

$$(x-x_c)^2 + (y-y_c)^2 = r^2 \text{ — [Equation of circle]}$$

$$\Rightarrow x^2 - 2x_c x + x_c^2 + y^2 - 2y_c y + y_c^2 = r^2$$

$$\Rightarrow x^2 + ax + x_c^2 + y^2 + by + y_c^2 = r^2 \quad \left[\begin{array}{l} a = -2x_c, \\ b = -2y_c \end{array} \right]$$

$$\Rightarrow ax + by + (x_c^2 + y_c^2 - r^2) = -(x^2 + y^2)$$

$$\Rightarrow ax + by + c = -(x^2 + y^2)$$

$$\left\{ \begin{array}{l} a = -2x_c \\ b = -2y_c \\ c = x_c^2 + y_c^2 - r^2 \end{array} \right\}$$

$$ax_1 + by_1 + c = -(x_1^2 + y_1^2)$$

$$ax_2 + by_2 + c = -(x_2^2 + y_2^2)$$

$$ax_3 + by_3 + c = -(x_3^2 + y_3^2)$$

$$\begin{array}{c} \vdots \\ \vdots \end{array} \quad \begin{array}{c} \vdots \\ \vdots \end{array} \quad \begin{array}{c} \vdots \\ \vdots \end{array} \quad \begin{array}{c} \vdots \\ \vdots \end{array}$$

$$\begin{bmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \\ \vdots & \vdots & \vdots \end{bmatrix}_{m \times 3} \begin{bmatrix} a \\ b \\ c \end{bmatrix}_{3 \times 1} = \begin{bmatrix} -(x_1^2 + y_1^2) \\ -(x_2^2 + y_2^2) \\ \vdots \end{bmatrix}_{n \times 1}$$

\uparrow m \nwarrow $n \times 3$ \uparrow n

$$\begin{bmatrix} a \\ b \\ c \end{bmatrix} = \underline{\underline{\text{pinv}(m) * n}}$$

$$x_c = -a/2, \quad y_c = -b/2,$$

$$r = \sqrt{x_c^2 + y_c^2 - c}$$