Assignment 9

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- 49. The Lagrangian of a particle of mass m moving in one dimension is L = $exp(\alpha t)\left[\frac{mx^2}{2} - \frac{kx^2}{2}\right]$, where α and k are positive constants. The equation of the particle is (2009)
 - (A) $\ddot{x} + \alpha \dot{x} = 0$

 - (B) $\ddot{x} + \frac{k}{m}x = 0$ (C) $\ddot{x} \alpha \dot{x} + \frac{k}{m}x = 0$ (D) $\ddot{x} + \alpha \dot{x} + \frac{k}{m}x = 0$
- 50. Two monochromatic waves having frequencies ω and $\omega + \Delta\omega (\Delta\omega \ll \omega)$ and corresponding wavelength λ and $\lambda - \Delta \lambda (\Delta \lambda \ll \lambda)$ of same polarization, travelling along x-axis are superimposed on each other. The phase velocity and group velocity of the resultant wave are respectively given by (2009)
 - $\begin{array}{ll} (A) & \frac{\omega\lambda}{2\pi}, \frac{\Delta\lambda^2}{2\pi\Delta\lambda} \\ (B) & \omega\lambda, \frac{\Delta\lambda^2}{\Delta\lambda} \\ (C) & \frac{\omega\Delta\lambda}{2\pi}, \frac{\lambda\lambda}{2\pi\Delta\lambda} \\ (D) & \omega\Delta\lambda, \omega\Delta\lambda \end{array}$

Common data questions Common data questions 51 and 52 Consider a two level quantum system with energies $\epsilon_1 = 0$ and $\epsilon_2 = \epsilon$

- 51. The Helmholtz free energy of the system is given by (2009)
 - (A) $-k_BT \ln\left(1+e^{\frac{-\epsilon}{k_BT}}\right)$
 - (B) $k_B T ln \left(1 + e^{\frac{-\epsilon}{k_B T}}\right)$
 - (C) $\frac{3}{2}k_BT$
- 52. The specific heat of the system is given by (2009)
 - (A) $\frac{\epsilon}{k_B T} \frac{e^{\frac{-\epsilon}{k_B T}}}{\left(1 + e^{\frac{-\epsilon}{k_B T}}\right)^2}$
 - (B) $\frac{\epsilon^2}{k_B T^2} \frac{e^{\frac{-\epsilon}{k_B T}}}{\left(1 + e^{\frac{-\epsilon}{k_B T}}\right)}$
 - (C) $-\frac{\epsilon^2 e^{\frac{-\epsilon}{k_B T}}}{\left(1 + e^{\frac{-\epsilon}{k_B T}}\right)^2}$
 - (D) $\frac{e^{\frac{1}{2}}}{k_B T^2} \frac{e^{\frac{-\epsilon}{k_B T}}}{\left(1 + e^{\frac{-\epsilon}{k_B T}}\right)^2}$

Common data questions 53 and 54 A free particle of mass m moves along the xdirection. At t = 0, the normalized wave function of the particle is given by $\psi(x, 0) =$ $\frac{1}{(2\pi\alpha)^{1/4}}exp-\frac{x^2}{4a^2}+ix$, where α is a real constant 53. The expectation value of the momentum, in this state is

- (2009)
 - (A) $\hbar\alpha$

- (B) $\hbar \sqrt{\alpha}$
- (C) α
- (D) $\frac{\hbar}{\sqrt{a}}$

54. The expectation value of the particle energy is

(2009)

Common data questions 55 and 56 Consider the Zeeman splitting of a single electron system for the 3d to 3p electric dipole transition

55. The Zeeman spectrum is

(2009)

- (A) Randomly polarized
- (B) only π polarized
- (C) only σ polarized
- (D) both π and σ polarized

56. The fine structure line having the longest wavelength will split into (2009)

- (A) 17 components
- (B) 10 components
- (C) 8 components
- (D) 4 components

Linked Answer Questions Statement for Linked Answer Questions 57 and 58: The primitive translation vectors of the face centered cubic (fcc) lattice are

$$\hat{a}_1 = \frac{a}{2}(\hat{j} + \hat{k}); \hat{a}_2 = \frac{a}{2}(\hat{i} + \hat{k}); \hat{a}_1 = \frac{a}{2}(\hat{j} + \hat{i})$$

57. The primitive transition vectors of the fccreciprocal lattice are (2009)

(A)
$$\hat{b}_1 = \frac{2\pi}{a} (\hat{j} + \hat{k} - \hat{i}); \hat{b}_2 = \frac{2\pi}{a} (-\hat{j} + \hat{k} + \hat{i}); \hat{b}_3 = \frac{2\pi}{a} (\hat{j} - \hat{k} + \hat{i})$$

(B)
$$\hat{b}_1 = \frac{\pi}{a} (\hat{j} + \hat{k} - \hat{i}); \hat{b}_2 = \frac{\pi}{a} (-\hat{j} + \hat{k} + \hat{i}); \hat{b}_3 = \frac{\pi}{a} (\hat{j} - \hat{k} + \hat{i})$$

(C)
$$\hat{b}_1 = \frac{\pi}{2a} (\hat{j} + \hat{k} - \hat{i}); \hat{b}_2 = \frac{\pi}{2a} (-\hat{j} + \hat{k} + \hat{i}); \hat{b}_3 = \frac{\pi}{2a} (\hat{j} - \hat{k} + \hat{i})$$

(A)
$$\hat{b}_1 = \frac{2\pi}{a} (\hat{j} + \hat{k} - \hat{i}); \hat{b}_2 = \frac{2\pi}{a} (-\hat{j} + \hat{k} + \hat{i}); \hat{b}_3 = \frac{2\pi}{a} (\hat{j} - \hat{k} + \hat{i})$$
(B) $\hat{b}_1 = \frac{\pi}{a} (\hat{j} + \hat{k} - \hat{i}); \hat{b}_2 = \frac{\pi}{a} (-\hat{j} + \hat{k} + \hat{i}); \hat{b}_3 = \frac{\pi}{a} (\hat{j} - \hat{k} + \hat{i})$
(C) $\hat{b}_1 = \frac{\pi}{2a} (\hat{j} + \hat{k} - \hat{i}); \hat{b}_2 = \frac{\pi}{2a} (-\hat{j} + \hat{k} + \hat{i}); \hat{b}_3 = \frac{\pi}{2a} (\hat{j} - \hat{k} + \hat{i})$
(D) $\hat{b}_1 = \frac{3\pi}{a} (\hat{j} + \hat{k} - \hat{i}); \hat{b}_2 = \frac{3\pi}{a} (-\hat{j} + \hat{k} + \hat{i}); \hat{b}_3 = \frac{3\pi}{a} (\hat{j} - \hat{k} + \hat{i})$

58. The volume of the primitive cell of the fcc reciprocal lattice is (2009)

- (A) $4\left(\frac{\pi}{a}\right)^3$
- (B) $4\left(\frac{2\pi}{a}\right)^3$ (C) $4\left(\frac{\pi}{2a}\right)^3$
- (D) $4\left(\frac{3\pi}{a}\right)^3$

Statement for Linked Answer Questions 59 and 60: The Karnaugh map of logic circuit shown is below

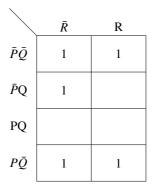


Fig. 0.1: 1

59. The minimized logic expression for the above map is

(2009)

- (A) $Y = \bar{PR} + \bar{Q}$
- (B) $Y = \bar{Q}.PR$
- (C) $Y = PR + \bar{Q}$
- (D) $Y = \bar{PR}.Q$

60. The corresponding logic implementation using gates is given as: (2009)

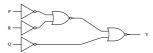


Fig. 0.2: option1

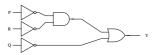


Fig. 0.3: option2

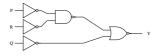


Fig. 0.4: option3

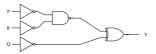


Fig. 0.5: option4