Tutorial5 new

April 7, 2022

1 Tutorial 5 - Options Intro

Please complete this tutorial to get an overview of options and an implementation of SMDP Q-Learning and Intra-Option Q-Learning.

1.0.1 References:

Recent Advances in Hierarchical Reinforcement Learning is a strong recommendation for topics in HRL that was covered in class. Watch Prof. Ravi's lectures on moodle or nptel for further understanding the core concepts. Contact the TAs for further resources if needed.

```
[10]:

A bunch of imports, you don't have to worry about these

'''

import numpy as np
import random
import gym
from gym.wrappers import Monitor
import glob
import io
import io
import matplotlib.pyplot as plt
from IPython.display import HTML
from tqdm import tqdm
```

```
[11]:
    The environment used here is extremely similar to the openai gym ones.
    At first glance it might look slightly different.
    The usual commands we use for our experiments are added to this cell to aid you work using this environment.
    '''

#Setting up the environment
from gym.envs.toy_text.cliffwalking import CliffWalkingEnv
env = CliffWalkingEnv()
env.reset()
```

```
#Current State
print(env.s)
# 4x12 grid = 48 states
print ("Number of states:", env.nS)
# Primitive Actions
action = ["up", "right", "down", "left"]
#correspond to [0,1,2,3] that's actually passed to the environment
# either go left, up, down or right
print ("Number of actions that an agent can take:", env.nA)
# Example Transitions
rnd_action = random.randint(0, 3)
print ("Action taken:", action[rnd_action])
next_state, reward, is_terminal, t_prob = env.step(rnd_action)
print ("Transition probability:", t_prob)
print ("Next state:", next_state)
print ("Reward recieved:", reward)
print ("Terminal state:", is_terminal)
env.render()
```

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Options We custom define very simple options here. They might not be the logical options for this settings deliberately chosen to visualise the Q Table better.

```
[15]: # We are defining two more options here
# Option 1 ["Away"] - > Away from Cliff (ie keep going up)
# Option 2 ["Close"] - > Close to Cliff (ie keep going down)

def Away(env,state):
```

```
optdone = False
    optact = 0
    if (int(state/12) == 0):
        optdone = True
    return [optact,optdone]
def Close(env,state):
    optdone = False
    optact = 2
    if (int(state/12) == 2):
        optdone = True
    if(int(state/12) == 3):
        optdone = True
    return [optact,optdone]
Now the new action space will contain
Primitive Actions: ["up", "right", "down", "left"]
Options: ["Away", "Close"]
Total Actions : ["up", "right", "down", "left", "Away", "Close"]
Corresponding to [0,1,2,3,4,5]
```

```
[15]: '\nNow the new action space will contain\nPrimitive Actions: ["up", "right", "down", "left"]\nOptions: ["Away", "Close"]\nTotal Actions: ["up", "right", "down", "left", "Away", "Close"]\nCorresponding to [0,1,2,3,4,5]\n'
```

2 Task 1

Complete the code cell below

```
[40]: #Q-Table: (States x Actions) === (env.ns(48) x total actions(6))
q_values_SMDP = np.zeros((48,6))

#Update_Frequency Data structure? Check TODO 4

update_frequency = np.zeros((48, 6))

seed = 42
```

```
rg = np.random.RandomState(seed)

# TODO: epsilon-greedy action selection function
def egreedy_policy(q_values,state,epsilon):
   if not q_values[state].any() or rg.rand() < epsilon:
        return rg.choice(q_values.shape[-1])
   else:
        return np.argmax(q_values[state])</pre>
```

3 Task 2

Below is an incomplete code cell with the flow of SMDP Q-Learning. Complete the cell and train the agent using SMDP Q-Learning algorithm. Keep the **final Q-table** and **Update Frequency** table handy (You'll need it in TODO 4)

```
[41]: | #### SMDP Q-Learning
      # Add parameters you might need here
      gamma = 0.9
      alpha = 0.4
      q_values = np.zeros((48,6))
      update_freq_smdp = np.zeros((48, 6))
      # Iterate over 1000 episodes
      for _ in tqdm(range(1000)):
          state = env.reset()
          done = False
          # While episode is not over
          while not done:
              # Choose action
              action = egreedy_policy(q_values, state, epsilon=0.1)
              # Checking if primitive action
              if action < 4:</pre>
                  # Perform regular Q-Learning update for state-action pair
                  state_next, reward, done , _= env.step(action)
                  action_next = np.argmax(q_values[state_next])
                  q_values[state, action] += alpha*(reward +
       -gamma*q_values[state_next, action_next] - q_values[state, action])
                  update_freq_smdp[state, action] += 1
              # Checking if action chosen is an option
```

```
reward_bar = 0
       if action == 4: # action => Away option
           state_t = state # state at which option was selected
                          # Time taken for option to terminate
           tau = 0
           optdone = False
           while (optdone == False):
               # Think about what this function might do?
               optact,optdone = Away(env,state)
               next_state, reward, done,_ = env.step(optact)
               tau = tau + 1 # Increase the time
               # Is this formulation right? What is this term?
               # reward_bar = gamma*reward_bar + reward # this is wrong
               reward_bar += (gamma**tau) * reward
               # Complete SMDP Q-Learning Update
               # Remember SMDP Updates. When & What do you update?
               state = next_state
           action_next = np.argmax(q_values[state])
           q_values[state_t, action] += alpha*(reward_bar +_
→(gamma**tau)*q_values[state, action_next] - q_values[state_t, action])
           update_freq_smdp[state_t, action] += 1
       if action == 5: # action => Close option
           state_t = state # state at which option was selected
           tau = 0
                          # Time taken for option to terminate
           optdone = False
           while (optdone == False):
               # Think about what this function might do?
               optact,optdone = Away(env,state)
               next_state, reward, done,_ = env.step(optact)
               tau = tau + 1 # Increase the time
               # Is this formulation right? What is this term?
               #reward_bar = gamma*reward_bar + reward
               reward_bar += (gamma**tau) * reward
```

```
# Complete SMDP Q-Learning Update

# Remember SMDP Updates. When & What do you update?

state = next_state

action_next = np.argmax(q_values[state])
q_values[state_t, action] += alpha*(reward_bar +__
(gamma**tau)*q_values[state, action_next] - q_values[state_t, action])
update_freq_smdp[state_t, action] += 1

q_values_smdp = q_values
```

100% | 1000/1000 [00:22<00:00, 43.57it/s]

4 Task 3

Using the same options and the SMDP code, implement Intra Option Q-Learning (In the code cell below). You *might not* always have to search through options to find the options with similar policies, think about it. Keep the **final Q-table** and **Update Frequency** table handy (You'll need it in TODO 4)

```
[42]: #### Intra-Option Q-Learning
      #### SMDP Q-Learning
      # Add parameters you might need here
      gamma = 0.9
      alpha = 0.4
      q_values = np.zeros((48,6))
      update_freq_intra = np.zeros((48, 6))
      # Iterate over 1000 episodes
      for _ in tqdm(range(1000)):
          state = env.reset()
          done = False
          # While episode is not over
          while not done:
              # Choose action
              action = egreedy_policy(q_values, state, epsilon=0.1)
              # Checking if primitive action
              if action < 4:
                  # Perform regular Q-Learning update for state-action pair
                  state_next, reward, done , _= env.step(action)
                  action_next = np.argmax(q_values[state_next])
```

```
q_values[state, action] += alpha*(reward +__
→gamma*q_values[state_next, action_next] - q_values[state, action])
           update_freq_intra[state, action ] += 1
       # Checking if action chosen is an option
       if action == 4: # action => Away option
           optdone = False
           while (optdone == False):
               optact,optdone = Away(env,state)
               next_state, reward, done, _ = env.step(optact)
               if ( not optdone ): # if not terminating
                 q_values[state, action] += alpha*(reward +__
→gamma*q_values[next_state, action] - q_values[state, action])
                 update_freq_intra[state, action] += 1
               else: # if terminating
                 max_action = np.argmax(q_values[state_next])
                 q_values[state, action] += alpha*(reward +__
→gamma*q_values[next_state, max_action] - q_values[state, action])
                 update freq intra[state, action] += 1
               state = next_state
       if action == 5: # action => Close option
           optdone = False
           while (optdone == False):
               # Think about what this function might do?
               optact,optdone = Away(env,state)
               next_state, reward, done,_ = env.step(optact)
               if ( not optdone ):
                 q_values[state, action] += alpha*(reward +_
→gamma*q_values[next_state, action] - q_values[state, action])
                 update_freq_intra[state, action] += 1
               else:
                 max_action = np.argmax(q_values[state_next])
                 q_values[state, action] += alpha*(reward +__
→gamma*q_values[next_state, max_action] - q_values[state, action])
                 update_freq_intra[state, action] += 1
               state = next_state
```

```
q_values_intra = q_values
                | 1000/1000 [00:35<00:00, 28.12it/s]
     100%|
         Task 4
     5
     Compare the two Q-Tables and Update Frequencies and provide comments.
[43]: # Use this cell for Task 4 Code
      import pprint
      import pandas as pd
      pp = pprint.PrettyPrinter(indent=4)
      pd.DataFrame(q_values_smdp.T)
[43]:
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      0 -3.691877 -8.449851 -5.867800
                                        -7.087039
                                                   -5.874626
                                                              -4.170851
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      1 -3.143860 -2.248663 -3.657367
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      2 -4.052660 -9.600215 -1.825237 -27.952182 -27.786626 -12.893277 -44.218248
      3 -4.104565 -7.519756 -6.817036 -7.134509
                                                   -4.764477
                                                              -7.136071
                                                                          -6.304913
      4 -3.463399 -6.346188 -6.311557
                                       -4.991570
                                                   -7.083544
                                                              -3.876638
                                                                         -3.771415
      5 -3.108303 -4.303297 -7.036353 -5.580064
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      [6 rows x 48 columns]
[44]: pd.DataFrame(q_values_intra.T)
```

3

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-8.376694

6

-8.426642

-8.448870

2

-8.782674 -8.681404 -8.549958 -8.173937

1 -6.446833 -8.939067 -11.616702 -12.155948 -1.045178 -10.296436

[44]:

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[45]: pd.DataFrame(update_freq_smdp.T)
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      [6 rows x 48 columns]
[46]: pd.DataFrame(update_freq_intra.T)
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```

[6 rows x 48 columns]

Use this text cell for your comments - Task 4

It can be clearly seen that Intra Q Learning makes more updtes compared to SMDP to the state action pairs (Infeered from the update frequency table). This leads to effective usage of sample by Intra Q learning.

6 (IGNORE)