

Combinational ATPG

- **Deterministic Test Pattern Generation**

- ◆ Boolean difference approach*
- ◆ Path sensitization method**
- ◆ D-Algorithm [Roth 1966] **
- ◆ PODEM [Goel 1981]**

- * Idea

- * Heuristics

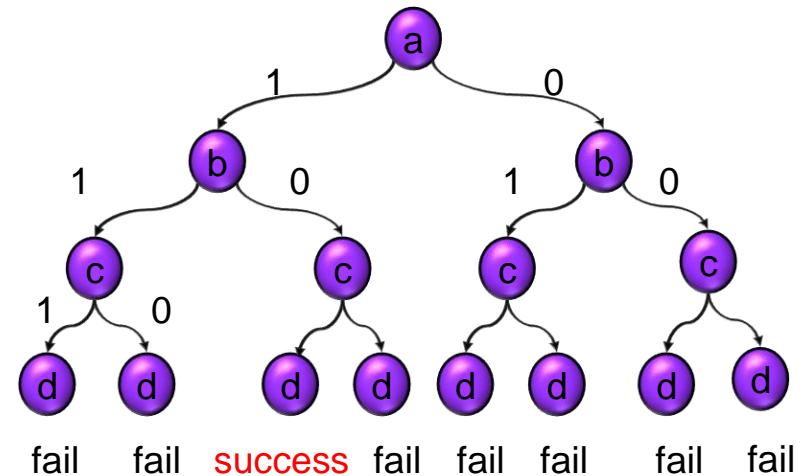
- * Algorithms

- * Summary

- ◆ FAN [Fujiwara 1983]**
- ◆ SAT-based [Larrabee 1992]*

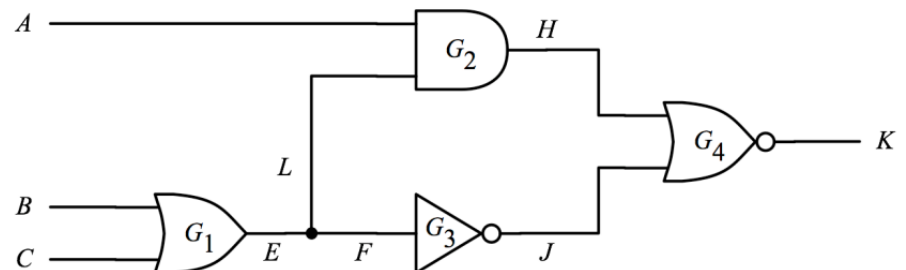
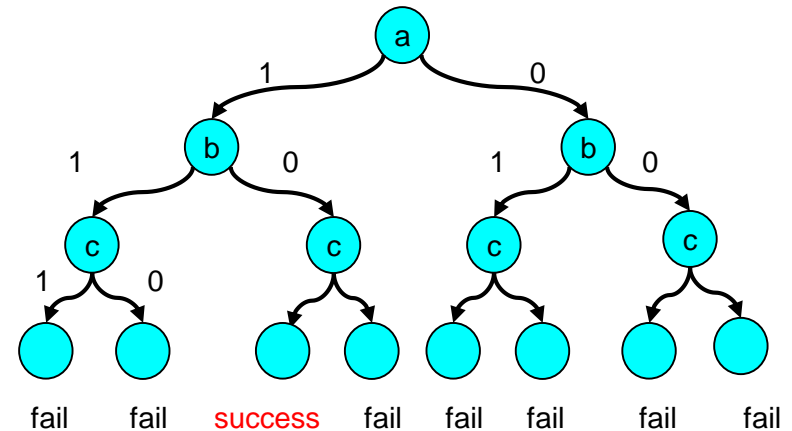
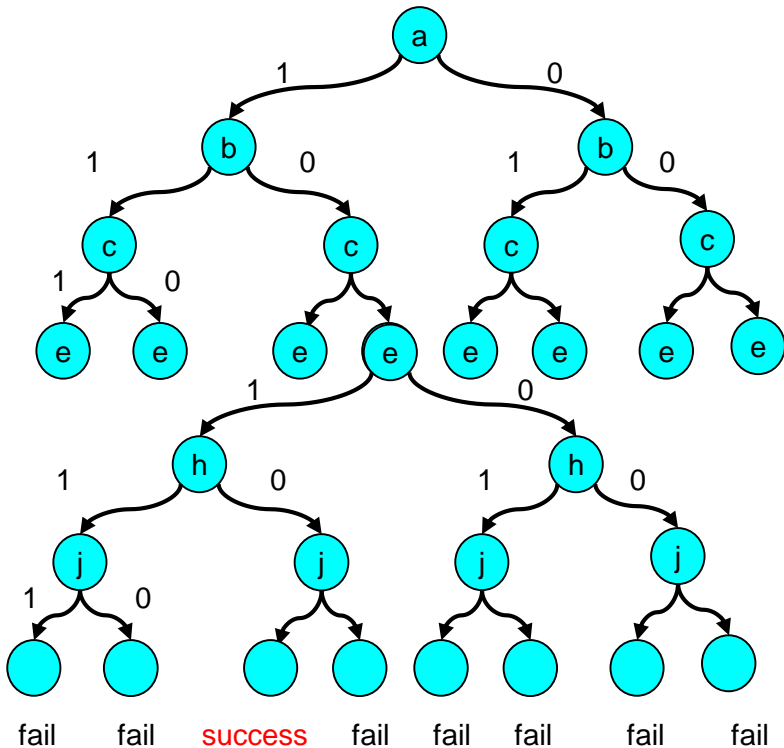
*Boolean-based methods

**path-based methods



$$2^6 \rightarrow 2^3$$

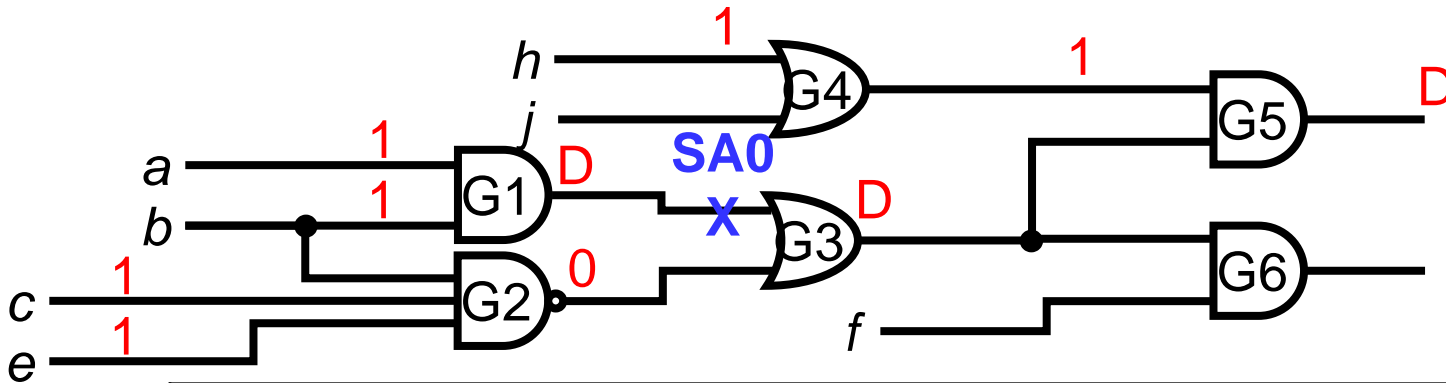
- D-alg. makes decision at **intern nodes**
 - ♦ 6 internal nodes
 - ♦ $2^6=64$ decisions! large
- PODEM makes decision at **PI**
 - ♦ 3 PI
 - ♦ $2^3=8$ decisions, smaller



PODEM [Goel 1981]

- *Path Oriented Decision Making (PODEM)*
- IDEAS:
 1. Only allow assignments to *PI only*
 - ♦ Doesn't assign internal nodes
 - ♦ Greatly reduces search tree
 2. Assigned PI are then *forward implication*
 - ♦ No justification needed (Why ? FFT)
 3. Flip last PI assignment when two conditions:
 - ♦ A. *Fault not activated*
 - ♦ B. *No propagation path* to any output

PODEM Example



Initial objective: $G_1 = 1$

Backtrace to PI: $b = 1$. simulation, objective not achieved

Backtrace to PI: $a = 1$. simulation, objective achieved

Objective: $G_2 = 0$ (propagate through G_3)

Backtrace to PI: $C = 1$. simulation, objective not achieved

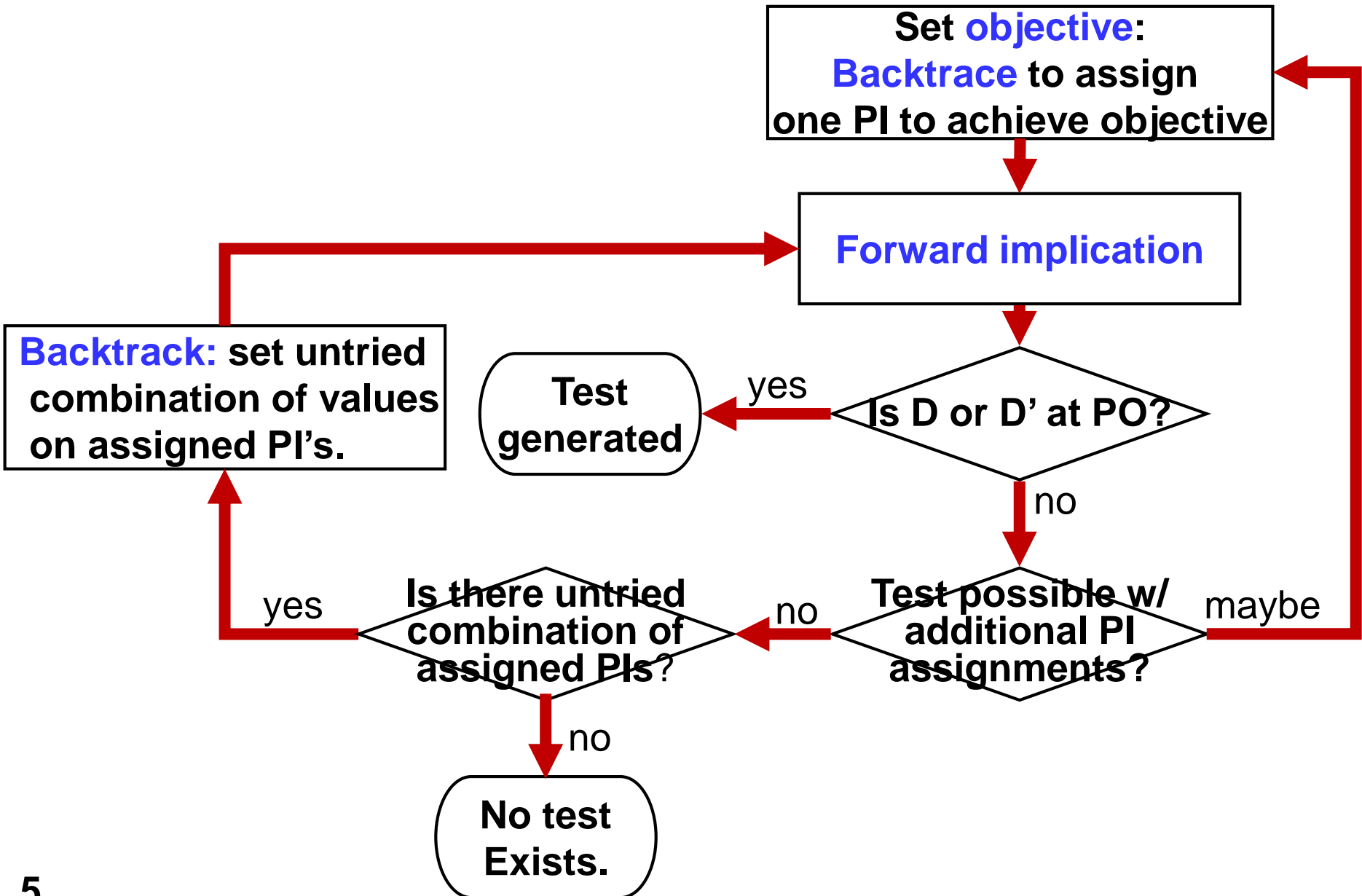
Backtrace to PI: $e = 1$. simulation, objective achieved

Objective: $G_4 = 1$ (we choose to propagate through G_5)

Backtrace to PI: $h = 1$. objective achieved.

Test Generated: $abcehjf = 11111XX$

Flowchart of PODEM

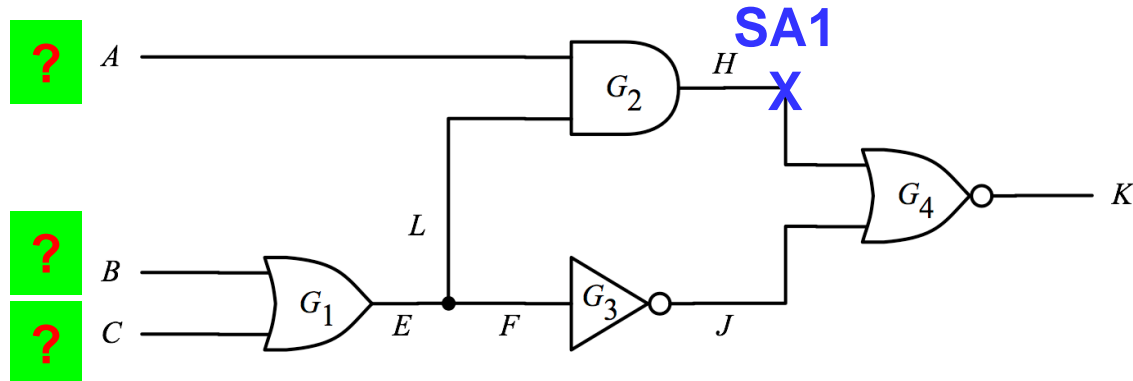


Components of PODEM

- Determine an *objective*
 - ◆ If D/D' has not appeared at the fault site,
 - * set objective to *activate fault*
 - ◆ If D/D' has appeared
 - * set objective to *propagate fault effect*
- Given objective, determine PI value
 - ◆ *Backtrace to PI*
 - ◆ *Backtrack* if conflict occurs
- NOTE: *Backtrace* is different from *backtrack*
 - ◆ Backtrace goes back to primary inputs of a certain signal
 - * In netlist
 - ◆ Backtrack goes back to last decision
 - * in decision tree

Quiz

**Q: Use PODEM to generate a test for H SA 1 fault
please mark your**
1. objective,
2. backtrace

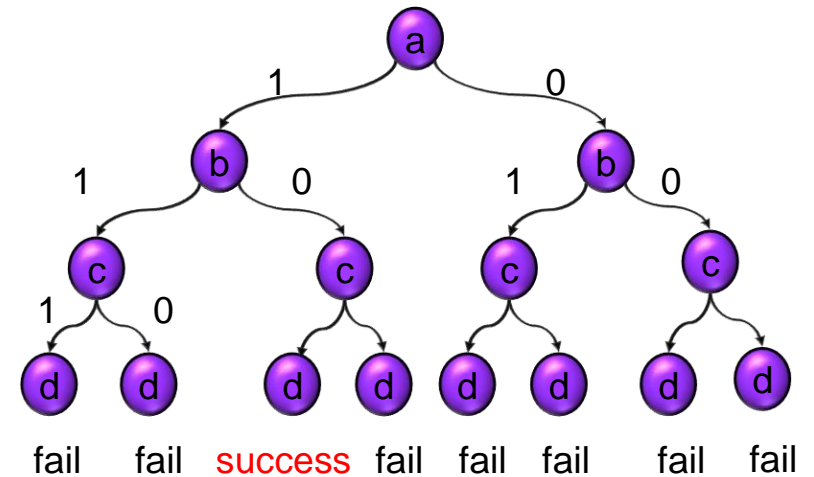


Totally 2 objectives, 2 backtraces

PODEM

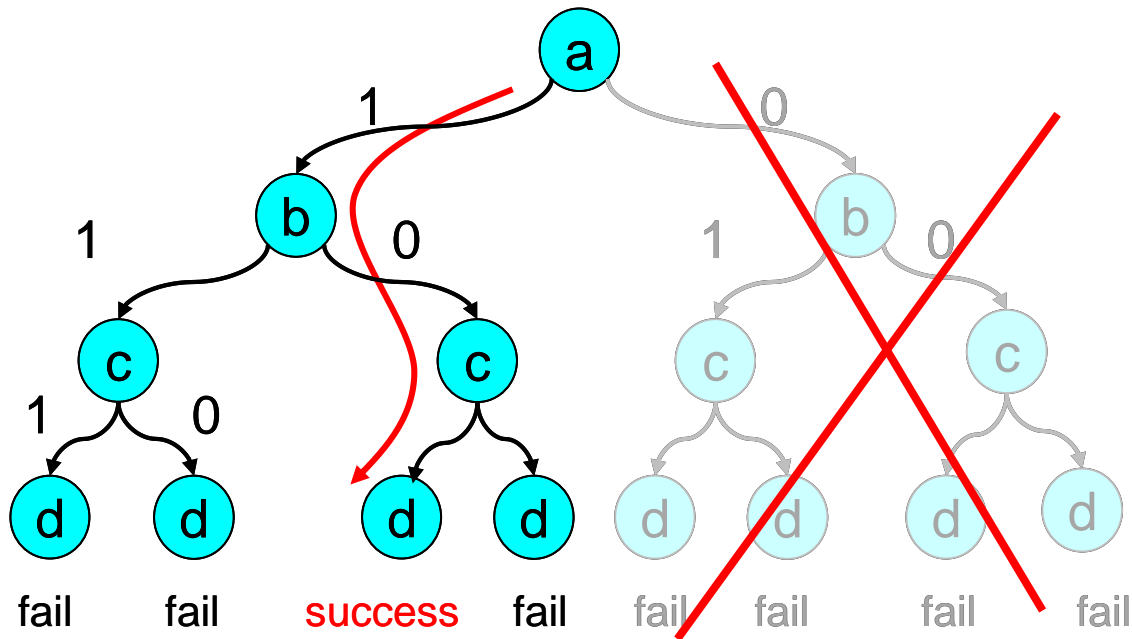
- PODEM [Goel 1981]

- ◆ Idea
- ◆ Heuristics
- ◆ Algorithms
- ◆ Summary



ATPG Decision Tree

- Need smart heuristics to speed up
 - ♦ 1. Prune **impossible sub-trees** ASAP
 - ♦ 2. Find **good assignments** ASAP
- Heuristics are experience-based rules that help correct decision
 - ♦ Note: Heuristics **Do NOT** guaranteed to be correct all the time



Questions to Be Answered

- PODEM proposed **three heuristics** to answer three questions:
 - ◆ Q1: What path to *backtrace*?
 - ◆ Q2: **What input value** to assign?
 - ◆ Q3: What path to **propagate D (D')** to PO?

**Good Heuristic = Simple
and Effective** (most of the time)

Q1: What Path to Backtrace?

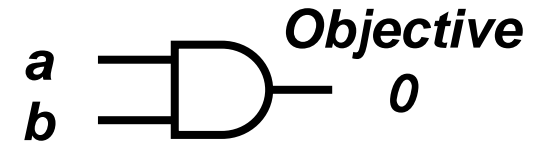
- **Decision Gate:**

- ♦ Only one input can control gate output to objective value

- * OR/NAND with output objective =1

- * AND/NOR with output objective =0

- ♦ choose easiest gate input



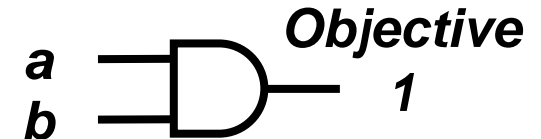
- **Implied Gate:**

- ♦ One input can't control gate output to objective value

- * OR/NAND with output objective =0

- * AND/NOR with output objective =1

- ♦ Choose hardest gate input

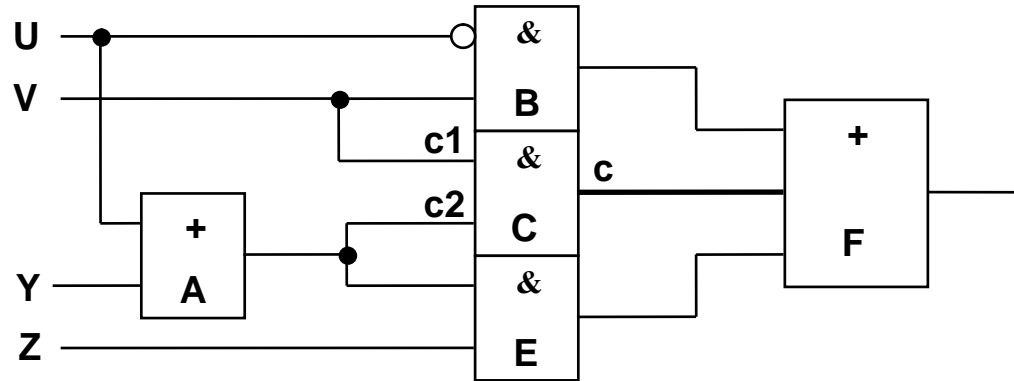


- Why? find out if test exists or not as soon as possible

Heuristic#1: Make Correct Backtrace ASAP

Example

- If objective is $c=0$; backtrace **c1**, then $V=0$ (decision gate)
- If objective is $c=1$; backtrace **c2**, then $U=1$ or $Y=1$ (imply gate)



- **Q: how do you know c1 is easy and c2 is hard?**
 - ◆ **Level of c1 smaller than level of c2**
 - ◆ **(Use other controllability measure, like SCOAP, also fine)**

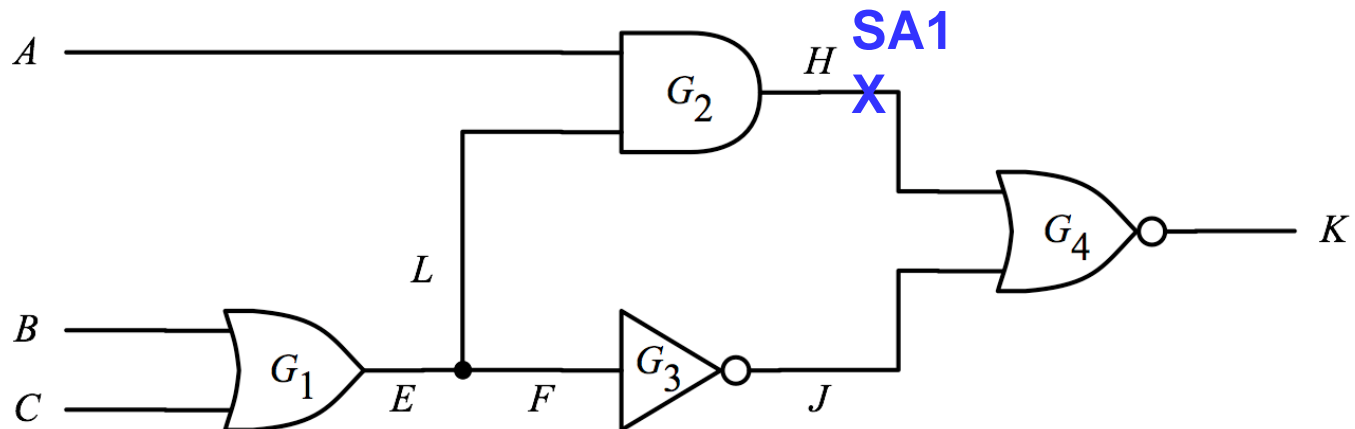
Quiz

Q: Given SCOAP, generate a test for H SA1 fault.

A1: Follow heuristic

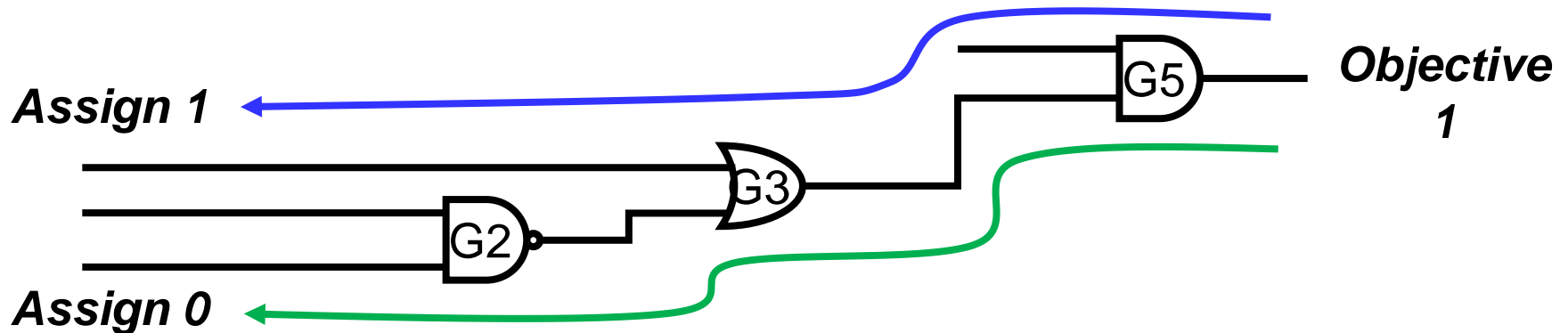
A2: Do not follow heuristic

	A	B	C	E	F	L	H	J	K
CC ⁰	1	1	1	3	3	3	2	3	5
CC ¹	1	1	1	2	2	2	4	4	6
CO	7	6	6	4	4	6	4	3	0



Q2: What Input Values to Assign?

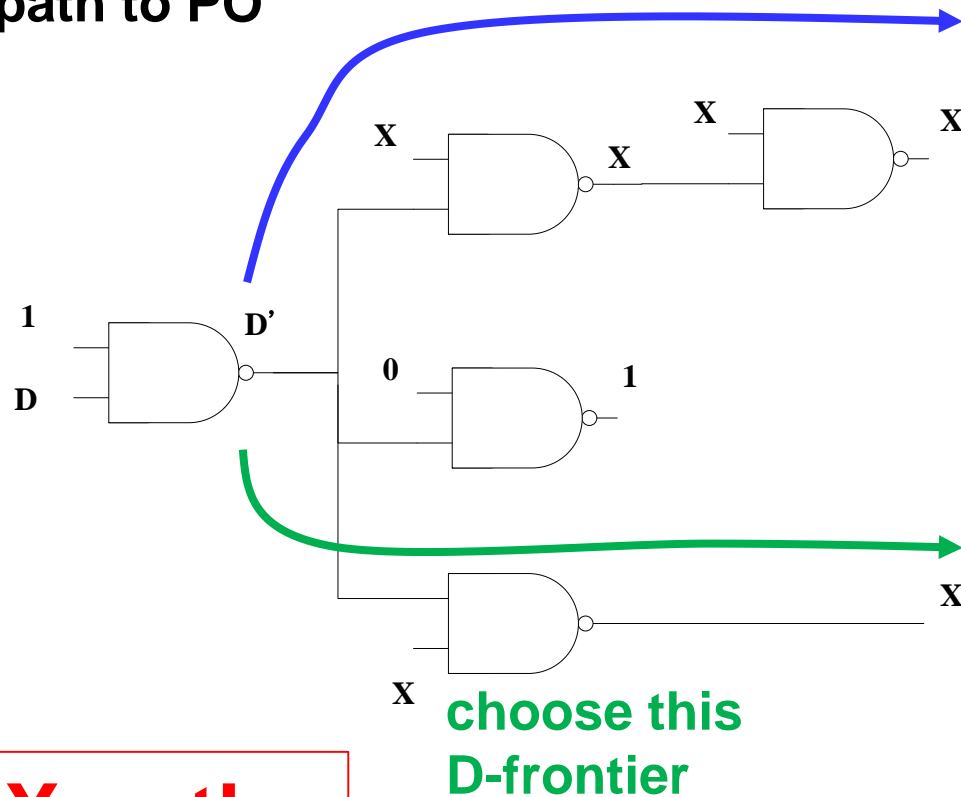
- If **even inversion parity** path
 - ♦ Assign same value as objective
- If **odd inversion parity** path
 - ♦ Assign opposite value to objective
- Why? This assignment is most likely to be correct



Heuristic#2: Inversion Parity for Assignment

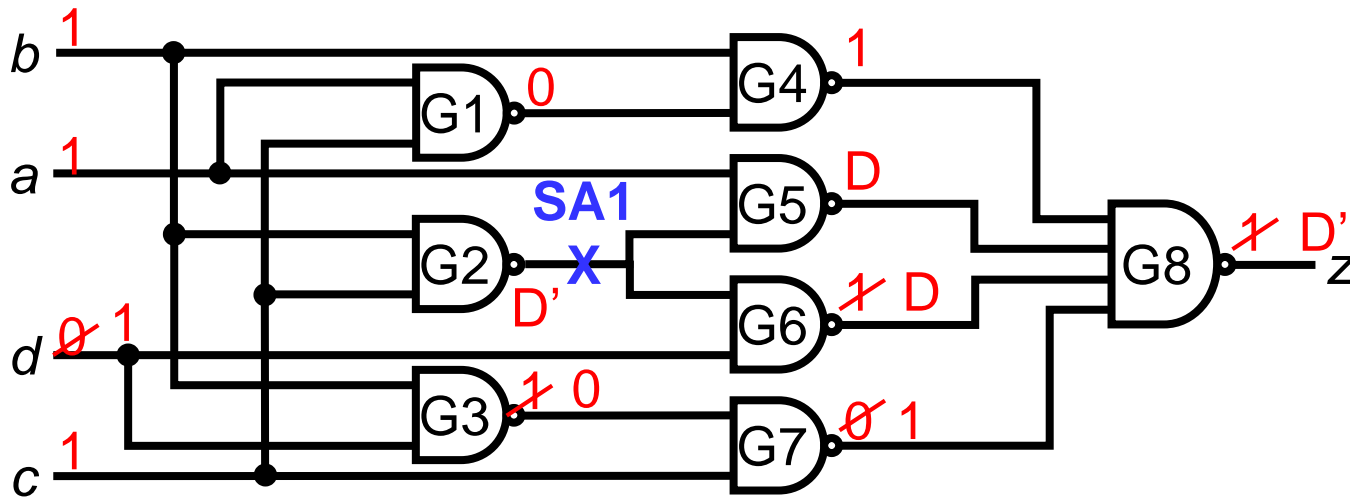
Q3: What Path to Propagate ?

- All gate output of the chosen path must have X values
 - ♦ Called **X-PATH**
- If more than one X-path to choose,
 - ♦ chose shortest X-path to PO
- If X-path disappear,
 - ♦ **backtrack**



Heuristic#3: X-path

PODEM Example w/ Backtrack



Initial objective: (G2, 0)

Backtrace to PI: $b = 1$

Initial objective: (G2, 0)

Backtrace to PI: $c = 1$

Implication: $G2 = D'$

Choose shortest X-path {G5}

Objective $a = 1$

Assign $a=1$

Implication: $G1 = 0, G4 = 1, G5 = D$

Try propagate through G8.

objective: (G6,1)

Backtrace to PI: $d = 0$

Implication: $G3 = 1, G7 = 0, G8 = 1$

X-path disappear!

Backtrack to most recent PI assignment:

$d = 0 \rightarrow d = 1$

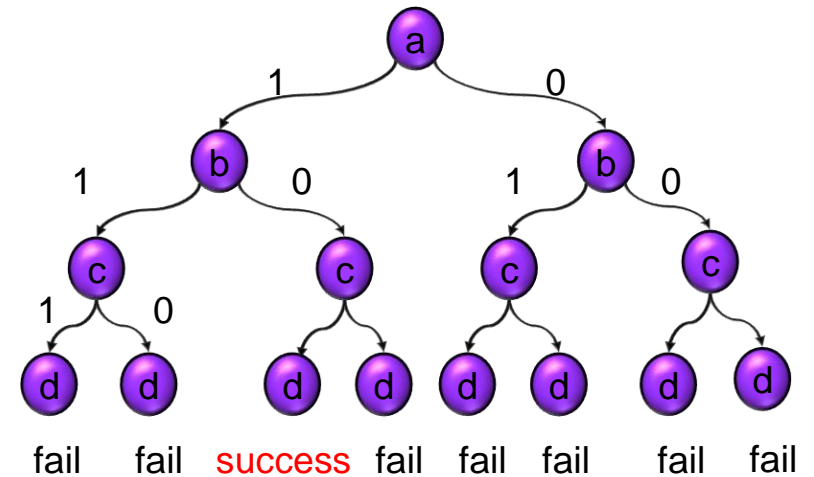
Implication: $G3 = 0, G6 = D, G8 = D'$

Test generated!

PODEM

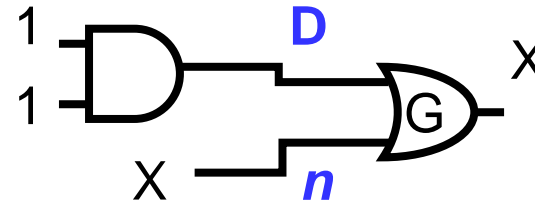
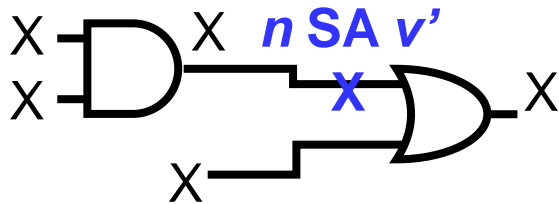
- PODEM [Goel 1981]

- ◆ Idea
- ◆ Heuristics
- ◆ Algorithms
- ◆ Summary



Objective

- Pick an objective: (1) fault activation (2) propagate fault effect



Objective (n, v) // target fault: **net n stuck-at v'**
// if fault has not been activated

1. if (net n is **unknown**)
2. return (n, v);

// else, propagate fault effect

3. select a gate **G** from D-frontier **on shortest X-path**
4. select an unassigned input n of G
5. if (gate G has non-controlling value)
6. $v =$ **non-controlling value of G** ; // AND $v=1$; OR, $v=0$
7. return (n, v); // n is objective net; v is objective value

Backtrace

- Translates objective to PI assignment
- **Depth-first search**: recursively calls itself until hits PI

```
Backtrace (n, vs) /* n is objective net; vs is objective y; */  
1. v = vs;  
2. while (n is gate output)  
3.   if (n is NAND or INVERTER or NOR) v = v'; // inversion parity  
4.   if (objective requires setting all inputs) // imply gate  
5.     a = hardest gate input;  
6.   else // decision gate  
7.     a = easiest gate input ;  
8.   n = a;  
9.   (n, v) = Backtrace (n, v); // recursive call  
   // out of while loop, n is now PI  
10. return (n, v) // assign PI n to value v
```

PODEM

- **Branch and bound** search algorithm

PODEM (*fault* , v_{fault})

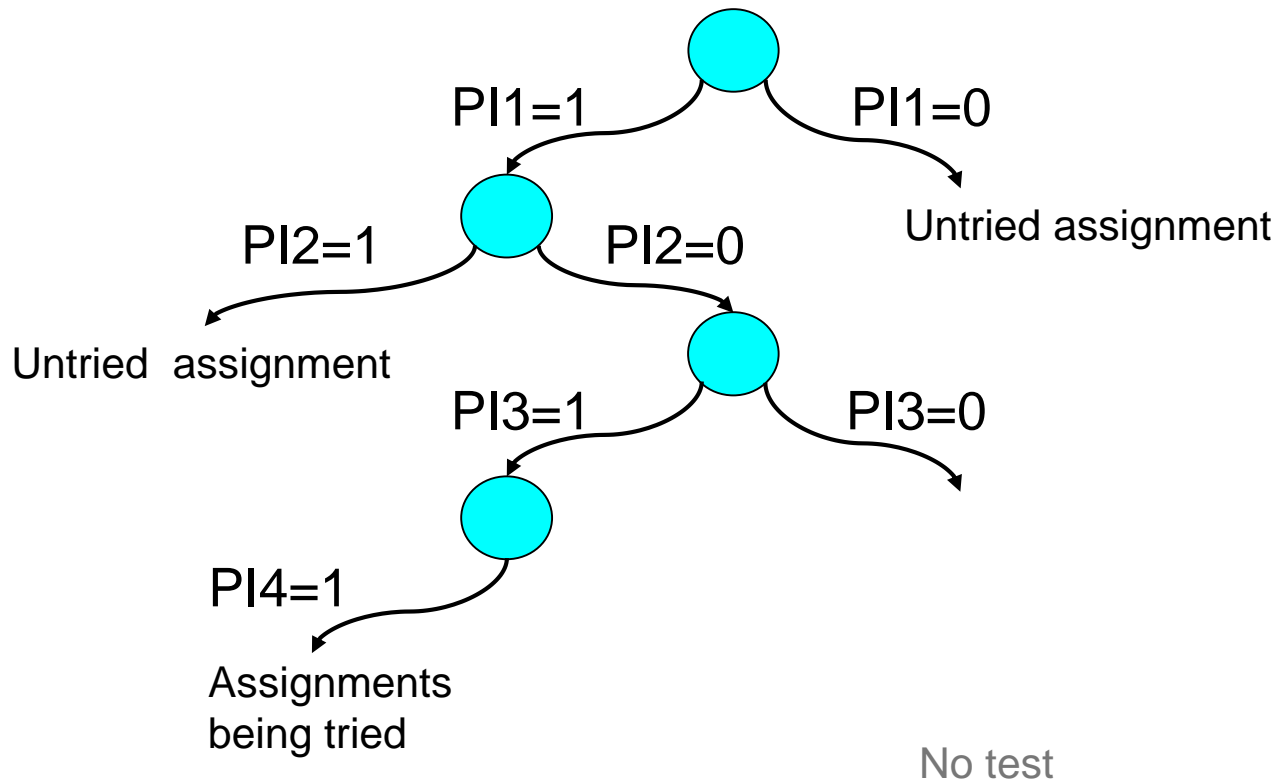
1. if (D or D' at PO) return (SUCCESS)
2. if (test impossible) return (FAILURE)
3. (n , v_s) = *Objective* (*fault*, v_{fault});
4. (pi , v) = *Backtrace* (n , v_s);
5. *Imply* (pi , v); // assign pi, forward implication
6. if (*PODEM* (*fault*, v_{fault}) == SUCCESS) return (SUCCESS);
 // backtrack
7. *Imply* (pi , v');
8. if (*PODEM* (*fault*, v_{fault}) == SUCCESS) return (SUCCESS);
9. *Imply* (pi , "X"); // release PI as unknown
10. return (FAILURE); // this node is pruned
14. end;

test impossible for 2 reasons:

- (1) target fault cannot be activated
- (2) X-path disappear

Decision Tree of PODEM (1)

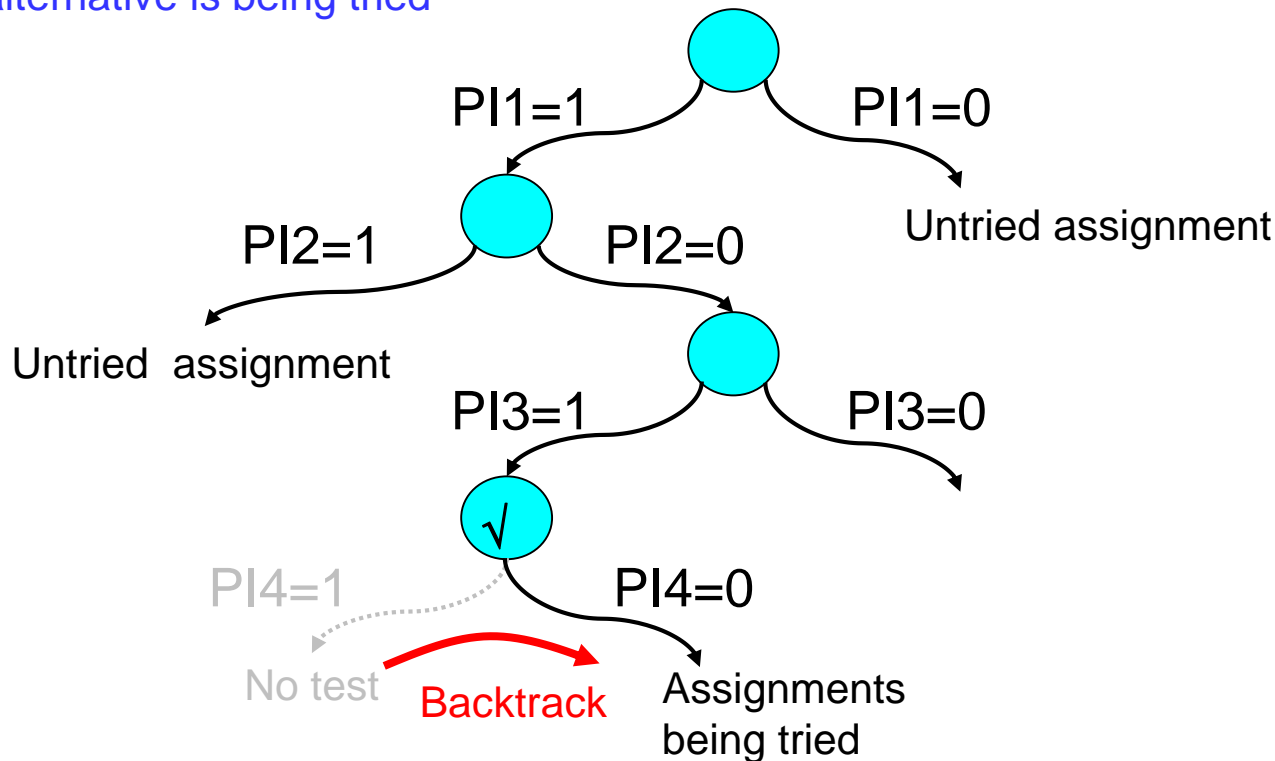
- **Branch and bound** search algorithm
 - ♦ Each decision is a PI



Decision Tree of PODEM (2)

- **Branch and bound** search algorithm
- **Chronological backtrack**: [DPLL satisfiability 1962]
 - ♦ Flip **last PI** that has not been tried

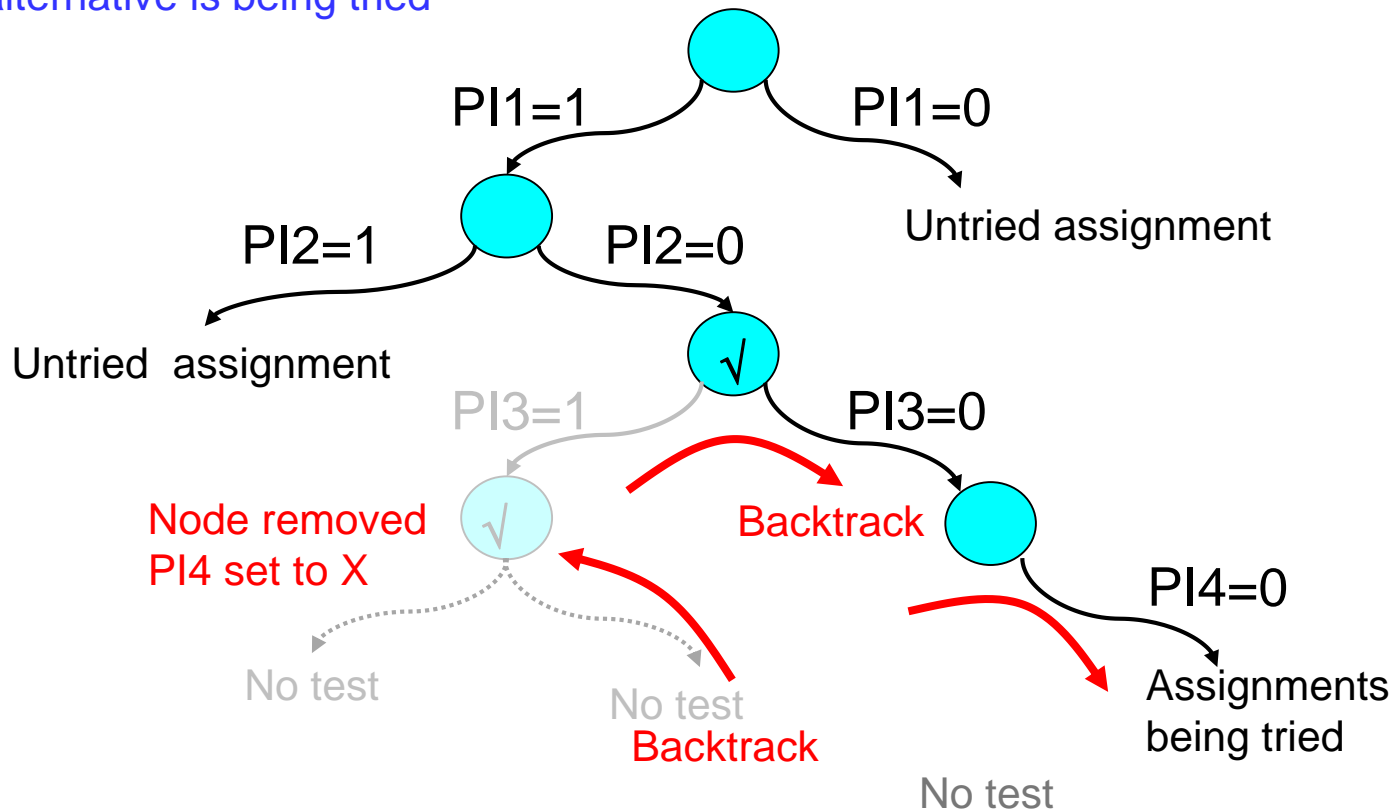
✓ : initial assignment rejected
alternative is being tried



Decision Tree of PODEM (3)

- **Branch and bound** search algorithm
 - ♦ A node is removed when **both** alternatives have been tried
 - ♦ Prune **PI3=1** subtree

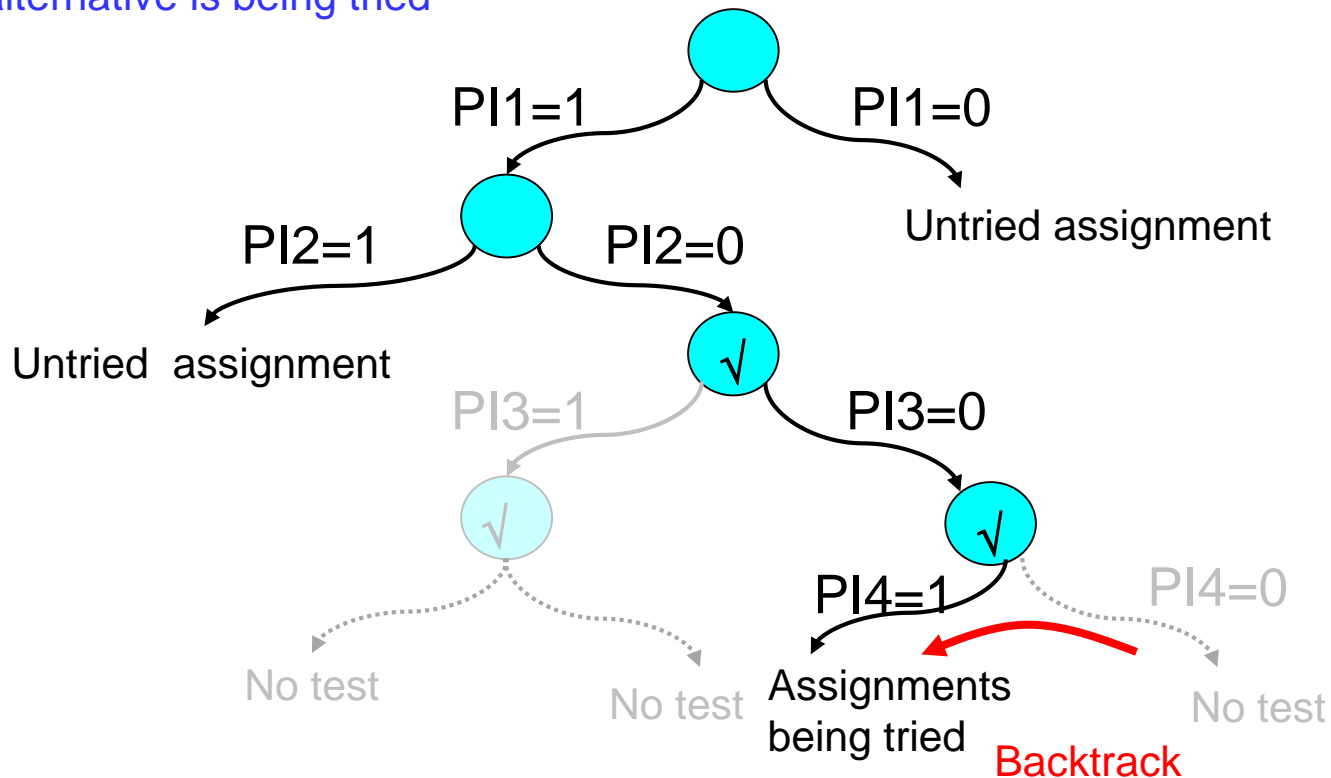
✓ : initial assignment rejected
alternative is being tried



Decision Tree of PODEM (4)

- **Branch and bound** search algorithm

✓ : initial assignment rejected
alternative is being tried

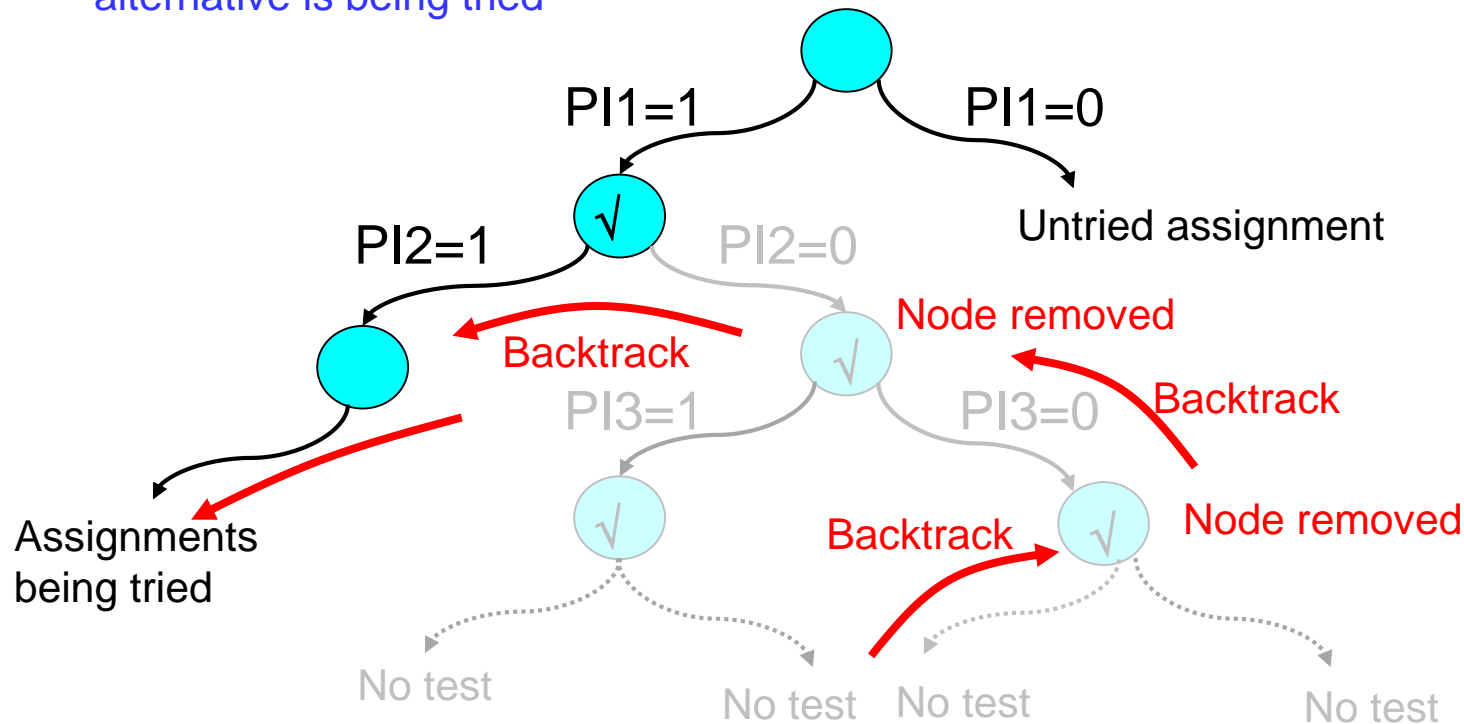


Decision Tree of PODEM (5)

- **Branch and bound** search algorithm

- ♦ Prune $PI3=0$ subtree
- ♦ Prune $PI2=0$ subtree

✓ : initial assignment rejected
alternative is being tried



PODEM: Summary

- **PODEM [Goel 1981]**
 - ◆ **Idea:**
 - * assign PI, not internal nodes
 - * forward implication only, no justification
 - ◆ **Heuristics**
 - * (1) backtrace easy/hard input for decision/imply gate
 - * (2) keep path inversion parity
 - * (3) propagate along X-path
 - ◆ **Algorithms**
 - * branch and bound search

FFT

- **Q1: Is PODEM a complete ATPG algorithm?**
- **Q2: Why does PODEM have no justification?**
- **Q3: Please give examples where heuristic #1/#2 gives wrong guess**