Assignment 2

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Question:

Without expanding at any stage , find the value of :

$$\begin{vmatrix} a & b & c \\ a+2x & b+2y & c+2z \\ x & y & z \end{vmatrix}$$
 (1)

Solution:

Let the given Determinant be

$$M = \begin{vmatrix} a & b & c \\ a + 2x & b + 2y & c + 2z \\ x & y & z \end{vmatrix}$$
 (2)

First we use Row operation on R_2 , $R_2 \to R_2 - 2R_3$

$$\Rightarrow M = \begin{vmatrix} a & b & c \\ a & b & c \\ x & y & z \end{vmatrix}$$
 (3)

Clearly from (3) in Determinant M , R_1 and R_2 are identical

$$\therefore M = \begin{vmatrix} a & b & c \\ a+2x & b+2y & c+2z \\ x & y & z \end{vmatrix} = 0 \qquad (4)$$