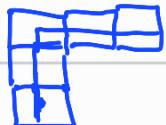


### Specifications for Hardware

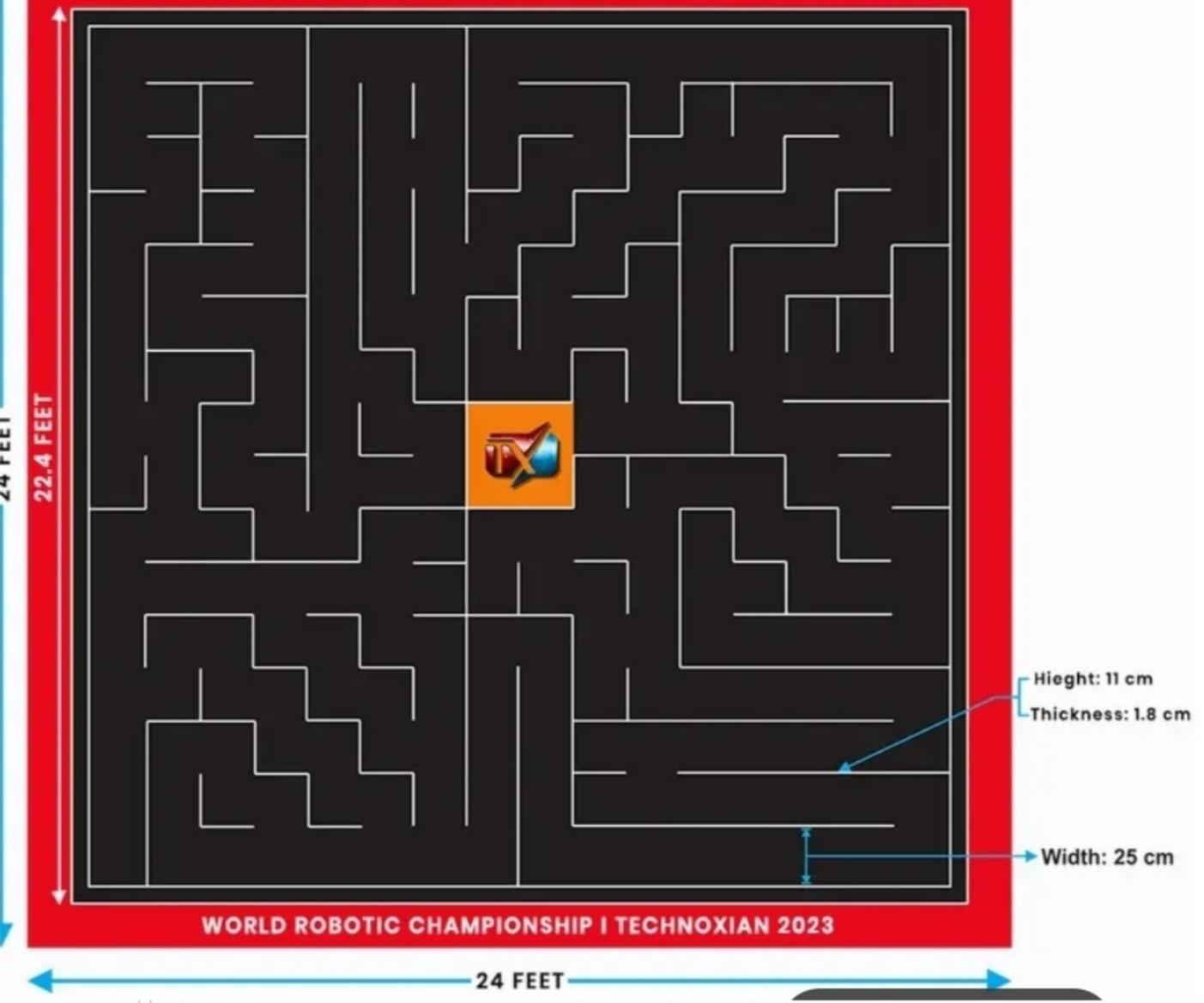
- ① Chassis (1)
- ② Motor Servo (2)
- ③ IR Sensor (2) / Ultrasonic sensors (3)
- ④ Caster Wheel
- ⑤ Wheels
- ⑥ Battery
- ⑦ Arduino Nano

May be before this to fill map we need flood fill but as we know the obstacles from start we can use

- ① A\* Algorithm (Global path planning).  
[ You don't need local path planning ]
- ② Particle Filter for localization.
- ③ Controllers



# MAZE SOLVER ARENA

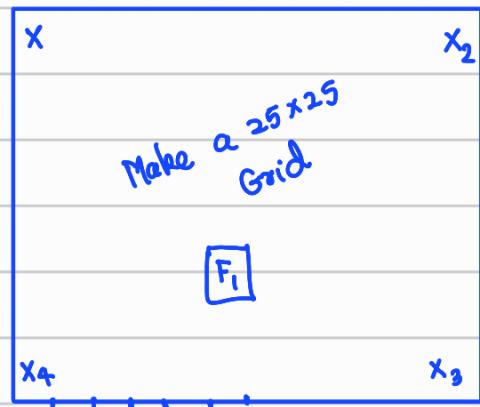


"4 corners" is kept "the robot"

$$\text{Per grid} = \frac{670.56}{26.8} = 25.02 \approx 25 \text{ cm}$$

$$670.56 \text{ cm} = 22 \text{ feet}$$

$$22 \text{ Feet} = 670.56 \text{ cm}$$

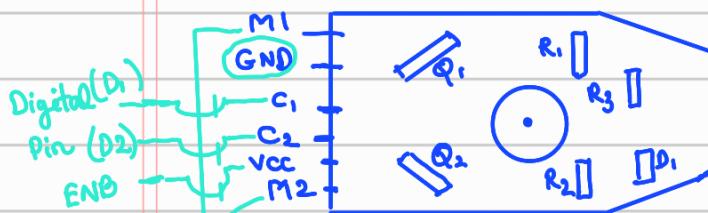


Micro Controller  
(Arduino)

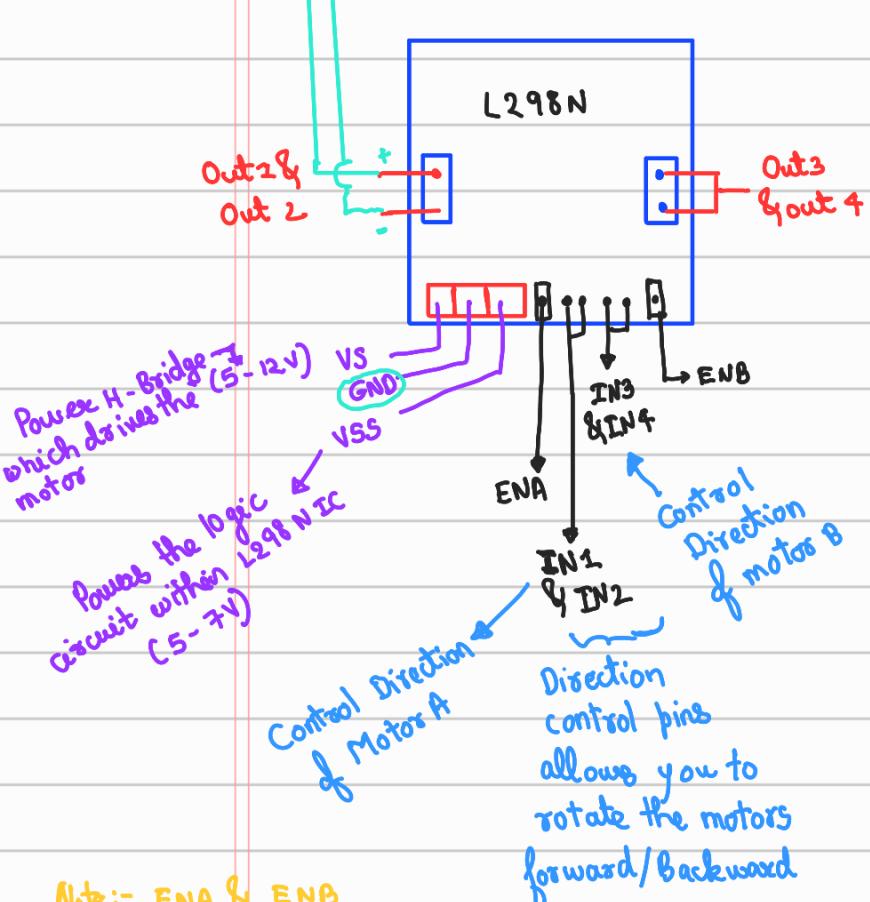
Motor Driver  
(L298N)

Motors  
(DC with encoder)  
N20

N20 <sup>micro</sup>  
gear motor encoder



Q1, Q2 → CC6101 hall effect sensor  
R1, R2, R3 → 3.3KΩ resistors  
D1 → LED

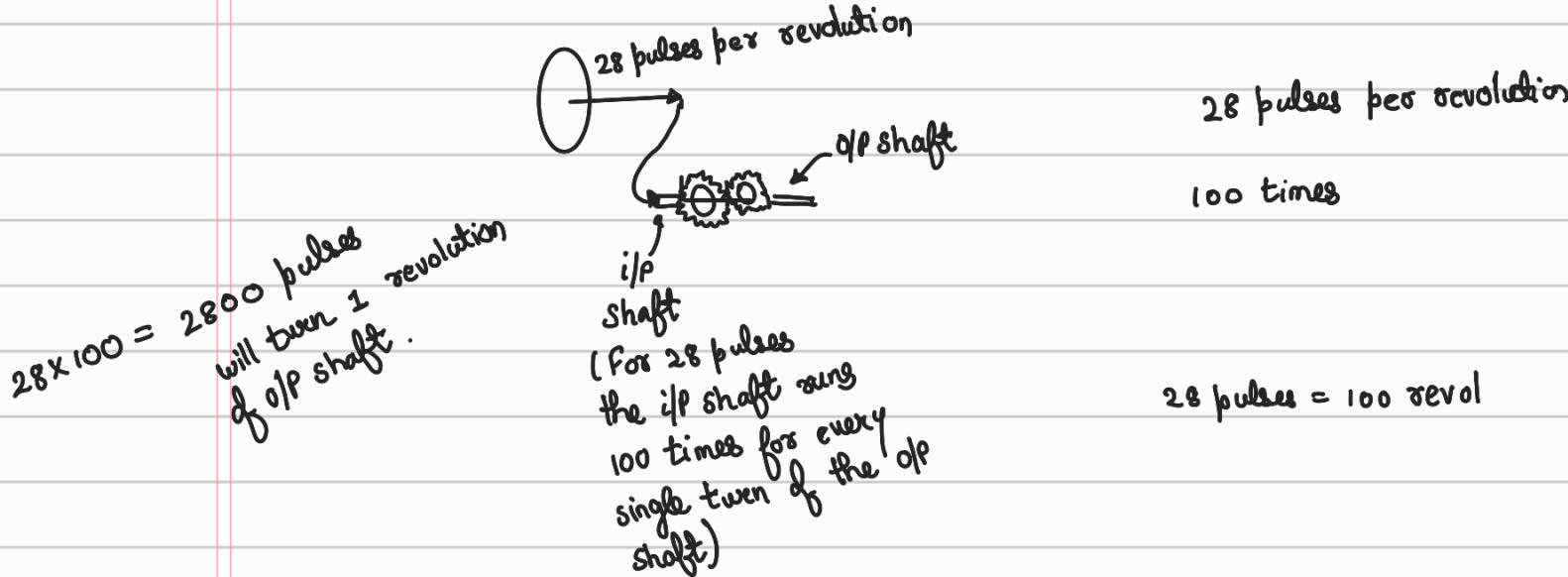


Note:- ENA & ENB

(When the jumper is in place the jumper is in full speed. If we want to control the speed we can connect to PWM pins of arduino & program)

[Power by 5V or GND logic]

## # Encoder to gear pulse ratio



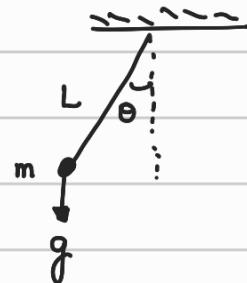
#

$$150 \text{ rpm} \times \pi d^{4.2 \text{ cm}} = 150 \times \pi \times 4.2 \\ = 1978 \text{ cm/min} \\ = 19.78 \text{ m/min}$$

$$F = ma$$

$$\ddot{\theta} = -\frac{g}{L} \sin(\theta) - \delta \dot{\theta}$$

$$\begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} \theta \\ \dot{\theta} \end{bmatrix}$$



$$\frac{d}{dt} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} x_2 \\ -\frac{g}{L} \sin(x_1) - \delta x_2 \end{bmatrix}$$

$$\text{Assume, } \frac{g}{L} = \frac{9.81 \text{ m/s}^2}{0.09 \text{ m}}$$

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} x_2 \\ -\sin(x_1) - \delta x_2 \end{bmatrix}$$

$$\delta = 0.1$$



saddle point.

## 1. Fixed points (F.P.)

$\begin{array}{c} \pi^{\circ} \\ \downarrow \\ 0^{\circ} \end{array}$

$$\bar{x} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}, \begin{bmatrix} \pi \\ 0 \end{bmatrix}$$

## 2. Linearization

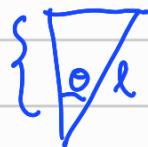
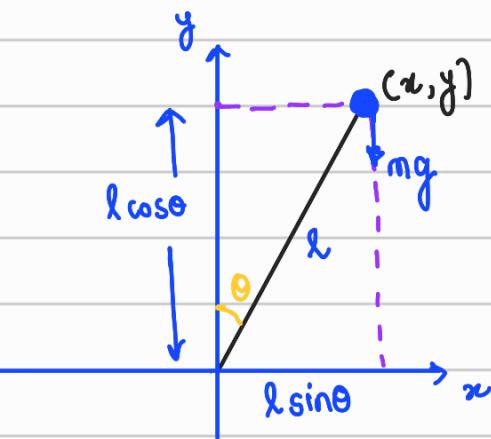
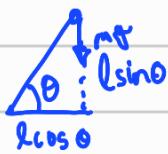
$$\frac{Df}{Dx} = \begin{bmatrix} 0 & 1 \\ -\cos(x_i) & -\delta \end{bmatrix}$$

$$A_p = \begin{bmatrix} 0 & 1 \\ -1 & -\delta \end{bmatrix}$$

$$A_v = \begin{bmatrix} 0 & 1 \\ 1 & -\delta \end{bmatrix}$$

Derivation of inverted pendulum

$$T = l \cdot mg \cdot \sin\theta$$



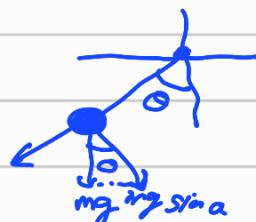
$$\cos\theta = \frac{x}{l}$$

$$y = l \cos\theta$$

$$\sin\theta = \frac{y}{l}$$

$$x = l \sin\theta$$

$$\begin{aligned} x &= l \sin\theta & \dot{x} &= l \cos\theta \dot{\theta} \\ y &= l \cos\theta & \dot{y} &= -l \sin\theta \dot{\theta} \end{aligned}$$

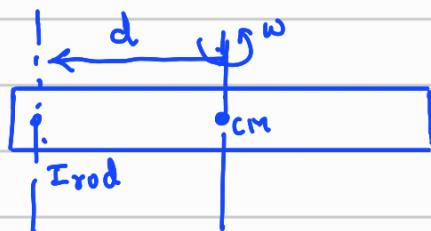
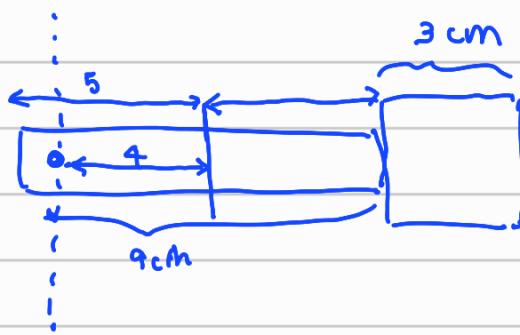


$$M = I \ddot{\theta}(t)$$

Net torque = Motor torque - Gravitational torque

$$I \ddot{\theta} = \tau - mgL \sin(\theta)$$

Assembly weight  $\rightarrow 24.979 \text{ g}$



$$I_s = I_{\text{cm}} + md^2$$

$$I_{\text{cm, rod}} = \frac{1}{12} m L^2$$

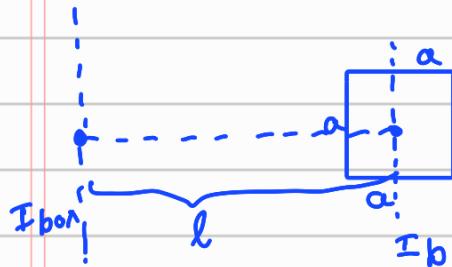
(This is the measure of how mass is distributed about the axis)

Rod weight  $\rightarrow 3.64 \text{ g}$

$$d = \frac{L}{2}$$

$$= \frac{1}{12} m L^2 + m \left( \frac{L}{2} \right)^2 = \frac{1}{3} m L^2$$

$$= \frac{1}{12} (0.00364) (0.1)^2 + m (0.04)^2 = 5.835 \times 10^{-6} \text{ kgm}^2$$



$$I_{\text{box}} = \frac{1}{6} m a^2 + m l^2$$

$$= \frac{1}{6} (0.02133) (0.03)^2 + (0.02133) (0.105)^2$$

$$= 2.383 \times 10^{-4} \text{ kgm}^2$$

### Weight

$$6.928 \times 10^{-4} \text{ kgm}^2 \quad (\text{10 coins})$$

Plate  $\rightarrow 10.56 \text{ g}$

Box  $\rightarrow 10.77 \text{ g} + (4.10) \times 10 = 51.77$

$$21.33 \text{ g} \rightarrow 0.02133 \text{ kg}$$

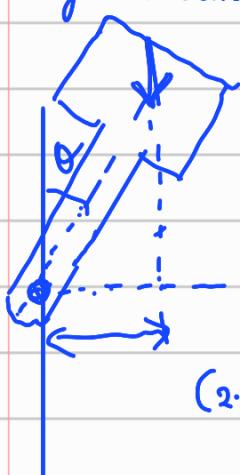
$$\begin{cases} 62.33 \text{ g} \\ 0.062 \text{ kg} \end{cases}$$

$$I_{\text{new}} = I_{\text{rod}} + I_{\text{box}}$$

$$= 5.835 \times 10^{-6} + 2.383 \times 10^{-4}$$

$$= 2.441 \times 10^{-4} \text{ kgm}^2$$

$$6.986 \times 10^{-4} \text{ kgm}^2 \quad (\text{10 coins})$$



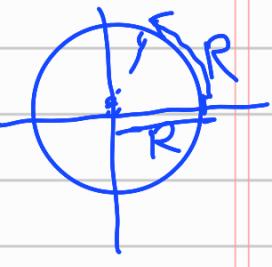
$$I_{\text{new}} \ddot{\theta} = T_{\text{rotated}} - mg L \sin(\theta) - (\text{friction})$$

$$(2.441 \times 10^{-4}) \ddot{\theta} = 0.07 - (0.02133)(9.81)(0.105) \sin(\pi/2)$$

$$\ddot{\theta} = \frac{0.07 - 0.021}{2.441 \times 10^{-4}} \sim 10 \text{ coins} \rightarrow 0.063 \text{ g}$$

$$89 \text{ rad/s}^2$$

$$\ddot{\theta} = \frac{0.07}{196.96} \text{ rad/s}^2$$



$$\tau = Nm = \left( \frac{kgm}{s^2} \right) m = \frac{kgm^2}{s^2}$$

$$I = kgm^2$$

$$\therefore \frac{\tau}{I} = \frac{kgm^2}{s^2} \times \frac{1}{kgm^2} = \frac{1}{s^2}$$

$$\begin{aligned} 0.013 \\ \ddot{\theta} = 53.27 \text{ rad/s}^2 \end{aligned}$$

$$mgl\sin(\theta) = \frac{kg}{s^2} m \cdot m = \frac{kgm^2}{s^2} = Nm$$

$$I = 6.75 \times 10^{-7}$$

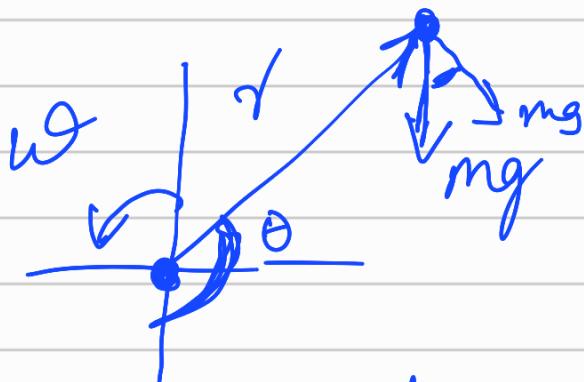
$$\ddot{\theta} = 86$$

Theoretical

$$I\ddot{\theta} = 0.04 \text{ Nm}$$

$$(2.441 \times 10^{-4})(200) = 0.04 \text{ Nm}$$

$$\text{Exper} \rightarrow (2.441 \times 10^{-4})(89) = 0.01 \text{ Nm}$$



$$mgr\cos\theta = \frac{dL}{dt} = I\alpha = I\ddot{\theta}$$

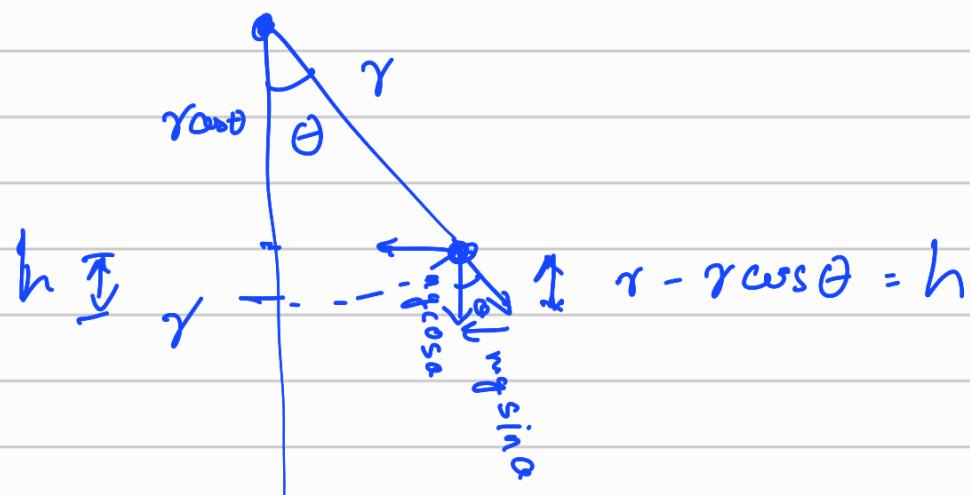
$$\cos\theta - \frac{I}{mgr} \ddot{\theta}$$

$$\theta = \cos^{-1} \left( \frac{I}{mgr} \ddot{\theta} \right)$$

$$y = f(u) \rightarrow \cos\theta = \frac{I}{mgr} \ddot{\theta}$$

$$\bar{y}_r = -1$$

$$\left\{ \begin{array}{l} y - y_r = 0 \\ \dot{y} - \dot{y}_r = 0 \end{array} \right. \quad \frac{\ddot{f}(\theta)}{m\gamma} + r = 0 \quad \rightarrow$$



$$P = mgh$$

$$F = \frac{1}{2} I \omega^2$$

$$= \frac{1}{2} I \omega^2$$

$$mgh + \frac{1}{2} I \omega^2 = \text{constant}$$

$$I \omega \dot{\omega} - rmg \sin \theta \omega = 0$$

$$T \rightarrow (\underline{I \omega}) - mg r \underline{\sin \theta} = 0$$

$$\cancel{\omega = \tau}$$

$$\eta_1 = \theta$$

$$\cancel{\dot{\omega} = \ddot{\theta}}$$

$$\eta_2 = \ddot{\theta}$$

$$\dot{\eta}_1 = \cancel{\eta_2} \quad \eta_2$$

$$\dot{\eta}_2 = \frac{mg \sin \theta}{I} + \frac{\tau}{I}$$

$$\ddot{\theta} = \frac{0.07 - 0.021}{2.44 \times 10^{-4}}$$

$$(2.44 \times 10^{-4}) \ddot{\theta} = \tau - 0.021$$

Case 1:-  $\tau = 0.034$

$$(2.44 \times 10^{-4}) \ddot{\theta} = 0.034 - 0.021 \\ = 0.013$$

$$\ddot{\theta} = \frac{0.013}{2.44 \times 10^{-4}} = 53.27 \text{ rad/s}^2$$

Case 2:-  $\tau = 0.01$

$$\ddot{\theta} = \frac{-0.011}{2.44 \times 10^{-4}} = -45.08 \text{ rad/s}^2$$