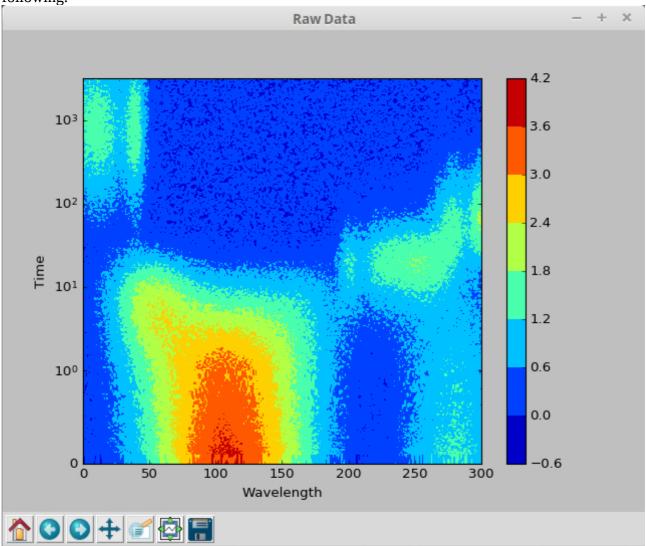


#### $\mathbf{A}$

1. Data should be in absorbance (not transmission) format. The file should be a CSV with the following formatting:

,	Wavelength $\lambda_1$ ,	Wavelength $\lambda_2$ ,
Time t <sub>1</sub> ,	$\Delta(t_1,\lambda_1)$ ,	$\Delta(\mathbf{t}_1,\lambda_2)$ ,
Time t <sub>2</sub> ,	$\Delta(\mathbf{t}_2,\lambda_1)$ ,	$\Delta(\mathbf{t}_2,\lambda_2)$ ,

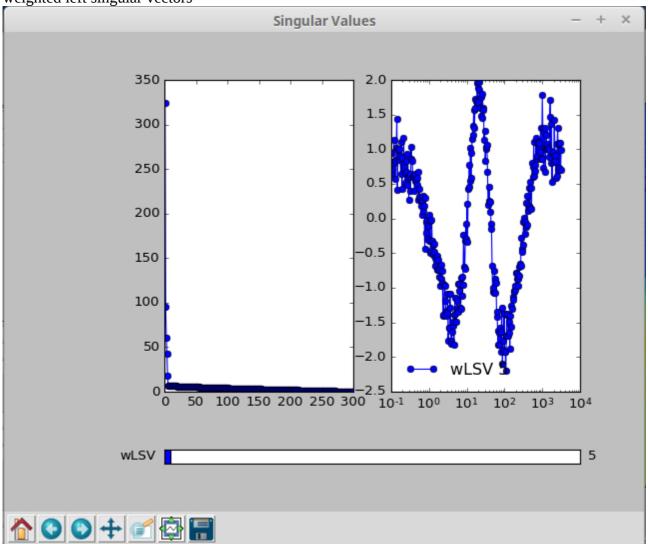
2. When the data is loaded, it will be displayed on a symbolic lin-log plot. This means that the a pseudo log scale will be used for negative time points. In addition, the plot will be linear between -1 and 1. Loading the file synthdata\_noise10.csv from the Data subdirectory should display the following.



3. The Time min/max and Wl min/max are <u>indices</u> for the range of data to be used for fitting. By default, the minimum time point is set to the index of time zero. The wavelengths are set to the full range by default. <u>Note:</u> python indexing begins at 0, -1 indicates the last item.

### $\mathbf{B}$

1. Once data has been loaded, the SVD button will allow you to explore the singular values and weighted left singular vectors



2. After examining the singular values and their corresponding left singular vectors, the GA button will run a global analysis based on the input parameters.

Alpha	Ó
wLSVs	5
Initial Guess	1 5 10 200 2000
Bounds	,(0 10000),(0 10000)

**Alpha**: will allow Tikhonov regularization if set to a value other than 0. By default it is 0, corresponding to an ordinary least-squares

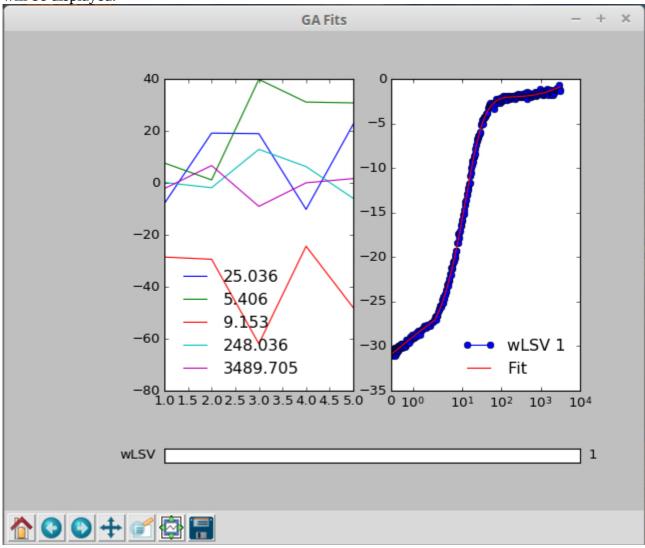
**wLSVs**: the number of wLSVs to include in the fit. A single number, e.g. 5, will include the first 5 vectors. Alternatively, a list can be entered to select specific vectors, with a space between the

number of each vector, e.g.: 1 2 4 5

**Initial Guess**: Will be a guess for each lifetime, separated by a space. The number of guesses must match the number of wLSVs used in the fit.

**Bounds**: Are fitting bounds for the non-linear solver. There must be a matching number of sets of bounds to number of guesses. The bounds are entered in the following format: (lower\_bound upper\_bound),(lower\_bound2 upper\_bound2),... with spaces separating the lower and upper bound for a single lifetime within the parantheses, and only a **comma** separating sets of bounds.

3. Using those values as initial parameters for the synthdata\_noise10, the following results screen will be displayed:



The slider on the bottom allows you to click through each wLSV and fit. You can rerun the fitting procedure if you are unhappy with the agreement of the fit with the vectors. The left panel contains the Decay Associated Spectra (i.e. the pre-exponential functions) for the corresponding lifetimes.

# <u>C</u>

1. These allow you to choose the type of matrix regularization and which sort of penalty matrix to use.

LDA Options

Regularization Method Regularization Matrix

Tikhonov

CLASSO

CElastic Net

CFused

The matrices are as follows:

- Identity is simply an identity matrix
- 1D is a first derivative approximation  $\frac{1}{2} \begin{bmatrix} 1 & -1 & 0 & & \dots \\ 0 & 1 & -1 & 0 & \dots \\ 0 & 0 & 1 & -1 & \dots \end{bmatrix}$

• 2D is a second derivative approximation:

$$\frac{1}{4} \begin{bmatrix}
-2 & 1 & 0 & \cdots \\
1 & -2 & 1 & 0 & \cdots \\
0 & 1 & -2 & 1 & \cdots
\end{bmatrix}$$

• Fused is a combination of the identity and first derivative matrices:

$$\begin{bmatrix} 1 & 0 & 0 & 0 & \cdots \\ 0 & 1 & 0 & 0 & \cdots \\ 0 & 0 & 1 & 0 & \cdots \\ \vdots & & & \vdots \\ 1 & -1 & 0 & & \cdots \\ 0 & 1 & -1 & 0 & \cdots \\ 0 & 0 & 1 & -1 & \cdots \\ \end{bmatrix}$$

## $\mathbf{D}$

1. These settings determine the number and scale of your lifetimes, as well as the alpha selection parameters. Note that for elastic net, the rho values are simply distributed on a scale from 0 to 1 in tenths, in addition to any alpha values you select.

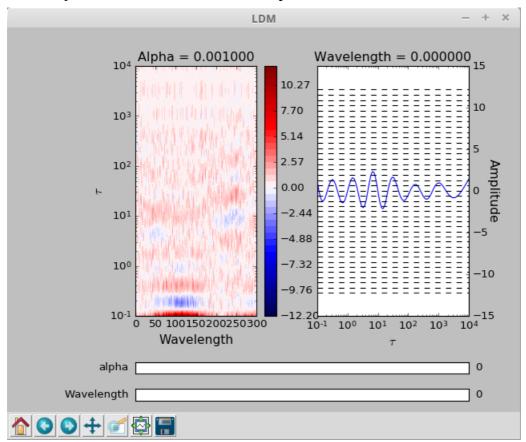
tentins, in addition to any aipha values you select.			
Lifetime Settings			
Min Tau	-1	Log Scale	
Max Tau	4	C Linear Scale	
Num Taus	100		
Alpha Min Alpha Max Num Alphas	Alpha 0.001 1.5 1000	Settings Simultaneous Independently Run LDA	

The lifetimes can be distributed along a linear or log scale. Note that here they are distributed along a log scale, and thus between 10<sup>-1</sup> and 10<sup>4</sup>.

The alphas are distributed along a linear scale. The selection of simultaneous or independently determines whether statistics are generated for all wavelengths together (simultaneous) or each independently.

2. Run LDA will produce a LDM like the following:

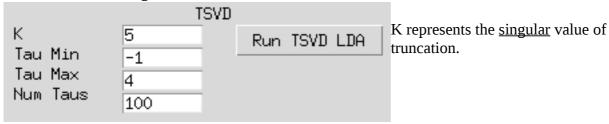
There will be horizontal dashed lines on the LDM corresponding to the lifetimes calculated from Global Analysis if it was run before the LDA procedure.



The alpha slider will allow you to slide through the LDMs produced at each alpha value. The right plot shows a single vertical slice through the LDM, at a particular wavelength. The wavelength slider allows you to look through the results at various wavelengths. The dashed lines represent the contour levels.

### $\mathbf{E}$

1. These settings are similar to those above, except for running a truncated SVD regularization instead of a matrix regularization method.



## $\mathbf{F}$

1. Pressing truncate will provide a low-rank approximation of the data matrix, with the point of truncation being the value entered in wLSVs in **section B**.