

# Compilation of Quantum Programs with Control Flow Primitives in Superposition

**Master Thesis** 

05.02.25

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#### Introduction

#### Introduction

- Idea of Quantum control flow first used by [Altenkirch and Grattage, 2005].
- Later, it was defined by [Ying et al., 2012].
- Most languages focus on classical control flow.
- Only recently, Quantum Control Machine, proposed by [Yuan et al., 2024].
  - An instruction set architecture.
  - Allows for quantum control flow with an assembly-like syntax.
  - Low-level design of the architecture and syntax  $\rightarrow$  complex programs.
- ⇒ Build upon the ideas, define a high-level quantum language with quantum control flow.
- ⇒ Plan to implement a compiler for it.

#### **Quantum Control Flow**

- First used by [Altenkirch and Grattage, 2005] to define functional programming language.
- For example, used to define Hadamard gate as function had:

```
had: Q \rightarrow Q
had: x \mapsto if^{\circ}x
then \{false \mid -true\}
else \{false \mid true\}
```

- Later, formally defined by [Ying et al., 2012].
- Allows for the execution of functions based on values in superposition.
- Results in superposition of the results of individual executions.

## Limitations — Reversibility

- Mainly limited by two principles: reversibility and synchronization.
- Instructions required to be reversible, as they are unitary transformations.
- ⇒ Control flow, as implemented in classical computers, not possible.
  - Landauer Embedding [Landauer, 1961] seems to offer solution.
  - Can make non-reversible function  $f: D \to D'$  reversible by outputting input value.
  - Result is  $g: D \to D' \times D$  with g(x) = (f(x), x).
  - However, output includes program history and the result depends on the history, they become entangled.
  - Leads to disruptive entanglement, invalid results [Yuan et al., 2024].

#### **Limitations** — Synchronization

- Program counter may become entangled with data.
- ⇒ Disruptive entanglement.
  - The principle of synchronization: Control flow must become independent from the data.
  - Program may include padding operations to ensure synchronization.
- ⇒ Loops cannot depend solely on value in superposition.
- ⇒ Instead, a loop must be bounded by classical value [Yuan et al., 2024].

#### **Quantum Control Machine**

- Quantum Control Machine (QCM), proposed by [Yuan et al., 2024]
- Focused on quantum control flow.
- Syntax and logic similar to classical assembly language
- Employs a branch control register bcr to enable reversible jumps.
- Instead of increasing IP by 1 after statement, increased by value of bcr.
- The bcr can then be reversibly modified.
  - To jump by 5, the bcr increased by 5
  - At its destination, decreased by 5 again.

#### Instructions

- Here, some instructions of the QCM are listed.
- For every instruction there exists a reversed instruction, e.g., radd is the subtraction operation.

Operation	Syntax	Semantics <sup>1</sup>	
No-op	nop	Only increases instruction pointer by the	
		bcr.	
Addition	add <i>ra rb</i>	Adds register <i>rb</i> to <i>ra</i> .	
Multiplication	mul <i>ra rb</i>	Multiplies register <i>ra</i> by <i>rb</i> .	
Jump	jmp <b>p</b>	Increases <i>bcr</i> by <i>p</i> .	
Conditional Jumps	jz <b>p ra</b>	Increases <i>bcr</i> by <i>p</i> if <i>ra</i> is 0.	
	jne <i>p ra rb</i>	Increases $bcr$ by $p$ if $ra$ is not equal to $rb$ .	

<sup>&</sup>lt;sup>1</sup> After all operations, the instruction pointer is increased by the value of the *bcr*.

An excerpt of the QCM instruction set with instructions used in later examples.

# (Non-) Reversible Example

- Example of a classical program and the reversible equivalent.
- Both programs calculate  $x^y$ .
- Neither are synchronized because loop is not bound by classical value.

```
add res $1
add r1 y
all: jz l2 r1
mul res x
radd r1 $1
jmp l1
rl2: nop
```

 $\label{lem:constraint} A \ non-reversible \ exponentiation \ algorithm.$ 

```
add res $1
add r1 y
all: rjne rl1 r1 y
rl2: jz l2 r1
mul res x
radd r1 $1
rl1: jmp l1
all: rjmp l2
```

A reversible exponentiation algorithm.

# **Reversible Synchronized Example**

- Synchronized implementation, calculating  $x^{\min y, \max}$ .
- *max* is a classical bound for loop.
- Line 9 includes padding instruction.

```
add
                     $1
               res
         add
               r1
                    max
3 11:
     rjne
               rl1
                    r1
                         max
4 rl2:
               12
         İΖ
                  r1
5 rl3:
         jg 13 r1
                        У
         mul res
7 r 1 4 :
               14
         jmp
8 13:
               rl3
         rjmp
                              ; padding
         nop
10 14:
         rile
               rl4
                    r1 v
         radd
               r1
                     $1
12 rl1:
         qmţ
         rjmp rl2
13 12:
```

A synchronized, reversible exponentiation algorithm.

#### **Language Overview**

- Idea for language: Provide high-level language with the capabilities of the QCM.
- Want to remove low-level concepts, add high-level ones.
- Jump instructions in superposition are removed → need to add other control flow primitives.
- Introduce multiple high-level concepts and control flow statements:
  - blocks and scopes,
  - different data types,
  - composite gates,
  - loop statements, unrolled at compile time, and
  - quantum if- and else-statements.

#### **Syntax**

- Define *CFG*<sub>Luie</sub> for our language.
- Start symbol is the program, consisting of gate declarations and a block.
- A block is a list of translatables, either statements or declarations.

```
egin{aligned} 	extit{CFG}_{	extit{Luie}} &= \left( 	extit{V}_{	extit{Luie}}, 	extit{\Sigma}_{	extit{Luie}}, 	extit{R}_{	extit{Luie}}, 	extit{prg}_{	extit{Luie}}, \dots 
ight) \ 	extit{V}_{	extit{Luie}} &= \left\{ egin{aligned} &: &: & \text{range}, \ (,), \dots 
ight\} \end{aligned} \ 	extit{Program} : & prg_{	extit{Luie}} & :: & = gDcl_1 \dots gDcl_n \ blk \ & blk \ & blk \ & :: & = t_1 \dots t_n \ \mid & \epsilon \end{aligned}
```

An example Luie program.

#### **Syntax**

- Three different statements: quantum if-statement, a loop statement, gate application.
- To combine qubit or register access: qubit argument.
- Expressions for numeric values or ranges.
- Fix set of defined gates → differentiate translations.

```
1 gate c_h_reg(control, reg) do
2  /* If-Statement */
3  qif control do
4  /* Loop Stat. | Expression */
5  for i in range(sizeof(reg)) do
6  /* Expression */
7  h reg[i];
8  end
9  end
10 end
11
12 const regSize : int = 3;
13 qubit c;
14 qubit[regSize] a;
15 c_h_reg c, a; // Gate Application
16  /* Dubit Argument */
```

An example Luie program.

#### Symbol Table

- Saves symbol information relevant for translation.
- Contains four types of symbols:
  - 1. named constants,
  - 2. quantum registers and qubits,
  - 3. qubit arguments, and
  - 4. composite gates.

```
Symbol Table := \{st \mid st : Identifier \dashrightarrow (\{const\} \times \mathbb{Q}) \\ \cup (\{qubit\} \times \mathbb{N} \times Identifier) \\ \cup (\{arg\} \times Qubit Argument) \\ \cup (\{gate\} \times Block \times Identifier^+)\}
```

#### Translation Function and Block Translation

- trans function translates program.
- Symbol table updated with gate declaration by up function.
- Block translation bt translates all translatables.
- Updates symbol table used in next translation.

```
st_1 = up(st_\epsilon, 	ext{gate c_h\_reg}...) = [c_h\_reg \mapsto (	ext{gate}, 	ext{qif control do}..., 	ext{control}, 	ext{reg})]
bt(	ext{const regSize}..., st_1) = tr_1 \qquad \text{where } (tr_1, st_2) = tt(	ext{const regSize}: 	ext{int} = 3;, st_1)
tr_2 \qquad \text{where } (tr_2, st_3) = tt(	ext{qubit c};, st_2)
tr_3 \qquad \text{where } (tr_3, st_4) = tt(	ext{qubit [regSize}] \text{ a};, st_3)
tr_4 \qquad \text{where } (tr_4, \_) = tt(	ext{c\_h\_reg c}, \text{ a};, st_4)
```

#### Translatable and Declaration Translation

- tt translates each translatable, differentiates between declaration and command.
- Declarations translated by dt.
- Update symbol table → function returns (updated) symbol table.
- Language allows for different variable scopes → same identifier can be used multiple times.
- ⇒ Unique identifier *uid* is generated for translation.

```
 \begin{split} tt(\texttt{c\_h\_reg c, a;}, st) &= (ct(\texttt{c\_h\_reg c, a;}, st), st) \\ tt(\texttt{qubit c;}, st) &= dt(\texttt{qubit c;}, st) \\ dt(\texttt{qubit c;}, st) &= (\texttt{qubit uid}_c;, up(st, \texttt{qubit c;})) \\ up(st, \texttt{qubit c;}) &= st[\texttt{c} \mapsto (\texttt{qubit}, 1, uid_c)] \end{split}
```

#### **Command Translation**

- Commands are translated with ct.
- Argument translation qt used to differentiate between qubits and register accesses, get uid.
- control adds the translated qArg as guard to all gate applications in translation.

$$st = [c \mapsto (qubit, 1, uid_c),$$
  
  $a \mapsto (qubit, 3, uid_a)]$ 

$$\begin{aligned} \textit{ct}(\texttt{if} \ \texttt{c} \ \texttt{do} \ \texttt{x} \ \texttt{a[0]}; \ \texttt{end}, \textit{st}) &= \textit{control}(\textit{qt}(\textit{c}, \textit{st}), \textit{bt}(\texttt{x} \ \texttt{a[0]};, \textit{st})) \\ &= \textit{control}(\textit{uid}_{\textit{c}}, \texttt{x} \ \textit{uid}_{\textit{a}}[\texttt{0}];) \\ &qt(\textit{c}, \textit{st}) = \textit{st}[\textit{c}]_3 = \textit{uid}_{\textit{c}} \\ &\textit{bt}(\texttt{x} \ \texttt{a[0]};, \textit{st}) = \texttt{x} \ \textit{qt}(\textit{a[0]}); = \texttt{x} \ \textit{uid}_{\textit{a}}[\texttt{0}]; \end{aligned}$$

$$control(uid_c, \times uid_a[0];) = ctrl(1) @ \times uid_c, uid_a;$$

#### **Overview**

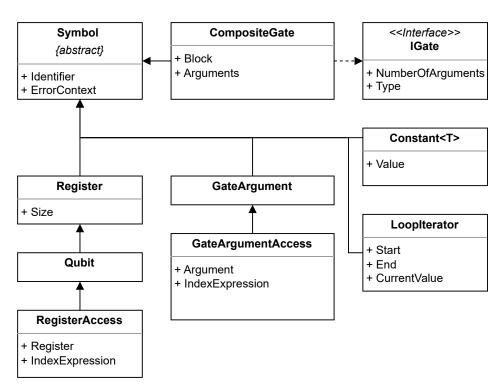
- The implementation of the compiler is differentiated into four different stages:
  - 1. the lexical and syntactic analysis,
  - 2. semantic analysis,
  - 3. code generation, and
  - 4. optimizations
- The process is managed by a static compiler class.
- It parses the command line parameters, handles the input and output of files, and calls the different stages.

```
./LUIECompiler --input "./program.luie" \
--output "./build/program.qasm" \
--optimization nullgate+peepingcontrol
```

A command line interface example.

## Symbols and Symbol Table

- Through out the whole compilation process, the symbol table is used to save and propagate symbol information.
- Additionally, it handles higher-level concepts such as variable contexts.
- It contains a dictionary that maps identifiers to the symbol objects.
- All symbol objects are derived from an abstract symbol class.



A diagram showing the hierarchy of symbol classes.

#### **Lexical and Syntactic Analysis**

- The first compilation stage is the lexical and syntactic analysis.
- Both the lexer and parser are created with the ANTLR4 tool.
- It generates the source code based on a given grammar.
- The implementation of the grammar is a more elaborate version of the syntax given previously.

```
parse : mainblock EOF;

mainblock : gateDeclaration* (declaration | statement)*;

block : (declaration | statement)*;
```

The basic structure of parsing rules for Luie.

#### **Semantic Analysis**

- The next step is the semantic analysis.
- An analysis without any context is not sufficient for non-syntactic constraints of the program.
- For example, the syntactic analysis may ensure gate declarations are always at the beginning of a program, but it cannot ensure that all identifiers in a gate application were previously defined.
- Our semantic analysis is divided into two parts:
  - 1. the declaration analysis and
  - 2. the type checking.
- Both parts are implemented as ANTLR listener classes.
- These traverse the parse tree and call both an enter and exit function for each grammar rule, e.g., EnterBlock and ExitBlock.

#### **Semantic Analysis**

- The declaration analysis ensures that all identifiers used were previously declared and all identifiers used in declarations are not already declared.
- This includes throwing warnings for declared but unused identifiers.
- Additionally, it prevents the use of a qubit in a code block that is guarded by the same qubit because this would lead to irreversible gates.
- The type checking ensures that symbols are used in the correct context.
- For example, while a qubit symbol can be used as the argument for a gate application, it
  does not represent a classical numerical value and, therefore, cannot be used in the context
  of a factor.
- Since we do not give the type of composite gate argument, its body cannot be type checked, and any invalid types are thrown at generation time.

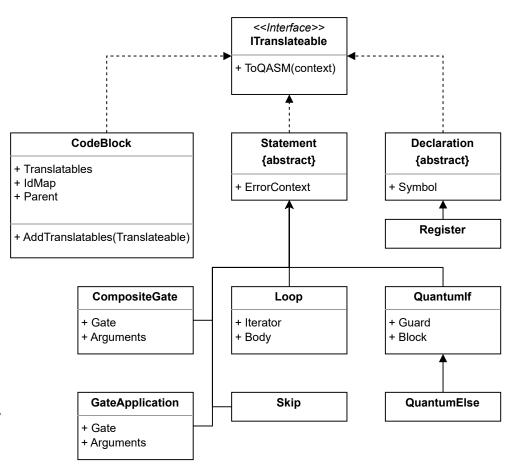
#### **Code Generation**

- First, the parse tree is traversed and the source code is translated to an in-memory representation.
- Next, this source code representation (SCR) is translated to the target code representation (TCR).
- Then, the TCR can be translated directly to the textual OpenQASM code.
- We want to go through the process with the example program from before.
- For simplicity, the named constant was replaced with a constant value.

An example Luie program to show the code generation process.

#### **Source Code Representation**

- All SCR objects implement the translatable interface, which requires a translation function.
- The are three main translatables: the code block, statement, and declaration classes.
- The block contains a list of translatables and is used for both the main block and the body of some statements.
- The declaration consists only of register declarations; the compile-time-only declarations are only saved in the symbol table.



A diagram showing the hierarchy of translatable classes.

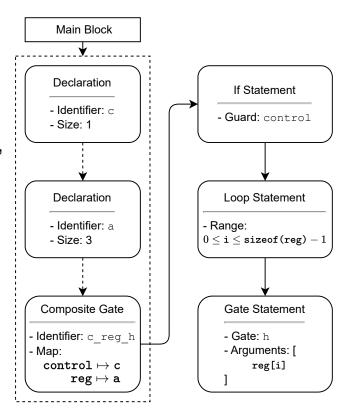
#### **Source Code Representation — Example**

- Any translation always consists of the main block.
- It contains three translatables.
- The first two are the declarations, and the last is the composite gate statement.
- The gate's body contains only an if-statement, which, in turn, contains a loop statement.
- The loop statement consists of a gate application.

```
gate c_h_reg(control, reg) do
qif control do
for i in range(sizeof(reg)) do
h reg[i];
end end end

qubit c; qubit[3] a;
c_h_reg c, a;
```

An example Luie program to show the code generation process.



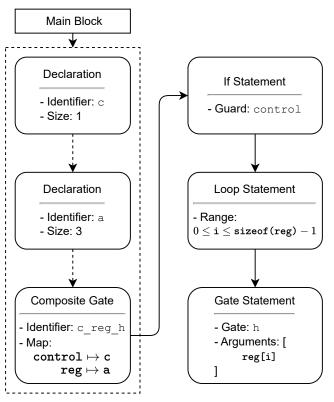
The SCR of the example program.

#### **Target Code Representation**

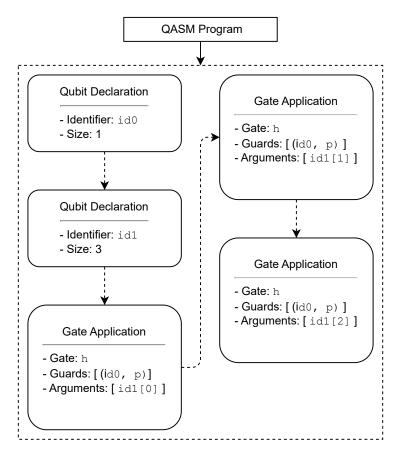
- The basis of the TCR is the QASMProgram object.
- It contains a list of Code objects, which are either declarations of gate applications.
- All SCR objects can be translated to a list of code objects and appended to the program object.
- The translations are as described in the translation section.
- For example, an if-statement adds a control qubit to all gate applications in the block translation.
- All code objects implement a ToCode function that returns the textual representation of the statement.
- To translate the program object, the code objects are simply iterated, converted to text, and written to a file.

$$ct(qif qArg do blk end, st) = control(qt(qArg, st), bt(blk, st))$$

# **Target Code Representation — Example**



The SCR of the example program.



The TCR of the example program.

#### Translated Example Program

- In the end, the TCR is converted to the OpenQASM program.
- For this, the version string and include header are prepended to the code.
- Additionally, for each quantum register, a classical one is declared, and the registers are measured and saved to the corresponding classical registers.
- These additions are performed right before the result is written to the output and after the optimization.

```
1 OPENQASM 3.0;
2 include "stdgates.inc";
3 qubit id0;
4 qubit[3] id1;
5 ctrl(1) @ h id0, id1[0];
6 ctrl(1) @ h id0, id1[1];
7 ctrl(1) @ h id0, id1[2];
8 bit id0_measurement;
9 measure id0 -> id0_measurement;
10 bit[3] id1_measurement;
11 measure id1 -> id1_measurement;
```

The OpenQASM translation of the example Luie program.

#### **Optimization**

- The compiler can perform optimizations to reduce both the number of gates and qubits.
- The optimizations are performed to the TCR to allow for more optimizations at the cost of performance.
- The compiler performs general peephole optimizations based on rules presented by [Garcia-Escartin and Chamorro-Posada, 2011].
- They can be divided into four rules:
  - 1. null gate,
  - 2. peeping control,
  - 3. Hadamard reduction, and
  - 4. control reversal.

#### **Null Gate and Peeping Control Rules**

- Null gates are combinations of gates under specific conditions that are equivalent to the identity gate.
- The simplest null gate version is the twofold application of a self-inverse gate.
- They can be removed entirely from the circuit.
- Our peeping control rules are a special case of null gates.
- In this case, the value of a control is known and the gate can be removed if it is not applied.
- Since the implementation of the rules differs greatly from the other null gate rules, it is separated as its own rule.

$$-H-H-=-X-X-=-I-$$

Null gates of self-inverse gates.

$$|0\rangle$$
 =  $-I$   $\psi\rangle$   $-U$  =  $-I$ 

Null gates for gates in specific conditions.

#### **Hadamard Reduction and Control Reversal Rules**

- The Hadamard reduction can reduce either an X or a Z gate surrounded by H gates to the
  other without the surrounding gates.
- The rule is also the basis for the control reversal.
- It emerges when the Hadamard reduction is combined with the control reversal of the controlled-Z gate.
- A controlled-not gate surrounded by Hadamard gates is equivalent to the target and control
  qubits exchanged without Hadamard gates.

$$-H-Z-H-=-X-$$

A Hadamard reduction rule.

Null gates for gates in specific conditions.

#### **Cricuit Graph**

- Instead of applying the rules directly to the program, it is translated to a circuit graph.
- Then, the graph is optimized and the result is translated back to an OpenQASM program.
- The circuit graph *C* is acyclic and directed.
- It consists of a set of nodes V split into input, output, and gate nodes and edges E.
- Additionally, it contains a set of qubits Q and two functions that map nodes  $Q_V$  and edges  $Q_E$  to qubits.

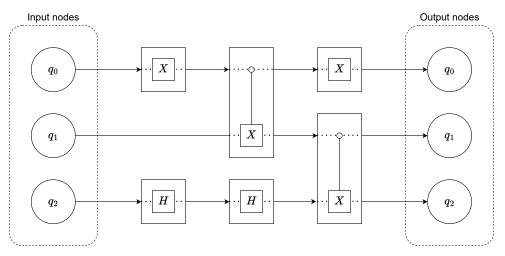
$$C = (V, E, Q, Q_E, Q_V)$$
 $V = \bigcup_{\substack{I \ \text{Input Nodes} \ Output Nodes}} \bigcup_{\substack{G \ Gate \ Nodes}} \bigcup_{\substack{G \ Q_V : I \cup O \rightarrow Q}} \bigcup_{\substack{G \ Q_F : E \rightarrow Q}} \bigcup_{\substack{G \ Q_E \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \ Av \neq V}} \bigcup_{\substack{G \ Gate \ Av \neq V}} \bigcup_{\substack{G \$ 

#### **Example Circuit Graph**

- Input and output nodes have only one outgoing or incoming edge, respectively.
- For each qubit, C contains an input-output node pair.
- Each edge coming into a gate node has a corresponding outgoing one with the same qubit.
- These represent an argument of the gate application.
- The wire for qubit q is represented by the path from the input to the output node where all edges map to q.

```
1 qubit[3] q;
2 x q[0];
3 Cx q[0], q[1];
4 x q[0];
5 h q[2];
6 h q[2];
7 Cx q[1], q[2];
```

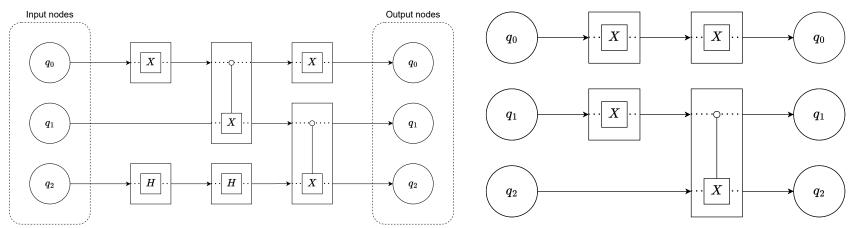




An example of a simple, unoptimized circuit graph.

# **Example Optimization Process I**

- To optimize the graph, each qubit wire is iterated.
- All subpaths up to a maximum length are checked for optimized alternatives.
- In the example, the peeping control rule can be applied to the first CX gate.
- Next, the HH null gate can be removed.

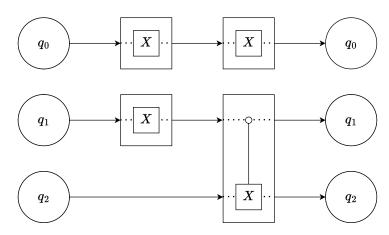


An example of a simple, unoptimized circuit graph.

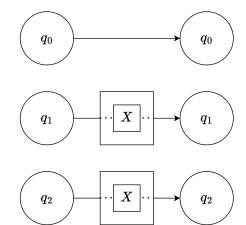
The circuit graph after the first optimization step.

# **Example Optimization Process II**

- While all qubit wires were iterated, there are still possible optimizations.
- This is because applying optimizations may enable others.
- Therefore, the optimization is repeated as long as the previous iteration applied optimizations.
- In the next iteration, the XX null gate can be removed.
- Additionally, a peeping control rule can be applied to the remaining CX gate.



The circuit graph after the first optimization step.



The completely optimized graph.

#### **Evaluation**

#### **Evaluation**

- The evaluation consists of two aspects:
  - 1. the optimizations performed by the compiler and
  - 2. the execution time of the compilation stages.
- As an example program, we use the quantum ripple-carry adder proposed by [Cuccaro et al., 2004].
- It takes two registers a and b as well as two qubits cin and cout.
- The adder adds the *a* register to the *b* register.
- The cin and cout qubits are used as input and output carry bits.
- In our implementation, it consists of CX and CCX gates.

#### **Evaluation**

## **Optimization Evaluation**

- For the optimization evaluation, we used both inputs with classical values and values in superposition.
- The first inputs were  $a = |1\rangle$  and  $b = |15\rangle$ .
  - Since the inputs are classical values, peeping control rules and null gate rules can be applied.
  - The circuit can be optimized such that the resulting one only contains gates that initialize the result.
  - Only two X gates remain.
  - While the first gate flips the first qubit of the a register, initializing it to  $|1\rangle$ , the second flips the carry output qubit, indicating a result of  $|16\rangle$ .
- The second inputs were  $a = \frac{1}{\sqrt{2}}(|0\rangle + |3\rangle)$  and  $b = |4\rangle$ .
  - Since the inputs are now values in superposition, peeping control rules and null gate rules can only partially be applied.
  - In this case, only twelve of 25 gates can be optimized.
  - For other inputs in superposition, even fewer gates are optimized.

#### **Evaluation**

#### **Performance Evaluation**

- To evaluate the performance, we compiled the adder with an input of  $a = \frac{1}{\sqrt{2}}(|0\rangle + |3\rangle)$  and b = 15 for different register sizes n.
- Since the program size does not change, the execution times of the semantic analysis remain constant.
- The code generation stage shows a linear increase, as the compiled program increases linearly with the register size.
- The optimization has the worst performance with an approximate quadratic increase.

Register Size n	Execution Time of Stages in ms				
riegister Size II	Semantic Analysis	Code Generation	Optimization		
64	27.3	47.8	711.6		
128	26.3	50.4	2292.4		
256	26.2	59.7	10755.7		
512	25.8	74.9	60204.7		
1024	26.1	109.1	405376.6		

The execution times compiling a quantum ripple-carry adder with different register sizes.

#### **Conclusion**

#### Conclusion

- The evaluation revealed aspects that can be improved.
- The optimizations are focused on high-level optimizations and work best in tandem with other tools.
- A possible improvement is the addition of hardware-focused features and transpilation to concrete devices.
- Additionally, the performance of the optimization stage could be improved by parallelization of the wire traversals.
- However, this would increase the complexity of the program as, e.g., race conditions need to be considered.
- Other general improvements could be the addition of type casting for the named constants.
- Furthermore, the predefined function could be expanded, and constants such as  $\pi$  or e could be added.
- Lastly, explicit measurements could be added.

#### References

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