

For a Geometric progression defined as follows

$$x[n] = x[0] r^n \quad (1)$$

$$X(z) = \sum_{n=-\infty}^{\infty} x[n] z^{-n} \quad (2)$$

$$= \sum_{n=0}^{\infty} x[0] r^n z^{-n} \quad (3)$$

$$= \sum_{n=0}^{\infty} x[0] (rz^{-1})^n \quad (4)$$

For $|rz^{-1}| < 1$

$$X(z) = \frac{x[0]}{1 - rz^{-1}} \quad (5)$$