

Question 11.16.3.64

Probability and Random Processes

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You are given that A and B are two events such that $\Pr(B) = \frac{3}{5}$, $\Pr(A|B) = \frac{1}{2}$ and $\Pr(A + B) = \frac{4}{5}$, then $\Pr(A)$ equals

Solution:

$$\Pr(A|B) = \frac{1}{2} \quad (1)$$

$$\frac{\Pr(AB)}{\Pr(B)} = \frac{1}{2} \quad (2)$$

$$\Pr(AB) = \frac{\Pr(B)}{2} \quad (3)$$

$$= \frac{3}{10} \quad (4)$$

$$\Pr(A + B) = \frac{4}{5} \quad (5)$$

$$\Pr(A) + \Pr(B) - \Pr(AB) = \frac{4}{5} \quad (6)$$

Substitute $\Pr(AB)$ from (??)

$$\Pr(A) = \frac{4}{5} - \Pr(B) + \Pr(AB) \quad (7)$$

$$= \frac{4}{5} - \frac{3}{5} + \frac{3}{10} \quad (8)$$

$$= \frac{1}{2} \quad (9)$$