

# Test without Fault Model

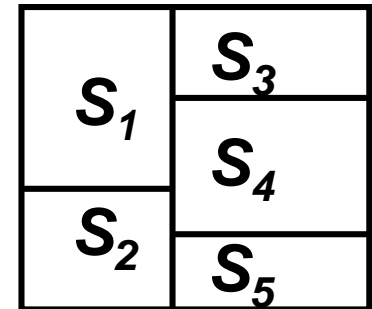
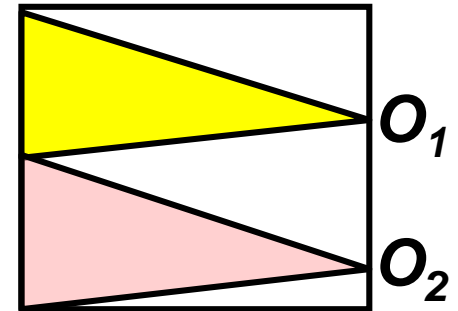
- Introduction
- Boolean Tests without Fault Model
  - ◆ Toggle Test
  - ◆ Design Verification
  - ◆ Exhaustive Test
  - ◆ **Pseudo Exhaustive Test (PET)**
    - \* Individual Output Verification
    - \* **Segment Verification**
      - **Path sensitization**
      - MUX Insertion
- Conclusion



Some examples in this PPT are from McCluskey's original lecture notes @Stanford University

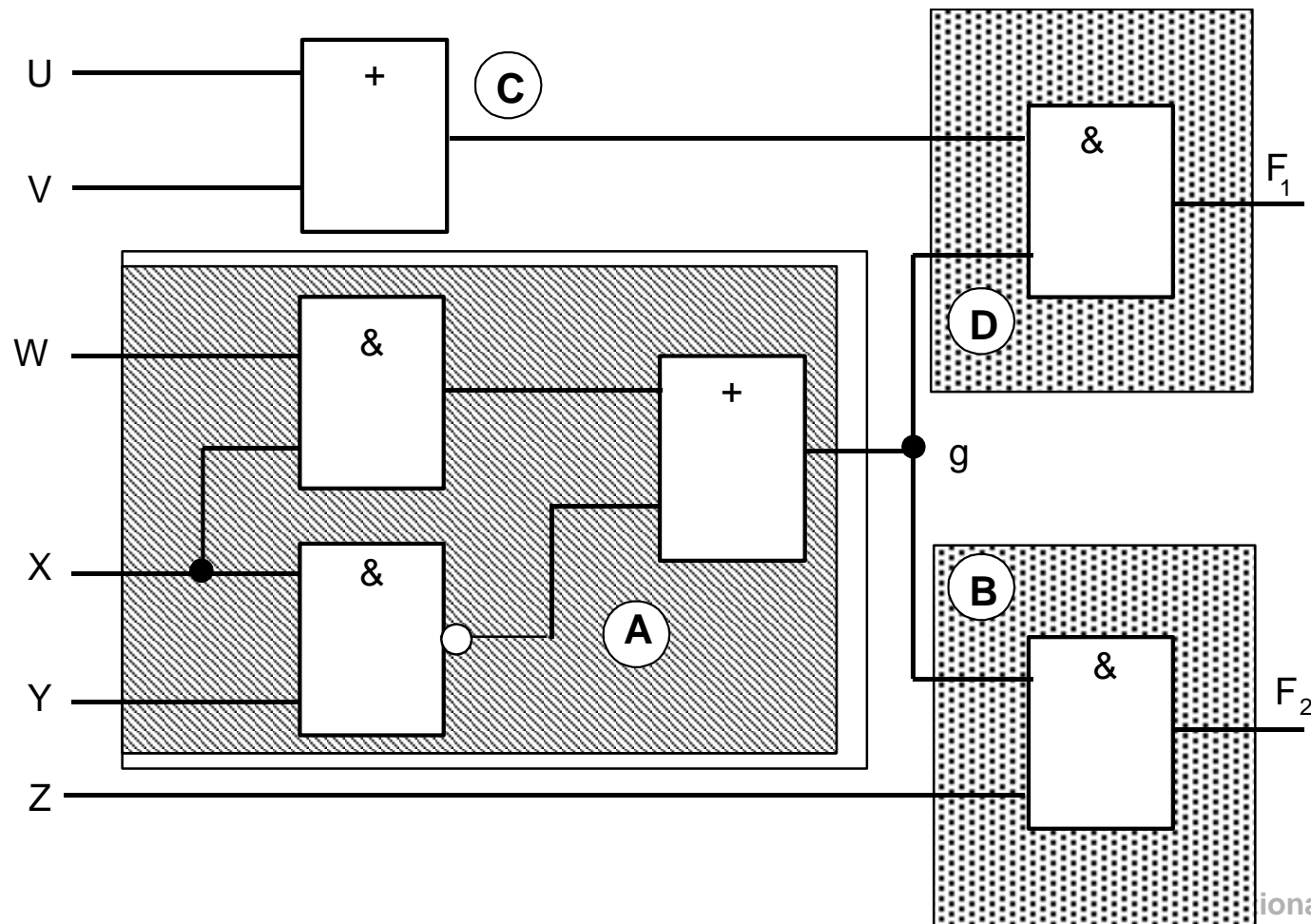
# Review: Pseudo Exhaustive Test

- Idea
  - ♦ Do not need exhaustive test for whole circuit
  - ♦ Test each circuit **partition** exhaustively
- Two categories:
  1. **Individual Output Verification (IOV)**
    - \* Exhaustive test of each output
    - \* Last video
  2. **Segment Verification**
    - \* Exhaustive test of each segment
    - \* This video



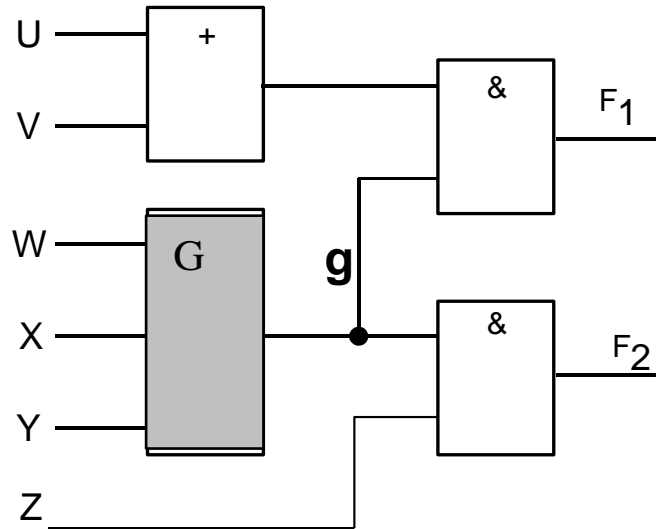
# Segment Verification [McCluskey 81]

- Idea: Partition circuit, test each segment exhaustively
- Example: Partitioned into **4 segments**: A, B, C, D



# Path Sensitization (1) - Test A

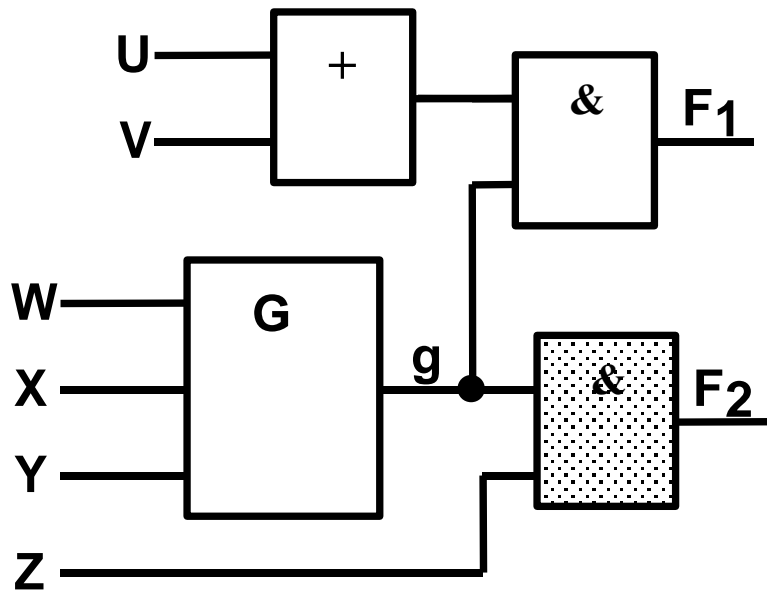
- Sensitize to F2: Set Z to 1
- 8 test patterns



	U	V	W	X	Y	Z	g	F <sub>1</sub>	F <sub>2</sub>
1			0	0	0	1	1		1
2			0	0	1	1	1		1
3			0	1	0	1	1		1
4			0	1	1	1	0		0
5			1	0	0	1	1		1
6			1	0	1	1	1		1
7			1	1	0	1	1		1
8			1	1	1	1	1		1

# Path Sensitization (2) - Test B

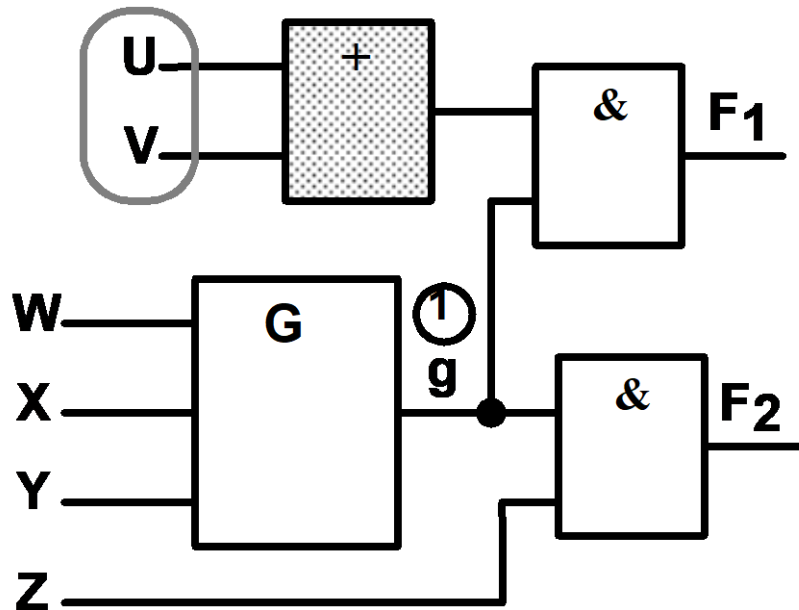
- Add two extra patterns



UV	WXY	Z	g	F <sub>1</sub>	F <sub>2</sub>
	000	1	1		1
	001	1	1		1
	010	1	1		1
	011	1	0		0
	100	1	1		1
	101	1	1		1
	110	1	1		1
	111	1	1		1
	111	0	1		0
	011	0	0		0

# Path Sensitization (3) - Test C

- Sensitized to F1
- No extra pattern needed

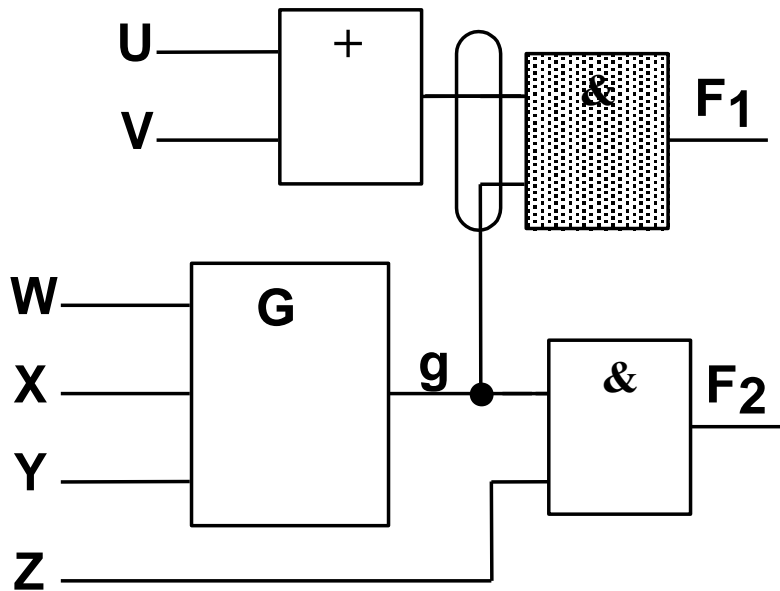


UV OR gate  
sensitized  
to F1 by  $g = 1$ .

UV	WXY	Z	g	F <sub>1</sub>	F <sub>2</sub>
	000	1	1		1
	001	1	1		1
	010	1	1		1
	011	1	0		0
00	100	1	1	0	1
01	101	1	1	1	1
10	110	1	1	1	1
11	111	1	1	1	1
	111	0	1		0
	011	0	0		0

# Path Sensitization (4) - Test D

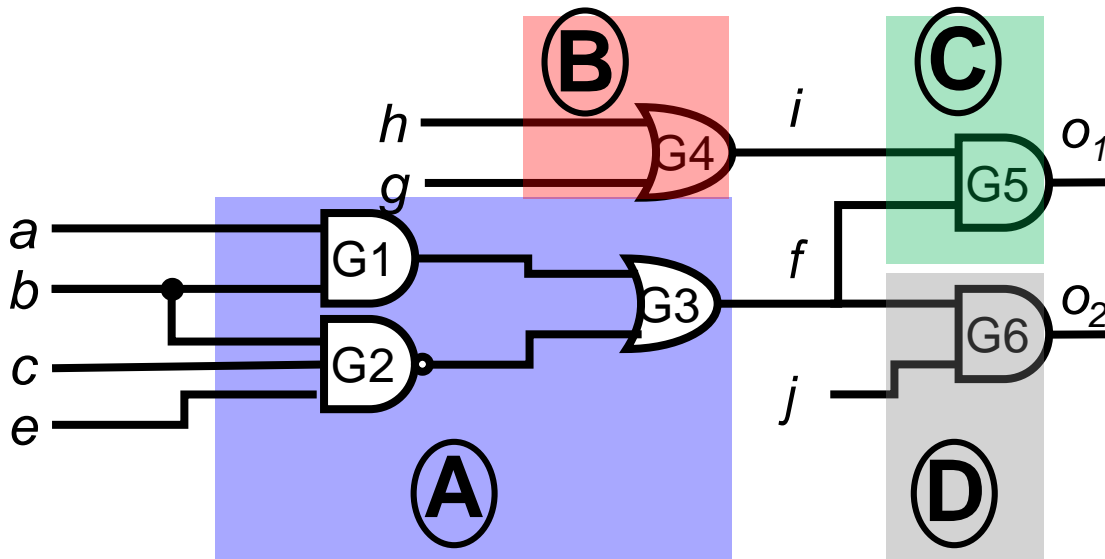
- No extra pattern needed
- Total **10** patterns



UV	WXY	Z	g	F <sub>1</sub>	F <sub>2</sub>
	000	1	1		1
	001	1	1		1
	010	1	1		1
00	011	1	0	0	0
00	100	1	1	0	1
01	101	1	1	1	1
10	110	1	1	1	1
11	111	1	1	1	1
	111	0	1		0
11	011	0	0	0	0

# Quiz

**Q: Exhaustive test length is  $2^7=128$ .  
Find minimum SV test for this circuit.  
Test length =?  
(Hint: ABCD 4 partitions.)**



	a	b	c	e	f	g	h	i	j
1	0	0	0	0					
2	0	0	0	1					
3	0	0	1	0					
4	0	0	1	1					
5	0	1	0	0					
6	0	1	0	1					
7	0	1	1	0					
8	0	1	1	1					
9	1	0	0	0					
10	1	0	0	1					
11	1	0	1	0					
12	1	0	1	1					
13	1	1	0	0					
14	1	1	0	1					
15	1	1	1	0					
16	1	1	1	1					
17									
18									
19									
20									



# Test without Fault Model

- Introduction
- Boolean Tests without Fault Model
  - ◆ Toggle Test
  - ◆ Design Verification
  - ◆ Exhaustive Test
  - ◆ **Pseudo Exhaustive Test (PET)**
    - \* Individual Output Verification
    - \* **Segment Verification**
      - Path sensitization
      - **MUX Insertion**
- Conclusions

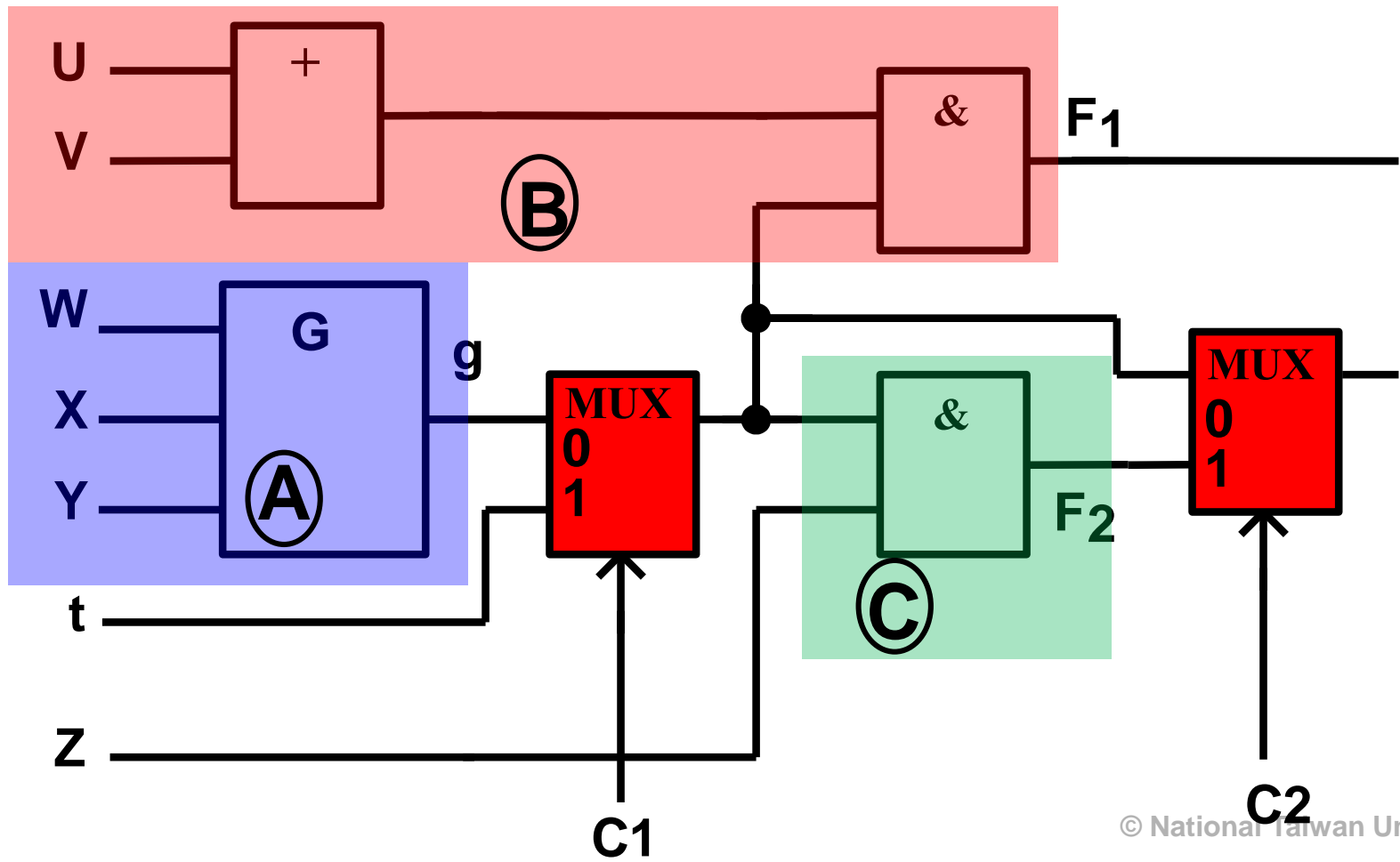


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**Any Simpler Method?**

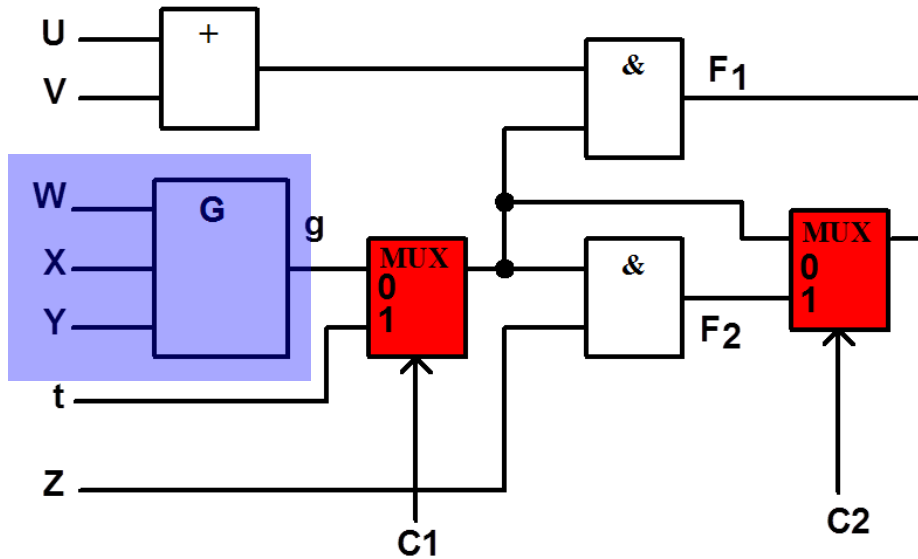
# MUX Insertion

- Partition into 3 segments: A, B, C
- Area overhead: 3 test signals, 2 MUX
- Fully control and observe each segment



# Test A

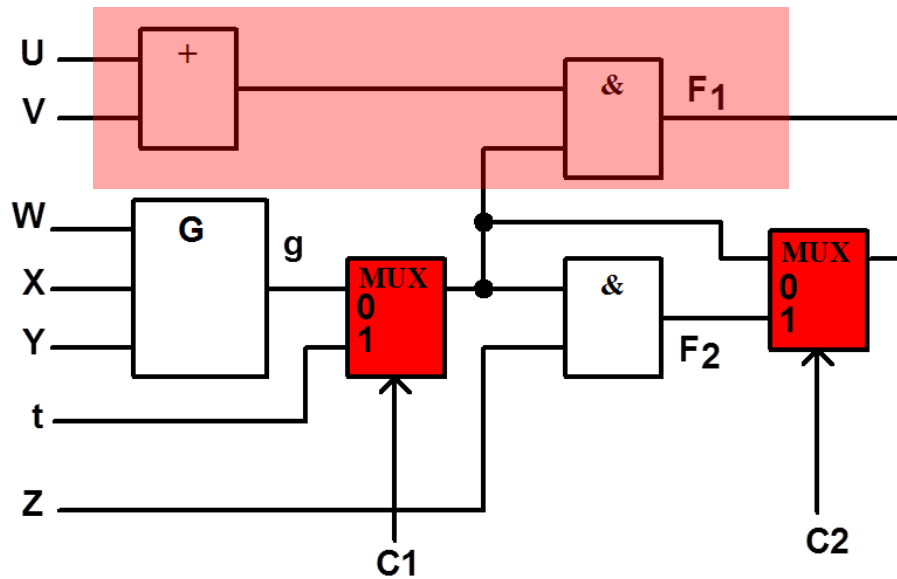
- 8 test patterns



	U	V	W	X	Y	Z	g	t	C <sub>1</sub>	C <sub>2</sub>
1			0	0	0		1		0	0
2			0	0	1		1		0	0
3			0	1	0		1		0	0
4			0	1	1		0		0	0
5			1	0	0		1		0	0
6			1	0	1		1		0	0
7			1	1	0		1		0	0
8			1	1	1		1		0	0
9										
10										
11										
12										
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14										
15										
16										
17										
18										
19										
20										

# Test B

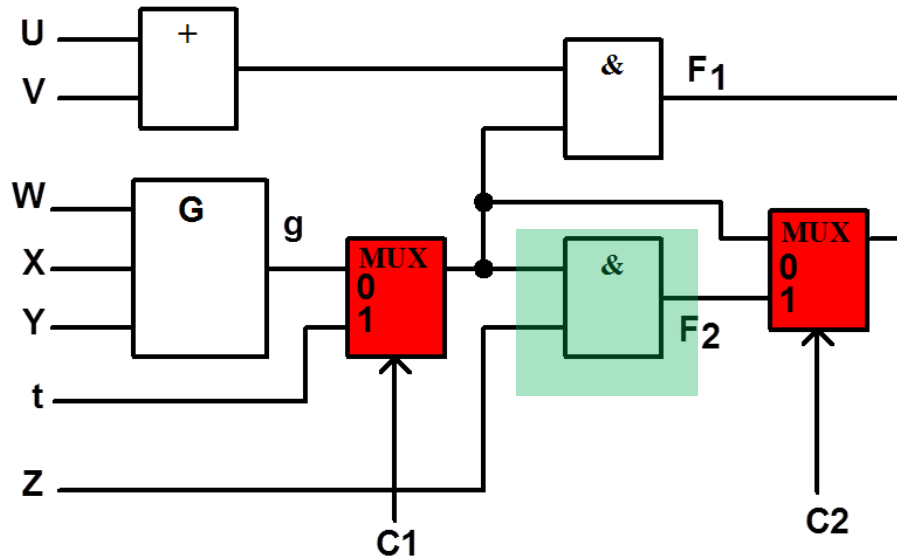
- add 8 test patterns



	U	V	W	X	Y	Z	g	t	C <sub>1</sub>	C <sub>2</sub>
1			0	0	0		1		0	0
2			0	0	1		1		0	0
3			0	1	0		1		0	0
4			0	1	1		0		0	0
5			1	0	0		1		0	0
6			1	0	1		1		0	0
7			1	1	0		1		0	0
8			1	1	1		1		0	0
9	0	0						0	1	
10	0	0						1	1	
11	0	1						0	1	
12	0	1						1	1	
13	1	0						0	1	
14	1	0						1	1	
15	1	1						0	1	
16	1	1						1	1	
17										
18										
19										
20										

# Test C

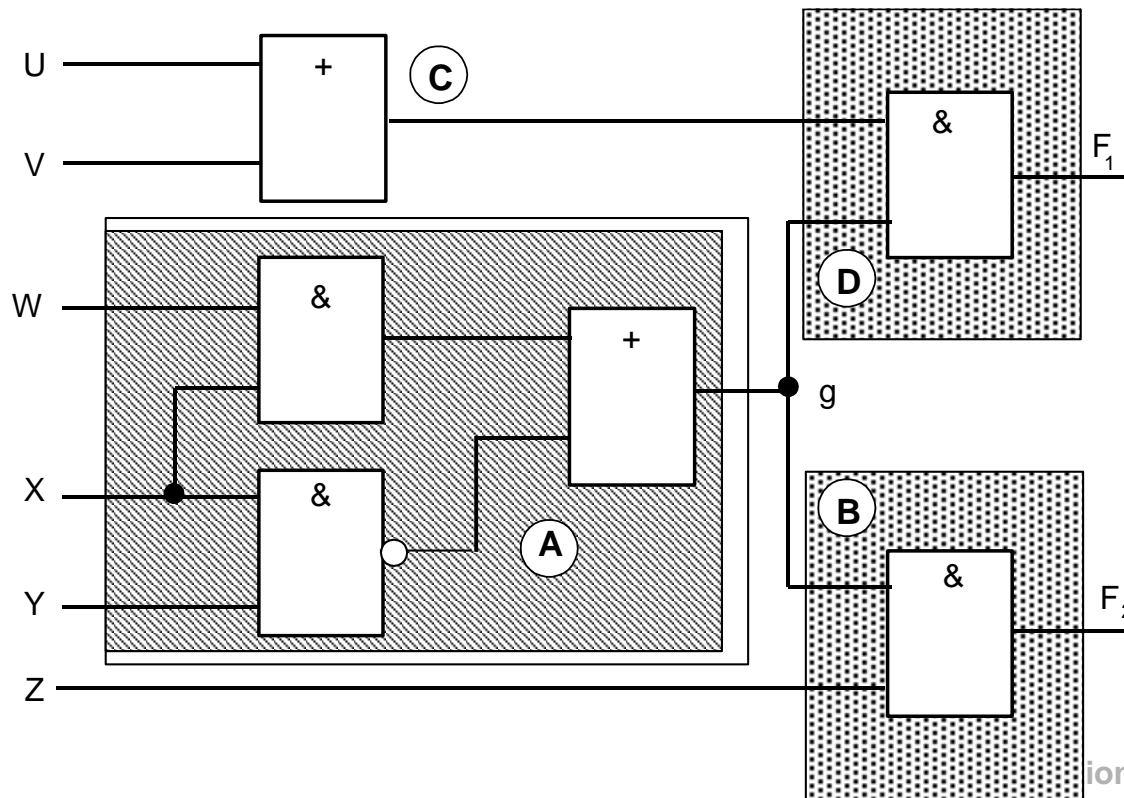
- add 4 test patterns
- totally test length = 20



	U	V	W	X	Y	Z	g	t	C <sub>1</sub>	C <sub>2</sub>
1			0	0	0		1		0	0
2			0	0	1		1		0	0
3			0	1	0		1		0	0
4			0	1	1		0		0	0
5			1	0	0		1		0	0
6			1	0	1		1		0	0
7			1	1	0		1		0	0
8			1	1	1		1		0	0
9	0	0						0	1	
10	0	0						1	1	
11	0	1						0	1	
12	0	1						1	1	
13	1	0						0	1	
14	1	0						1	1	
15	1	1						0	1	
16	1	1						1	1	
17						0		0	1	1
18						0		1	1	1
19						1		0	1	1
20						1		1	1	1

# Conclusion

- Exhaustive test = **64**
- PET Individual Output Verification = **32**
- PET Segment Verification
  - ♦ Path sensitization = **10**
  - ♦ MUX = **20**



# Summary

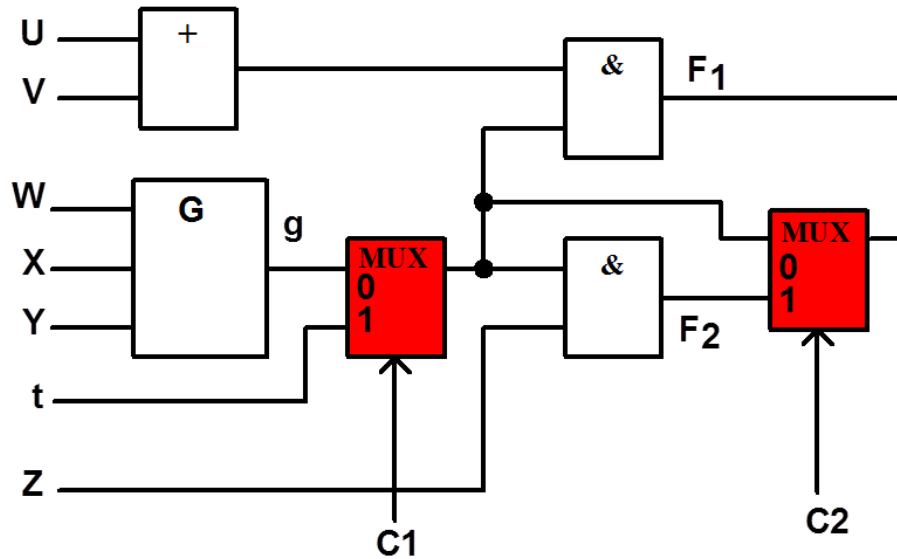
- Pseudo Exhaustive Test (PET)
  - ◆ Individual Output Verification
    - \* Test each output exhaustively
  - ◆ Segment Verification
    - \* Test each segment exhaustively
- Two SV techniques
  - ① Path sensitization
    - ◆ Sensitize by test pattern
    - ◆ No hardware but difficult to find test
  - ② MUX Insertion
    - ◆ Add MUX to control/observe
    - ◆ Need hardware but easier to find test
- PET effectively **reduce test length**. Good for **BIST**



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# FFT

- Q: Can we do better than 20 ?

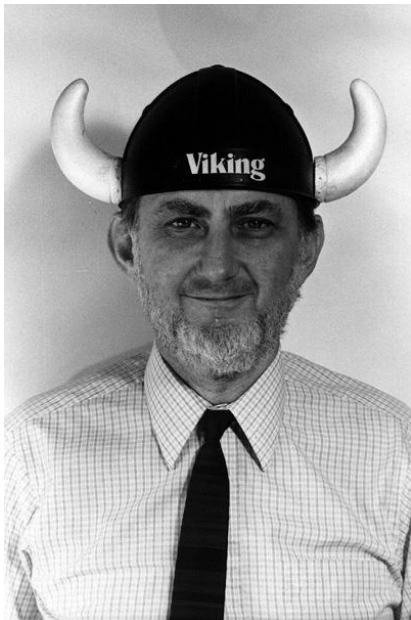
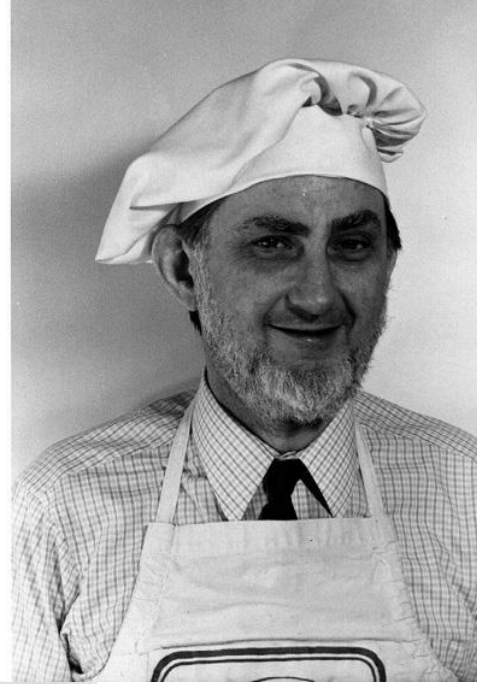
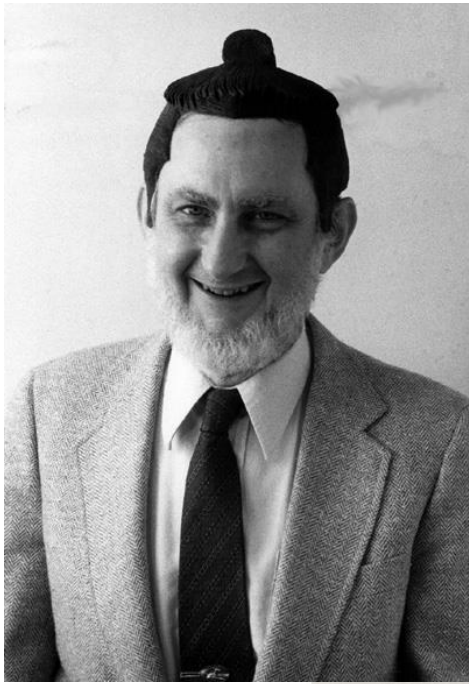


	U	V	W	X	Y	Z	g	t	C <sub>1</sub>	C <sub>2</sub>
1			0	0	0		1		0	0
2			0	0	1		1		0	0
3			0	1	0		1		0	0
4			0	1	1		0		0	0
5			1	0	0		1		0	0
6			1	0	1		1		0	0
7			1	1	0		1		0	0
8			1	1	1		1		0	0
9	0	0						0	1	
10	0	0						1	1	
11	0	1						0	1	
12	0	1						1	1	
13	1	0						0	1	
14	1	0						1	1	
15	1	1						0	1	
16	1	1						1	1	
17						0		0	1	1
18						0		1	1	1
19						1		0	1	1
20						1		1	1	1



# References

- [Hennie 64] F.C. Hennie “Fault detection experiments for sequential circuits”, Symposium on switching and automata theory, 1964.
- [Kime 66] C. R. Kime, “An organization for checking experiments on sequential circuits, IEEE Trans. Electron,” Comput. EC-U, 113-115, 1966.
- [McCluskey 81] E.J. McCluskey, S. Bozorgui-Nesbat, “Design for autonomous test”, IEEE Trans. on Ckt. and System, Volume: 28, Issue: 11, Nov 1981.
- [McCluskey 84] E.J. McCluskey, “Verification Testing – A Pseudo exhaustive Test Technique,” IEEE Trans. On Computers, C-33(6), pp541-546, 1984.
- [Moore 56] E. F. Moore, "Gedanken experiments on sequential machines," in Automata Studies. Princeton, 1956.
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# Exercise

- Show PET test for this circuit

