

<sup>1</sup>

# **Tutorial: Becoming Full-Stack AI Researchers**

<sup>2</sup>

<sup>3</sup>

Working Draft

<sup>4</sup>

Authors<sup>1</sup>

<sup>5</sup>

<sup>1</sup>Yale University

<sup>6</sup>

Version: December 31, 2025

## <sup>7</sup> 1 Introduction

<sup>8</sup> Large language models (LLMs) and their surrounding ecosystem have evolved rapidly,  
<sup>9</sup> creating a landscape where the best researchers are expected to navigate multiple  
<sup>10</sup> layers of the AI stack. From downloading sharded model checkpoints to deploying  
<sup>11</sup> distributed reinforcement learning pipelines, a modern AI researcher must operate as  
<sup>12</sup> both an engineer and a scientist.

<sup>13</sup> **Problem** The traditional division of labor, where some focus only on mathematical  
<sup>14</sup> modeling and others only on systems, has given way to a full-stack expectation: the  
<sup>15</sup> ability to move fluidly between data handling, model training, evaluation, deploy-  
<sup>16</sup> ment, and interpretability. However, we cannot find resources that can introduce AI  
<sup>17</sup> researchers to understand the entirety of the technical stack.

<sup>18</sup> **Contribution** In the Fall 2025 semester at Yale University, we organised a **Be-**  
<sup>19</sup> **coming Full-Stack AI Researchers** working group. This tutorial paper and its  
<sup>20</sup> accompanying GitHub repository emerged out of the working group. Our goal is not  
<sup>21</sup> just to introduce individual frameworks in isolation, but to show how they fit together  
<sup>22</sup> into an end-to-end research workflow. We emphasize hands-on, reproducible, and  
<sup>23</sup> extensible practices. Each section is written by contributors who prepared minimal  
<sup>24</sup> working examples (MWEs), demos, slides, and live presentations, thereby capturing  
<sup>25</sup> both the technical details and the practical challenges encountered by new users.

<sup>26</sup> **Application** This tutorial can be used as the starting point of a one-semester course  
<sup>27</sup> on modern AI development as well as for self-study of interested learners who have  
<sup>28</sup> basic familiarity with Python. Our intended audience includes graduate students,  
<sup>29</sup> postdoctoral researchers, and faculties who want to broaden their AI engineering  
<sup>30</sup> capabilities. By the end of this tutorial, readers should be able to replicate common  
<sup>31</sup> workflows, adapt them to their own research problems, and understand the broader  
<sup>32</sup> design space of tools and frameworks that constitute modern AI development.

<sup>33</sup> **Organization** This tutorial is organized into modules covering the full AI develop-  
<sup>34</sup> ment pipeline:

- <sup>35</sup> • **Foundations:** PyTorch, JAX, and TensorFlow fundamentals
- <sup>36</sup> • **LLMs as Black Boxes:** Inference, evaluation, deployment, and serving

- **Post-Training:** Supervised fine-tuning (SFT) and reinforcement learning (RL)
  - **Agentic Systems:** Software and hardware agents, multi-step reasoning
  - **Systems:** Distributed training (Ray), efficient serving (vLLM), memory optimization (DeepSpeed)
- Each module includes minimal working examples (MWEs), detailed explanations, and practical exercises.
- Acknowledgements** This course is generously supported by the Wu Tsai Institute at Yale University. We thank Ping Luo, John Lafferty, Linjun Zhang, Anurag Kashyap, Theo Saarinen, and Yuxuan Zhu for helpful comments and suggestions.

46 **2 PyTorch, JAX, and TensorFlow**

47 **2.1 Motivation and Background**

48 Modern deep learning frameworks like TensorFlow, PyTorch, and JAX were created  
49 with the goals of

- 50 1. Efficient tensor (matrix) operations at scale, and  
51 2. Automatic differentiation for optimization algorithms.

Consider a loss function  $L(\theta)$  depending on model parameters  $\theta \in \mathbb{R}^d$ . Training typically happens via the gradient descent algorithm

$$\theta_{t+1} = \theta_t - \eta \nabla_\theta L(\theta_t),$$

52 where  $\eta$  is the learning rate. Computing  $\nabla_\theta L(\theta)$  by hand is infeasible for complex  
53 neural networks. These frameworks automate it by building a *computational graph*  
54 and applying reverse-mode differentiation (backpropagation).

55 They are written with GPU and TPU in mind for efficient parallel computation so  
56 that linear algebra operations and auto diff are executed faster than can be done on  
57 CPUs with numpy.

58 **2.2 Historical Context and Ecosystem**

59 In 2015, Google introduced its first large-scale public framework, TensorFlow. In 2018,  
60 Google introduced JAX, a functional, composable approach with transformations like  
61 `jit`, `grad`, and `pmap`, optimised for TPUs. TensorFlow was once popular but is now  
62 on its way to depreciation.

63 Meanwhile, in 2016, Facebook introduced PyTorch, which became the default for  
64 most academic work. Rumours have it that nowadays, Google and xAI work mostly  
65 with JAX, OpenAI and Meta/Facebook work mostly with PyTorch, and Anthropic  
66 uses both.

67 **2.3 Strengths and Hardware Compatibility**

68 **PyTorch.** Strengths: Vast ecosystem (Hugging Face, PyTorch Lightning) and greater  
69 community support. GPU-first.

70 **JAX.** Strengths: clean functional abstractions, XLA compiler, flexibility in creating  
71 customised kernels. TPU-first.

72 **2.4 Core Programming Model and Syntax**

73 Here is a simple example written in PyTorch and in Jax. With PyTorch, we can do

```
74     import torch  
75  
76     x = torch.tensor([2.0], requires_grad=True)  
77     y = x**2 + 3*x + 1  
78     y.backward()    # compute dy/dx  
79     print(x.grad)  # prints tensor([7.])  
80
```

The gradient follows

$$y = x^2 + 3x + 1,$$
$$\frac{dy}{dx} = 2x + 3 = 7 \text{ at } x = 2.$$

81 Equivalently, in JAX, we can do

```
82     import jax  
83     import jax.numpy as jnp  
84  
85     def f(x):  
86         return x**2 + 3*x + 1  
87  
88     grad_f = jax.grad(f)  
89     print(grad_f(2.0))  # prints 7.0  
90
```

91 **2.5 Ecosystem and Tooling**

92 Each framework is surrounded by a rich ecosystem of higher-level libraries.

- 93 • **PyTorch:** PyTorch Lightning provides structured training loops and experiment  
94 organization. The Hugging Face Transformers library, while framework-agnostic,  
95 has its deepest integration with PyTorch.

- 96     • **JAX:** Flax and Haiku are neural network libraries built specifically for JAX,  
97       offering functional-style model definitions.

98     For distributed and large-scale training, each framework offers its own primitives.

- 99     • **PyTorch:** the `torch.distributed` package implements data-parallel and  
100      model-parallel training across multiple GPUs and nodes.

- 101     • **JAX:** the `pmap` transformation allows parallel execution of functions across  
102      multiple devices (TPUs or GPUs), with automatic sharding of arrays.

103     For the compatibility with the computational hardware,

- 104     • **PyTorch:** Built directly on top of CUDA/cuDNN for GPU acceleration.

- 105     • **JAX:** Relies on XLA, which in turn generates CUDA kernels when targeting  
106      NVIDIA GPUs. Compatible with both GPUs and TUPs.

107     Finally, orchestration frameworks such as **Ray** integrate with all three, providing  
108      a higher-level interface for scaling training jobs beyond a single machine.

## 109     2.6 Installation and Getting Started

110     Installation depends on hardware.

- 111     • PyTorch: `pip install torch torchvision torchaudio`. Select CUDA ver-  
112       sion if using GPUs.

- 113     • JAX: `pip install jax jaxlib`, or TPU runtime via Colab/Cloud.

114     Typical pitfalls include

- 115     • CUDA version mismatches between PyTorch and system drivers.

- 116     • Installing JAX with the wrong CUDA wheel.

- 117     • Mixing conda and pip environments without care.

<sub>118</sub> **3 Scaling Laws for Neural Language Models**

<sub>119</sub> **3.1 Motivation: Predictable Improvement**

<sub>120</sub> One of the most remarkable discoveries in modern AI is that model performance  
<sub>121</sub> scales predictably with key factors: model size, dataset size, and compute budget.  
<sub>122</sub> Understanding these **scaling laws** enables:

- <sub>123</sub> • **Resource planning:** Predict performance before training expensive models  
<sub>124</sub> • **Optimal allocation:** Balance parameters, data, and compute efficiently  
<sub>125</sub> • **Research prioritization:** Identify bottlenecks and high-leverage improvements  
<sub>126</sub> • **Capability forecasting:** Anticipate future model capabilities

<sub>127</sub> The power of scaling laws lies in their predictability across orders of magnitude,  
<sub>128</sub> allowing researchers to extrapolate from smaller experiments to larger deployments.

<sub>129</sub> **3.2 Power Law Foundations**

<sub>130</sub> Scaling laws typically follow **power law** relationships of the form:

$$L = \frac{\alpha_0}{p^\alpha} \quad (1)$$

<sub>131</sub> where:

- <sub>132</sub> •  $L$  is the loss (or error metric)  
<sub>133</sub> •  $p$  is a scaling parameter (e.g., number of parameters, dataset size)  
<sub>134</sub> •  $\alpha_0$  is a constant  
<sub>135</sub> •  $\alpha$  is the scaling exponent

<sub>136</sub> **3.2.1 Why Power Laws?**

<sub>137</sub> Power laws arise from **scale invariance**: scaling the input  $p$  by a factor  $k$  produces a  
<sub>138</sub> proportional response  $f(kp) = k^\beta f(p)$ . This property necessarily leads to relationships  
<sub>139</sub> of the form  $L = cp^\alpha$ .

<sup>140</sup> **3.2.2 Log-Log Linearity**

<sup>141</sup> Taking logarithms of Equation ??:

$$\log L = \log \alpha_0 - \alpha \log p \quad (2)$$

<sup>142</sup> This linearity in log-log space is the signature of power laws and enables easy  
<sup>143</sup> fitting and extrapolation.

<sup>144</sup> **3.3 Kaplan Scaling Laws (2020)**

<sup>145</sup> Kaplan et al. [kaplan2020] conducted extensive experiments to characterize how  
<sup>146</sup> language model loss scales with:

- <sup>147</sup> •  $N$  = Number of model parameters
- <sup>148</sup> •  $D$  = Dataset size (number of tokens)
- <sup>149</sup> •  $C$  = Compute budget (FLOPs)

<sup>150</sup> **3.3.1 Key Findings**

**Loss vs. Model Size.**

$$L(N) \propto N^{-\alpha_N} \quad \text{where } \alpha_N \approx 0.076 \quad (3)$$

<sup>151</sup> Larger models achieve lower loss, with diminishing returns following a power law.

**Loss vs. Dataset Size.**

$$L(D) \propto D^{-\alpha_D} \quad \text{where } \alpha_D \approx 0.095 \quad (4)$$

<sup>152</sup> More training data improves performance, but with diminishing returns similar to  
<sup>153</sup> model size.

**Loss vs. Compute.**

$$L(C) \propto C^{-\alpha_C} \quad \text{where } \alpha_C \approx 0.050 \quad (5)$$

154 Given fixed compute, how should one allocate between model size and training  
155 tokens?

156 **Optimal Allocation (Kaplan).** Kaplan et al. recommended:

- 157 • Most compute should go toward larger models  
158 • Dataset size can remain relatively modest  
159 • This led to models like GPT-3 (175B parameters, 300B tokens)

160 **3.4 Chinchilla Scaling Laws (2022)**

161 Hoffmann et al. [chinchilla2022] revisited Kaplan’s experiments and found different  
162 optimal allocations.

163 **3.4.1 Key Revision**

164 **Main Finding:** For compute-optimal training, model size ( $N$ ) and dataset size ( $D$ )  
165 should scale equally with compute budget ( $C$ ):

$$N \propto C^{0.50}, \quad D \propto C^{0.50} \quad (6)$$

166 **3.4.2 Implications**

167 **Previous Models Were Over-Parameterized.** Models like GPT-3 used too many  
168 parameters for their training data:

- 169 • GPT-3: 175B parameters, 300B tokens  
170 • Chinchilla: 70B parameters, 1.4T tokens  
171 • Result: Chinchilla outperformed GPT-3 despite fewer parameters

172 **Modern Approach.** Post-Chinchilla models follow this guidance:

- 173 • LLaMA-65B: 65B parameters, 1.4T tokens  
174 • Mistral-7B: 7B parameters, scaled appropriately  
175 • Emphasis on high-quality training data

<sub>176</sub> **3.4.3 Three Scaling Regimes**

<sub>177</sub> Understanding when different factors dominate:

<sub>178</sub> **Small-Scale Regime.** Model capacity is the bottleneck:

- <sub>179</sub> • Increasing  $N$  yields largest improvement
- <sub>180</sub> • Limited by model expressiveness
- <sub>181</sub> • Example: Sub-billion parameter models

<sub>182</sub> **Medium-Scale Regime.** Dataset size becomes limiting:

- <sub>183</sub> • Need more diverse training data
- <sub>184</sub> • Diminishing returns from just scaling  $N$
- <sub>185</sub> • Example: 1B–100B parameter range

<sub>186</sub> **Large-Scale Regime.** Compute efficiency matters most:

- <sub>187</sub> • Both  $N$  and  $D$  must scale together
- <sub>188</sub> • Infrastructure and optimization critical
- <sub>189</sub> • Example: 100B+ parameter models

<sub>190</sub> **3.5 Practical Applications**

<sub>191</sub> **3.5.1 Model Development Planning**

Given compute budget  $C$ , determine optimal:

$$N^* = k_1 \cdot C^{0.50} \tag{7}$$

$$D^* = k_2 \cdot C^{0.50} \tag{8}$$

<sub>192</sub> where  $k_1, k_2$  are task-dependent constants.

193 **3.5.2 Performance Prediction**

194 Estimate final loss before training:

$$L_{\text{pred}} = \frac{\alpha_0}{N^{\alpha_N} \cdot D^{\alpha_D}} \quad (9)$$

195 This enables cost-benefit analysis for model development.

196 **3.5.3 Bottleneck Identification**

197 If current performance is:

- 198 • **Far from predicted:** Optimization or data quality issues
- 199 • **Close to predicted but insufficient:** Need more  $N$ ,  $D$ , or  $C$
- 200 • **Better than predicted:** Architecture or training innovations

201 **3.6 Data Availability Constraints**

202 Scaling laws assume unlimited high-quality data, but reality imposes limits:

203 **3.6.1 Internet-Scale Data**

204 Estimates suggest:

- 205 • 10-100 trillion tokens of web text available
- 206 • Quality varies dramatically
- 207 • Deduplication reduces effective size
- 208 • Multilingual data has different coverage

209 **3.6.2 Synthetic Data**

210 When natural data exhausted:

- 211 • **Distillation:** Learn from stronger models
- 212 • **Self-play:** Generate and curate own data
- 213 • **Targeted generation:** Focus on capability gaps
- 214 • **Quality over quantity:** Careful curation and filtering

215 **3.7 Downstream Task Performance**

216 Pretraining scaling predicts downstream capabilities:

217 **3.7.1 Emergent Abilities**

218 Some capabilities appear suddenly at scale:

219 • Multi-step reasoning

220 • In-context learning

221 • Code generation

222 • Multilingual transfer

223 **Debate:** Whether these are truly emergent or merely crossing evaluation thresh-  
224 olds.

225 **3.7.2 Fine-Tuning Efficiency**

226 Larger pretrained models typically:

227 • Require less fine-tuning data

228 • Converge faster in fine-tuning

229 • Transfer better across domains

230 • Benefit more from parameter-efficient methods (LoRA)

231 **3.8 Inference Scaling**

232 Beyond training, inference costs matter:

233 **3.8.1 Performance vs. Inference Cost**

234 Tradeoffs:

235 • **Larger models:** Better quality, higher latency/cost

236 • **Smaller models:** Worse quality, lower latency/cost

237 • **Quantization:** Reduces inference cost at slight quality loss

238 **3.8.2 Deployment Considerations**

239 For production:

$$\text{Total Cost} = \text{Training Cost} + (\text{Inference Cost} \times \text{Number of Requests}) \quad (10)$$

240 Since models serve billions of requests, inference costs often dominate. This  
241 motivates:

- 242 • Smaller, cheaper models when sufficient
- 243 • Knowledge distillation from large to small models
- 244 • Efficient architectures (Mixture-of-Experts)
- 245 • Quantization and pruning

246 **3.9 Limitations and Future Directions**

247 **3.9.1 Limitations of Current Scaling Laws**

- 248 • **Architecture dependence:** Scaling exponents may differ for different architectures
- 250 • **Task specificity:** Downstream tasks may not scale identically to pretraining loss
- 252 • **Data quality:** Scaling laws assume i.i.d. data; quality matters
- 253 • **Multimodality:** Vision-language models may follow different laws

254 **3.9.2 Open Questions**

- 255 • How do Mixture-of-Experts models scale?
- 256 • Do different modalities (vision, audio) follow similar laws?
- 257 • How does post-training (RL, fine-tuning) scale?
- 258 • Are there fundamental limits to scaling?
- 259 • How do architectural innovations affect scaling?

260 **3.10 Summary**

261 Key takeaways:

- 262 • Model performance scales predictably with size, data, and compute
- 263 • Power laws enable performance prediction across orders of magnitude
- 264 • Chinchilla scaling: balance parameters and data equally
- 265 • Practical implications for model development and deployment
- 266 • Consider both training and inference costs
- 267 • Data availability and quality impose real constraints

268 Understanding scaling laws is essential for:

- 269 • **Research:** Prioritize high-leverage improvements
- 270 • **Development:** Allocate resources optimally
- 271 • **Deployment:** Balance quality and cost
- 272 • **Strategy:** Anticipate future capabilities

273 As the field matures, scaling laws will continue evolving, but their fundamental  
274 insight—that AI progress is predictable and scalable—remains transformative.

275 **4 Ray: A Distributed Computing Framework**

276 **4.1 Motivation and Background**

277 As compute and memory requirements of LLMs keep increasing, single-server set-  
278 tings can no longer accommodate their development, training, and serving needs.  
279 Ray [raypaper] addresses this challenge by enabling fast and easy application scaling  
280 to distributed environments. It provides scalable libraries to support the complete  
281 life-cycle of ML applications, pythonic primitives for intuitive development, and  
282 integration with existing tools and infrastructure like Kubernetes, AWS, and Azure.

283 At its core, Ray utilizes three main abstractions:

- 284 • **Tasks (remote functions):** A Python function decorated with `@ray.remote`.  
285 Each invocation launches a stateless parallel computation executed on any  
286 available CPU or GPU.
- 287 • **Actors:** A Python class decorated with `@ray.remote` becomes an actor. Unlike  
288 tasks, actors are *stateful*—they live on a worker process and can preserve variables  
289 across multiple method calls.
- 290 • **Worker Node:** Under the hood, Ray maintains a pool of worker nodes, which  
291 consist of multiple physical processes. Each node hosts a *raylet* process, which  
292 manages the node’s shared resources, and one or more worker processes respon-  
293 sible for task submission and execution.

294 Ray’s cluster hosts the head node, which contains the *Global Control Store*(GCS),  
295 a server managing cluster-level metadata and operations like scheduling. For fault  
296 tolerance, Ray introduced an ownership model, which can be combined with lineage  
297 reconstruction to recover lost objects in the event of a node’s failure. These components  
298 contribute to Ray’s core principles for API simplicity and generality, while enabling  
299 system performance and reliability. More information about Ray’s architecture can  
300 be found in the designated architecture whitepaper [rayarchitecture].

301 **4.2 Historical Context and Ecosystem**

302 Researchers at UC Berkeley’s RISELab introduced Ray at 2018 [raypaper] and it has  
303 since evolved into a widely adopted ecosystem for scaling AI and Python workloads.  
304 Today, Ray is maintained by Anyscale and supports a range of libraries for specialized  
305 tasks:

- **Ray RLlib**: High-Performance RL
- **Ray Serve**: Scalable & Programmable Model Serving.
- **Ray Tune**: Scalable Hyperparameter Tuning.
- **Ray Train**: Distributed Model Training
- **Ray Data**: Distributed Data Processing

### 311 4.3 Core Programming Model and Syntax

312 The minimal Ray program utilizes standard Python. To enable Ray, we import and  
 313 initialize it:

```
314     import ray
315     ray.init() # connect to cluster or start locally
316
```

317 **Remote functions (tasks)**. Decorate a Python function with `@ray.remote` to  
 318 execute it as a parallel task:

```
319     @ray.remote
320     def square(x):
321         return x * x
322
323     futures = [square.remote(i) for i in range(4)]
324     print(ray.get(futures)) # [0, 1, 4, 9]
325
```

326 **Actors**. Use actors to encapsulate state across multiple method calls. An actor is a  
 327 class decorated with `@ray.remote` and runs persistently on a worker process:

```
328     @ray.remote
329     class Counter:
330         def __init__(self):
331             self.value = 0
332         def increment(self):
333             self.value += 1
```

```
334     return self.value  
335  
336     counter = Counter.remote()  
337     print(ray.get(counter.increment.remote())) # 1  
338
```

339 **Workers.** Behind the scenes, Ray launches a pool of worker processes (Python  
340 interpreters). Tasks and actors are scheduled onto these workers by the Ray runtime.  
341 While you rarely interact with workers directly, you can control resource allocation  
342 (e.g., CPUs, GPUs) when defining tasks or actors:

```
343     @ray.remote(num_cpus=2)  
344     def heavy_task(x):  
345         return x ** 2  
346
```

347 Here, Ray will schedule `heavy_task` only on workers with at least two available CPUs.

#### 348 4.4 Strengths, Weaknesses, and Integration

349 **Strengths.** The Python-first design of Ray lowers the barrier for distributed com-  
350 puting. Its modular libraries (Tune, RLlib, Serve) cover end-to-end machine learning  
351 workflows. It integrates naturally with PyTorch, TensorFlow, and JAX.

352 **Weaknesses.** Ray introduces runtime overhead for small-scale tasks, and cluster  
353 management may require careful tuning for performance. It is best suited for medium  
354 to large-scale AI applications in distributed environments rather than fine-grained  
355 parallelism in single-server settings.

#### 356 4.5 Installation and Getting Started

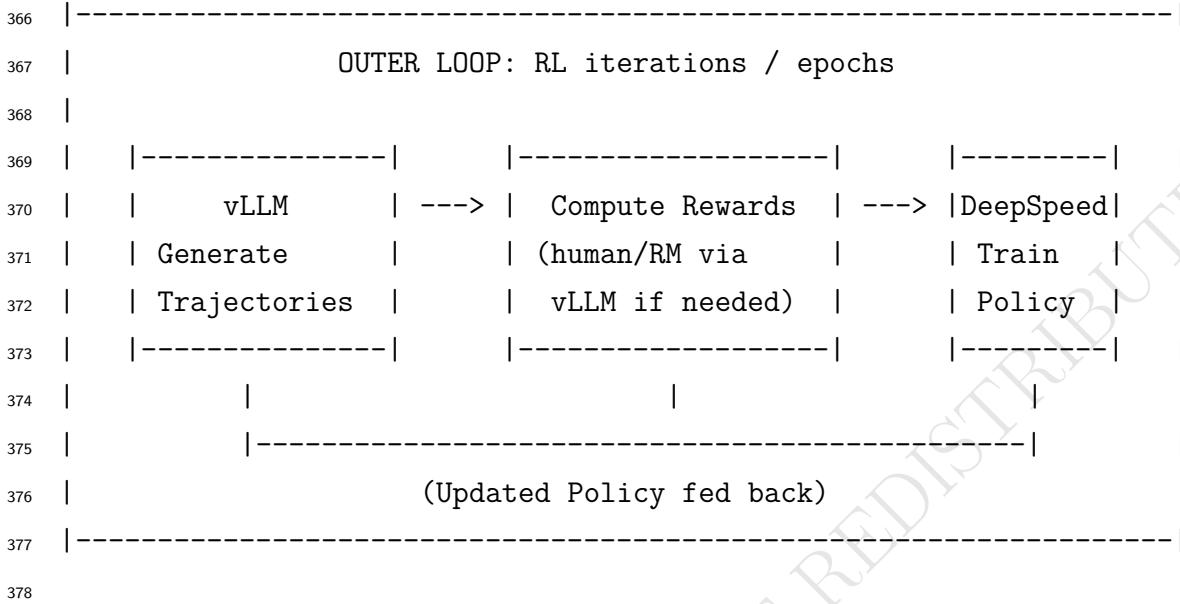
357 Ray can be installed with:

```
358     pip install ray  
359
```

360 Launching Ray locally requires no configuration. To connect to a multi-node  
361 cluster, one can start the head node with `ray start --head` and join worker nodes  
362 with `ray start --address='...'`.

<sup>363</sup> Ray can also be combined with orchestration systems such as Kubernetes or Slurm  
<sup>364</sup> for deployment on HPC or cloud environments.

365 **5 vLLM**



379 **5.1 Motivation**

380 Imagine a reinforcement learning (RL) training loop: we **generate trajectories**,  
381 compute rewards, and **update the policy** model.

382 **vLLM** and **DeepSpeed** act as *system-level optimizers* for these two core stages.

383 **vLLM** accelerates **trajectory generation** and **reward inference**, making large-scale  
384 sampling highly efficient through optimized GPU memory management (PagedAttention).

386 DeepSpeed accelerates **policy training**, enabling distributed, memory-efficient optimi-  
387 zation (via ZeRO) for massive models.

388 Together, they form the backbone of a scalable RL pipeline—vLLM for the inference-  
389 heavy side, DeepSpeed for the training-heavy side—both maximizing GPU utilization  
390 across the loop.

391 **5.2 Section 1—The KV Cache and Why It Matters**

392 **5.2.1 Attention Mechanism Formula**

393 The general form of the **scaled dot-product attention** is:

$$\text{Attention}(Q, K, V) = \text{softmax} \left( \frac{QK^T}{\sqrt{d_k}} \right) V,$$

394 where we have

- 395 •  $Q$  = Query matrix  
396 •  $K$  = Key matrix  
397 •  $V$  = Value matrix  
398 •  $d_k$  = Dimension of the key vectors (used for scaling)

399 At each decoding step, the model must compute attention between the *current*  
400 token(s) and *all past key-value pairs* to determine what context is most relevant.

#### 401 5.2.2 2. Computational Cost Without Caching

402 During **autoregressive generation**, each new token requires recomputing the attention  
403 using *all* previous tokens:

$$\text{Attention}_t = \text{softmax} \left( \frac{Q_t K_{1:t}^T}{\sqrt{d_k}} \right) V_{1:t}.$$

404 That means for every new token  $t$ , you rebuild  $K_{1:t}$  and  $V_{1:t}$ . This leads to **quadratic**  
405 **time complexity**  $O(T^2)$  for a sequence of length  $T$ . This becomes very expensive for  
406 long sequences.

407 Generating the 4th token  
408  
409 |-----|  
410 | tok 1 | tok 2 | tok 3 | <-- already processed  
411 |-----|  
412 ^  
413 | attend to all  
414 [ tok 4 ]

#### 415 5.2.3 3. KV Caching: The Core Idea

416 **KV caching** avoids recomputing  $K$  and  $V$  for the prefix every step.

- 417 • On the first pass, compute  $K$  and  $V$  for the prompt/prefix and **store** them.  
418 • On each new token, compute only the new  $Q$ , and **reuse** cached  $K, V$ .

419 This keeps the cost *per new token* closer to  $O(T)$  instead of  $O(T^2)$ .

420 5.2.4 4. Why KV Cache Is Not Trivial in Serving

421 Real LLM serving is not a single long sequence:

- 422 • Many requests arrive at different times.  
423 • Each request has a different length.  
424 • Some requests finish, some keep generating.

425 So we must keep many KV caches in GPU memory, all growing at different speeds.

426 5.2.5 5. Baseline vs With KV Cache

Compute Keys/Values   Recomputed each step   Reused from cache
Complexity   $\$ O(T^2) \$   \$ O(T) \$  $
Speed   Slow for long sequences   Much faster

430 5.2.6 6. Throughput via Batching, and Its Two Problems

431 To use the GPU efficiently, we **batch** requests. But in practice:

- 432 1. **Asynchronous arrivals:** requests don't start together.  
433 2. **Variable lengths:** prompts/outputs differ; some finish early.

434 This leads to idle threads and poor packing unless we **rebatch every decoding iteration** (a.k.a. *iteration-level scheduling / cellular batching*).

436 5.2.7 7. KV Cache Still Has Issues

437 Even with better batching, many concurrent, variable-length requests cause **GPU memory fragmentation**—turning into a GPU memory management problem that  
438 439 Section 2 addresses.

440 5.3 Section 2—PagedAttention: Solving the KV Cache Memory Problem

441 5.3.1 1. Motivation: KV Cache Fixes Computation, but Creates a Mem-  
442 ory Challenge

443 KV caching saves compute but each request's cache **grows autoregressively** as  
444 new tokens are generated. With many concurrent requests, caches grow and finish at  
445 different times, stressing GPU memory.

446 5.3.2 2. The Naïve Way: Consecutive (Contiguous) Allocation

447 |-----|  
448 | [Req A (50 tok)] [Req B (30 tok)] [Req C (80)] |  
449 |-----|

450 If B finishes early, we get a hole:

451 |-----|  
452 | [Req A (50 tok)] [cleared (30 tok)] [Req C (80)] [Req D (60)] |  
453 |-----|

454 Now A or C may want to grow, but the memory right next to them is not free.

455 This leads to:

- 456 • fragmentation,  
457 • expensive copies/reallocations,  
458 • or rejecting new/longer requests.

459 5.3.3 3. The “Cut It Up” Idea—Why It’s Hard

460 Splitting a request’s KV into smaller chunks would pack memory better, *but* then  
461 attention has to reconstruct the correct order—hard to track without structure.

462 |-----|  
463 | [Req A (50 tok)] [Req B (30 tok)] [Req C (80)] |  
464 |-----|  
  
465 |-----|  
466 | [Req A (50 tok)] [Req D part 1 (30 tok)] [Req C (80)] [Req D part 2 (30)] |  
467 |-----|

468 5.3.4 4. The Breakthrough: PagedAttention

469 **PagedAttention** slices GPU memory into **uniform pages** (small fixed-size blocks,  
470 e.g. a fixed number of tokens per page). Each request’s KV cache is a *list of pages*,  
471 not one big block.

472 GPU pages: P1 | P2 | P3 | P4 | P5 | P6 | ...  
473 Req A → P1, P2  
474 Req B → P3  
475 Req C → P4, P5  
476 A grows → take P6 (no moves, just add a page)

#### 477 5.3.5 5. The Page Table (Indirection)

478 A lightweight **page table** maps *logical token indices* → *(page, offset)*:  
479 token 37 → page\_table[37//page\_size] + (37 % page\_size)  
480 Attention kernels read K/V via this mapping, so KV can be physically scattered yet  
481 **logically contiguous**.

#### 482 5.3.6 6. Benefits

- 483 • Avoids large reallocations when a request grows.
- 484 • Reuses freed pages from finished requests.
- 485 • Greatly reduces fragmentation.
- 486 • Enables many concurrent, variable-length sequences.

#### 487 5.3.7 7. Interaction with Scheduling

488 Because vLLM also does per-iteration / cellular scheduling, PagedAttention makes it  
489 feasible to mix:

- 490 • long-running chats,
- 491 • short bursts,
- 492 • reward-model-style inference

493 on the same GPU without running into “I can’t fit that request” issues.

### 494 5.4 Section 3—Inside vLLM: How Paging and Scheduling Work Together

#### 495 5.4.1 1. Goal

496 Keep the GPU highly utilized despite **asynchronous arrivals** and **variable-length**  
497 **requests**.

498    **5.4.2 2. Runtime Pipeline**

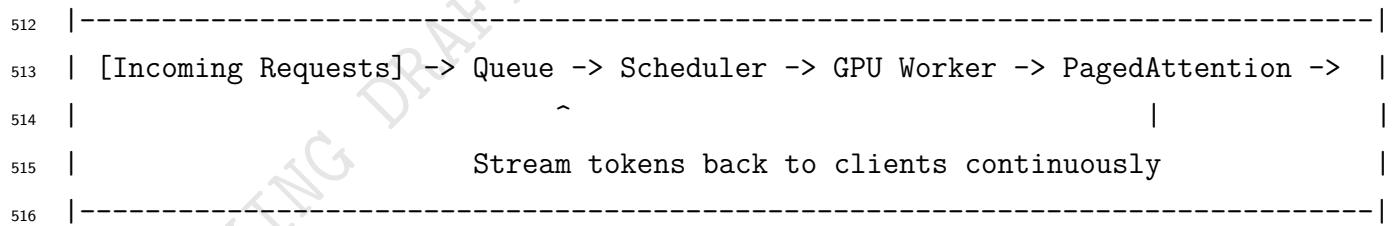
499    User/API → Request Queue → Scheduler (per-iteration) → GPU Workers → PagedAttention →

- 500    • **Request Queue:** holds incoming work
- 501    • **Scheduler:** mixes new and ongoing requests instead of waiting for a full batch;  
502       also removes finished sequences (those that reached EOS or max length)
- 503    • **GPU Workers:** run attention kernels; read K/V via page table; write new  
504       K/V into free pages
- 505    • **PagedAttention:** provides flexible KV memory without copies
- 506    • **Streaming:** return tokens as they are ready while continuing decoding

507    **5.4.3 3. Why This Works**

- 508    • PagedAttention allows **dynamic batching** without moving memory.
- 509    • The scheduler keeps batches full each iteration.
- 510    • Memory stays compact and reusable; fewer OOMs and higher throughput.

511    **5.4.4 4. Concept Diagram**



517    **5.5 Section 4—Minimal “How to Run” Demos**

518    **5.5.1 4.1 Install**

```
519 # Fresh environment recommended
520 # If you're in Jupyter, the line below installs into the notebook kernel.
521 # If you're in a real project, prefer requirements.txt or pyproject.toml
522 %pip install -U vllm transformers accelerate openai
```

523 5.5.2 4.2 Pick a model

524 Qwen3-4B-Instruct-2507

```
525 from vllm import LLM, SamplingParams
526 import torch
527
528 # Check GPU
529 if torch.cuda.is_available():
530     print(f"GPU: {torch.cuda.get_device_name(0)}")
531 else:
532     print("No GPU found, vLLM will be limited")
533
534 # Create the model
535 llm = LLM(
536     model="Qwen/Qwen2-1.5B-Instruct",
537     trust_remote_code=True,
538 )
539
540 # Sampling params
541 params = SamplingParams(
542     temperature=0.7,
543     top_p=0.9,
544     max_tokens=200,
545     skip_special_tokens=False
546 )
547
548 prompts = [
549     "Tell me a short story about a robot.",
550     "List three benefits of paged KV cache for LLM serving."
551 ]
552
553 outputs = llm.generate(prompts, params)
554
555 for i, output in enumerate(outputs):
556     print(f"\n{'='*50}")
```

```
557     response = output.outputs[0].text
558     print(f"Response {i+1}: {response}")
```

WORKING DRAFT: DO NOT REDISTRIBUTE

## 559 6 DeepSpeed Tutorial

560 Focus: why DeepSpeed, the core ZeRO idea.

### 561 6.1 Section 1 — Why DeepSpeed: The GPU Memory Problem in Training

#### 562 6.1.1 1) Motivation

563 Training large models hits a **memory wall**. Even with big GPUs... the forward +  
564 backward pass stores many tensors simultaneously.

#### 565 6.1.2 2) What consumes memory during training

Component	What it is	Notes
<b>Model Parameters</b>	The trainable weights	$\approx 1 \times$ model size
<b>Activations</b>	Intermediates saved for backward	scales with batch $\times$ seq $\times$ hidden
<b>Gradients</b>	Produced by backprop	$\approx 1 \times$ model size
<b>Optimizer States</b>	For Adam: momentum ( $m$ ), variance ( $v$ )	$\approx 2 \times$ model size
<b>Temporary Buffers</b>	Workspace for matmuls/communication	dynamic overhead

566 567 With Adam, per-GPU memory can be **4–6×** the model size.

#### 568 6.1.3 3) Why naïve data parallel wastes memory

569 Every GPU **replicates**:

- 570     • model parameters  
571     • gradients  
572     • optimizer states

573 So if 4 GPUs train a model with Adam:

- 574     • each one keeps params  
575     • each one keeps grads  
576     • each one keeps Adam's  $m$ ,  $v$  states

577 That means total memory across the cluster is  $4 \times$  bigger than needed, but **each**  
578 **individual GPU** still has to fit:

- 579       • parameters  
580       • gradients  
581       • optimizer ( $2 \times$  params)

582 So 4 GPUs do **not** make a single GPU need less memory — they just let you do  
583 bigger *data* throughput.

#### 584 6.1.4 4) Why model parallel is NOT a good idea

585 Model parallelism = splitting the computation across multiple GPUs instead of a full  
586 copy. Each GPU **computes a subset of layers**.

- 587       • **Manual partitioning** – Layers or tensors must be explicitly assigned to GPUs.  
588       • **High communication cost** – GPUs must constantly exchange activations and  
589        gradients.  
590       • **Sequential dependencies** – Layers depend on outputs from previous GPUs,  
591        creating idle “pipeline bubbles.”  
592       • **Backward complexity** – Gradients must flow across devices, increasing syn-  
593        chronization overhead.

594 In short: This reduces both memory *and* compute per GPU, but adds cross-GPU  
595 communication for every layer.

#### 596 6.1.5 4) DeepSpeed’s core idea

597 **ZeRO (Zero Redundancy Optimizer)** partitions these states **across** devices  
598 instead of replicating them, cutting memory per GPU roughly by the number of  
599 devices.

### 600 6.2 Section 2 — ZeRO: The Heart of DeepSpeed

#### 601 6.2.1 Big idea

602 Don’t replicate all training states on each GPU; **shard** them. Communication  
603 reconstructs what’s needed on the fly.

604    **6.2.2 ZeRO's three stages**

**Stage 1 — Shard optimizer states** In optimizers like **Adam** or **AdamW**, at step  $t$  each trainable parameter  $\theta_i$  has **optimizer states** that keep track of its historical updates — for example:

$$\begin{aligned} m_i^t &\leftarrow \beta_1 m_i^{t-1} + (1 - \beta_1) g_i^t, \\ v_i^t &\leftarrow \beta_2 v_i^{t-1} + (1 - \beta_2)(g_i^t)^2, \\ \theta_i^t &\leftarrow \theta_i^{t-1} - \alpha \frac{m_i^t / (1 - \beta_1^t)}{\sqrt{v_i^t / (1 - \beta_2^t)} + \varepsilon}, \end{aligned}$$

605    where

- 606    1.  $m_i$  = first moment (momentum term);  
607    2.  $v_i$  = second moment (variance term);  
608    3.  $g_i$  = gradient of that parameter;  
609    4.  $\theta_i$  = parameter value itself.

Each parameter  $\theta_i$  updates only using its own  $m_i$ ,  $v_i$ , and  $g_i$ . In vector form, Adam's update is applied elementwise:

$$\theta \leftarrow \theta - \alpha \frac{m}{\sqrt{v} + \varepsilon}.$$

610    So if we split the vector of parameters into chunks, each chunk can be updated  
611    entirely on its own — as long as it has access to its local  $m$ ,  $v$ , and  $g$ .

612    Because the optimizer states are independent:  
613    - We can shard the  $m$  and  $v$  tensors across GPUs.  
614    - GPU 0 stores  $m, v$  for parameters [0^25%], GPU 1 for [25^50%], etc.  
615    - Each GPU updates its subset of parameters using its own local optimizer states.

616    **Naïve DP:**

- 616    • GPU0: params + grads + optimizer  
617    • GPU1: params + grads + optimizer  
618    • GPU2: params + grads + optimizer  
619    • GPU3: params + grads + optimizer

620 So 4 copies of everything.

621 **ZeRO-1:** *partition* optimizer states across GPUs. Everyone still has:

- 622 • parameters

- 623 • gradients

624 but **only one GPU** keeps optimizer states for a subset of params.

625 GPU0: gets optimizer states [0-25%]

626 GPU1: gets optimizer states [25-50%]

627 GPU2: gets optimizer states [50-75%]

628 GPU3: gets optimizer states [75-100%]

629 No communication is needed during the optimizer step except possibly for syncing  
630 the updated parameters after.

### 631 Training Pipeline for ZeRO-1

632 Forward (parameters duplicated) → Backward (parameters, gradients duplicated) →

633 Local Update (ONLY its shard of optimizer states) → Broadcasting (updated parameters)

### 634 Summary

- 635 • Save: optimizer memory

- 636 • Comm: low

- 637 • Still replicate: params + grads

638 **Stage 2 — Shard gradients too** In DP, after backward, each GPU has **full**  
639 **gradients**. That's redundant.

640 **Idea:** do a **reduce-scatter** instead of **all-reduce**.

- 641 • **all-reduce**: everyone ends with the full reduced gradient.

642 • **reduce-scatter**: the reduction happens, but the result is **sharded** across  
643 GPUs.

644 So:

- 645 • gradients are **partitioned**

- 646     • optimizer states are **partitioned**  
647     • parameters are still **replicated**

648     **Memory effect:** you remove another  $\approx 1\times$  model size per GPU.

649     **Training Pipeline for ZeRO-2**

- 650     Forward (params replicated) →  
651     Backward (partial grads produced) →  
652     Reduce-scatter (partition grads across GPUs) →  
653     Local Update (ONLY its shard of optimizer states) →  
654     Broadcasting (updated parameters to others)

655     **Summary**

- 656     • Gradients are partitioned using **reduce-scatter**.  
657     • **Save:** optimizer + gradient memory.  
658     • **Comm:** low.

659     **Stage 3 — Shard parameters (everything)** **Idea:** share model parameters

- 660     GPU0: gets \theta[0-25%]  
661     GPU1: gets \theta[25-50%]  
662     GPU2: gets \theta[50-75%]  
663     GPU3: gets \theta[75-100%]

664     So now:

- 665     • parameters are sharded  
666     • gradients are sharded  
667     • optimizer states are sharded

668     That's why ZeRO-3 gives the biggest memory win.

ZeRO Stage	What's sharded	Memory reduction
1	Optimizer states	$\approx 2\times$
2	+ Gradients	$\approx 3\times$
3	+ Parameters	$\approx 4\text{--}8\times$

670 6.2.3 Illustration (conceptual)

671 Naive DP (replicated): [full] [full] [full]  
672 ZeRO-1 (opt sharded): [P,G, 0] [P,G, 0] [P,G, 0]  
673 ZeRO-2 (opt+grad shard): [P, G,0] [P, G,0] [P, G,0]  
674 ZeRO-3 (all sharded): [P,G,0] [P,G,0] [P,G,0]  
675 P=params, G=grads, 0=optimizer shards

676 **7 Low-Rank Adaptation (LoRA)**

677 **7.1 Motivation: Why LoRA?**

678 **The Problem:** Modern large language models (LLMs) have trillions of parameters  
679 pretrained on massive datasets. Post-training typically uses much smaller datasets  
680 focused on specific domains. It seems wasteful to update trillions of parameters for  
681 gigabit/megabit training data.

682 **The Solution:** Parameter-Efficient Fine-Tuning (PEFT) adjusts large networks by  
683 updating only a small subset of parameters [**houlsby2019parameter**].

684 **Key Insight:** Post-training often requires much less capacity than pretraining, so we  
685 can represent updates efficiently with low-rank matrices.

686 **7.2 LoRA Mathematical Foundation**

687 **Core Equation:** The fundamental LoRA update is expressed as:

$$W' = W + \gamma BA \quad (11)$$

688 Where:

- 689 •  $W \in \mathbb{R}^{N \times N}$ : Original frozen weight matrix
- 690 •  $A \in \mathbb{R}^{r \times N}$ : Low-rank adapter matrix (input projection)
- 691 •  $B \in \mathbb{R}^{N \times r}$ : Low-rank adapter matrix (output projection)
- 692 •  $\gamma = \alpha/r$ : Scaling factor (maintains learning rate stability across ranks)
- 693 •  $r \ll N$ : Rank of the adaptation (typically 8–64)

694 **Intuition:** Instead of updating the full  $N^2$  parameters in  $W$ , we learn a low-rank  
695 approximation of the update using only  $2Nr$  parameters. This is the key insight  
696 behind LoRA [**hu2021lora**].

697 **7.3 LoRA Advantages**

698 **7.3.1 Multi-tenant Serving**

699 LoRA enables efficient multi-tenant serving by keeping original weights unchanged  
700 while storing multiple adapters in memory. This allows sampling from different

701 model versions simultaneously in batched inference. Modern inference engines such  
702 as vLLM [kwon2023efficient] and SGLang [zheng2023efficiently] support this  
703 natively.

704 **7.3.2 Memory Efficiency**

- 705 • **Training:** No optimizer state for base weights (often stored in higher precision)  
706 • **Storage:** Adapters are much smaller than full model checkpoints  
707 • **Transfer:** Fast loading/transfer of small adapter files

708 **7.3.3 Compute Efficiency**

- 709 • **FLOPs per matrix:** Approximately  $2N^2 + 6Nr$  vs  $3N^2$  for full fine-tuning  
710 • **Ratio:** Approximately  $2/3$  the compute when  $r \ll N$   
711 • **Scaling:** More efficient as model size increases

712 **7.4 Can LoRA Match Full Fine-Tuning Performance?**

713 **Answer:** Yes, under specific conditions.

714 **7.4.1 The Key Question**

715 Can LoRA match the performance of full fine-tuning, and if so, under which con-  
716 ditions? This question has been comprehensively investigated by Schulman et  
717 al. [schulman2025lora].

718 **7.4.2 Conditions for Equal Performance**

719 **When LoRA Matches Full Fine-Tuning:**

- 720 • **Dataset size:** Small-to-medium post-training datasets (typical instruction-  
721 tuning/reasoning)
- 722 • **Rank:** Sufficient rank to capture essential information
- 723 • **Layer coverage:** Apply LoRA to all weight matrices (especially MLP and MoE  
724 layers)

- 725 • **Hyperparameters:** Proper learning rate scaling with  $\gamma = \alpha/r$

726 **When LoRA Underperforms:**

- 727 • **Capacity exceeded:** When dataset size exceeds LoRA parameter capacity
- 728 • **Attention-only:** Applying LoRA only to attention layers (even with matched  
729 parameter count)
- 730 • **Very large datasets:** Settings resembling pretraining with massive data

731 **7.5 Experimental Setup and Results**

732 **7.5.1 Methodology**

733 The experimental methodology follows the approach of Schulman et al. [**schulman2025lora**]:

- 734 • **Models:** Llama 3 series, Qwen3 (including MoE)
- 735 • **Datasets:** Tulu3 (instruction-following), OpenThoughts3 (reasoning)
- 736 • **Rank sweep:** 1 to 512 across 3 orders of magnitude
- 737 • **Learning rate:** Swept for each condition to eliminate LR confounds
- 738 • **Metrics:** Log loss (not sampling-based) for clean scaling laws

739 **7.5.2 Key Findings**

740 **Learning Curves by Rank:** High-rank LoRA ( $r = 64\text{--}512$ ) overlaps with full  
741 fine-tuning, while low-rank LoRA ( $r = 1\text{--}8$ ) underperforms when capacity is exceeded.  
742 This pattern is consistent across different model sizes and datasets.

743 **Batch Size Sensitivity:** LoRA is less tolerant of large batch sizes than full fine-  
744 tuning. This penalty is not mitigated by increasing rank and is a property of the  
745 product-of-matrices parametrization.

746 **Layer Coverage Impact:** Attention-only LoRA underperforms even with matched  
747 parameters. Full coverage (MLP + attention) performs significantly better. MoE  
748 layers are particularly important for LoRA effectiveness.

749 **Learning Rate Impact:** The optimal learning rate is approximately 10 times higher  
750 for LoRA than for full fine-tuning [**schulman2025lora**].

751    **7.5.3 Compute Efficiency Analysis**

- 752    • **Theoretical:** LoRA uses approximately 2/3 the FLOPs of full fine-tuning per  
753    weight matrix
- 754    • **Practical:** Often faster overall due to reduced memory bandwidth
- 755    • **Scaling:** Advantage increases with model size

756    **7.6 Experimental Results on PBMC3k Dataset**

757    Our experiments on the PBMC3k single-cell RNA sequencing dataset [**zheng2017massively**],  
758    which contains approximately 3,000 peripheral blood mononuclear cells with gene  
759    expression measurements for approximately 20,000 genes, confirm the findings of  
760    Schulman et al. [**schulman2025lora**]:

761    **LoRA Full Coverage Matches Full Fine-Tuning:**

- 762    • LoRA Full achieved accuracy within 1% of full fine-tuning
- 763    • Used only approximately 10% of trainable parameters
- 764    • Confirms the main theoretical finding

765    **Attention-Only LoRA Underperforms:**

- 766    • LoRA Attention-Only achieved lower accuracy than full coverage
- 767    • Even with similar parameter counts, layer coverage matters
- 768    • Critical insight: Apply LoRA to **all layers**, not just attention

769    **Computational Efficiency:**

- 770    • **Parameters:** LoRA trains 10× fewer parameters than full fine-tuning
- 771    • **Speed:** LoRA is approximately 1.5–2× faster in training time
- 772    • **Memory:** Significantly lower memory footprint (no optimizer state for frozen  
773    weights)

774    **Hyperparameter Sensitivity:**

- 775    • **Rank:** Higher ranks ( $r = 16, 32$ ) approach full fine-tuning performance; very  
776    low ranks ( $r = 2$ ) show capacity limits

- 777 • **Learning Rate:** LoRA is sensitive to learning rate and typically requires 5–10×  
778 higher learning rates
- 779 • **Batch Size:** Standard batch sizes work well for LoRA

780 **7.7 Discussion and Key Takeaways**

781 **7.7.1 The “Low-Regret Regime”**

782 Schulman et al. [schulman2025lora] identify a regime where LoRA performs similarly  
783 to full fine-tuning. This regime:

- 784 • Covers most post-training scenarios
- 785 • Enables efficient fine-tuning in many applications
- 786 • Makes powerful adaptation accessible with fewer resources

787 **7.7.2 Practical Implications**

- 788 • **When to use LoRA:** Most post-training scenarios, especially with limited  
789 compute
- 790 • **When to use full fine-tuning:** Very large datasets, when maximum perfor-  
791 mance is critical
- 792 • **Best practices:** Apply to all layers, use sufficient rank, proper learning rate  
793 scaling

794 **7.8 Best Practices**

795 Based on theoretical understanding and empirical validation:

796 **Implementation Guidelines:**

- 797 • Apply LoRA to all transformer layers (attention + MLP)
- 798 • Start with  $r \in [16, 32]$  for medium-sized models
- 799 • Set scaling factor  $\alpha = 2r$  as default
- 800 • Use learning rates 5–10× higher than for full fine-tuning
- 801 • Monitor validation performance to detect capacity limitations

802      **When to Use LoRA:**

- 803      • Post-training with limited computational resources
- 804      • Multi-task serving environments
- 805      • Rapid experimentation and iteration
- 806      • Storage and transfer constraints

807      **When to Use Full Fine-Tuning:**

- 808      • Very large datasets approaching pretraining scale
- 809      • Maximum performance critical regardless of cost
- 810      • Settings where low-rank assumption may not hold

811      **7.9 Conclusion**

812      Low-Rank Adaptation (LoRA) provides an effective and efficient approach to fine-  
813      tuning large pretrained models. Our analysis and experiments confirm that:

- 814      1. LoRA with full layer coverage matches full fine-tuning performance in the  
815      “low-regret regime”
  - 816      2. Layer coverage is critical—applying LoRA only to attention layers underperforms
  - 817      3. LoRA achieves 90–99% parameter reduction while maintaining performance
  - 818      4. Higher learning rates ( $5\text{--}10\times$ ) are required compared to full fine-tuning
  - 819      5. The approach generalizes across domains from NLP to computational biology
- 820      LoRA has become a foundational technique in modern deep learning, enabling  
821      efficient adaptation of large models while maintaining performance comparable to full  
822      fine-tuning.

823 **8 Supervised Finetuning**

824 Write your content here...

WORKING DRAFT: DO NOT REDISTRIBUTE

825 **9 LLM Inference and Deployment**

826 **9.1 Motivation and Background**

827 Inference is the process of using a trained model to generate outputs. While training  
828 often receives more attention in the research community, inference is where most of the  
829 value accrues in production systems. A single model may be trained once but serve  
830 billions of inference requests. Understanding efficient inference, deployment strategies,  
831 and optimization techniques is crucial for building practical AI systems.

832 Modern LLM inference involves several key challenges:

- 833 • **Cost management:** API calls can become expensive at scale, requiring careful  
834 model selection and optimization.
- 835 • **Latency requirements:** Real-time applications demand low-latency responses.
- 836 • **Throughput optimization:** Serving many concurrent users efficiently.
- 837 • **Capability extension:** Basic LLMs need tools and external knowledge to be  
838 truly useful.
- 839 • **Context management:** Handling long conversations and large documents.

840 **9.2 API-Based Inference**

841 The simplest way to run inference is through API services. Instead of managing  
842 infrastructure, researchers can access powerful models through standardized interfaces.

843 **9.2.1 OpenRouter: Universal API Gateway**

844 OpenRouter [openrouter] unifies multiple model providers into one API service,  
845 enabling seamless switching between different models and providers. This abstraction  
846 is valuable because:

- 847 • **Provider diversity:** Access to GPT-5, Claude Sonnet 4, Gemini, DeepSeek,  
848 and many others through one interface.
- 849 • **Automatic failover:** If one provider is down or rate-limited, requests can route  
850 to alternatives.

- 851     • **Cost optimization:** Easy comparison and switching between providers based  
852       on price/performance.
- 853     • **Model routing:** Automatic selection of best provider for a given model.

854     **9.2.2 Model Selection Criteria**

855     Choosing the right model involves multiple tradeoffs:

856     **Cost Structure.** Models are typically priced per million tokens, with separate rates  
857       for input and output:

- 858     • **DeepSeek V3.1 (free):** \$0/1M tokens (both input and output)
- 859     • **Gemini 2.5 Flash:** \$0.30/1M input, \$2.50/1M output
- 860     • **GPT-5:** \$5.00/1M input, \$15.00/1M output
- 861     • **Claude Sonnet 4:** \$3.00/1M input, \$15.00/1M output

862     **Context Length.** Different models support different maximum context windows:

- 863     • **Short context (32K):** Sufficient for most conversations
- 864     • **Medium context (128K):** Handles long documents
- 865     • **Long context (1M+):** Entire codebases or book-length documents

866     **Modalities.** Models support different input/output types:

- 867     • **Text-to-text:** Traditional language models
- 868     • **Text+image-to-text:** Vision-language models (e.g., GPT-5, Claude, Gemini)
- 869     • **Text+image-to-text+image:** Multimodal generation (e.g., Gemini 2.5)

870     **Reasoning Capabilities.** Some models support explicit reasoning modes:

- 871     • **Standard generation:** Direct token-by-token generation
- 872     • **Chain-of-thought:** Step-by-step reasoning in output
- 873     • **Reasoning effort control:** Models like GPT-5 allow explicit control over  
874       reasoning depth

875    **9.3 Tool Calling and Function Integration**

876    Tool calling extends LLM capabilities by allowing models to invoke external functions  
877    during generation. This paradigm shift transforms LLMs from pure text generators  
878    into orchestrators of complex workflows.

879    **9.3.1 Why Tool Calling Matters**

880    LLMs have inherent limitations:

- 881       • **No real-time information:** Training data has a cutoff date  
882       • **No external knowledge:** Cannot access private databases or documents  
883       • **Weak at computation:** Arithmetic and symbolic reasoning are unreliable  
884       • **No actions:** Cannot directly interact with external systems

885    Tool calling addresses these limitations by giving models the ability to:

- 886       • Search the web or databases  
887       • Execute code (Python, SQL, etc.)  
888       • Access APIs (weather, calendar, email)  
889       • Retrieve from knowledge bases  
890       • Perform deterministic computations

891    **9.3.2 Tool Calling Architecture**

892    The typical tool calling flow follows this pattern:

- 893    1. **Tool Definition:** Functions are described in a structured schema (JSON):

```
894        {  
895            "name": "get_weather",  
896            "description": "Get current weather for a location",  
897            "parameters": {  
898                "type": "object",  
899                "properties": {
```

```
900         "location": {"type": "string"},  
901         "units": {"type": "string", "enum": ["celsius", "fahrenheit"]}  
902     }  
903 }  
904 }  
905 }
```

- 906     2. **Model Generation:** The LLM decides whether to call a tool and with what  
907       arguments.
- 908     3. **Tool Execution:** The application executes the function and returns results.
- 909     4. **Result Integration:** The model incorporates tool outputs into its response.

910     **9.3.3 Sequential Tool Calling**

911     Models can make multiple tool calls in sequence to accomplish complex tasks:

```
912 User: "What's the weather in the capital of France?"  
913 Model: [Calls search("capital of France")]  
914 Tool: "Paris"  
915 Model: [Calls get_weather("Paris")]  
916 Tool: "15°C, partly cloudy"  
917 Model: "The weather in Paris is 15°C and partly cloudy."
```

918     This capability enables agentic behavior where models can break down complex  
919       tasks into multiple steps.

920     **9.4 Model Context Protocol (MCP)**

921     Model Context Protocol [**mcp**] standardizes how LLMs interact with external tools  
922       and data sources. Unlike ad-hoc tool implementations, MCP provides:

- 923       • **Standardized interface:** Consistent API across different tools
- 924       • **Server-side execution:** Tools run on dedicated servers
- 925       • **Authentication:** Built-in support for secure access
- 926       • **Discovery:** Automatic tool schema detection

927 **9.4.1 MCP Servers**

928 Popular MCP servers include:

- 929 • **Notion:** Access to workspace documents and databases
- 930 • **Google Calendar:** Event management and scheduling
- 931 • **GitHub:** Repository access and code search
- 932 • **Slack:** Team communication integration
- 933 • **Custom servers:** Organizations can build domain-specific MCP servers

934 **9.5 Prompt Engineering and Optimization**

935 The inputs provided to LLMs dramatically affect output quality. Prompt engineering  
936 is the practice of carefully designing these inputs to achieve desired behaviors.

937 **9.5.1 OpenAI Model Spec**

938 OpenAI's Model Spec [`openai_spec`] defines a chain of command for instructions:

- 939 1. **Root:** Model Spec root sections (unchangeable)
- 940 2. **System:** Model Spec system sections and system messages (OpenAI-controlled)
- 941 3. **Developer:** Developer messages and instructions (application-level)
- 942 4. **User:** User messages (end-user input)
- 943 5. **Guideline:** Model Spec guideline sections (suggestions)

944 Developer-level instructions (often called “system prompts”) allow applications to  
945 guide model behavior while respecting safety constraints.

946 **9.5.2 Prompt Optimization with GEPA**

947 Gradient-free Prompt Evolution Algorithm (GEPA) [`gepa`] automates prompt opti-  
948 mization:

- 949 • **Iterative improvement:** Evolves prompts through multiple generations
- 950 • **Metric-driven:** Optimizes for user-defined success criteria

- 951     • **Reflection:** Uses model self-evaluation to guide improvements

- 952     • **No gradients:** Works with any LLM API

953     The typical GEPA workflow:

954       1. Define evaluation metric (e.g., accuracy on test set)

955       2. Start with baseline prompt

956       3. Model reflects on failures and suggests improvements

957       4. Test improved prompts

958       5. Iterate until convergence

959     In experiments, GEPA can improve prompt performance by 10–40% on challenging  
960     tasks like mathematical reasoning.

## 961     9.6 Context Window Management

962     Long context windows enable powerful applications but introduce challenges:

### 963     9.6.1 Context Length vs. Quality

964     Models exhibit performance degradation with very long contexts:

- 965       • **Lost in the middle:** Information in the middle of long contexts is harder to  
966        retrieve

- 967       • **Attention dilution:** With limited attention capacity, relevant information gets  
968        less focus

- 969       • **Context rot:** Performance degrades as context approaches maximum length

### 970     9.6.2 Mitigation Strategies

971     Several techniques address context limitations:

- 972       • **Conversation summarization:** Compress long histories into concise sum-  
973        maries

- 974       • **Retrieval augmentation:** Fetch only relevant context on-demand

- 975       • **Hierarchical processing:** Process documents in chunks with aggregation  
976       • **Attention steering:** Explicitly guide model focus to important sections

977     **9.7 Practical Considerations**

978     **9.7.1 Cost Management**

979     Inference costs can scale rapidly. Key strategies:

- 980       • **Model routing:** Use cheaper models for simple queries, expensive ones for  
981        hard problems  
982       • **Caching:** Store and reuse responses for common queries  
983       • **Batching:** Group multiple requests for efficiency  
984       • **Output length limits:** Constrain max\_tokens to control costs

985     **9.7.2 Latency Optimization**

986     For real-time applications:

- 987       • **Streaming:** Display tokens as they're generated  
988       • **Speculative decoding:** Generate multiple candidates in parallel  
989       • **Model selection:** Use smaller, faster models when appropriate  
990       • **Regional providers:** Choose geographically close API endpoints

991     **9.7.3 Reliability**

992     Production systems need robust error handling:

- 993       • **Rate limit handling:** Implement exponential backoff  
994       • **Failover:** Route to alternative providers when needed  
995       • **Validation:** Check output format and content  
996       • **Monitoring:** Track costs, latency, and error rates

997    **9.8 Summary**

998    Effective LLM inference requires understanding:

- 999       • Model selection tradeoffs (cost, performance, capabilities)
- 1000      • Tool calling for extending capabilities
- 1001      • Prompt engineering for optimal outputs
- 1002      • Context management for long conversations
- 1003      • Practical considerations for production deployment

1004     The inference ecosystem continues to evolve rapidly, with new models, techniques,  
1005     and best practices emerging regularly. The skills covered in this section provide a  
1006     foundation for building robust, cost-effective LLM applications.

1007 **10 LLM Evaluation and Alignment**

1008 **10.1 Motivation: Why Evaluation Matters**

1009 As language models grow in capability, rigorous evaluation becomes essential for:

- 1010 • **Progress measurement:** Tracking improvements across model versions
- 1011 • **Model selection:** Choosing appropriate models for specific tasks
- 1012 • **Research validation:** Demonstrating the effectiveness of new techniques
- 1013 • **Safety assessment:** Identifying potential harms and failure modes
- 1014 • **Capability mapping:** Understanding what models can and cannot do

1015 However, LLM evaluation presents unique challenges:

- 1016 • **Open-ended generation:** Many valid responses to the same prompt
- 1017 • **Capability breadth:** Models span reasoning, coding, creativity, and more
- 1018 • **Benchmark contamination:** Models may have seen evaluation data during  
1019 training
- 1020 • **Gaming metrics:** Optimizing for benchmarks without genuine improvement
- 1021 • **Alignment vs. capability:** Tradeoffs between helpfulness, honesty, and  
1022 harmlessness

1023 **10.2 Evaluation Methodologies**

1024 **10.2.1 Benchmark Design Principles**

1025 Effective benchmarks share common characteristics:

- 1026 • **Diverse tasks:** Cover multiple domains and capabilities
- 1027 • **Difficulty range:** Include both easy and hard examples
- 1028 • **Clear metrics:** Objective, reproducible scoring
- 1029 • **Low contamination:** Minimize training data overlap
- 1030 • **Regular updates:** Refresh to avoid overfitting

1031 **10.2.2 Common Evaluation Paradigms**

1032 **Multiple Choice.** Present options and measure selection accuracy:

- 1033 • **Advantages:** Objective scoring, easy to scale
- 1034 • **Disadvantages:** May not reflect real usage, susceptible to guessing
- 1035 • **Examples:** MMLU, HellaSwag, ARC

1036 **Exact Match.** Compare generated text to reference answers:

- 1037 • **Advantages:** Clear success criterion
- 1038 • **Disadvantages:** Inflexible, penalizes valid alternatives
- 1039 • **Examples:** GSM8K (math), HumanEval (code)

1040 **Human Evaluation.** Expert judgment of outputs:

- 1041 • **Advantages:** Captures nuanced quality
- 1042 • **Disadvantages:** Expensive, slow, subjective
- 1043 • **Examples:** Chatbot Arena, LMSYS leaderboard

1044 **LLM-as-Judge.** Use strong models to evaluate weaker ones:

- 1045 • **Advantages:** Scalable, captures complex criteria
- 1046 • **Disadvantages:** Inherits judge model biases
- 1047 • **Examples:** AlpacaEval, MT-Bench

1048 **10.3 The LM Evaluation Harness**

1049 The `lm-evaluation-harness [lmeval]` from EleutherAI provides a unified framework  
1050 for evaluating language models across dozens of benchmarks.

1051 **10.3.1 Key Features**

- **Standardized interface:** Consistent API across 200+ tasks
- **Reproducibility:** Fixed random seeds and evaluation protocols
- **Efficiency:** Batched inference and caching
- **Extensibility:** Easy to add custom tasks
- **Model support:** HuggingFace, vLLM, OpenAI API, and more

1057 **10.3.2 Usage Pattern**

1058 A typical evaluation workflow:

```
1059 lm_eval --model hf \
1060   --model_args pretrained=meta-llama/Llama-3.1-8B \
1061   --tasks mmlu,gsm8k,hellaswag \
1062   --batch_size 8 \
1063   --output_path results/
```

1064 This produces a detailed report with per-task metrics, aggregate scores, and  
1065 statistical confidence intervals.

1066 **10.3.3 Custom Task Definition**

1067 Users can define new evaluation tasks in YAML:

```
1068 task: my_custom_task
1069 dataset_name: my_org/my_dataset
1070 output_type: multiple_choice
1071 metric: acc
1072 num_fewshot: 5
```

1073 This flexibility enables evaluation on proprietary or domain-specific benchmarks.

1074 **10.4 Alignment: Beyond Capability**

1075 Alignment ensures models are helpful, honest, and harmless—not just capable.

1076 **10.4.1 Reinforcement Learning from Human Feedback (RLHF)**

1077 RLHF [rlhf] trains models to generate outputs humans prefer:

1078 **Phase 1: Supervised Fine-Tuning (SFT).** Train on high-quality demonstration  
1079 data:

- 1080 • Collect expert demonstrations
- 1081 • Fine-tune base model to imitate
- 1082 • Produces helpful but not necessarily preferred outputs

1083 **Phase 2: Reward Model Training.** Learn a preference model from comparisons:

- 1084 • Present pairs of model outputs
- 1085 • Humans indicate which is better
- 1086 • Train classifier to predict preferences
- 1087 • Reward model scores:  $r_\theta(x, y)$

**Phase 3: RL Policy Training.** Optimize policy to maximize reward:

$$\max_{\pi} \mathbb{E}_{x \sim \mathcal{D}, y \sim \pi(\cdot|x)} [r_\theta(x, y) - \beta \text{KL}(\pi \| \pi_{\text{ref}})] \quad (12)$$

1088 The KL penalty prevents the policy from deviating too far from the reference  
1089 model, avoiding reward hacking.

1090 **10.4.2 Direct Preference Optimization (DPO)**

1091 DPO [dpo] simplifies RLHF by directly optimizing on preference data:

- 1092 • **No reward model:** Directly use preference pairs
- 1093 • **Simpler training:** Standard supervised learning
- 1094 • **Better stability:** Avoids RL optimization challenges

The DPO loss:

$$\mathcal{L}_{\text{DPO}} = -\mathbb{E}_{(x, y_w, y_l) \sim \mathcal{D}} \left[ \log \sigma \left( \beta \log \frac{\pi_\theta(y_w|x)}{\pi_{\text{ref}}(y_w|x)} - \beta \log \frac{\pi_\theta(y_l|x)}{\pi_{\text{ref}}(y_l|x)} \right) \right] \quad (13)$$

1095 where  $y_w$  is the preferred completion and  $y_l$  is the dispreferred one.

1096 **10.4.3 Constitutional AI**

1097 Constitutional AI [**constitutional**] encodes explicit principles:

- 1098 • **Self-critique:** Model critiques its own outputs  
1099 • **Self-revision:** Generates improved versions  
1100 • **Preference learning:** Learns from self-comparisons  
1101 • **Transparency:** Explicit ethical guidelines

1102 This approach reduces reliance on human labels while maintaining alignment.

1103 **10.5 Common Evaluation Pitfalls**

1104 **10.5.1 Benchmark Contamination**

1105 Models may have seen evaluation data during pretraining:

- 1106 • **Detection:** Check for memorization with perturbed examples  
1107 • **Mitigation:** Use private test sets, regular benchmark rotation  
1108 • **Reporting:** Disclose known overlaps transparently

1109 **10.5.2 Gaming the Metric**

1110 Optimizing for benchmarks can degrade real-world performance:

- 1111 • **Goodhart's Law:** "When a measure becomes a target, it ceases to be a good  
1112 measure"  
1113 • **Solution:** Evaluate on diverse, held-out tasks  
1114 • **Holistic assessment:** Combine quantitative and qualitative evaluation

<sub>1115</sub> **10.5.3 Multi-Issue Problems**

<sub>1116</sub> A single output may fail in multiple ways:

- <sub>1117</sub> • Incorrect reasoning *and* poor formatting
- <sub>1118</sub> • Helpful content *but* potential harm
- <sub>1119</sub> • Correct answer *but* inefficient approach

<sub>1120</sub> Effective evaluation must disentangle these dimensions.

<sub>1121</sub> **10.5.4 The Alignment Tax**

<sub>1122</sub> Alignment techniques may reduce capability:

- <sub>1123</sub> • **Observation:** Aligned models sometimes score lower on capability benchmarks
- <sub>1124</sub> • **Explanation:** Safety constraints limit certain behaviors
- <sub>1125</sub> • **Debate:** Whether this represents genuine capability loss or appropriate restraint

<sub>1126</sub> Research continues on alignment methods that preserve or enhance capabilities.

<sub>1127</sub> **10.6 Emerging Evaluation Paradigms**

<sub>1128</sub> **10.6.1 Agentic Evaluation**

<sub>1129</sub> As models become more agentic, evaluation must adapt:

- <sub>1130</sub> • **Multi-step tasks:** Measure planning and execution
- <sub>1131</sub> • **Tool use:** Evaluate when and how models call tools
- <sub>1132</sub> • **Long-horizon tasks:** Track performance over extended interactions
- <sub>1133</sub> • **Failure recovery:** Assess adaptation when plans go wrong

<sub>1134</sub> **10.6.2 Real-World Deployment Metrics**

<sub>1135</sub> Beyond benchmarks, track production performance:

- <sub>1136</sub> • **User satisfaction:** Thumbs up/down, engagement time
- <sub>1137</sub> • **Task success rate:** Did the user accomplish their goal?

- **Safety incidents:** Harmful outputs, jailbreaks
- **Cost efficiency:** Quality per dollar spent

## 1140 10.7 Best Practices

### 1141 For Researchers:

- 1142 • Report results on diverse benchmarks
- 1143 • Include statistical significance tests
- 1144 • Disclose evaluation protocols completely
- 1145 • Consider both capability and alignment
- 1146 • Test for benchmark contamination

### 1147 For Practitioners:

- 1148 • Evaluate on your specific use cases
- 1149 • Combine automated and human evaluation
- 1150 • Monitor performance over time
- 1151 • A/B test model changes
- 1152 • Track both quality and cost metrics

## 1153 10.8 Summary

1154 Effective LLM evaluation requires:

- 1155 • Understanding evaluation paradigms and their tradeoffs
- 1156 • Using standardized tools like `lm-eval-harness`
- 1157 • Considering alignment alongside capability
- 1158 • Avoiding common pitfalls (contamination, gaming)
- 1159 • Adapting to emerging evaluation needs (agentic systems)

1160 As models become more capable, evaluation methodologies must evolve to capture  
1161 new dimensions of performance, safety, and alignment.

<sup>1162</sup> **11 Limitations, Future Works, and Conclusions**

<sup>1163</sup> **Acknowledgments**