

# 1-1.7-5

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## Question:

Find the value of  $p$  for which the points  $A\begin{pmatrix} -5 \\ 1 \end{pmatrix}$ ,  $B\begin{pmatrix} 1 \\ p \end{pmatrix}$ , and  $C\begin{pmatrix} 4 \\ -2 \end{pmatrix}$  are collinear?

## Solution:

Given,

points	values
<b>A</b>	$\begin{pmatrix} -5 \\ 1 \end{pmatrix}$
<b>B</b>	$\begin{pmatrix} 1 \\ p \end{pmatrix}$
<b>C</b>	$\begin{pmatrix} 4 \\ -2 \end{pmatrix}$

TABLE 1 0: values of the geometrical points in given question

if three points are collinear then their slope should be equal.

$$\begin{aligned}
 \text{slope of AB} &= B - A \\
 &= \begin{pmatrix} 1 \\ p \end{pmatrix} - \begin{pmatrix} -5 \\ 1 \end{pmatrix} \\
 &= \begin{pmatrix} 1 + 5 \\ p - 1 \end{pmatrix} \\
 &= \begin{pmatrix} 6 \\ p - 1 \end{pmatrix} \\
 &= 6 \begin{pmatrix} 1 \\ \frac{p-1}{6} \end{pmatrix}
 \end{aligned}$$

$$\therefore \text{slope} = \frac{p-1}{6}. \quad (0.1)$$

$$\begin{aligned}
 \text{slope of BC} &= C - A \\
 &= \begin{pmatrix} 4 \\ -2 \end{pmatrix} - \begin{pmatrix} 1 \\ p \end{pmatrix} \\
 &= \begin{pmatrix} 4 - 1 \\ -2 - p \end{pmatrix} \\
 &= \begin{pmatrix} 3 \\ -2 - p \end{pmatrix} \\
 &= 3 \begin{pmatrix} 1 \\ \frac{-2-p}{3} \end{pmatrix}
 \end{aligned}$$

$$\therefore \text{slope} = \frac{-2-p}{3}. \quad (0.2)$$

slope AB = slope of BC

$$\begin{aligned}
 \frac{p-1}{6} &= \frac{-p-2}{3} \\
 3(p-1) &= 6(-p-2) \\
 p-1 &= -2p-4 \\
 p &= -1
 \end{aligned}$$

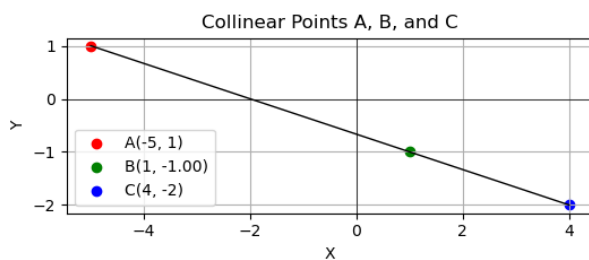


Fig. 0.1: plot for collinear points