

Assignment 7

AI24BTECH11008- Sarvajith

27. A cantilever beam of length 2 m with a square section of side length 0.1 m is loaded vertically at the free end. The vertical displacement at the free end is 5mm. The beam is made of steel with Young's modulus of $2.0 \times 10^{11} \frac{N}{m^2}$. The maximum bending stress at the fixed end of the cantilever is (2018)
- (A) 20.0 MPa
 (B) 37.5 MPa
 (C) 60.0 MPa
 (D) 75.0 MPa
28. A cylinder of radius 250mm and weight, $W = 10\text{kN}$ is rolled up an obstacle of height 50mm by applying a horizontal force P at its centre as shown in the figure. All interfaces are assumed frictionless. The minimum value of P is. (2018)

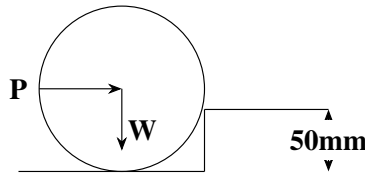


Fig. 0.1: 1

- (A) 4.5kN
 (B) 5.0kN
 (C) 6.0kN
 (D) 7.5kN
29. A plate in equilibrium is subjected to uniform stress along its edges with magnitude $\sigma_{xx} = 30\text{MPa}$ and $\sigma_{yy} = 50\text{MPa}$ as shown in the figure. The Young's Modulus of

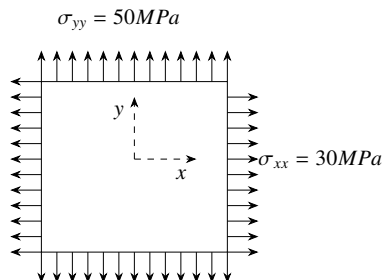


Fig. 0.2: 2

the material is $2 \times 10^{11} \frac{N}{m^2}$ and the Poissons's ratio is 0.3. If σ_{zz} is negligibly small and assumed to be zero, then the strain ϵ_{zz} is (2018)

- (A) -120×10^{-6}
- (B) -60×10^{-6}
- (C) 0.0
- (D) 120×10^{-6}

30. The figure shows a simply supported beam PQ of uniform flexural rigidity EI carrying two moments M and $2M$. The slope at P will be (2018)

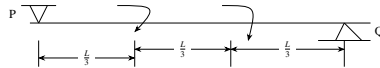


Fig. 0.3: 3

- (A) 0
- (B) $\frac{ML}{9EI}$
- (C) $\frac{ML}{6EI}$
- (D) $\frac{ML}{3EI}$

31. A $0.5m \times 0.5m$ square concrete pile is to be driven in a homogeneous clayey soil having undrained shear strength, $c_u = 50kPa$ and unit weight, $\gamma = 18.0 \frac{kN}{m^3}$. The design capacity of the pile is 500 kN. The adhesion factor α is given as 0.75. The length of the pile required for the above design load with a factor of safety of 2.0 is (2018)

- (A) 5.2m
- (B) 5.8 m
- (C) 11.8 m
- (D) 12.5 m

32. A closed tank contains 0.5 m thick layer of mercury (specific gravity = 13.6) at the bottom. A 2.0 m thick layer of water lies above the mercury layer. A 3.0 m thick layer of oil (specific gravity = 0.6) lies above the water layer. The space above the oil layer contains air under pressure. The gauge pressure at the bottom of the tank is $196.2 \frac{kN}{m^2}$. The density of water is $1000 \frac{kg}{m^3}$ and the acceleration due to gravity is $9.81 \frac{m}{s^2}$. The value of pressure in the air space is (2018)

- (A) $92.214 \frac{kN}{m^2}$
- (B) $95.644 \frac{kN}{m^2}$
- (C) $98.922 \frac{kN}{m^2}$
- (D) $99.321 \frac{kN}{m^2}$

33. A rapid sand filter comprising a number of filter beds is required to produce 99 MLD of potable water. Consider water loss during backwashing as 5%, rate of filtration as $6.0 \frac{m}{h}$ and length to width ratio of filter bed as 1.35. The width of each filter bed is to be kept equal to 5.2 m. One additional filter bed is to be provided to take care of break-down, repair and maintenance. The total number of filter beds required will be (2018)

- (A) 19
- (B) 20
- (C) 21
- (D) 22

34. A priority intersection has a single-lane one-way traffic road crossing an undivided two-lane two-way traffic road. The traffic stream speed on the single-lane road is 20 kmph and the speed on the two-lane road is 50 kmph. The perception-reaction time is 2.5 s, coefficient of longitudinal friction is 0.38 and acceleration due to gravity is 9.81 m/s^2 . A clear sight triangle has to be ensured at this intersection. The minimum lengths of the sides of the sight triangle along the two-lane road and the single-lane road, respectively will be (2018)

- (A) 50 m and 20 m
- (B) 61 m and 18 m
- (C) 111 m and 15 m
- (D) 122 m and 36 m

35. The following details refer to a closed traverse: The length and direction (whole circle

| Line | Consecutive coordinate | | | |
|------|------------------------|--------------|-------------|-------------|
| | Northing (m) | Southing (m) | Easting (m) | Westing (m) |
| PQ | — | 437 | 173 | — |
| QR | 101 | — | 558 | — |
| RS | 419 | — | — | 96 |
| SP | — | 83 | — | 634 |

TABLE 0: Consecutive coordinates for lines

bearing) of closure, respectively are (2018)

- (A) 1 m and 90°
- (B) 2 m and 90°
- (C) 1 m and 270°
- (D) 2 m and 270°

36. A square area (on the surface of the earth) with side 100 m and uniform height, appears as 1 cm^2 on a vertical aerial photograph. The topographic map shows that a contour of 650 m passes through the area. If focal length of the camera lens is 150 mm, the height from which the aerial photograph was taken, is (2018)

- (A) 800 m
- (B) 1500 m
- (C) 2150 m
- (D) 3150 m

37. The solution at $x = 1, t = 1$ of the partial differential equation $\frac{\partial^2 u}{\partial x^2} = 25 \frac{\partial^2 u}{\partial t^2}$ subject to initial conditions of $u(0) = 3x$ and $\frac{\partial u}{\partial t}(0) = 3$ is (2018)

- (A) 1
- (B) 2
- (C) 4

(D) 6

38. The solution (up to three decimal places) at $x = 1$ of the differential equation $\frac{d^2y}{dx^2} + 2\frac{dy}{dx} + y = 0$ subject to boundary conditions $y(0) = 1$ and $\frac{dy}{dx}(0) = -1$ is (2018)
39. Variation of water depth (y) in a gradually varied open channel flow is given by the first order differential equation

$$\frac{dy}{dx} = \frac{1 - e^{-\frac{10}{3} \ln y}}{250 - 45e^{-3 \ln y}}$$

Given initial condition: $y(x = 0) = 0.8m$. The depth (in m, up to three decimal places) of flow at a downstream section at $x = 1$ m from one calculation step of Single Step Euler Method is (2018)