PySQUID, a Statistical Analysis and Optimization Tool for Bi-SQUID Circuits

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**Abstract**. Start your abstract here…

1. Introduction

Today, DC SQUIDs are extensively used in applications as sensitive magnetometers such as microscopy, readout electronics, nondestructive test, biomagnetism applications. [1] DC SQUID consists parallel Josephson Junction in superconductive loop. (Figure 1) DC SQUID’s voltage response against external applied magnetic field is non-linear, this situation may cause difficulties in application and limit the dynamic range of sensor. (Figure XX) As a result, researchers tend to investigate DC SQUID based circuits, which is more linear than conventional DC SQUIDs (Bi-SQUID, arrays of SQUIDs, …, etc.). Bi-SQUID is one of the alternative solutions. Instead of the conventional DC SQUID, Bi-SQUID is designed by adding a parallel Josephson junction to typical DC SQUID. (Figure 1) Bi-SQUID ‘s voltage response against external applied magnetic field is more linear than DC SQUID. [2](Figure YY)

External applied magnetic field response of Bi-SQUID characterized by set of differential equations, there is no easy analytic way to solve these equations. [3] Therefore, numerical analysis plays critical role for this type of systems. Modelling and simulation tools can support design studies by using numerical methods. However, there is no viable modelling and simulation library/application exist for Bi-SQUIDs. Thus, we developed an open-source and user-friendly statistical analysis tool for SQUIDs/Bi-SQUIDs.

JSim,

We developed an open-source and user-friendly statistical analysis tool for SQUIDs/Bi-SQUIDs.  PySQUID is an open-source and user-friendly statistical analysis tool for SQUIDs/Bi-SQUIDs.  Our Python library gives the average voltage response of SQUID/Bi-SQUID for each corresponding normalized applied external magnetic flux as an output. The normalized applied external magnetic flux range can be determined by the user. Moreover, our simulation tool provides multiple runs for the statistical analysis of Bi-SQUID. Users can determine margin and data range for one of the input parameters, and the tool generates gaussian distributed random numbers in a specific margin and data range for the said parameter. After that, the voltage response in an external applied magnetic field is achieved in the defined margin. These output sets, provide a wide range of design options to the user who can easily observe a reliable working range of Bi-SQUID circuits and can optimize Bi-SQUID design problems by using this output dataset.

Diagram

Description automatically generated with medium confidence

**Figure 1** SQUID (left) and Bi-SQUID (right).

1. Theory and Methodology

## Theory

Figure XX shows Bi-SQUID circuit representation with applied external magnetic field and normalized bias current (ib = Ib/Ic). We assumed that , Ic = Ic1 = Ic2.We can represent normalized currents flow through Josephson Junctions by using RCSJ model. [4]

Diagram, schematic

Description automatically generated

Figure Bi-SQUID circuit representation.

## Methodology

## Algorithm

1. PySQUID Features

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## Library Organization

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1. Results
2. Conclusion
3. Anknowledgeemnt

The circuits are fabricated in the clean room for analog-digital superconductivity (CRAVITY), AIST.

References

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1. A reference

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1. Another reference
2. More references