Heuristic Search

Outline

- Generate-and-test
- Hill climbing
- Simulated annealing
- Best-first search
- Means-ends analysis
- Constraint satisfaction

Algorithm

- 1. Generate a possible solution.
- 2. Test to see if this is actually a solution.
- 3. Quit if a solution has been found. Otherwise, return to step 1.

- Acceptable for simple problems.
- Inefficient for problems with large space.

- Exhaustive generate-and-test.
- Heuristic generate-and-test: not consider paths that seem unlikely to lead to a solution.
- Plan generate-test:
 - Create a list of candidates.
 - Apply generate-and-test to that list.

Example: coloured blocks

"Arrange four 6-sided cubes in a row, with each side of each cube painted one of four colours, such that on all four sides of the row one block face of each colour is showing."

Example: coloured blocks

Heuristic: if there are more red faces than other colours then, when placing a block with several red faces, use few of them as possible as outside faces.

Hill Climbing

• Searching for a goal state = Climbing to the top of a hill

Hill Climbing

- Generate-and-test + direction to move.
- Heuristic function to estimate how close a given state is to a goal state.

Algorithm

- 1. Evaluate the initial state.
- Loop until a solution is found or there are no new operators left to be applied:
 - Select and apply a new operator
 - Evaluate the new state:

```
goal \rightarrow quit
```

better than current state → new current state

Algorithm

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goal \rightarrow quit
```

better than current state → new current state

not try all possible new states!

Example: coloured blocks

<u>Heuristic function</u>: the sum of the number of different colours on each of the four sides (solution = 16).

 Heuristic function as a way to inject task-specific knowledge into the control process.

Steepest-Ascent Hill Climbing (Gradient Search)

- Considers all the moves from the current state.
- Selects the best one as the next state.

Steepest-Ascent Hill Climbing (Gradient Search)

Algorithm

- 1. Evaluate the initial state.
- 2. Loop until a solution is found or a complete iteration produces no change to current state:
 - Apply all the possible operators
 - Evaluate the best new

```
state: goal → quit
better than current
state → new current
state
```

Steepest-Ascent Hill Climbing (Gradient Search)

Algorithm

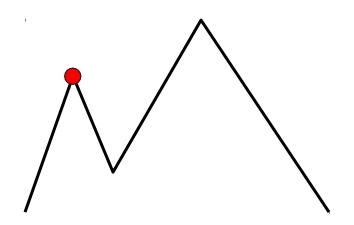
- 1. Evaluate the initial state.
- Loop until a solution is found or a complete iteration produces no change to current state:
 - SUCC = a state such that any possible successor of the current state will be better than SUCC (the worst state).
 - For each operator that applies to the current state, evaluate the new state:

```
goal \rightarrow quit better than SUCC \rightarrow set SUCC to this state
```

- SUCC is better than the current state → set the new current

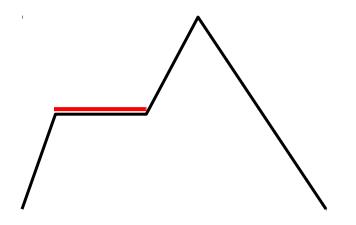
Local maximum

A state that is better than all of its neighbours, but not better than some other states far away.



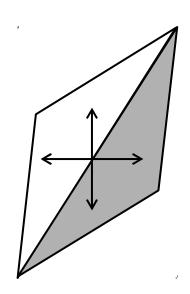
Plateau

A flat area of the search space in which all neighbouring states have the same value.



Ridge

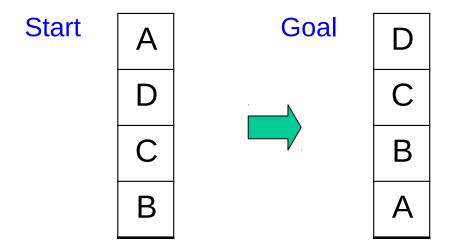
The orientation of the high region, compared to the set of available moves, makes it impossible to climb up. However, two moves executed serially may increase the height.

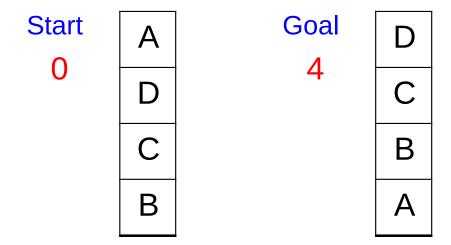


Ways Out

- Backtrack to some earlier node and try going in a different direction.
- Make a big jump to try to get in a new section.
- Moving in several directions at once.

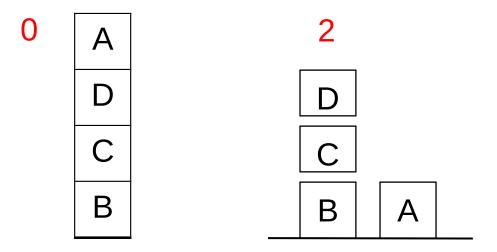
- Hill climbing is a local method:
 Decides what to do next by looking only at the "immediate" consequences of its choices.
- Global information might be encoded in heuristic functions.

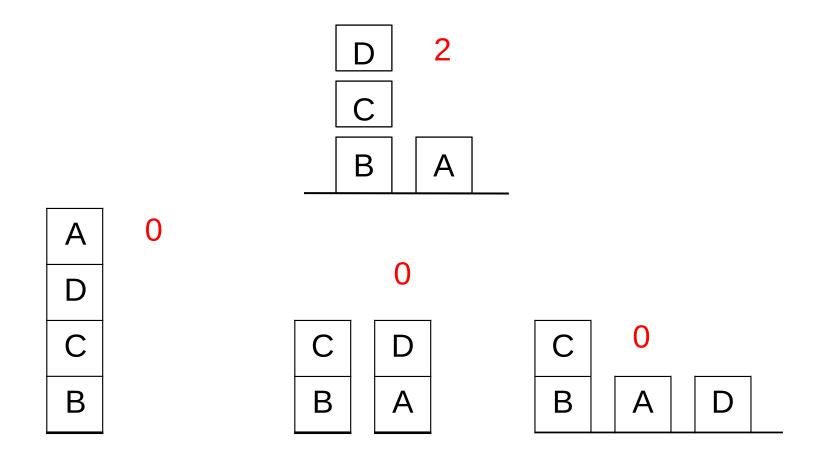


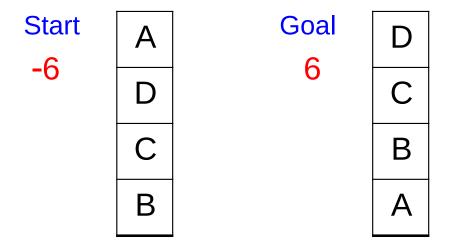


Local heuristic:

- +1 for each block that is resting on the thing it is supposed to be resting on.
- -1 for each block that is resting on a wrong thing.



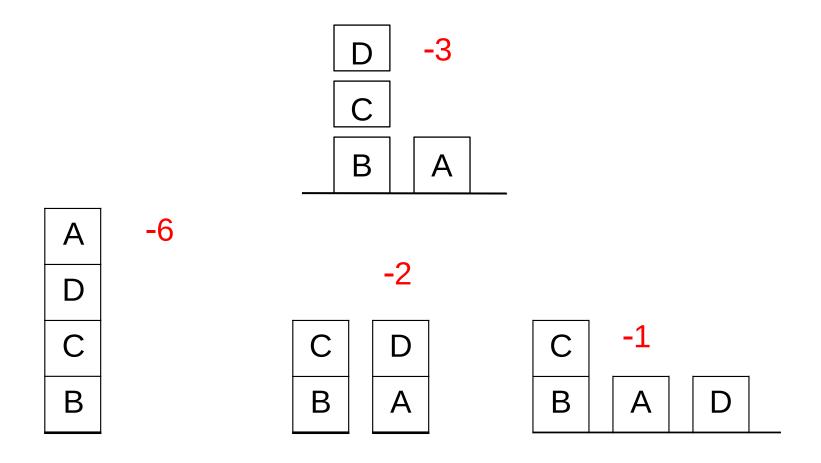




Global heuristic:

For each block that has the correct support structure: +1 to every block in the support structure.

For each block that has a wrong support structure: -1 to every block in the support structure.



Hill Climbing: Conclusion

- Can be very inefficient in a large, rough problem space.
- Global heuristic may have to pay for computational complexity.
- Often useful when combined with other methods, getting it started right in the right general neighbourhood.

• A variation of hill climbing in which, at the beginning of the process, some downhill moves may be made.

- To do enough exploration of the whole space early on, so that the final solution is relatively insensitive to the starting state.
- Lowering the chances of getting caught at a local maximum, or plateau, or a ridge.

Physical Annealing

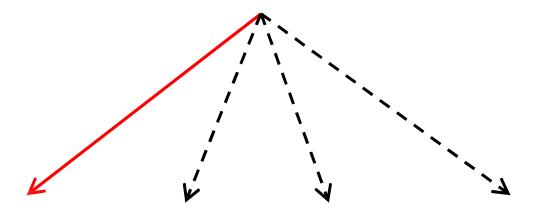
- Physical substances are melted and then gradually cooled until some solid state is reached.
- The goal is to produce a minimal-energy state.
- Annealing schedule: if the temperature is lowered sufficiently slowly, then the goal will be attained.
- Nevertheless, there is some probability for a transition to a higher energy state: $e^{-\Delta E/kT}$.

Algorithm

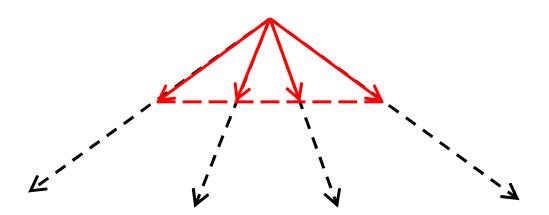
- 1. Evaluate the initial state.
- 2. Loop until a solution is found or there are no new operators left to be applied:
 - Set T according to an annealing schedule
 - Selects and applies a new operator
 - Evaluate the new state:

```
goal \rightarrow quit \Delta E = Val(current state) - Val(new state) \Delta E < 0 \rightarrow new current state else \rightarrow new current state with probability e^{-\Delta E/kT}.
```

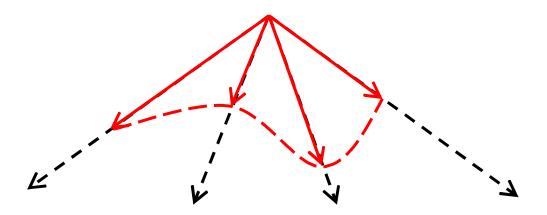
- Depth-first search:
 - Pro: not having to expand all competing branches
 - Con: getting trapped on dead-end paths

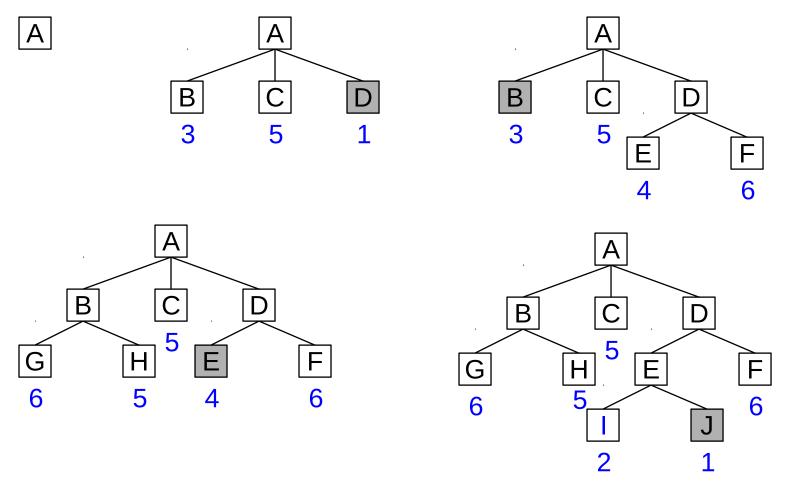


- Breadth-first search:
 - Pro: not getting trapped on dead-end paths
 - Con: having to expand all competing branches



⇒ Combining the two is to follow a single path at a time, but switch paths whenever some competing path looks more promising than the current one.





 OPEN: nodes that have been generated, but have not examined.

This is organized as a priority queue.

CLOSED: nodes that have already been examined.

Whenever a new node is generated, check whether it has been generated before.

Algorithm

- 1. OPEN = {initial state}.
- Loop until a goal is found or there are no nodes left in OPEN:
 - Pick the best node in OPEN
 - Generate its successors
 - For each successor:

new \rightarrow evaluate it, add it to OPEN, record its parent generated before \rightarrow change parent, update successors

• Greedy search:

h(n) = cost of the cheapest path from node n to a goal state.

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- Uniform-cost search:
 - g(n) = cost of the cheapest path from the initial state to node n.

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Neither optimal nor complete

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Neither optimal nor complete

- Uniform-cost search:
 - g(n) = cost of the cheapest path from the initial state to node n.

Optimal and complete, but very inefficient

• Algorithm A* (Hart et al., 1968):

$$f(n) = g(n) + h(n)$$

- h(n) = cost of the cheapest path from node n to a goal state.
- g(n) = cost of the cheapest path from the initial state to node n.

Algorithm A*:

$$f^*(n) = g^*(n) + h^*(n)$$
 $h^*(n)$ (heuristic factor) = estimate of
 $h(n)$.

 $g^*(n)$ (depth factor) = approximation of $g(n)$ found by A^* so far.