \frac{10}{2} [2a + (10-1)5]$$

$$S_{10} = \frac{10}{2} [2a + 45]$$

$$75 \times 2 = 20a + 450$$

$$150 - 450 = 20a$$

$$-300 = 20a$$

$$a = -\frac{300}{20}$$

$$a = -15$$

Ans. 26.

(II - viiiA)

C.I.	f
5-15	60
15-25	110
25-35	210 - f <sub>0</sub>
35-45	230 - f <sub>1</sub>

Rough

45 - 55	150	<del>f<sub>2</sub></del>
55 - 65	50	

$$f_1 = 230, f_2 = 150, f_0 = 210$$

~~(i, ii) = A for working (i)~~

$$\begin{aligned} \text{Mode} &= l + \left[ \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right] \times h \quad \text{for working (i)} \\ &= 35 + \left[ \frac{230 - 210}{460 - 210 - 150} \right] \times 10 \quad \text{for working (ii)} \\ &= 35 + \left[ \frac{20^2}{180} \times 10 \right] \quad \text{using (i) for (ii)} \end{aligned}$$

$$= 35 + 2$$

$$= \boxed{37}$$

$$3A = 38 + 8A$$

SEG

$$\begin{array}{r} 23 \\ 2 \\ 460 \\ 360 \\ \hline 150 \\ 150 \\ \hline 36 \end{array}$$

## SECTION-C

Ams. 27.

(i.) Coordinates of A = (2, 2)

Coordinates of B = (5, 4)

Coordinates of C = (7, 6)

(ii.) If the points are collinear then,

$$AB + BC = AC$$

$$AB = \sqrt{(5-2)^2 + (4-2)^2} \quad \{ (x_2 - x_1)^2 + (y_2 - y_1)^2 \}$$

$$AB = \sqrt{9 + 4}$$

$$AB = \sqrt{13} \text{ unit}$$

$$BC = \sqrt{(7-5)^2 + (6-4)^2}$$

15

$$BC = \sqrt{4 + 4}$$

unit

$$AC = \sqrt{(7-2)^2 + (6-2)^2}$$

$$AC = \sqrt{25 + 16}$$

$$AC = \sqrt{41}$$

$$\therefore \sqrt{13} + \sqrt{8} \neq \sqrt{41}$$

~~steeped type~~  $\therefore$  The points are not collinear.

Ans. 28. (Choice - I)

$$AB = 10 \text{ cm}, AQ = 7 \text{ cm}, CQ = 5 \text{ cm}$$

$BC = ?$

$AR = AQ$  (equal tangents from point A) {tangents from a point outside the circle are equal in length}

$$AR = 7 \text{ cm}$$

~~steeped type~~  
25  
16  
541

15

$$BC = \sqrt{4+4}$$

↙

$$BC = \sqrt{8} \text{ unit}$$

$$AC = \sqrt{(7-2)^2 + (6-2)^2}$$

$$AC = \sqrt{25 + 16}$$

$$AC = \sqrt{41}$$

$$\therefore \sqrt{13} + \sqrt{8} \neq \sqrt{41}$$

~~is not lieg~~

~~is not lieg~~  $\therefore$  The points are not collinear.

Ans. 28. (Choice - I)

$$AB = 10 \text{ cm}, AQ = 7 \text{ cm}, CQ = 5 \text{ cm}$$

$$BC = ?$$

$AR = AL$  ( equal tangents from point A ) { tangents from a point outside the circle are equal in length }

$$AR = 7 \text{ cm}$$

$$\frac{25}{16} = \frac{25}{41}$$

$$AB = AR + BR$$

$$BR = AB - AR$$

$$BR = 10 - 7$$

$$BR = 3 \text{ cm}$$

$$BR = BP = 3 \text{ cm} \quad \left( \begin{array}{l} \text{equal tangents from } B \\ 1. \end{array} \right)$$

$$CQ = 5 \text{ cm} = CP \quad \left\{ \begin{array}{l} \text{equal tangents from } C \\ 2. \end{array} \right.$$

$$BC = BP + CP \quad \left\{ \begin{array}{l} \text{from } 1. \text{ & } 2. \\ 1. \end{array} \right.$$

$$BC = 3 + 5$$

$$BC = 8 \text{ cm}$$

Ams. 29.

Let us assume that  $\sqrt{2}$  is rational.  
Then,  $\frac{a}{b}$  is its simplest where 'a' and 'b' are

O.T.Q

P.T.O.

co-prime integers,  $b \neq 0$

$$\sqrt{2} = \frac{a}{b}$$

at sub ratio not matching with  
minimum longitude of  $\sqrt{2}$ , result

squaring both the sides we get

$$2 = \frac{a^2}{b^2}$$

$$2b^2 = a^2$$

Thus, 2 divides  $a^2 \quad \{ \because \text{it divides } b^2 \}$

$\Rightarrow$  2 divides  $a \quad \{ \because 2 \text{ is prime & divides } a^2 \}$  — (2)

Let  $a = 2c$  for some integer  $c$

$$a^2 = 4c^2$$

$$2b^2 = 4c^2 \quad [ \text{from (1)} ]$$

$$b^2 = 2c^2$$

Thus, 2 divides  $b^2 \quad \{ \because 2 \text{ divides } c^2 \}$

$\Rightarrow$  2 divides  $b \quad \{ \because 2 \text{ is prime & divides } b^2 \}$  — (3)

From (2) and (3) we get 2 as a common factor of  $a$  and  $b$

But this contradicts the fact that  $a$  and  $b$  are co-primes.

This contradiction has arisen due to our wrong assumption  
Therefore,  $\sqrt{2}$  is irrational number.

Q2

Ans.  $30^\circ$

C.

$$(\csc \theta - \cot \theta)^2 = \frac{1 - \cos \theta}{1 + \cos \theta}$$

From L.H.S.

$$\begin{aligned} & (\csc \theta - \cot \theta)^2 \\ &= \csc^2 \theta + \cot^2 \theta - 2 \csc \theta \cot \theta \quad \{(a-b)^2 = a^2 + b^2 - 2ab\} \\ &= \frac{1}{\sin^2 \theta} + \frac{\cos^2 \theta}{\sin^2 \theta} - 2 \times \frac{1}{\sin \theta} \times \frac{\cos \theta}{\sin \theta} \\ &= \frac{1}{\sin^2 \theta} + \frac{\cos^2 \theta}{\sin^2 \theta} - \frac{2 \cos \theta}{\sin^2 \theta} \\ &= \frac{1 + \cos^2 \theta - 2 \cos \theta}{\sin^2 \theta} \end{aligned}$$

$$\begin{aligned}
 &= \frac{(1-\cos\theta)^2}{1-\cos^2\theta} \quad \left\{ \begin{array}{l} \therefore a^2 + b^2 - 2ab = (a-b)^2 \\ \therefore \sin^2\theta + \cos^2\theta = 1 \end{array} \right\} \\
 &= \frac{(1-\cos\theta)(1-\cos\theta)}{(1-\cos\theta)(1+\cos\theta)} \quad \left\{ \begin{array}{l} \therefore a^2 - b^2 = (a+b)(a-b) \end{array} \right\} \\
 &= \frac{1-\cos\theta}{1+\cos\theta} \\
 &= R.H.S.
 \end{aligned}$$

Therefore, Proved.

### Ques. 31 (Choice - I)

Let the cost of 1 pencil be ₹ x and cost of 1 pen be ₹ y.

Then, acc ATQ,

$$5x + 7y = 250 \quad (1)$$

$$7x + 5y = 302 \quad (2)$$

Multiplying (1) by 7 and (2) by 5 and subtracting (1) from (2)

$$\begin{array}{r} 35x + 49y = 1750 \\ 35x + 25y = 1510 \\ \hline 24y = 240 \end{array}$$

$$y = \frac{240}{24}$$

$$y = ₹ 10$$

Substituting  $y = 10$  in (1), we get,

$$5x + 7(10) = 250$$

$$5x = 250 - 70$$

$$5x = 180$$

$$x = \frac{180}{5}$$

$$x = ₹ 36$$

Cost of one pencil = ₹ 36

Cost of one pen = ₹ 10

Ques. 32. (Choice - I)

(i.) Total no. of red king = 2

Total no. of cards = 52

$P(\text{getting a king of red colour}) = \frac{\text{favourable outcome}}{\text{Total no. of outcomes}}$

2

52

1

26

(ii.) Diamond suit has 1 queen  $\left( \text{QD, QH} \right) \leftarrow \text{Twice}$

$P(\text{getting the queen of diamonds}) = \frac{1}{52}$

(iii.) There are total 4 ace (one in each suit)

$P(\text{getting an ace}) = \frac{4}{52} = \frac{1}{13}$

## SECTION-D

Ans. 39.

C.I (lower limits)

More than 40 (or equal to)

More than 44 (or equal to)

More than 48 (or equal to)

More than 52 (or equal to)

More than 56 (or equal to)

More than 60 (or equal to)

More than 64 (or equal to)

c.f.

100

$$(100-4) = 96$$

$$96-10 = 86$$

~~$$86-30 = 56$$~~

~~$$56-24 = 32$$~~

~~$$32-18 = 14$$~~

~~$$14-12 = 2$$~~

Coordinates  $\rightarrow$  (40, 100)

(44, 96)

(48, 86)

(52, 56)

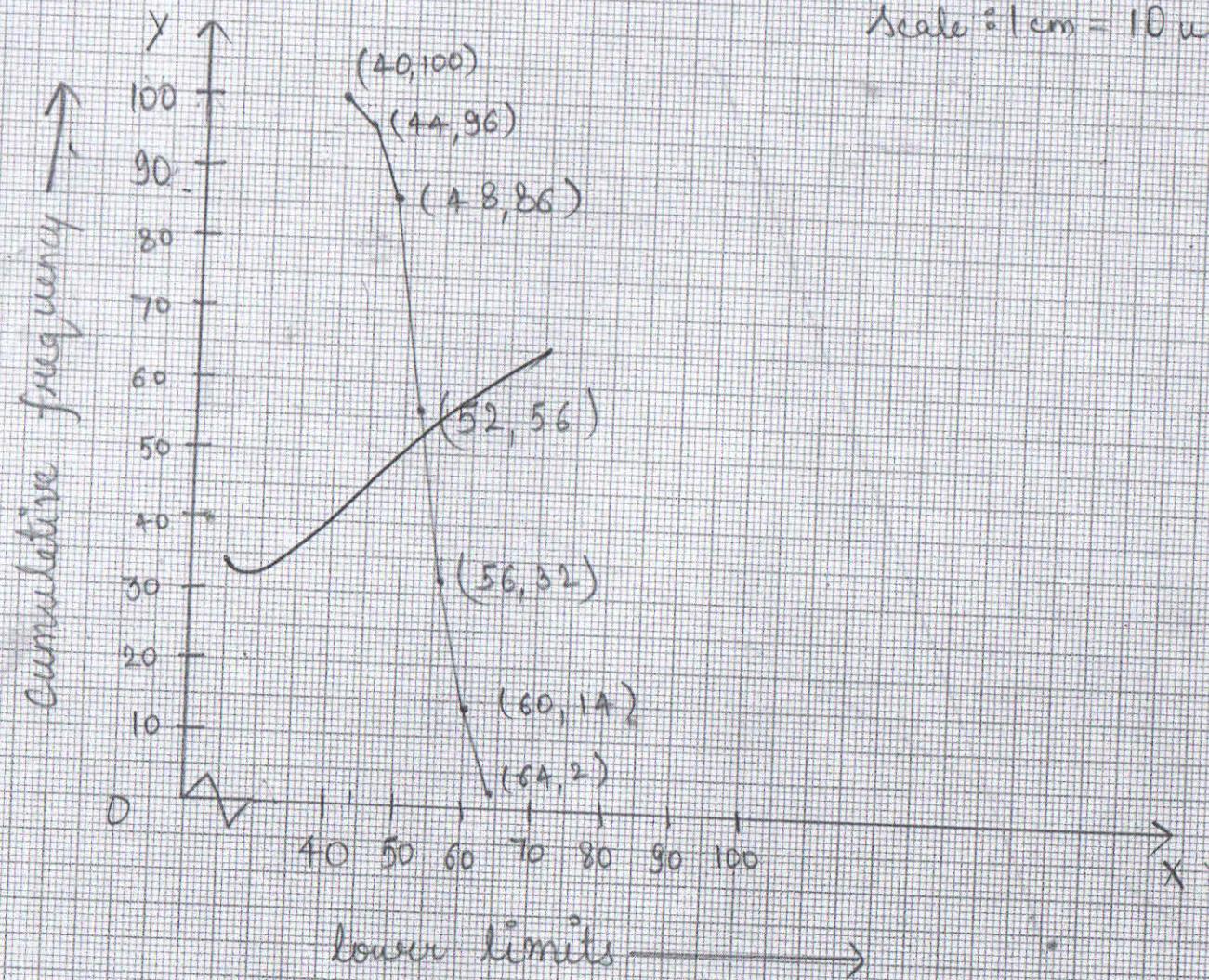
(56, 32)

(60, 14)

(64, 2)

Ans. 39.

Scale: 1 cm = 10 units



$$\begin{array}{r} 8.5 \\ \times 0.29 \\ \hline 88 \end{array}$$

27

$$\begin{array}{r} 50.28 \\ \times 159 \\ \hline 18640 \\ 352 \\ \hline 802 \\ -28 \\ \hline 10721 \end{array}$$

$$\begin{array}{r} 50.29 \\ \times 140 \\ \hline 1800 \\ 352 \\ \hline 7040 \\ -5029 \\ \hline 1971 \end{array}$$

$$\begin{array}{r} 52.58 \\ \times 117 \\ \hline 352 \\ 525 \\ \hline 5980 \end{array}$$

$$\begin{array}{r} 32.6 \\ \times 50.1 \\ \hline 1630 \\ + 160 \\ \hline 1630 \end{array}$$

$$\begin{array}{r} 32.6 \\ \times 50.1 \\ \hline 1630 \\ + 160 \\ \hline 1630 \end{array}$$

$$\begin{array}{r} 32.6 \\ \times 50.1 \\ \hline 1630 \\ + 160 \\ \hline 1630 \end{array}$$

$$\begin{array}{r} 32.6 \\ \times 50.1 \\ \hline 1630 \\ + 160 \\ \hline 1630 \end{array}$$

$$\begin{array}{r} 32.6 \\ \times 50.1 \\ \hline 1630 \\ + 160 \\ \hline 1630 \end{array}$$

$$\begin{array}{r} 32.6 \\ \times 50.1 \\ \hline 1630 \\ + 160 \\ \hline 1630 \end{array}$$

$$\begin{array}{r} 32.6 \\ \times 50.1 \\ \hline 1630 \\ + 160 \\ \hline 1630 \end{array}$$

$$\begin{array}{r} 32.6 \\ \times 50.1 \\ \hline 1630 \\ + 160 \\ \hline 1630 \end{array}$$

$$\begin{array}{r} 32.6 \\ \times 50.1 \\ \hline 1630 \\ + 160 \\ \hline 1630 \end{array}$$

$$\begin{array}{r} 32.6 \\ \times 50.1 \\ \hline 1630 \\ + 160 \\ \hline 1630 \end{array}$$

$$\begin{array}{r} 32.6 \\ \times 50.1 \\ \hline 1630 \\ + 160 \\ \hline 1630 \end{array}$$

$$\begin{array}{r} 32.6 \\ \times 50.1 \\ \hline 1630 \\ + 160 \\ \hline 1630 \end{array}$$

Ques. 33. ~~(a) Area of square = area of circle which is 7 cm away from center~~

$$\begin{aligned} \text{Area of the square} &= (\text{side})^2 \\ &= (14)^2 \\ &= 196 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of 4 quadrants} &= 4 \times \left[ \frac{\theta}{360^\circ} \times \pi r^2 \right] \\ &= 4 \times \left[ \frac{90^\circ}{360^\circ} \times \frac{22}{7} \times 3.5^{0.5} \times 3.5 \right] \\ &= \left( 4 \times \frac{1}{4} \times 22 \times 0.5 \times 3.5 \right) \\ &= 38.5 \text{ cm}^2 \end{aligned}$$

$$\text{Area of circle} = \pi r^2$$

~~$$= \frac{22}{7} \times 4^2 = \frac{22}{7} \times (4)^2$$~~

$$= \frac{352}{7} = 50.29 \text{ cm}^2 \text{ (approx.)}$$

## SECTION - 7

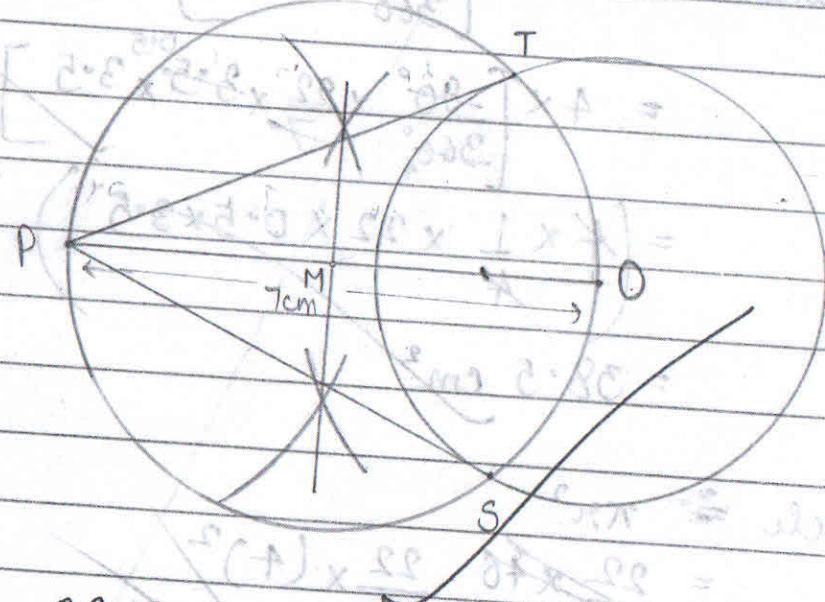
~~Area of shaded region = Area of square - (Area of 4 circles)~~

$$= 196 - (38.5 + 50.29)$$

$$= (196 - 88.79)$$

$$= \underline{107.21 \text{ cm}^2} \text{ (approx)}$$

Ans. 34.



PT and PS are the required tangents.

P.T.O.

Steps of construction:

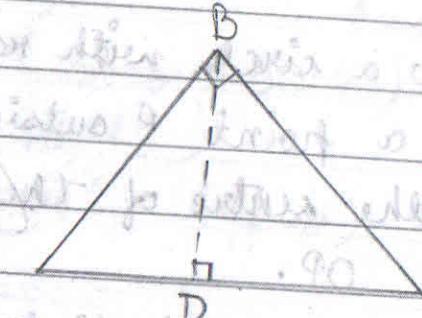
1. Draw a circle with radius 3 cm
2. Take a point P outside the circle which is 7 cm away from the centre of the circle.
3. Join OP.
4. Draw the perpendicular bisector of OP which intersects it at M.
5. Taking M as centre and radius equal to PM draw another circle.
6. Mark the points of intersection of bigger circle and smaller circle as T and S
7. Join PT and PS.

## SECTION-D

Ans. 35.

$\triangle ABC$  is a right - angled  $\triangle$  with  $\angle B = 90^\circ$

$AC \rightarrow$  hypotenuse



To prove:  $AC^2 = AB^2 + BC^2$

Const.: Draw  $AD \perp AC$

Proof:

In  $\triangle ADB$  and  $\triangle ABC$

$$\angle ADB = \angle ABC = 90^\circ$$

$$\angle DAB = \angle BAC \text{ (common)}$$

$\therefore \triangle ADB \sim \triangle ABC$  (AA-similarity criterion),

$$\Rightarrow \frac{AD}{AB} = \frac{AB}{AC}$$

$$\Rightarrow AB^2 = AD \times AC \quad \text{--- (1.)}$$

In  $\triangle BDC$  and  $\triangle ABC$

$$\angle BDC = \angle ABC = 90^\circ$$

$$\angle BCD = \angle ACB \text{ (common)}$$

$\therefore \triangle BDC \sim \triangle ABC$  (AA-similarity criterion)

$$\Rightarrow \frac{BD}{BC} = \frac{DE}{AC}$$

$$\Rightarrow BC^2 = AC \times DC \quad \text{--- (2.)}$$

Adding (1.) & (2.) we get,

$$AB^2 + BC^2 = AD \times AC + AC \times DC$$

$$AB^2 + BC^2 = AC(AD + DC)$$

$$AB^2 + BC^2 = AC \times AC$$

$$\boxed{AB^2 + BC^2 = AC^2}$$

Proved

Ans. 36. (Choice-I)

$$\begin{array}{r} -x+4 \\ x^2+x-1 ) \overline{-x^3+3x^2-3x+5} \\ -x^3-x^2+x \\ + + - \\ \hline \end{array}$$

$$\begin{array}{r} 4x^2-4x+5 \\ 4x^2+4x-4 \\ - - + \\ \hline \end{array}$$

$$-8x+9$$

$$\text{Divisor} = x^2+x-1$$

$$\text{Dividend} = -x^3+3x^2-3x+5$$

$$\text{Remainder} = -8x+9$$

$$\text{Quotient} = -x+4$$

According to the division algorithm

$$\text{Dividend} = \text{Divisor} \times \text{Quotient} + \text{Remainder}$$

$$-x^3+3x^2-3x+5 = (-x+4)(-x+4) + (-8x+9)$$

$$-x^3 + 3x^2 - 3x + 5 = x^2 - 4x - 4x + 16 - 8x + 9 \quad \text{R.H.S.}$$

$$\begin{aligned} -x^3 + 3x^2 - 3x + 5 &= (x^2 + x - 1) \times (-x + 4) + (-8x + 9) \\ &= -x^3 + 4x^2 - x^2 + 4x + x - 4 - 8x + 9 \\ &= -x^3 + 3x^2 - 3x + 5 \\ &= \text{L.H.S.} \end{aligned}$$

∴ Proved.

Ams. 37.

AC → height of building = 20m

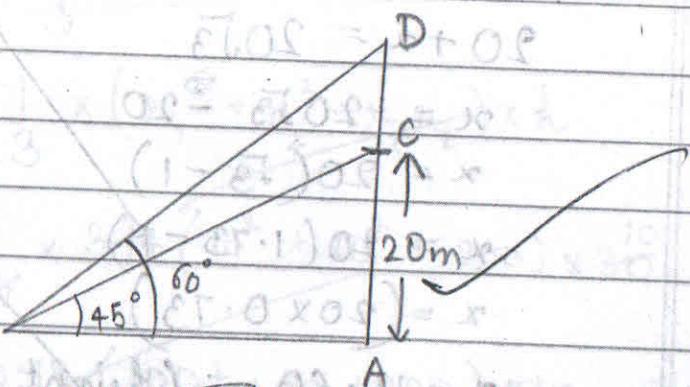
CD → height of transmission tower  
 $CD = x$  m.

AB → distance of the point from the foot of the building =  $y$  m

In  $\triangle ABC$

$\angle CAB = 90^\circ$  [building stands vertical on the ground]

$$\therefore \tan 45^\circ = \frac{AC}{AB} \Rightarrow 1 = \frac{AC}{y} \Rightarrow y = 20 \text{ m} \quad \text{--- (1)}$$



In  $\triangle ADB$

$\angle DAB = 90^\circ$  (building stands vertical on the ground)

$$\therefore \tan 60^\circ = \frac{AD}{AB}$$

$$\Rightarrow \sqrt{3} = \frac{20+x}{y}$$

$$\Rightarrow \sqrt{3} = \frac{20+x}{20}$$

} from (1.)

$$20+x = 20\sqrt{3}$$

$$x = 20\sqrt{3} - 20$$

$$x = 20(\sqrt{3} - 1)$$

$$x = 20(1.73 - 1)$$

$$x = (20 \times 0.73)$$

$$x = 14.60 \text{ m. (height of tower)}$$

$$\begin{array}{r} 20 \\ \times 1.73 \\ \hline 14.60 \end{array}$$

Ans. 38.

(Choice I)

$$h = 30 \text{ cm}$$

$$r_1 = 10 \text{ cm}$$

$$r_2 = 20 \text{ cm}$$

Capacity = Volume

$$\begin{aligned}
 \text{Volume of frustum of a cone} &= \frac{1}{3} \pi (r_1^2 + r_1 r_2 + r_2^2) \times h \\
 &= \frac{1}{3} \pi (10^2 + 10 \times 20 + 20^2) \times 30 \\
 &= \frac{1}{3} \times 3.14 (100 + 200 + 400) \times 10 \\
 &= 3.14 (100 + 400 + 200) \times 10 \\
 &= 3.14 \times 700 \times 10 \\
 &= 2198 \times 10 \\
 &= 21980 \text{ cm}^3
 \end{aligned}$$

Ans. 39. In front of graph paper

Ans. 40. Choice (II)

Let the sides of the two squares be  $x$  m and  $y$  m resp.

ATQ, Perimeter of square =  $4 \times$  side

$$\text{ATQ}, 4x - 4y = 24$$

$$4(x-y) = 24$$

$$x-y = 6$$

$$x = 6+y$$

Area of square =  $(\text{side})^2$

ATQ,

$$x^2 + y^2 = 468$$

$$x^2 + (6+y)^2 + y^2 = 468 \quad (\text{from } ①)$$

$$36 + y^2 + 12y + y^2 = 468$$

$$2y^2 + 12y + 36 - 468 = 0$$

$$2y^2 + 12y - 432 = 0$$

$$2(y^2 + 6y - 216) = 0$$

$$y^2 + 6y - 216 = 0$$

$$y^2 + 18y - 12y - 216 = 0$$

$$y(y+18) - 12(y+18) = 0$$

$$(y+18)(y-12) = 0$$

$$y = -18 \quad \text{E}$$

$$y = 12$$

We consider  $y = 12$  m because distance cannot be negative

$$x = 12 + 6$$

$$= 18 \text{ m}$$

Sides of two squares are 18 m and 12 m.

$$\begin{array}{r} 216 \\ 108 \\ 54 \\ 27 \\ 27 \\ 9 \\ 9 \\ 3 \\ 3 \\ 1 \end{array}$$

$$\begin{array}{r} 18 \\ 12 \\ 36 \\ 18 \\ 18 \\ 36 \\ 216 \end{array}$$

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