

EE387 – Signal Processing

Lab01

PART 1: Basic Signal Representation in MATLAB

1.

```
% Function for Ramp signal function
% t = length of time
% m = slope of the ramp function
% ad = advance (positive), delay (negative) factor
```

```
function y = ramp(t,m,ad)
```

```
n = length(t);
y = zeros(1,n);
for i = 1:n,
    if t(i)>= -ad,
        y(i) = m*(t(i) + ad);
    end
end
```

```
end
```

```
%Function for Unit Step functions
% t = length of time
% ad = advance (positive), delay (negative) factor
```

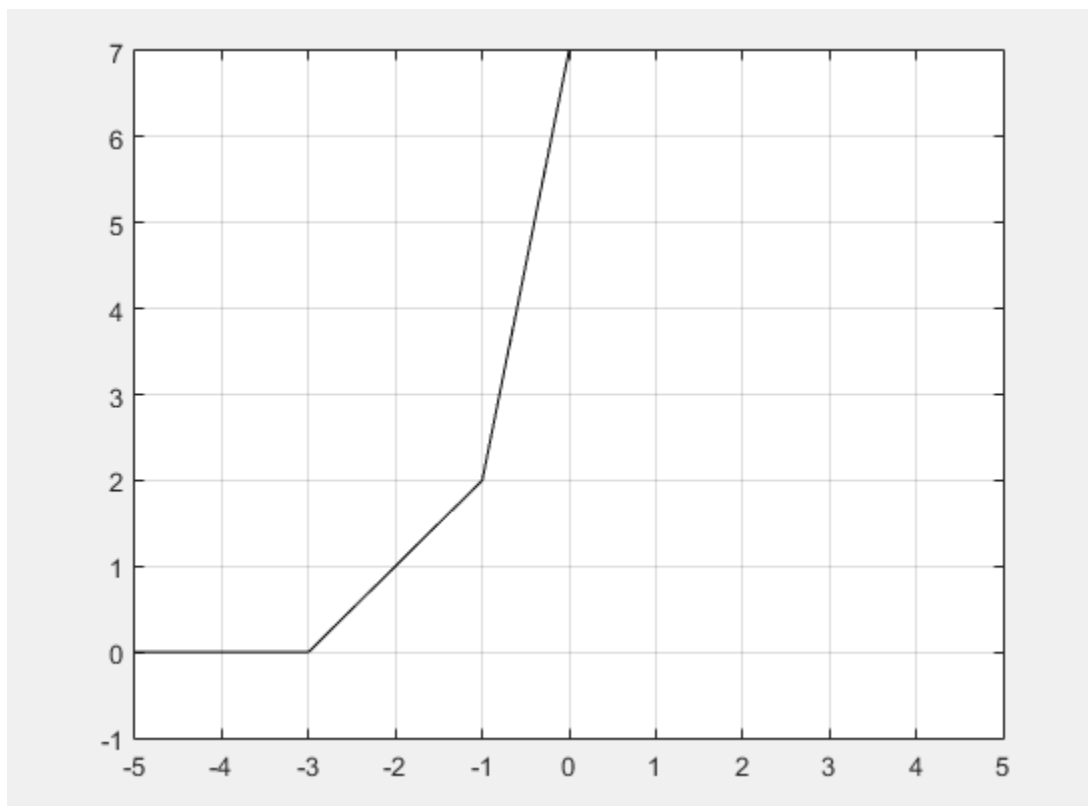
```
function y = ustep(t,ad)
n = length(t);
y = zeros(1,n);
for i = 1:n,
    if t(i)>= -ad
        y(i) = 1;
    end
end
end
```

%Write a Matlab program and necessary functions to generate the following signal:

$y(t) = r(t+3) - 2r(t+1) + 3r(t) - u(t-3)$

%Then plot it and verify analytically that the obtained figure is correct.

```
clear all;  
Ts=0.01; t= -5:Ts:5;  
y1 = ramp(t,1,3);  
y2 = ramp(t,-2,1);  
y3 = ramp(t,3,0);  
y4 = ustep(t,-3);  
y = y1-2*y2+3*y3-y4;  
plot(t,y,'k');  
axis([-5 5 -1 7]); grid
```



2. For the damped sinusoidal signal $x(t) = 3e^{-t}\cos(4\pi t)$ write a MATLAB program to generate $x(t)$ and its envelope, then plot.

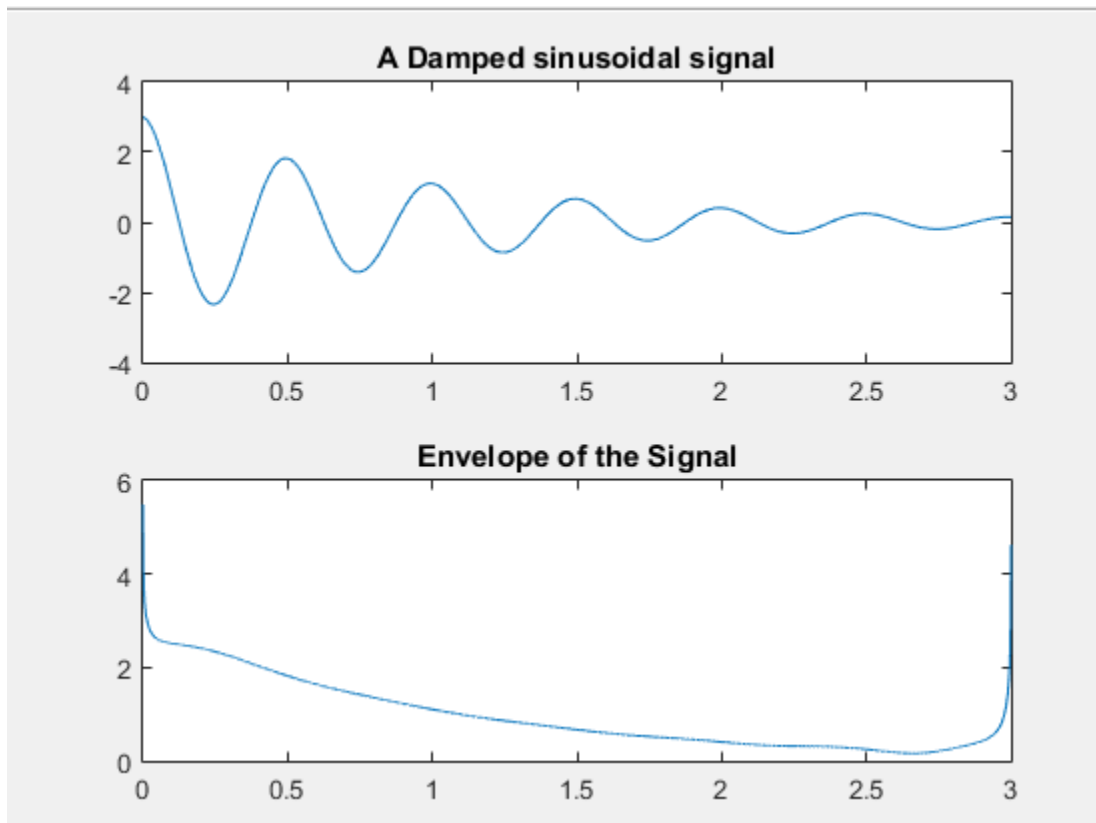
%For the damped sinusoidal signal $x(t) = 3e^{-t}\cos(4\pi t)$ write a MATLAB program to generate $x(t)$ and its envelope, then plot.

%Damped sinusoidal signal

```
t = 0:1/1000:3;  
x_t = 3.*exp(-t).*cos(4*pi*t);  
subplot(2,1,1)  
plot(t,x_t)  
title('Damped sinusoidal signal')
```

%use command hilbert to find the envelope of a signal

```
r = abs(hilbert(x_t));  
subplot(2,1,2)  
plot(t,r)  
title('Envelope of the Signal')
```



PART 2: Time-Domain Convolution

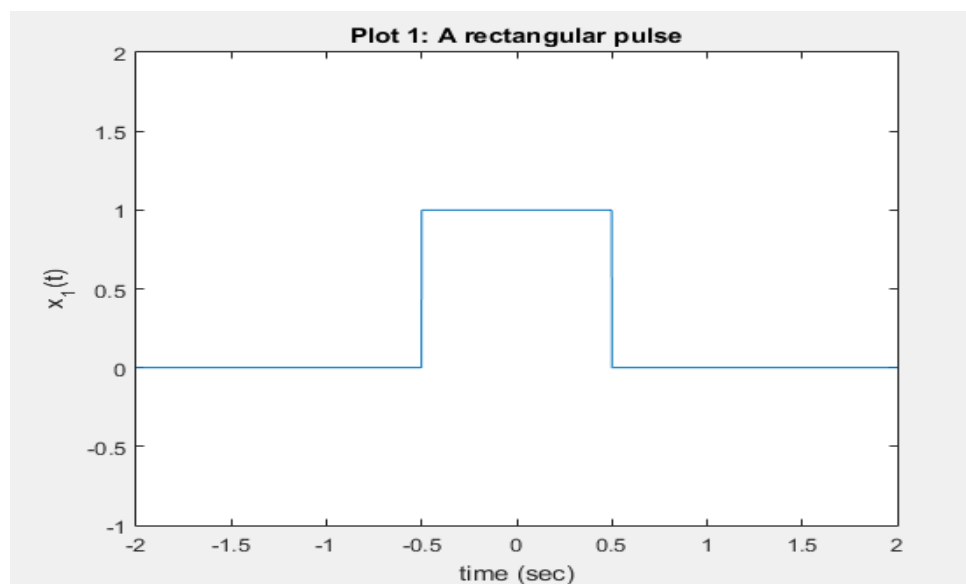
Creating a rectangular pulse in MATLAB

```
% Function for rectangular pulse function
function x = rect(t)

n = length(t);
x = zeros(1, n);
    for i = 1:n
        if t(i) >= -0.5 && t(i) < 0.5
            x(i) = 1;
        end
    end
end

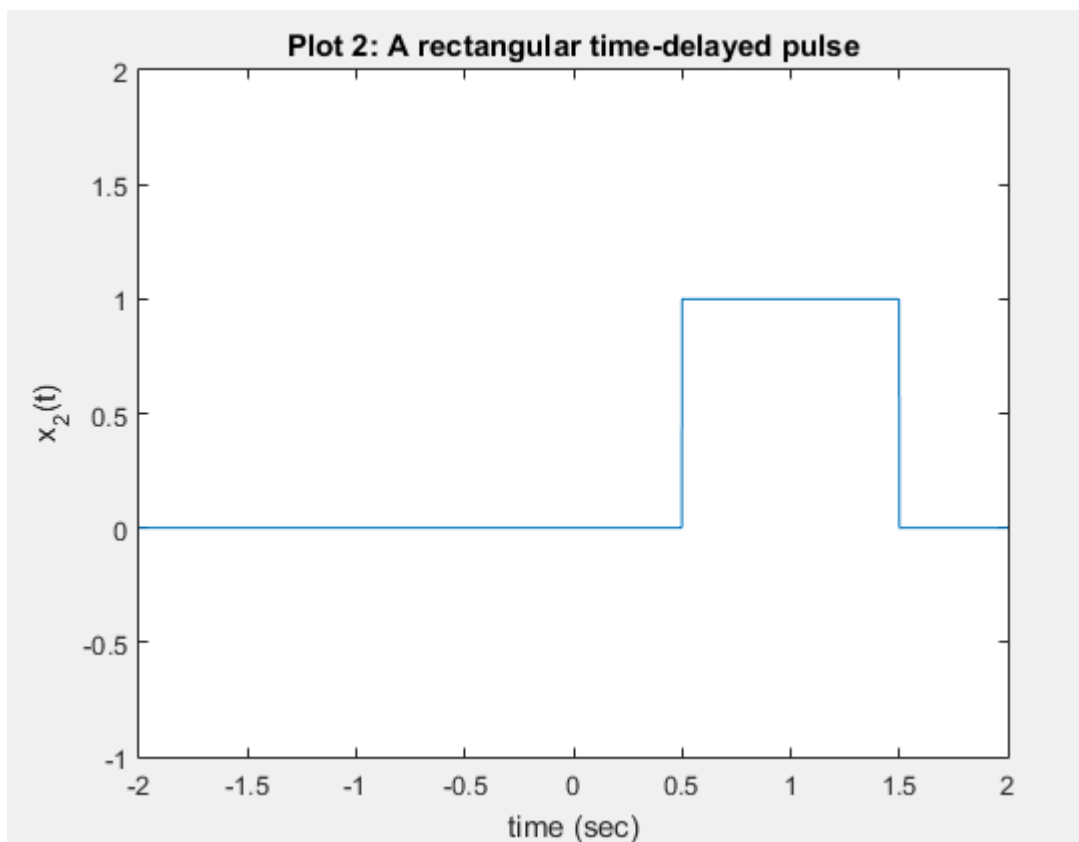
% Main function for plotting time-delayed signal
% This function takes in a vector t of sample instants and
% outputs the
% corresponding rectangular pulse contained in the function x
fs = 1000;
Ts = 1/fs;

t = -5:Ts:5;
x1 = rect(t);
plot(t,x1);
axis([-2 2 -1 2])
xlabel('time (sec)');
ylabel('x_1(t)');
title('Plot 1: A rectangular pulse');
```



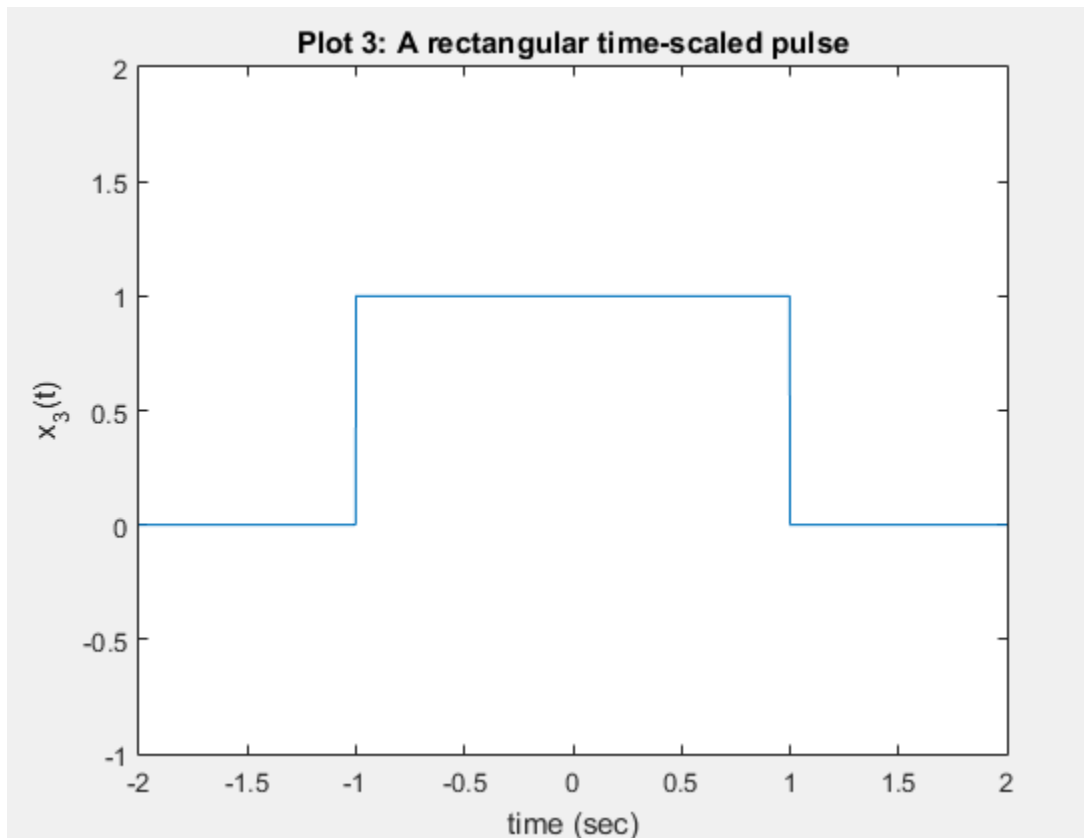
Elementary Signal Operations

```
% First let's create and plot the time-delayed signal,  
%  $x_2(t) = \text{rect}(t-1)$   
  
fs = 1000;  
Ts = 1/fs;  
t = -5:Ts:5;  
x2 = rect(t-1);  
  
plot(t,x2);  
axis([-2 2 -1 2])  
xlabel('time (sec)');  
ylabel('x_2(t)');  
title('Plot 2: A rectangular time-delayed pulse');
```



```
% Now let's try to make the time-scaled signal  $x_3(t) = \text{rect}(t/2)$ 
fs = 1000;
Ts = 1/fs;
t = -5:Ts:5;
x3 = rect(t/2);

plot(t,x3);
axis([-2 2 -1 2])
xlabel('time (sec)');
ylabel('x_3(t)');
title('Plot 3: A rectangular time-scaled pulse');
```



```
%Also create the following signal  $x_4(t) = \text{rect}(t) + (1/2)\text{rect}(t-1)$ 
%and perform a time reversal as:  $x_5(t) = x_4(-t) = \text{rect}(-t) + (1/2)\text{rect}(-t-1)$ .
%Finally you can also create the signal:  $x_6(t) = x_4(1-t) = \text{rect}(1-t) + (1/2)\text{rect}(-t)$ .
% use the MATLAB subplot command to plot all these signals in a single plot
```

```
fs = 1000;
Ts = 1/fs;
t = -5:Ts:5;
```

```
% Rectangular pulse
x1 = rect(t);
subplot(3,2,1)
plot(t,x1);
axis([-2 2 -1 2])
xlabel('time (sec)');
ylabel('x_1(t)');
title('Plot 1: A rectangular pulse');
```

```
% A rectangular time-delayed pulse
x2 = rect(t-1);
subplot(3,2,2)
plot(t,x2);
axis([-2 2 -1 2])
xlabel('time (sec)');
ylabel('x_2(t)');
title('Plot 2: A rectangular time-delayed pulse');
```

```
% A rectangular time-scaled pulse
x3 = rect(t/2);
subplot(3,2,3)
plot(t,x3);
axis([-2 2 -1 2])
xlabel('time (sec)');
ylabel('x_3(t)');
title('Plot 3: A rectangular time-scaled pulse');
```

```
%  $x_4(t)$  addition of  $x_1$  and half of  $x_2$ 
x4 = x1 + 0.5 * x2;
subplot(3,2,4);
plot(t,x4);
axis([-2 2 -1 2])
xlabel('time (sec)');
ylabel('x_4(t)');
title('Plot 4:  $x_4 = x_1 + 0.5x_2$ ');
```

```

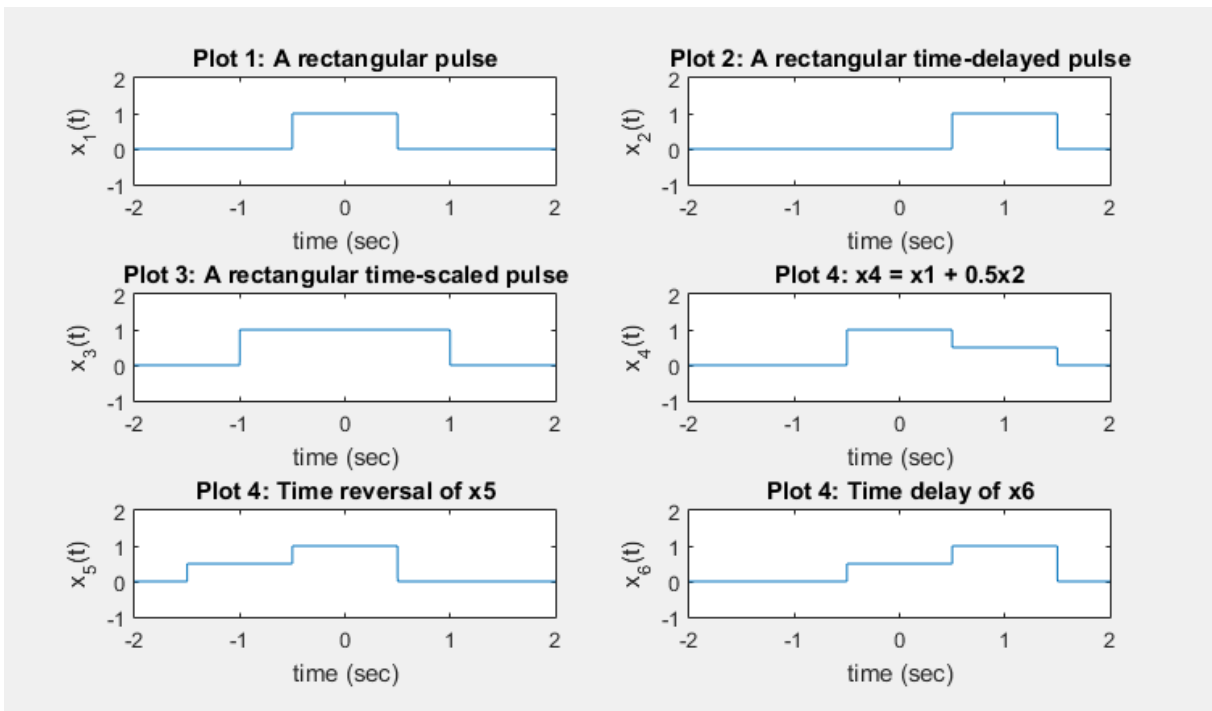
% x5(t) time reversal of x4(t)
x5 = rect(-t) + 0.5 * rect(-t-1);
subplot(3,2,5);
plot(t,x5);
axis([-2 2 -1 2])
xlabel('time (sec)');
ylabel('x_5(t)');
title('Plot 4: Time reversal of x5');

```

```

% x6(t) time delay of x5(t)
x6 = rect(1-t) + 0.5 * rect(-t);
subplot(3,2,6);
plot(t,x6);
axis([-2 2 -1 2])
xlabel('time (sec)');
ylabel('x_6(t)');
title('Plot 4: Time delay of x6');

```



Convolution

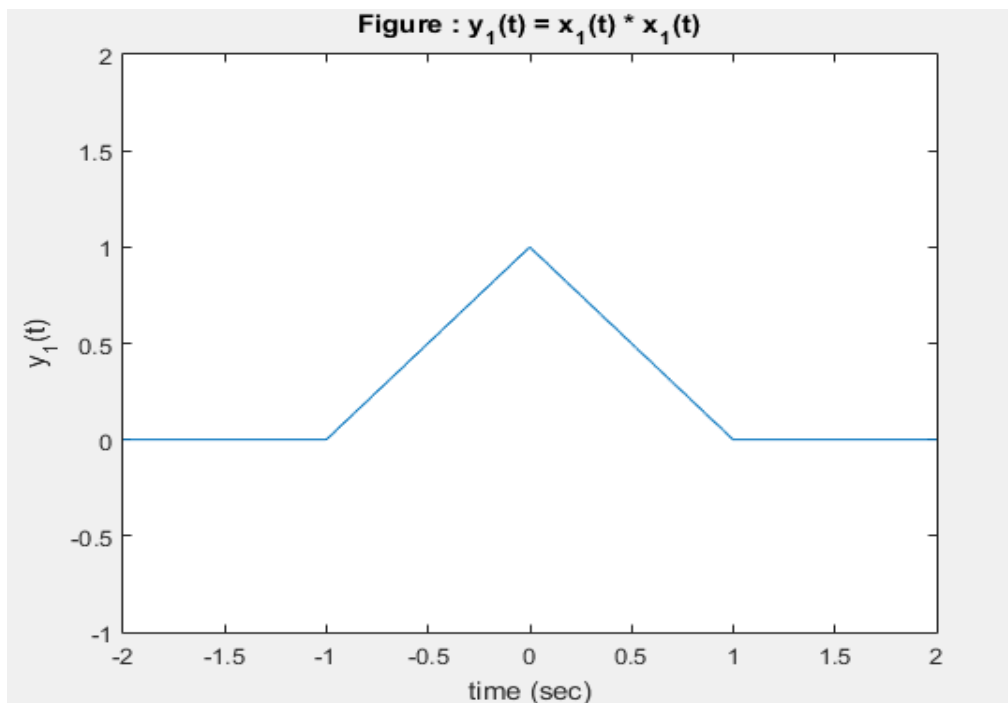
```
%Convolution
fs = 1000;
Ts = 1/fs;
t = -5:Ts:5;
x1 = rect(t);

close all;

y = conv(x1, x1);

length(y)
length(t)
%we need to create a separate time axis for the signal y as
ty = -10:Ts:10;
y1 = Ts * conv(x1, x1);

plot(ty, y1);
axis([-2 2 -1 2]);
xlabel('time (sec)');
ylabel('y_1(t)');
title('Figure : y_1(t) = x_1(t) * x_1(t)');
```



Exercise

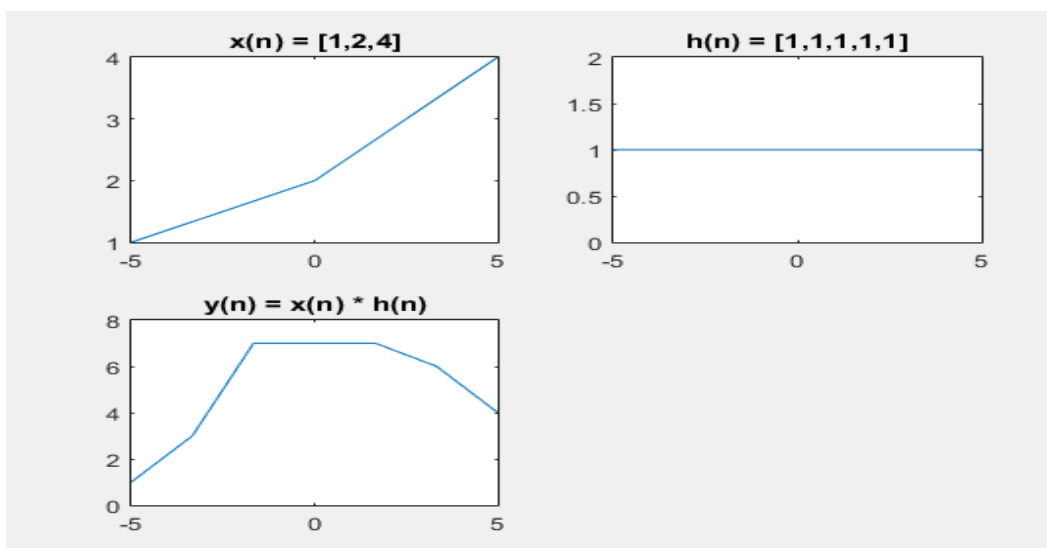
Perform convolution on discrete time signals $x(n)$ and $h(n)$, i.e., $y(n) = x(n) * h(n)$ using MATLAB. For each set of signals, plot $x(n)$, $h(n)$ and $y(n)$ as subplots in the same figure.

- i . $x(n) = \{1, 2, 4\}$, $h(n) = \{1, 1, 1, 1, 1\}$
- ii . $x(n) = \{1, 2, 3, 4, 5\}$, $h(n) = \{1\}$
- iii . $x(n) = h(n) = \{1, 2, 0, 2, 1\}$

```
i)
x1 = [1, 2, 4];
h1 = [1, 1, 1, 1, 1];
y1 = conv(x1, h1);
t1 = linspace(-5,5,3);
t2 = linspace(-5,5,5);
t3 = linspace(-5,5,7);

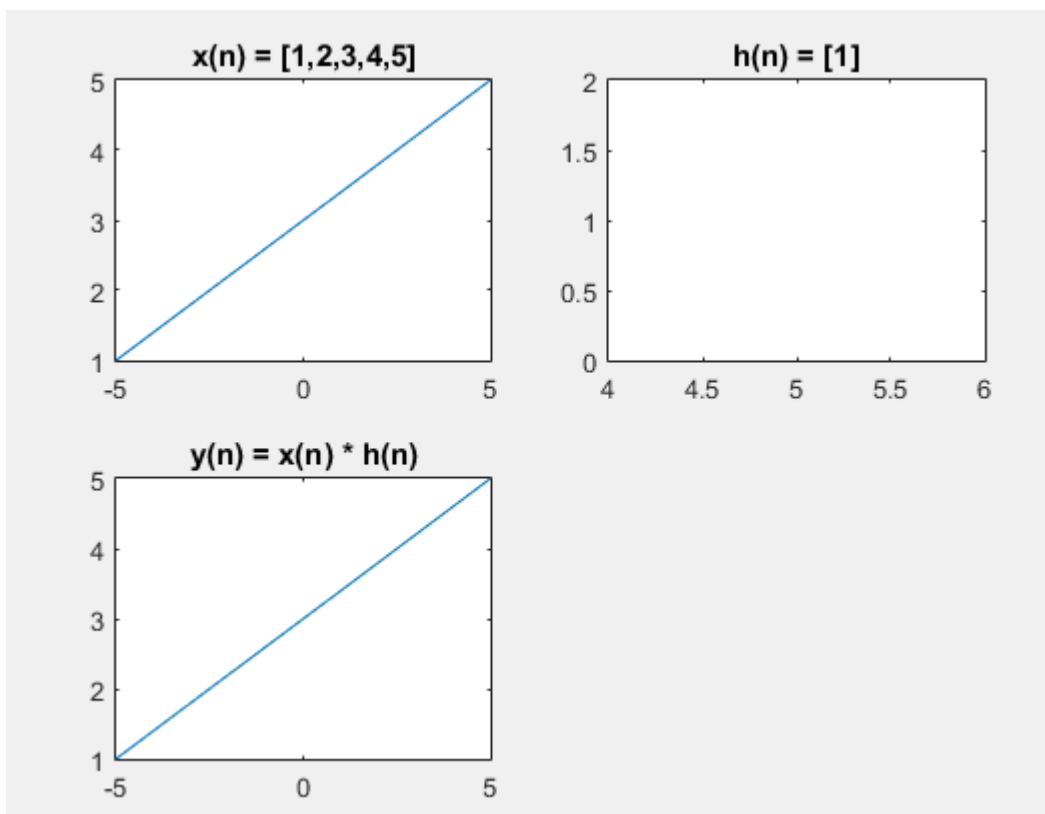
subplot(2,2,1);
plot(t1,x1);
title('x(n) = [1,2,4]');

subplot(2,2,2);
plot(t2,h1);
title('h(n) = [1,1,1,1,1]');
subplot(2,2,3);
plot(t3,y1);
title('y(n) = x(n) * h(n)');
```



ii)

```
x2 = [1, 2, 3, 4, 5];  
h2 = 1;  
y2 = conv(x2, h2);  
t1 = linspace(-5,5,5);  
t2 = linspace(-5,5,1);  
t3 = linspace(-5,5,5);  
  
subplot(2,2,1);  
plot(t1,x2);  
title('x(n) = [1,2,3,4,5]');  
  
subplot(2,2,2);  
plot(t2,h2);  
title('h(n) = [1]');  
  
subplot(2,2,3);  
plot(t3,y2);  
title('y(n) = x(n) * h(n)');
```



```

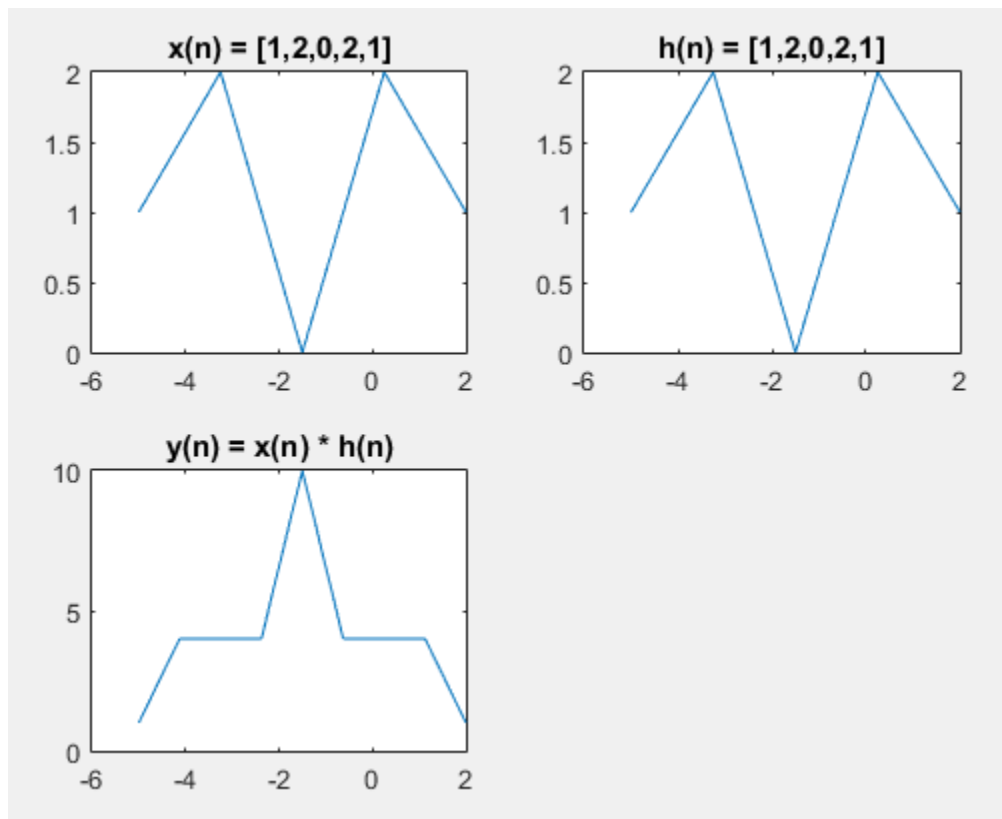
iii)
x3 = [1, 2, 0, 2, 1];
h3 = [1, 2, 0, 2, 1];
y3 = conv(x3, h3);
t1 = linspace(-5,2,5);
t2 = linspace(-5,2,5);
t3 = linspace(-5,2,9);

subplot(2,2,1);
plot(t1,x3);
title('x(n) = [1,2,0,2,1]');

subplot(2,2,2);
plot(t2,h3);
title('h(n) = [1,2,0,2,1]');

subplot(2,2,3);
plot(t3,y3);
title('y(n) = x(n) * h(n)');

```



2. Assume a system with the following impulse response:

$$h(n) = (0.5)^n \quad \text{for } 0 \leq n < 4$$
$$= 0 \quad \text{elsewhere}$$

Determine the input $x(n)$ that will generate the output sequence $y(n) = \{1, 2, 2.5, 3, 3, 3, 2, 1, 0, \dots\}$. Plot $h(n)$, $y(n)$ and $x(n)$ in one figure.

```
t1 = linspace(0,5,5);  
h1 = h(t1);  
y1 = [1, 2, 2.5, 3, 3, 3, 2, 1, 0];  
x1 = deconv(y1, h1);  
  
t2 = linspace(0,5,9);  
t3 = linspace(0,5,5);  
  
subplot(2,2,1);  
plot(t1,h1);  
title('h(n)');  
subplot(2,2,2);  
plot(t2,y1);  
title('y(n)');  
subplot(2,2,3);  
plot(t3,x1);  
title('x(n) is deconvolution of y1,h1');
```

