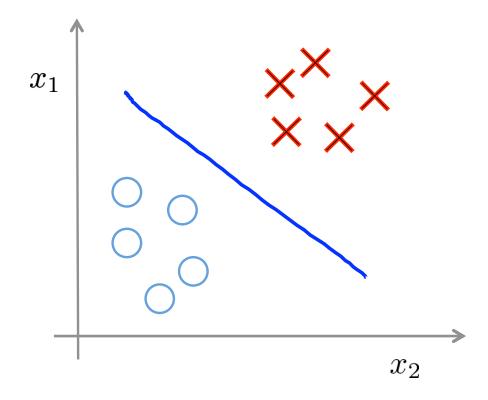


Machine Learning

Clustering

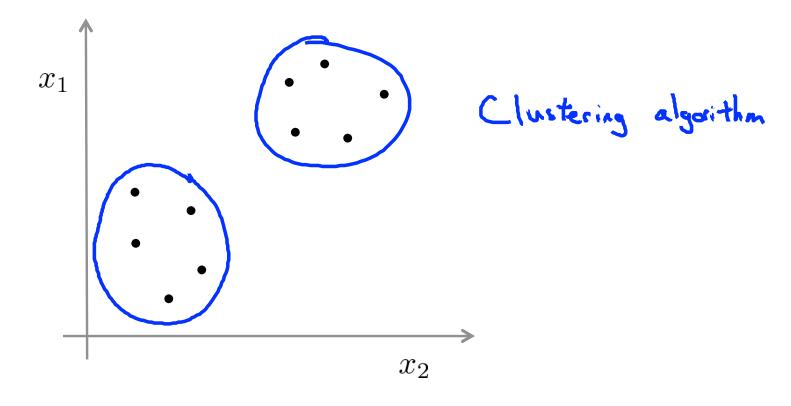
Unsupervised learning introduction

Supervised learning



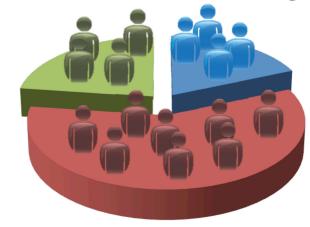
Training set: $\{(x^{(1)}, y^{(1)}), (x^{(2)}, y^{(2)}), (x^{(3)}, y^{(3)}), \dots, (x^{(m)}, y^{(m)})\}$

Unsupervised learning



Training set: $\{x^{(1)}, x^{(2)}, x^{(3)}, \dots, x^{(m)}\}$

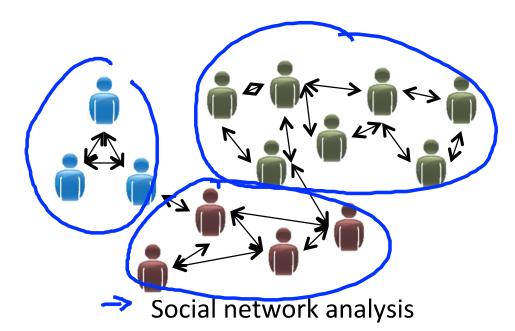
Applications of clustering



Market segmentation

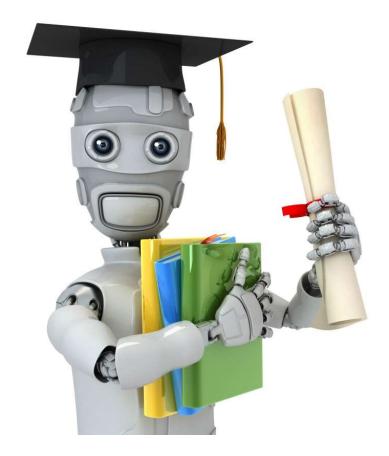


Organize computing clusters





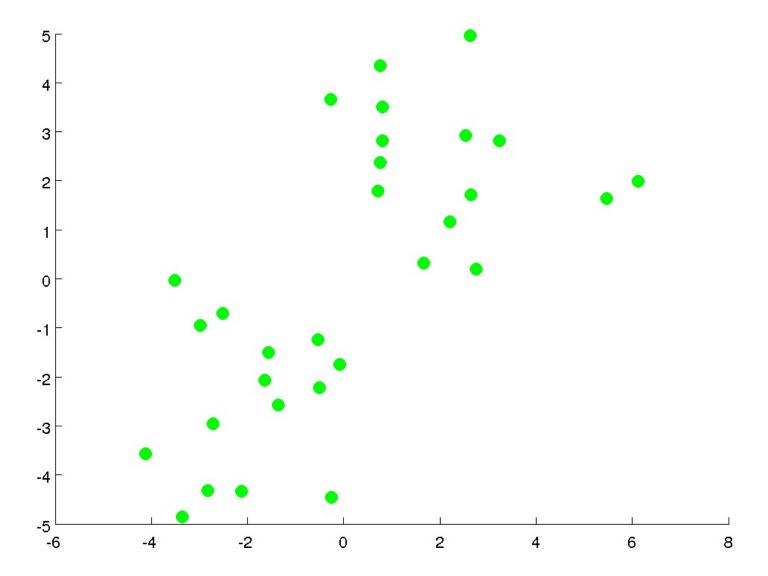
Astronomical data analysis

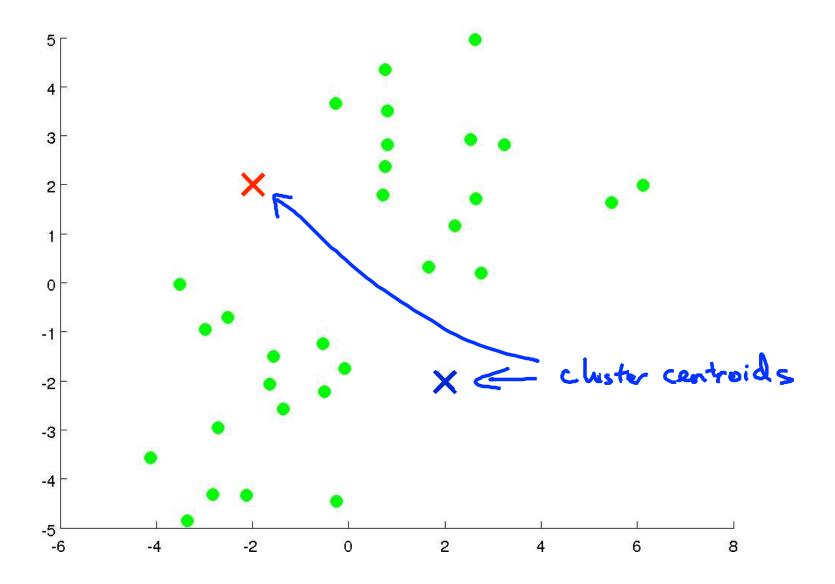


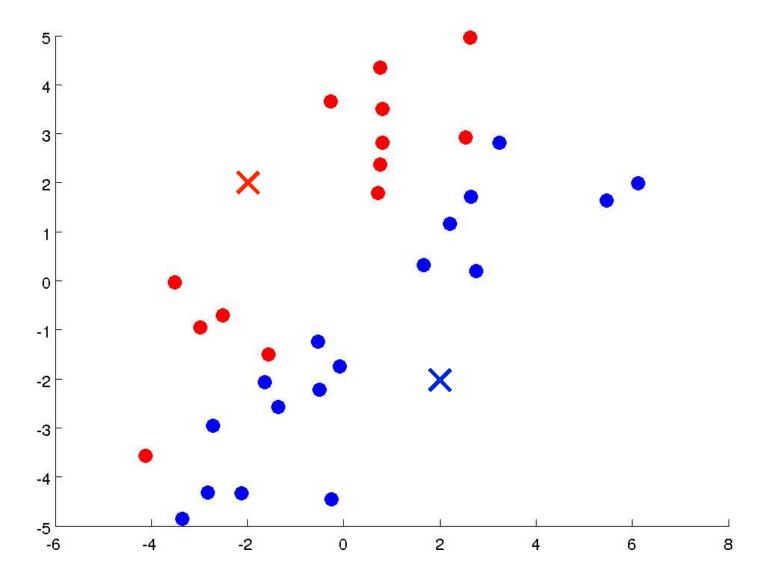
Machine Learning

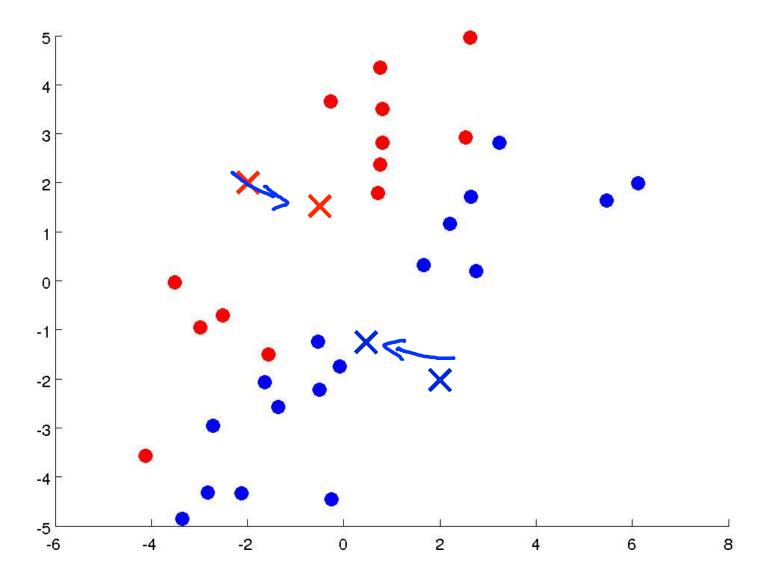
Clustering

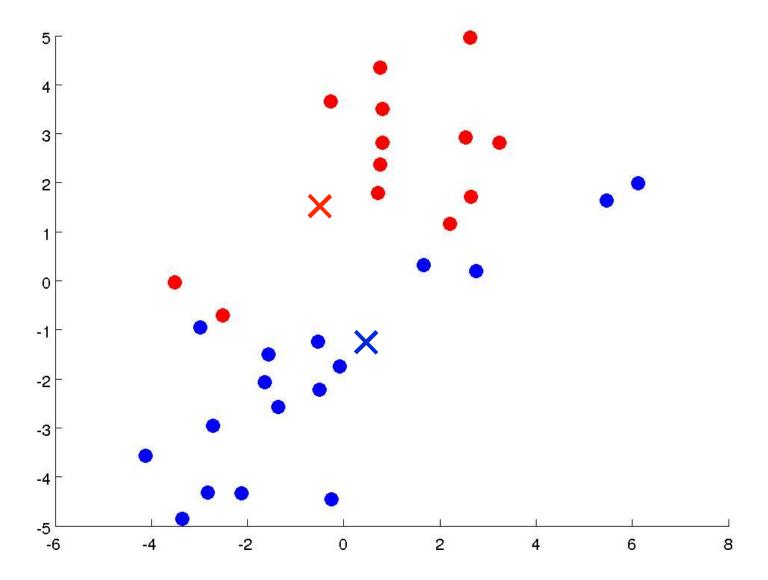
K-means algorithm

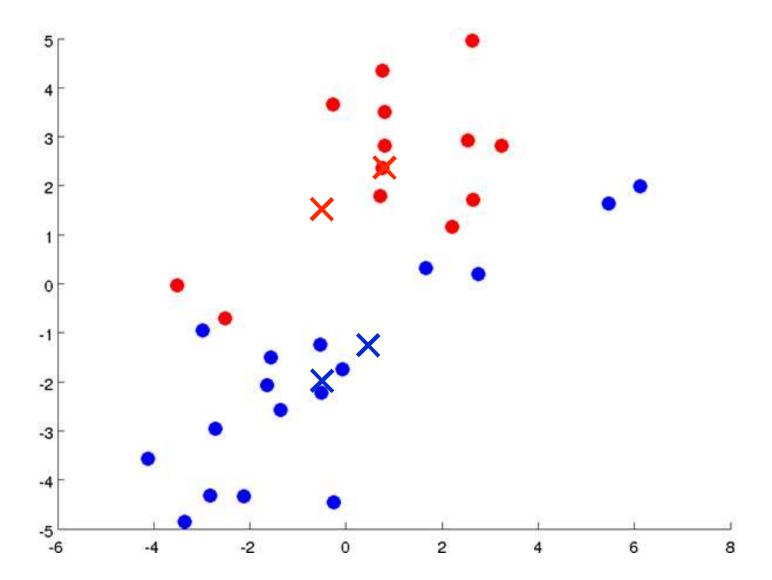


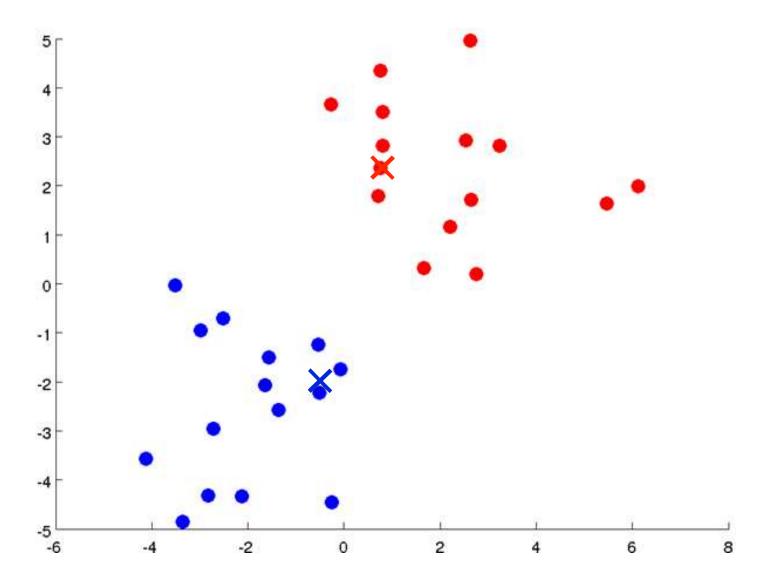


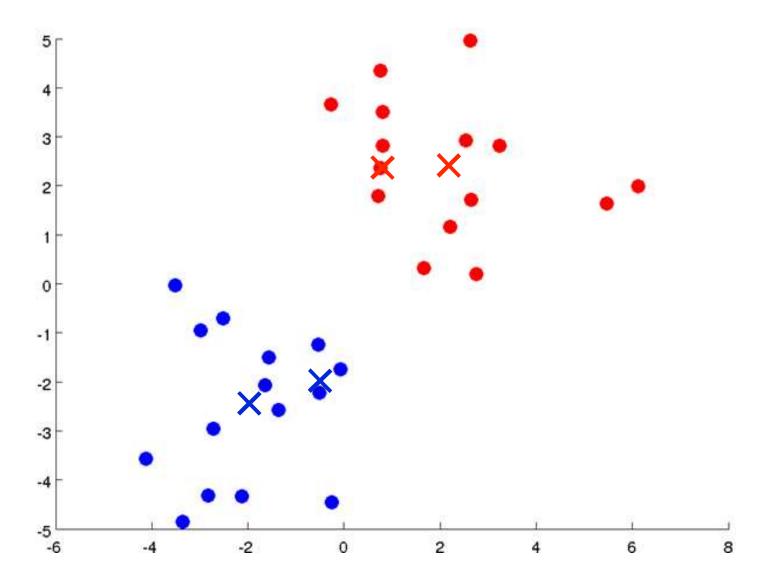


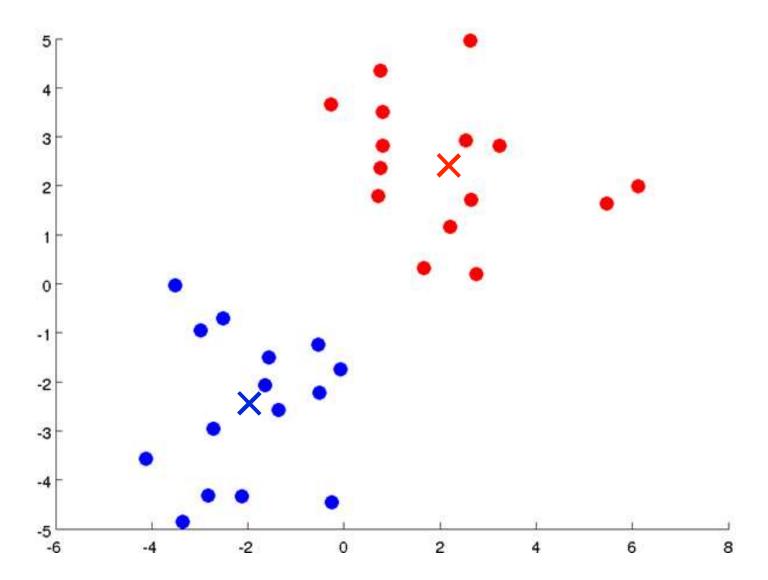












Input:

- K (number of clusters) Training set $\{x^{(1)}, x^{(2)}, \dots, x^{(m)}\}$

$$x^{(i)} \in \mathbb{R}^n$$
 (drop $x_0 = 1$ convention)

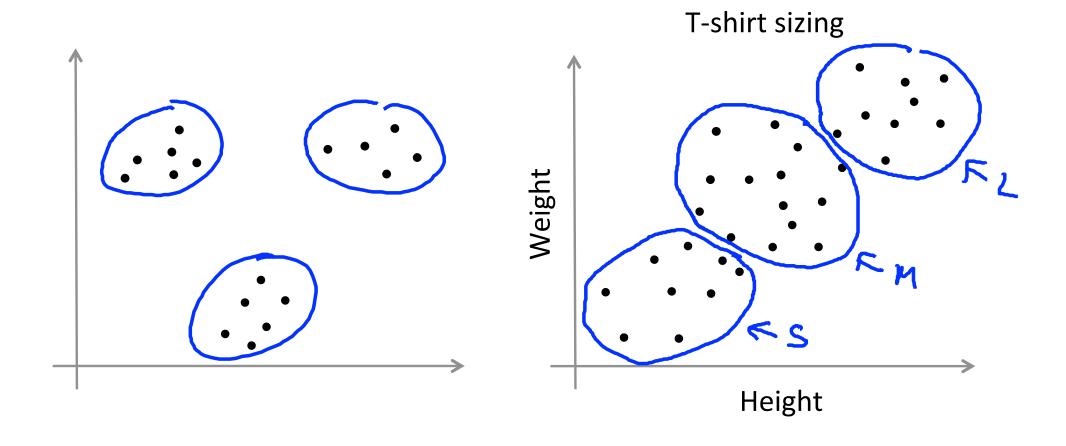


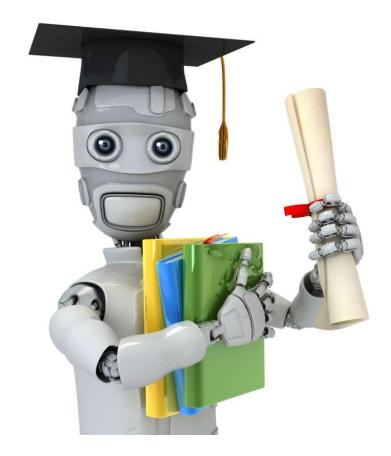
Randomly initialize K cluster centroids $\mu_1, \mu_2, \ldots, \mu_K \in \mathbb{R}^n$ Repeat { The step of the s

$$\underline{c^{(i)}}$$
 := index (from 1 to K) of cluster centroid

K-means for non-separated clusters

S,M,L





Machine Learning

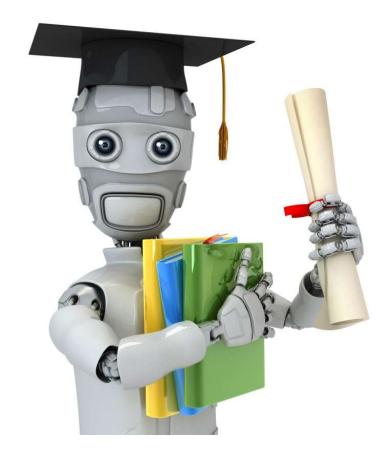
Clustering Optimization objective

K-means optimization objective

- $\rightarrow c^{(i)}$ = index of cluster (1,2,...,K) to which example $x^{(i)}$ is currently assigned
- k e {1,3, ,, k} $\rightarrow \mu_k$ = cluster centroid k ($\mu_k \in \mathbb{R}^n$)
 - $\mu_{c^{(i)}}$ = cluster centroid of cluster to which example $x^{(i)}$ has been assigned $x^{(i)} \rightarrow 5$

Optimization objective:

```
Randomly initialize K cluster centroids \mu_1, \mu_2, \ldots, \mu_K \in \mathbb{R}^n
Repeat {
        for i = 1 to m
            c^{(i)} := \mathsf{index} (from 1 to K ) of cluster centroid
                    closest to x^{(i)}
        for k = 1 to K
             \mu_k := average (mean) of points assigned to cluster k
```



Machine Learning

Clustering Random

initialization

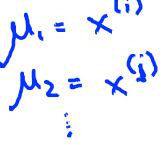
Randomly initialize K cluster centroids $\mu_1, \mu_2, \ldots, \mu_K \in \mathbb{R}^n$

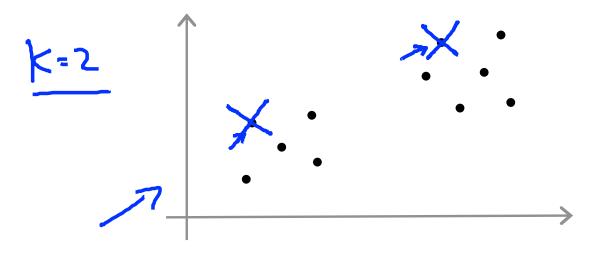
Random initialization

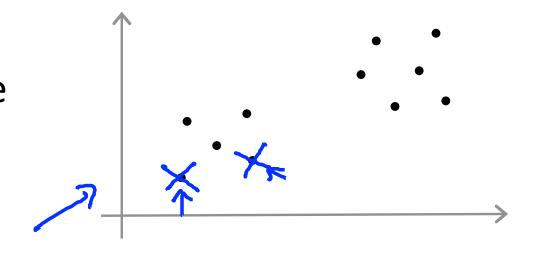
Should have K < m

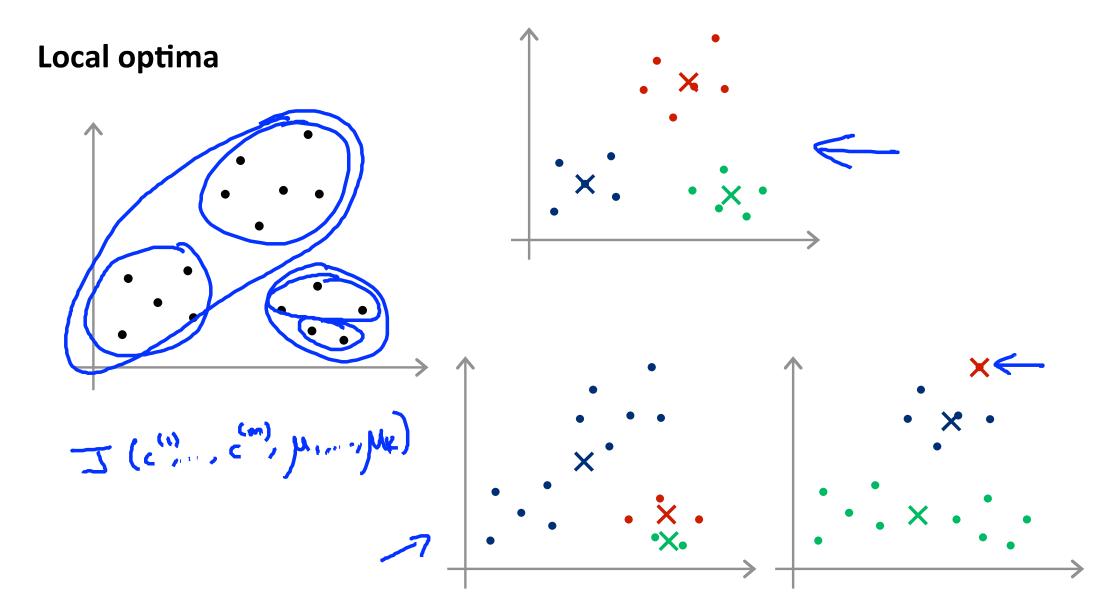
Randomly pick \underline{K} training examples.

Set μ_1, \dots, μ_K equal to these K examples. $\mu_1 = \chi_1$







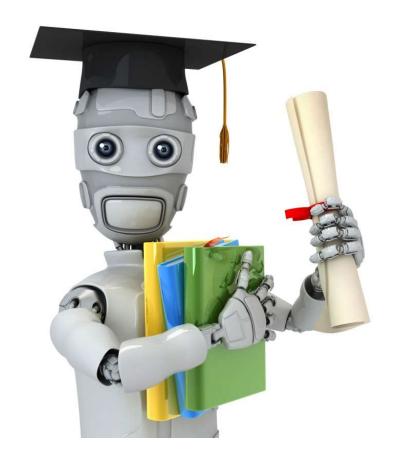


Random initialization

```
For i = 1 to 100 {
```

```
Randomly initialize K-means. Run K-means. Get c^{(1)},\dots,c^{(m)},\mu_1,\dots,\mu_K. Compute cost function (distortion) J(c^{(1)},\dots,c^{(m)},\mu_1,\dots,\mu_K) }
```

Pick clustering that gave lowest cost $J(c^{(1)},\ldots,c^{(m)},\mu_1,\ldots,\mu_K)$

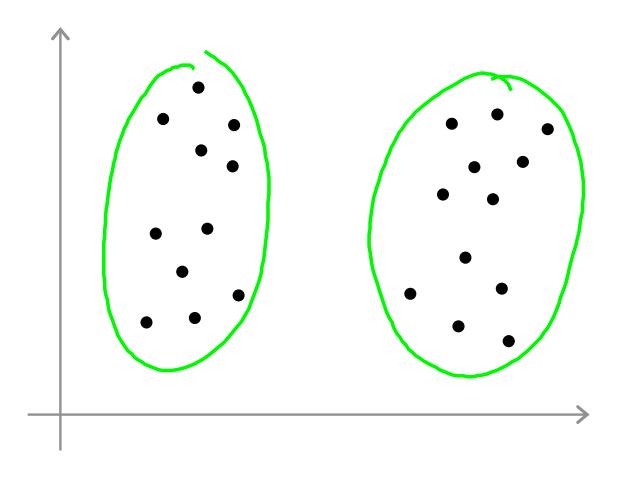


Machine Learning

Clustering

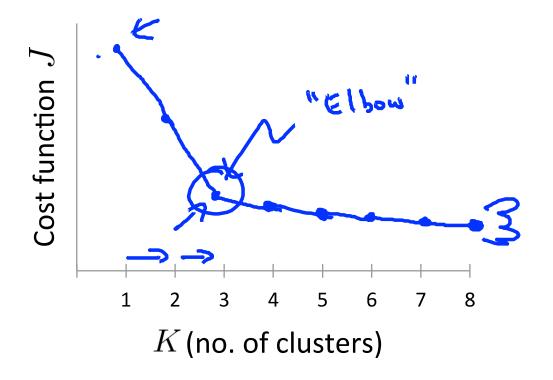
Choosing the number of clusters

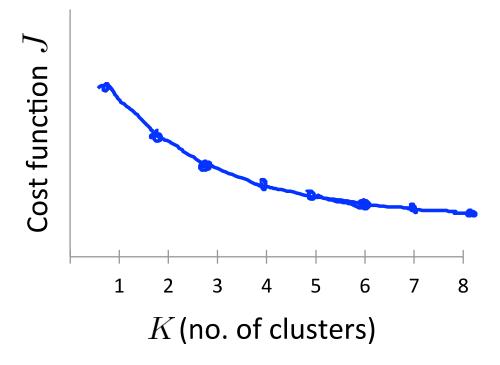
What is the right value of K?



Choosing the value of K

Elbow method:





Choosing the value of K

Sometimes, you're running K-means to get clusters to use for some later/downstream purpose. Evaluate K-means based on a metric for how well it performs for that later purpose.

