

Multidisciplinary Design Optimization of a Series Hybrid Electric Vehicle (HEV) Powertrain

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Introduction

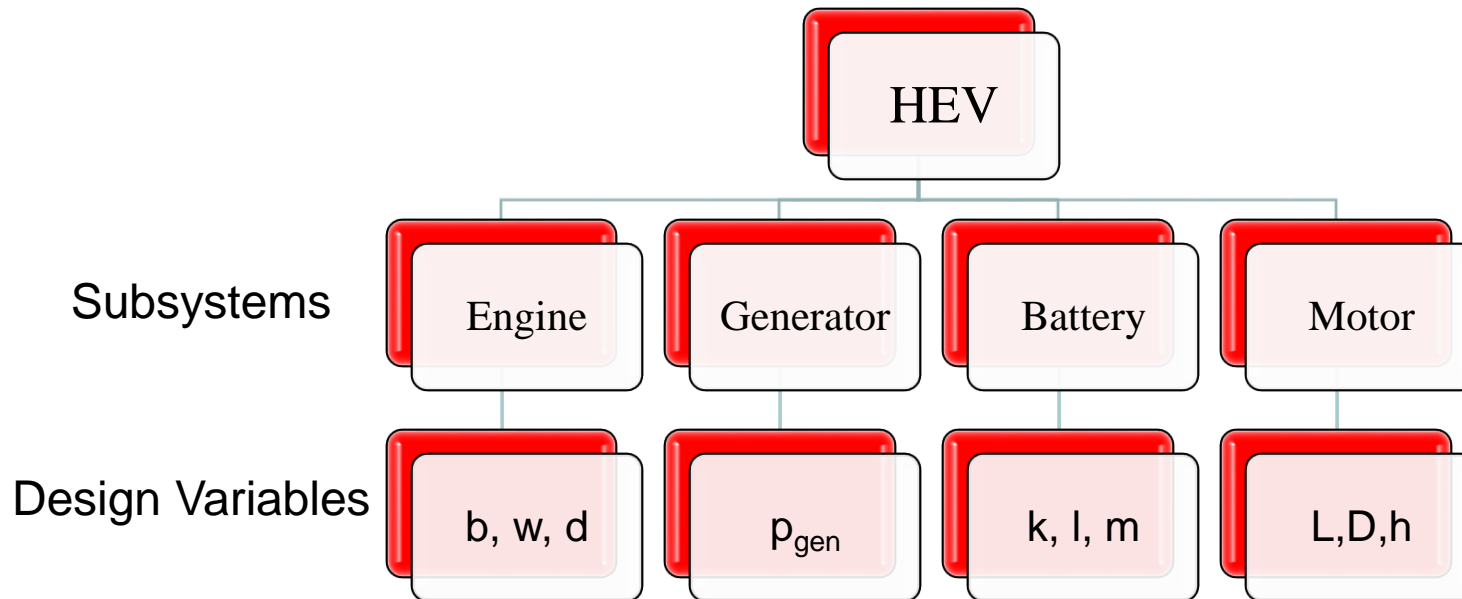
- A Hybrid Electric (HEV) is a type of vehicle that combines a conventional internal combustion engine (ICE) propulsion system with an electric propulsion system
- HEVs are becoming increasingly common among the automakers
- HEVs can reduce the fuel consumption as well as emissions
- A HEV is a large-scale, complex system in which each of the components may have a large impact on the overall performance of the system.
- A system level optimization is needed to improve the overall performance of the design.



Photo: chevrolet.com

Overall System Decomposition:

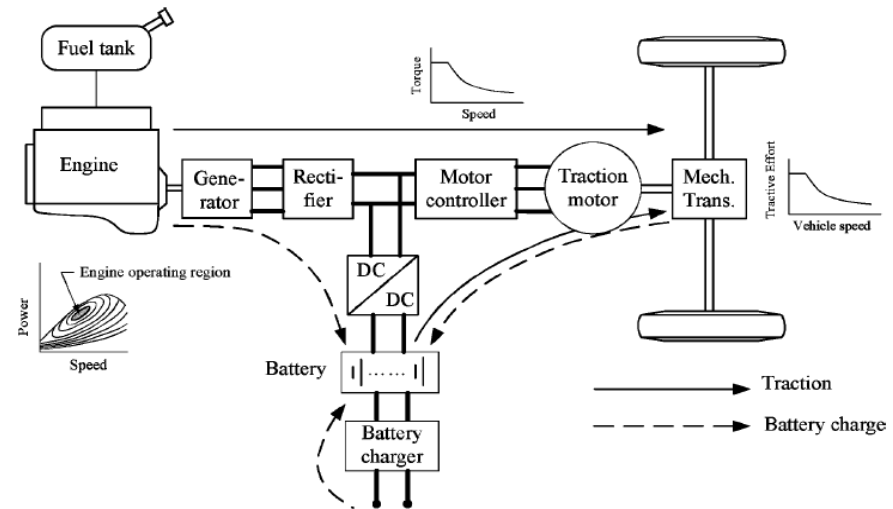
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Overall System Objective

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- **System Level Objective:**
 - Minimizing the mass of the car (motor, engine, and battery)
- **Tradeoffs:**
 - Subsystems are connected to each other through the voltage (output voltage of the generator is a function of the engine power, and voltage is the input to the motor and battery)
 - System level objective conflicts with the subsystem objective (mass of the system and power of the engine)



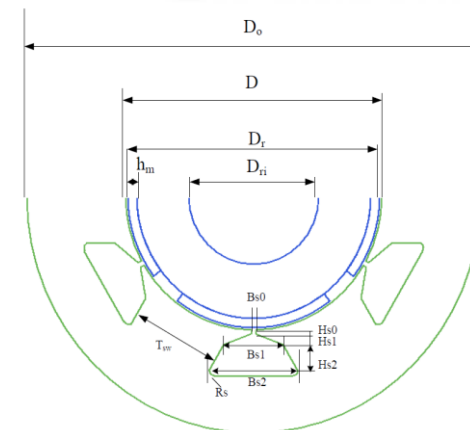
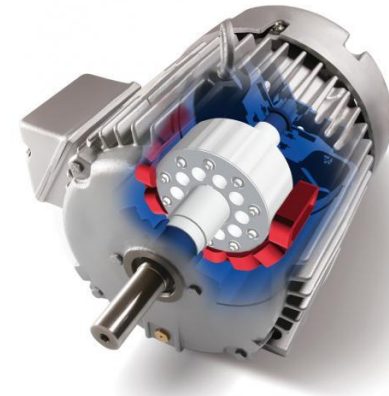
Series HEV architecture

Series hybrid electric vehicle (Ehsani, Mehrdad, Yimin Gao, and John M. Miller. "Hybrid electric vehicles: architecture and motor drives." *Proceedings of the IEEE* 95.4 (2007): 719-728.)

Subsystem: Electric Motor

- Motor Type: AC Permanent Magnet Synchronous Motor (PMSM)
- Objective: Maximizing the Efficiency while minimizing the mass and volume
- Challenges: Complicated equations, large number of design variables, effect of topology on the performance of the system, and nonlinearities.

AC permanent-magnet motor cutaway



SMPM machine geometry parameters

Subsystem: Electric Motor

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Objective:

$$\min f = 0.33 * mass + 0.33 * (1 - eff) + 0.33 * Vol$$

s.t:

$$g1: D - 300 \leq 0$$

$$g2: L - 200 \leq 0$$

$$g3: h_m - 12 \leq 0$$

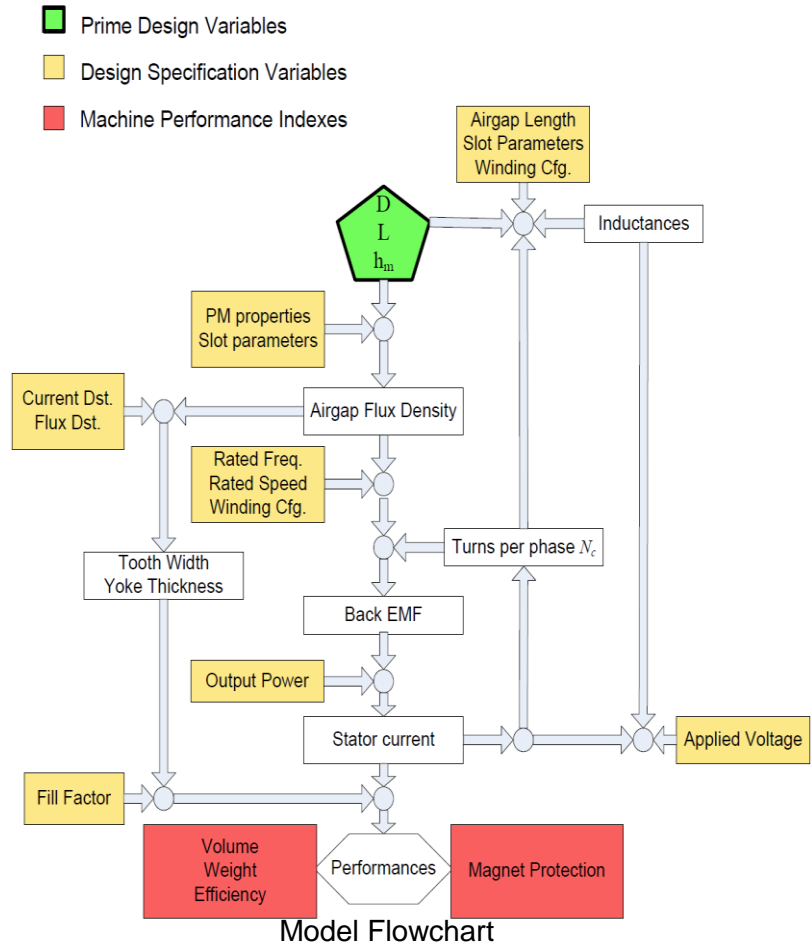
$$g4: -D \leq 0$$

$$g5: -L \leq 0$$

$$g6: -h_m \leq 0$$

Design Variables	
D	Stator diameter on the airgap side
L	machine axial length
h	thickness of the permanent magnet in the radial direction

Design Parameter	Chosen Value
Slot opening B_{s0}	2mm
Slot tip height H_{s0}	1mm
Steel lamination factor	1
Slot fill factor	40%
Power	15000 w
Air gap	1mm



Subsystem: Electric Motor

Monotonicity Analysis

	D	L	h_m
f	N/A	N/A	N/A
g1	+	NA	NA
g2	NA	+	NA
g3	NA	NA	+
g4	-	0	0
g5	0	-	0
g6	0	0	-

By MP2: g1 and g4 are active w.r.t D

By MP2: g2 and g5 are active w.r.t L

By MP2: g3 and g6 are active w.r.t h_m

Results:

Numerical methods used in the model to solve and find some of the unknowns. As a result a derivative free algorithm (PSO) was implemented to solve the Optimization problem.

Design Variables	Optimum Value	Objective Function	Optimum Value
D(mm)	112	Weight(kg)	36.5
L(mm)	90.7	Eff	95.7%
h_m (mm)	5.6	Volume	0.0047
		Output Equation (objective)	91.2

Optimal design found by PSO

Summary Model- Subsystem: Battery

Minimize (f) $W_{pack} = k * n * m * w_{cell}$

Subject to (g₁) $201 - k * n * 1.2 \leq 0$

(g₂) $6500 - m * 232 \leq 0$

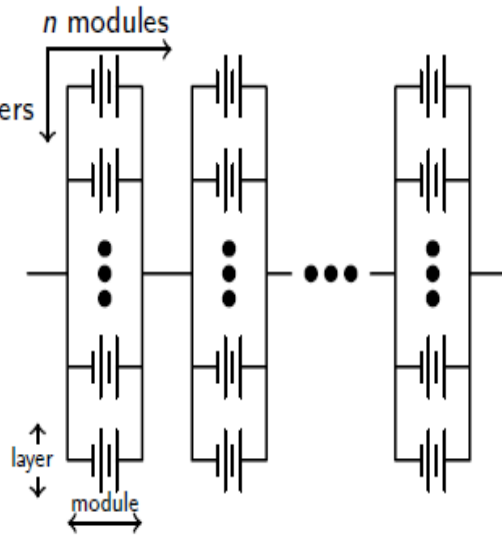
(g₃) $38.15 - k * n * m * 0.2784 \leq 0$

Design Variables:

k – number of cells
in series per
module

n – number of
modules

m – number of
layers



g1: $V_{pack} = n * k * V_{cell}$ (voltage constraint)

g2: $I_{pack} = m * I_{cell}$ (current constraint)

g3: $P_{pack} = V_{pack} * I_{pack}$ (power constraint)

Design Parameters

w_{cell} – weight of each cell

V_{cell} – Output Voltage of individual cell

I_{cell} – Current rating of individual cell

P_{pack} – Output power of battery pack

W_{pack} – weight of battery pack

V_{pack} – Output Voltage of battery pack

I_{pack} – Current rating of battery pack

Variables=3 # Constraints=3

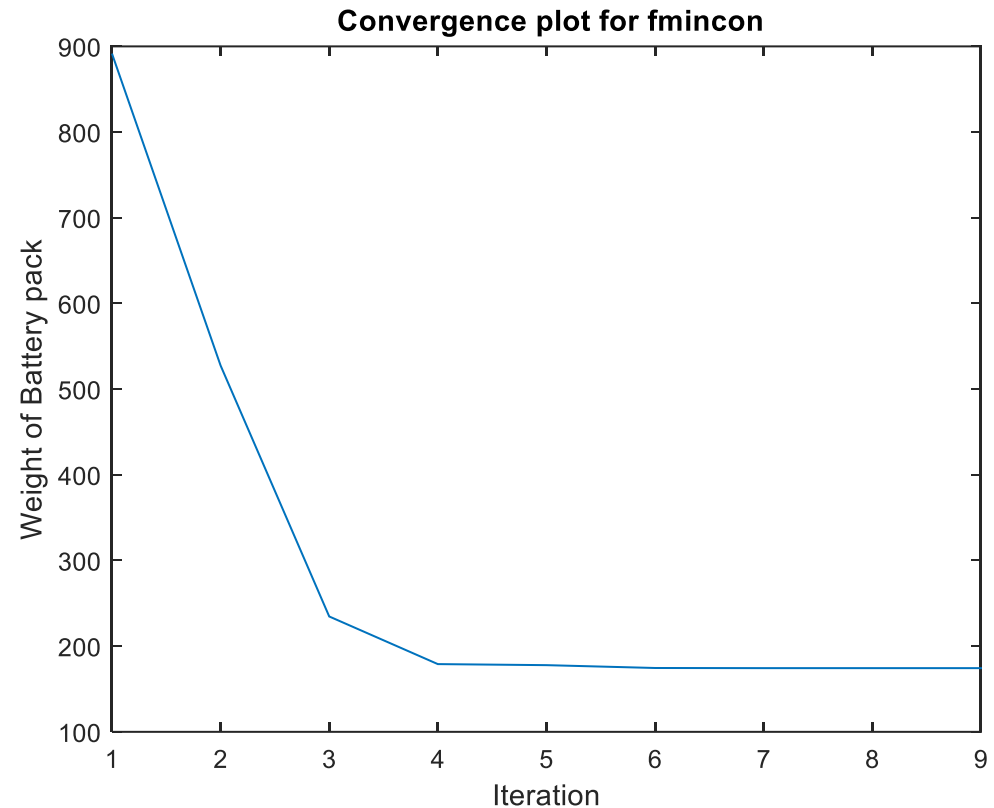
Xue, Nansi, et al. "Design of a lithium-ion battery pack for PHEV using a hybrid optimization method." *Applied Energy* 115 (2014): 591-602.

Solution Process- Subsystem: Battery

	k	n	m
f	+	+	+
g_1	-	-	X
g_2	X	X	-
g_3	-	-	-

Monotonicity Table

- Function is always increasing, but constraints are decreasing, so problem is well bounded.
- Potentially all constraints can be active, but difficult to say which is dominant.
- Used fmincon to obtain solution.



	k	m	n	W
Initial	40	40	15	891.6
Final (Optimum)	13	13	28	175.79

Summary Model- Subsystem: Engine

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Objective

$$\min_{b, w, dI} f(b, w, dI) = K_0 * w * [p_{me} - P_0 * \eta_t \eta_v]$$

Constraints

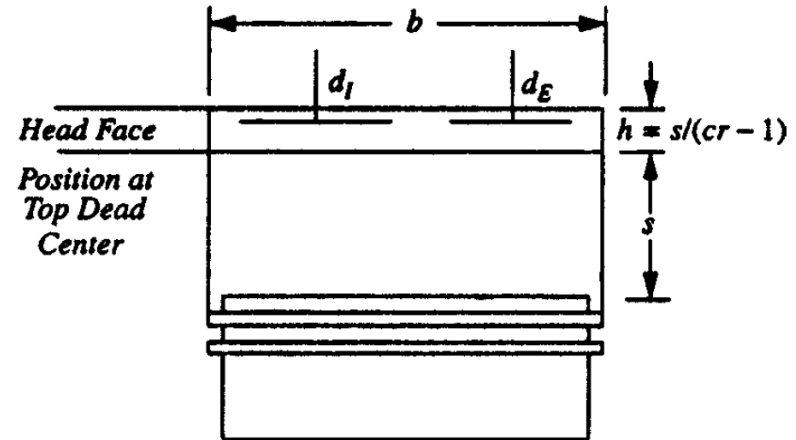
$$g_1(b) = b - P_1 < 0$$

$$g_2(w, dI) = P_3 * w - dI^2 < 0$$

$$g_3(w) = w - K_7 < 0$$

$$g_4(cr, b) = cr - 13.2 + 0.045 * b < 0$$

$$g_5(dI) = K_4 * dI - 30 < 0$$



Multidisciplinary Robust Design Optimization of an Internal Combustion Engine, Charles D. McAllister, Timothy W. Simpson, Vol. 12, MARCH 2003, ASME.

Variables (3):

Cylinder Bore, Engine rpm, Intake valve diameter

Parameters

$$P_0 = \rho * \frac{Q}{A_f}$$

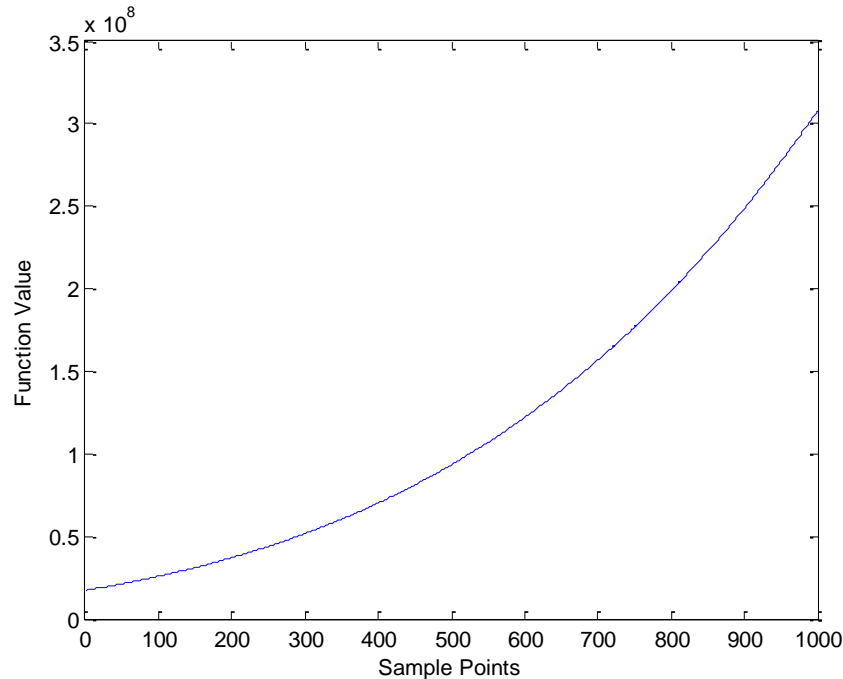
$$P_1 = \frac{L_1}{K_1} * N_c$$

$$P_2 = 9.428 * 10^{-5} \left(4 \frac{V}{\pi} N_c \right) K_6 C_s$$

Design Variable	Lower Bound	Upper Bound
b (cylinder bore)	70 mm	90 mm
dI (intake valve diameter)	25 mm	50 mm
w (rpm at peak power)	5000 rpm	12000 rpm

Subsystem: Engine

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	b	dI	w
f	+	N/A	+
g1	+	N/A	N/A
g3	N/A	-	+
g4	N/A	N/A	+
g5	+	N/A	N/A
g6	N/A	+	N/A

SQP fmincon implemented for optimization study.

$w = 6061$ rpm, $b = 36.1$ mm, $dI = 76.9$ mm,
Power = 173 kW, Mass = 104.1261 kg

System Level

Objective:

Minimize (f) $M = M_E + M_B + M_M$

Subject to (g1) $100 \leq V_{Gen} \leq 300$
and all subsystem constraints for
engine, battery and motor

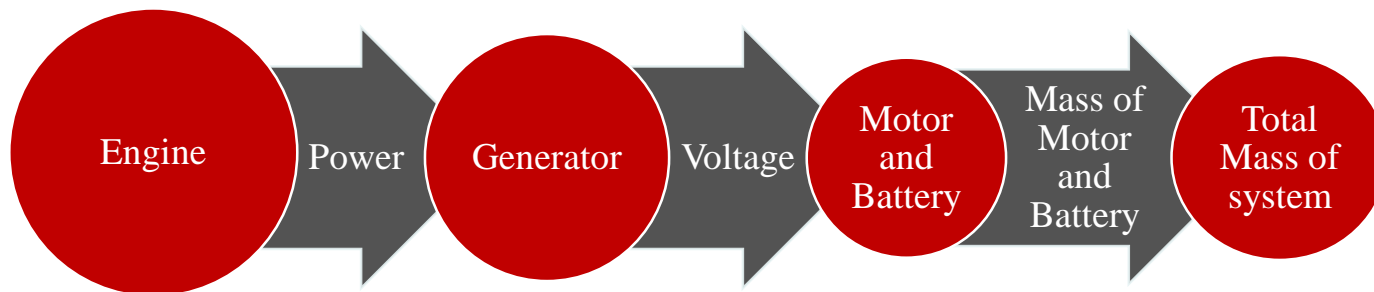
Design Variables:

M_E Mass of Engine

M_B Mass of Battery

M_M Mass of Motor

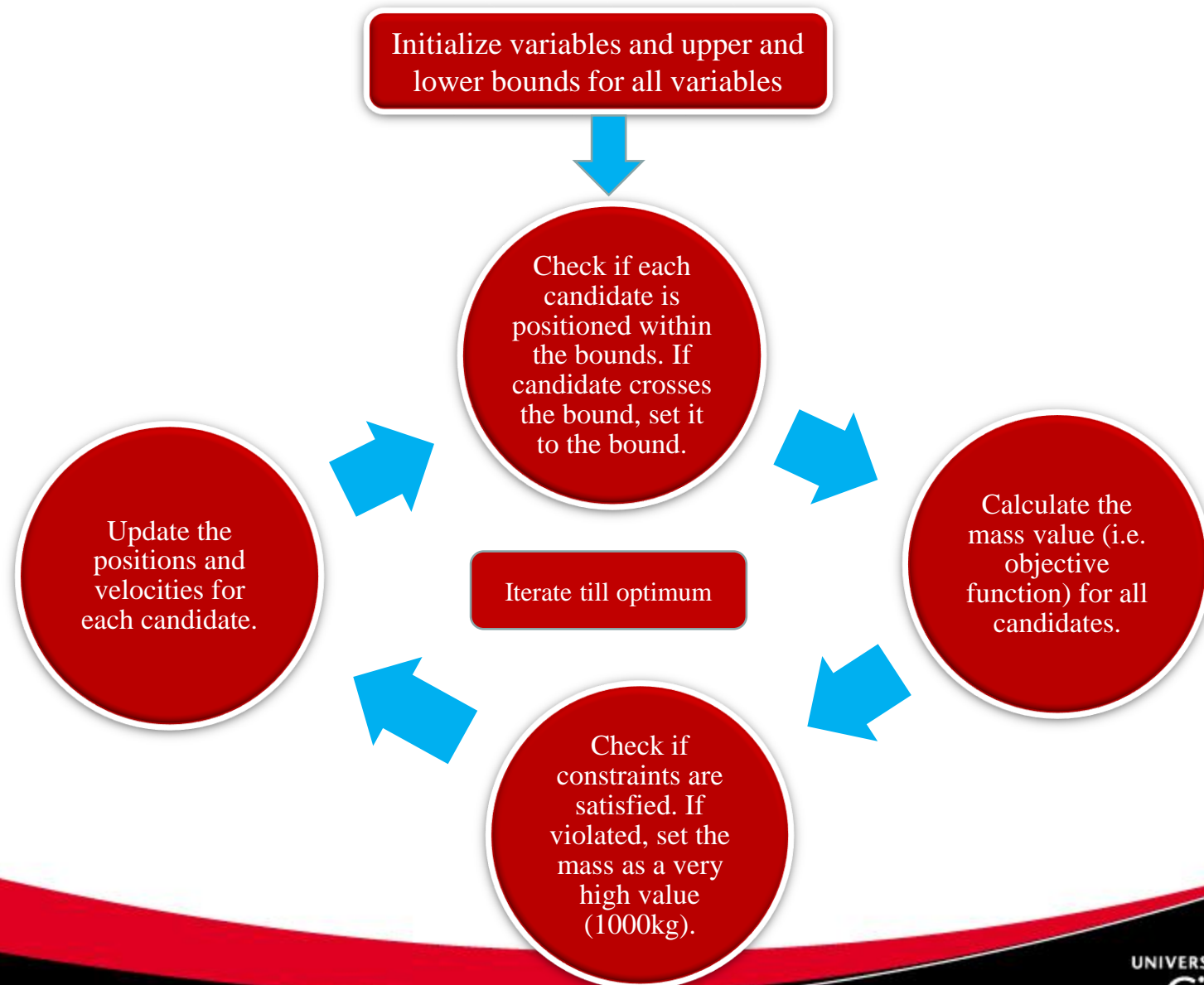
Variables=10, # Constraints=2, and all variables have bounds



System level design flowchart

PSO Algorithm:

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System Level Results:

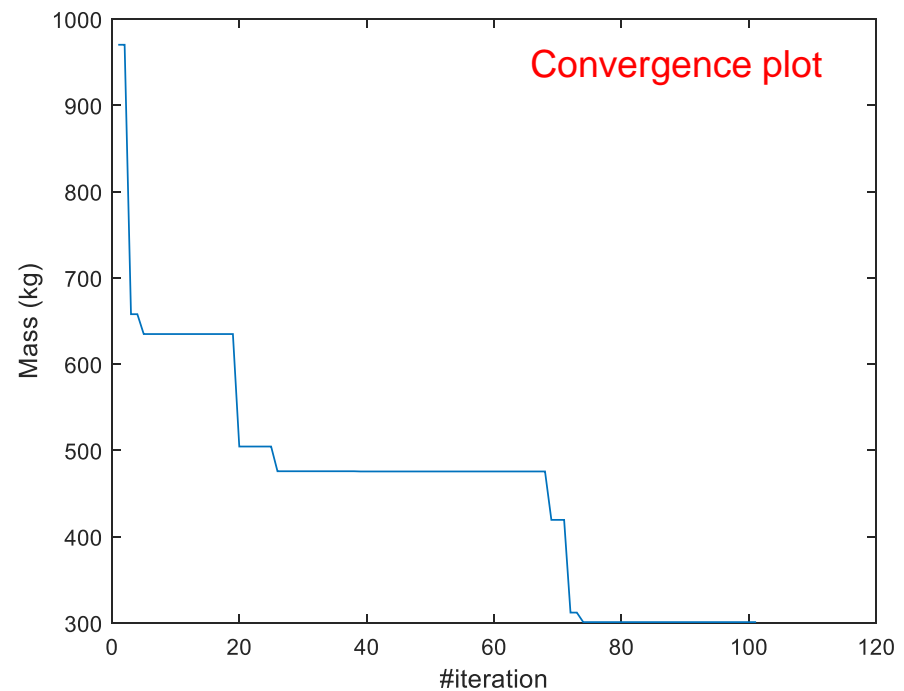
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w	b	di	k	l	m	D	lst	h	Nc	Mass
5000	31.02	87.64	10	10	31	144.83	73.08	11.43	30	249.65
6061	36.1	76.9	13	13	28	112	90.6	5.6	72	316.41

Optimal design variables and objective

Trial	Mass
1	249.64
2	257.26
3	214.09
4	253.68
5	218.48
Mean	238.63
SD	20.63

Optimal mass over iterations



Key Learnings:

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- How to break down a complex system into subsystems
- How to optimize a complex system
- Importance of the linking variables on the overall system's objective
- The conflicts that the subsystem objectives may have with the overall system objective
- Using the penalty function