

Q. FOL into CNF

$$\forall x [\exists z \text{ Animal}(z) \wedge \text{Kills}(x, z)] \Rightarrow [\forall y \rightarrow \text{Loves}(y, x)]$$

A.]

$$\forall x [\neg \exists z \neg \{(\text{Animal}(z) \wedge \text{Kills}(x, z))\} \vee [\forall y \rightarrow \text{Loves}(y, x)]]$$

$$\forall x [\neg \exists z \neg \text{Animal}(z) \vee \neg \text{Kills}(x, z)] \vee [\forall y \rightarrow \text{Loves}(y, x)]$$

$$\forall x [\forall z \neg \text{Animal}(z) \vee \neg \text{Kills}(x, z)] \vee [\forall y \rightarrow \text{Loves}(y, x)]$$

$$\forall x \forall y \forall z [\neg \text{Animal}(z) \vee \neg \text{Kills}(x, z)] \vee [\neg \text{Loves}(y, x)]$$

$$\forall x [\neg \text{Animal}(G(x)) \vee \neg \text{Kills}(x, G(x))] \vee [\neg \text{Loves}(F(x), x)]$$

$$[\neg \text{Animal}(G(x)) \vee \neg \text{Kills}(x, G(x))] \vee [\neg \text{Loves}(F(x), x)]$$

$$[\neg \text{Animal}(G(x)) \vee \neg \text{Loves}(F(x), x)] \vee [\neg \text{Kills}(x, G(x)) \vee \neg \text{Loves}(F(x), x)]$$

2.] Convert the sentences into FOL & prove using resolution.

i.] Cold & precipitation \rightarrow snow

$$\text{Cold}(x) \wedge \text{precipitation}(x) \Rightarrow \text{snow}(x)$$

$$\rightarrow (\text{Cold}(x) \wedge \text{precipitation}(x)) \vee \text{snow}(x)$$

$$\rightarrow \neg \text{Cold}(x) \vee \neg \text{precipitation}(x) \vee \text{snow}(x)$$

ii.] January \rightarrow cold

$$\text{January}(x) \Rightarrow \text{cold}$$

$$\rightarrow \text{January}(x) \vee \text{cold}(x)$$

iii.] Clouds \rightarrow precipitation

$$\text{clouds}(x) \Rightarrow \text{precipitation}(x)$$

$$\rightarrow \text{clouds}(x) \vee \neg \text{precipitation}(x)$$

iv.] January(x)

v.] Clouds(x)

To prove :- snow(x)

\rightarrow Resolution of (i) & (ii)

$$\text{vi.}] \rightarrow \text{precipitation}(x) \vee \text{snow}(x) \vee \neg \text{January}(x)$$

\rightarrow Resolution of (vi) & (iv)

$$\text{vii.}] \rightarrow \text{precipitation}(x) \vee \text{snow}(x)$$

\rightarrow Resolution of (vii) & (iii)

$$\text{viii.}] \rightarrow \text{snow}(x) \vee \neg \text{clouds}(x)$$

\rightarrow Resolution of (viii) & (v)

snow(x) , & Hence proved.