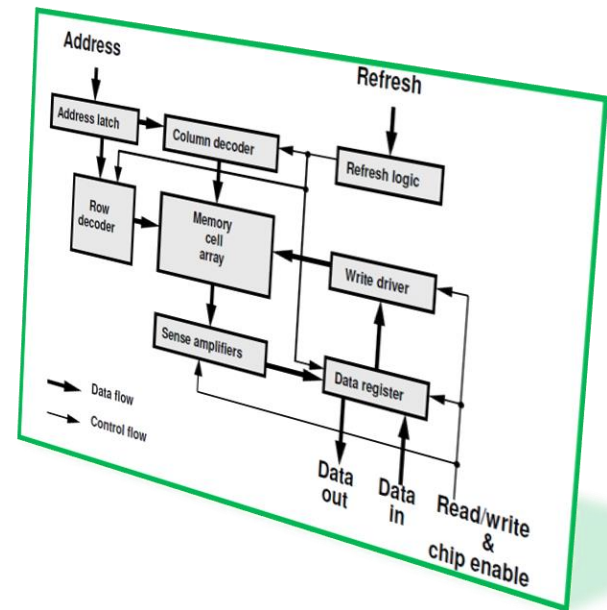


# Memory Testing

- Introduction
- Memory Fault Model
- **Memory Test Algorithms**
  - ◆ Classical algorithms
  - ◆ March algorithms
- Memory Fault Simulation
- Memory Test Generation
- Memory BIST



# Memory Test Algorithms

- A **Test algorithm** is a finite sequence of **test elements**
- A **test element** contains a number of
  1. **Memory operations**
    - \* Read or Write
  2. **Data pattern** (aka. **data background**)
    - \* Zero or One
  3. **Address sequence**
    - \* **Ascending or Descending**
- **Test (time) Complexity** of test algorithm is expressed in terms of  $N$ 
  - ♦  $N$  = memory size = number of memory cells
  - ♦ Higher complexity means **longer test time**

**Mem. Test Alg. is Different from ATPG Alg.**

# Memory Test (Time) Complexity

| Size | $N$   | $10N$ | $N \lg N$ | $N^{1.5}$ | $N^2$ |
|------|-------|-------|-----------|-----------|-------|
| 1M   | 0.01s | 0.1s  | 0.2s      | 11s       | 3h    |
| 16M  | 0.16s | 1.6s  | 3.9s      | 11m       | 33d   |
| 64M  | 0.66s | 6.6s  | 17s       | 1.5h      | 1.43y |
| 256M | 2.62s | 26s   | 1.23m     | 12h       | 23y   |
| 1G   | 10.5s | 1.8m  | 5.3m      | 4d        | 366y  |
| 4G   | 42s   | 7m    | 22.4m     | 32d       | 59c   |
| 16G  | 2.8m  | 28m   | 1.6h      | 261d      | 936c  |

$N$  = number of memory cells; 100MHz test speed

**Linear Complexity Feasible for Production Tests**

# QUIZ

Q: Which one is correct about memory testing?

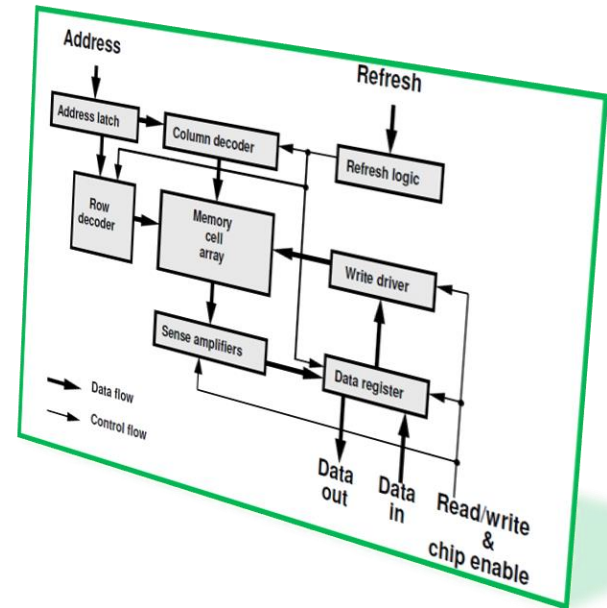
A) Higher complexity means longer CPU time

B) Test algorithm means a finite sequence of test elements, which contain: memory operation, data pattern, and address sequence

C) ( $N \log N$ ) Complexity is acceptable for large memory

# Memory Testing

- Introduction
- Memory Fault Model
- Memory Test Algorithms
  - ◆ Classical algorithms
    - \* MSCAN
    - \* Checkerboard
    - \* GALPAT
    - \* Butterfly
  - ◆ March algorithms
- Memory Fault Simulation
- Memory Test Generation
- Memory BIST

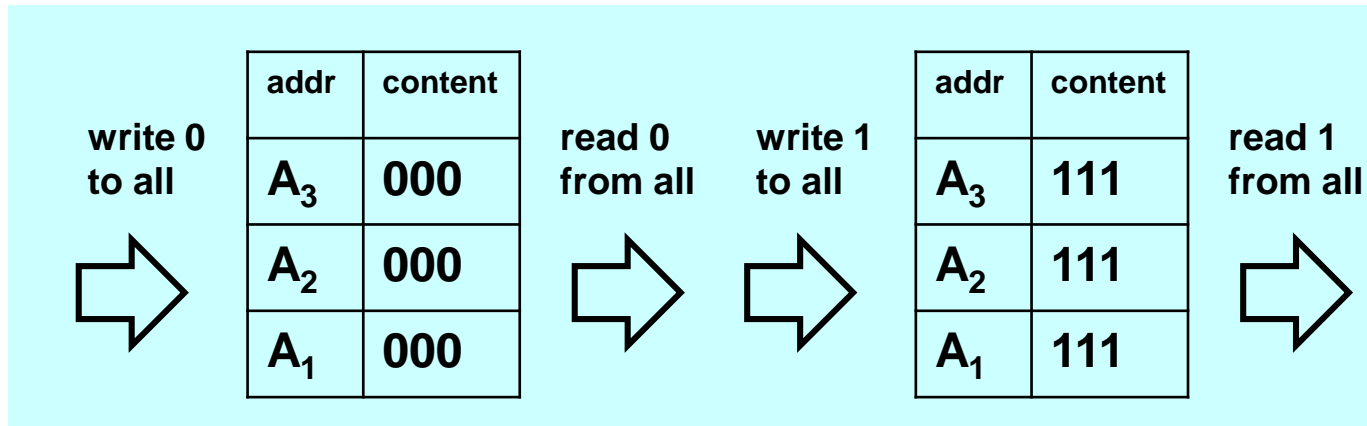


# MSCAN

- aka. **zero-one algorithm**
- Detects all **SAF**
- Detects  $\langle \uparrow/0 \rangle$  TF, not  $\langle \downarrow/1 \rangle$
- Does NOT detect all AF, CF
- Complexity is  $4N$ 
  - ♦ 4 operations each cell

## MSCAN

1. **Write zero** to every cell
2. **Read zero** from every cell
3. **Write one** to every cell
4. **Read one** from every cell



# Checkerboard

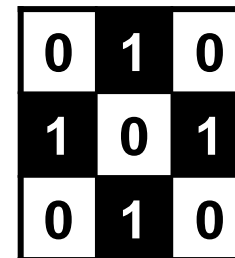
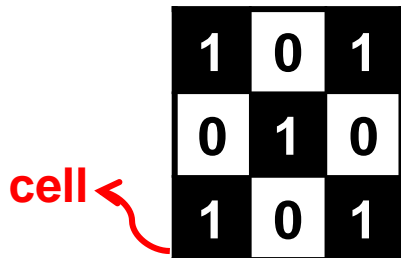
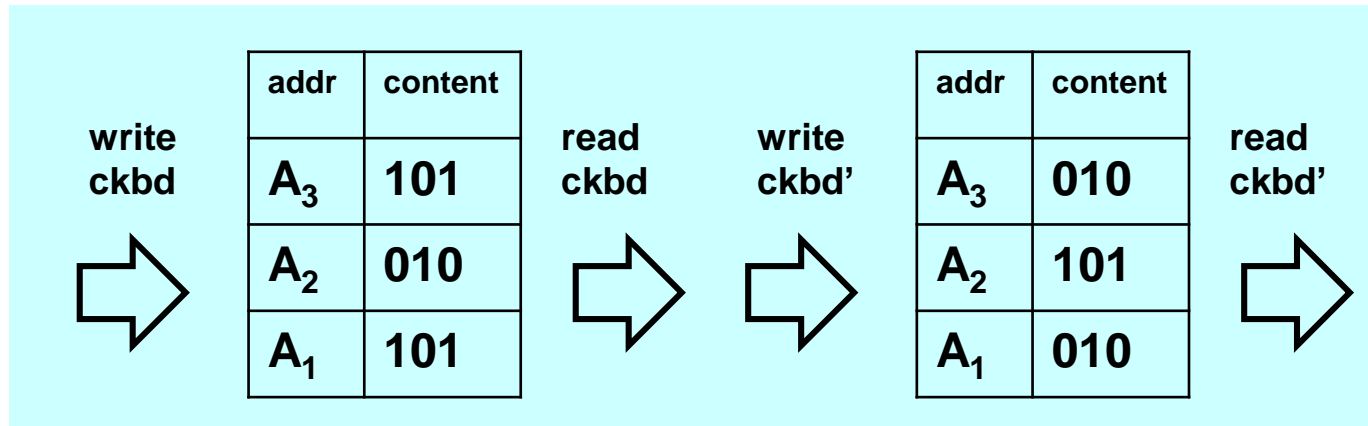
- Detects all **SAF** and half **TF**
- Does NOT detect all **AF**, **CF**
- Complexity is  $4N$

Same as MSCAN but  
Detects *Bridging Fault*

## CHECKERBOARD

1. Write **ckbd pattern** to all cells
2. **Read** ckbd pattern from all cells
3. Write **ckbd' pattern** to all cells
4. **Read** ckbd' pattern from all cells

ckbd means 01 alternating  
ckbd' is complement of ckbd



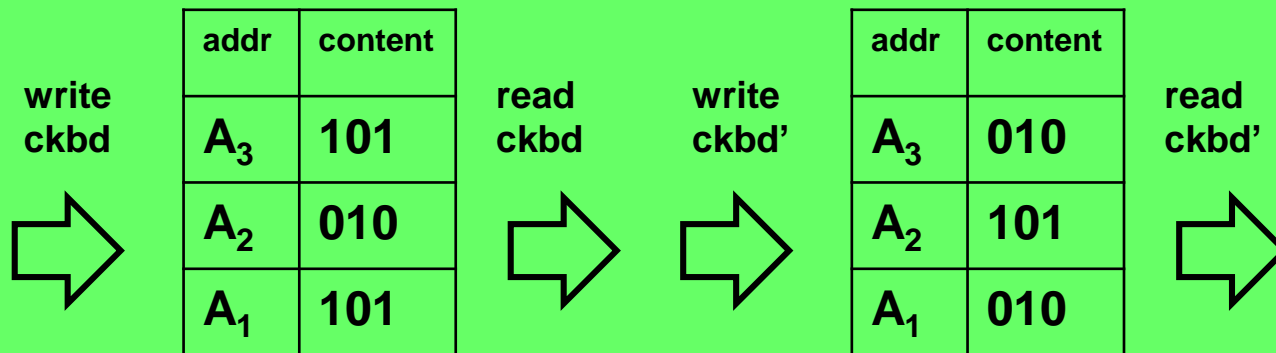
# QUIZ

**Q1: Can checkerboard detect OR-type AF between  $A_1$  and  $A_2$ ?**

**ANS:**

**Q2: Can checkerboard detect OR-type AF between  $A_1$  and  $A_3$ ?**

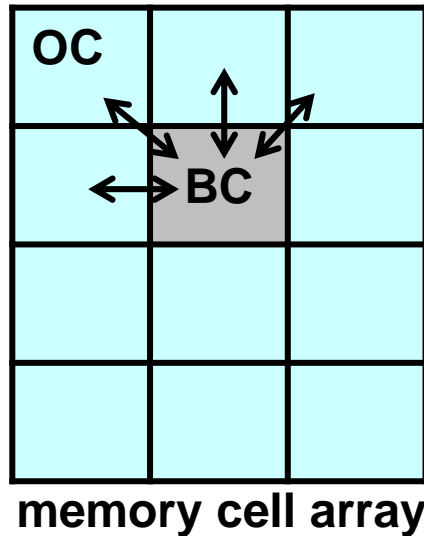
**ANS:**





# Galloping Test (GALPAT)

- Aka. *Ping-pong test*
- Detects all **SAF**, **TF**
- Detects **CF**, and **AF**
- Complexity is  $4N^2$ 
  - ♦ Line 2:  $2N^2$
  - ♦ Line 4:  $2N^2$



## GALPAT

1. Write **background 0** to all cells;
2. For BaseCell = 0 to N-1  
    **Complement BC**;  
    For OtherCell = 0 to N-1, OC != BC;  
        **Read BC**; **Read OC**;  
    **Complement BC**;
3. Write **background 1** to all cells;
4. Repeat Step 2;

**Too Long! Only for Characterization**

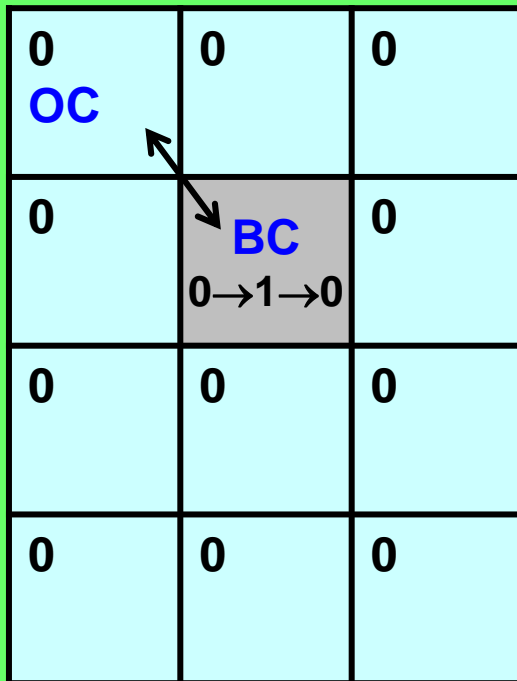
# QUIZ

Suppose BC is aggressor and OC is victim.

Q1: Can we detect  $CF_{st} <1; 0/1>$ ?

Q2: Can we detect  $CF_{id} <\uparrow; 0/1>$ ?

Q3: Can we detect  $CF_{in} <\uparrow; \forall/\downarrow>$ ?



## GALPAT

1. Write **background 0** to all cells;
2. For BaseCell = 0 to N-1  
    **Complement BC**;  
    For OtherCell = 0 to N-1, OC != BC;  
        **Read BC**; **Read OC**;  
        **Complement BC**;
3. Write **background 1** to all cells;
4. Repeat Step 2;

# Butterfly Algorithm

- Detects **SAF** and **TF**
- Does not detect all **CF, AF**
- Complexity is  **$10 N \log N$** 
  - ♦ 5 reads for each *dist*
  - ♦ *dist* **doubles** each loop
  - ♦ Repeated in line 4

|   |   |             |   |   |  |
|---|---|-------------|---|---|--|
|   |   | 6           |   |   |  |
|   |   | 1           |   |   |  |
| 9 | 4 | BC<br>5, 10 | 2 | 7 |  |
|   |   | 3           |   |   |  |
|   |   | 8           |   |   |  |
|   |   |             |   |   |  |

memory cell array



```

BUTTERFLY    // given MAXDIST < 0.5 col/row size
1. Write background 0;
2. For BaseCell = 0 to N-1
    Complement BC; dist = 1;
    While dist ≤ MAXDIST
        Read cell @ dist north from BC;
        Read cell @ dist east from BC;
        Read cell @ dist south from BC;
        Read cell @ dist west from BC;
        Read BC;    dist = dist * 2;
    Complement BC;
3. Write background 1;
4. Repeat Step 2;
    
```

# Summary

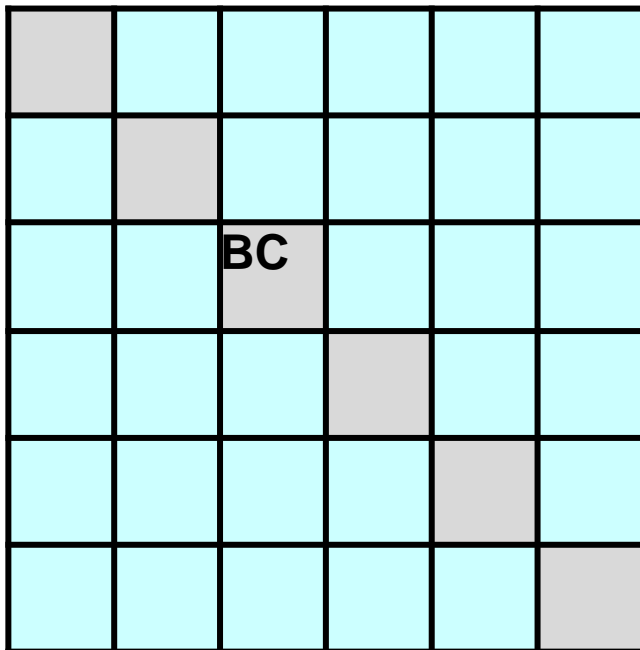
- **Test algorithm** is a finite sequence of **test elements**
  - ♦ which are: **Memory operation**, **Data pattern**, **Address sequence**
  - ♦ **Test complexity** means **test time** (not CPU time)
- Four classical test algorithms
  - ♦ MSCAN and Checkerboard's **fault coverage NOT good**
  - ♦ GALPAT and Butterfly are **too slow**
- Need **linear-time** test algorithms with good fault coverage
  - ♦ **March test algorithms** (see 16.3)

|              | SAF | AF | TF | CF | Complexity    |
|--------------|-----|----|----|----|---------------|
| MSCAN        | D   | -  | -  | -  | $4N$          |
| Checkerboard | D   | -  | -  | -  | $4N$          |
| GALPAT       | D   | D  | D  | D  | $4N^2$        |
| Butterfly    | D   | -  | D  | -  | $10 N \log N$ |

D: all detected;  
- : not all detected

# FFT

- Q: In GALPAT, choosing all cells as base cell is slow. Can we choose only cells on the diagonal line as BC? What is complexity?
- Q: Why do we choose cells in the same column and row of BC in Butterfly test?



## GALPAT-DIAGONAL

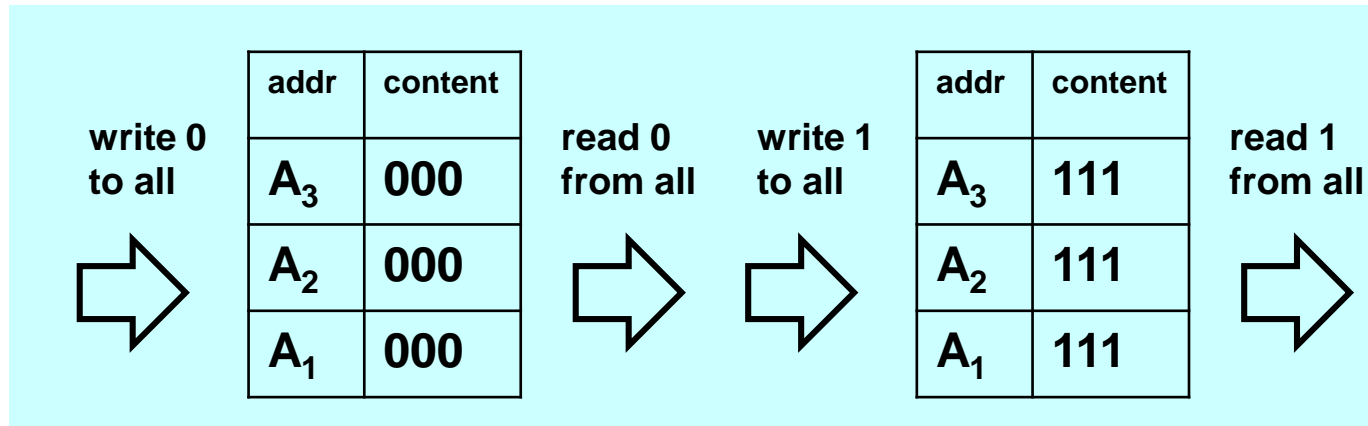
1. Write background 0 to all cells;
2. For BaseCell = 0 to N-1  
    // BC must be on diagonal line  
    Complement BC;  
    For OtherCell = 0 to N-1, OC != BC;  
        Read BC; Read OC;  
    Complement BC;
3. Write background 1 to all cells;
4. Repeat Step 2;

# MSCAN [Breuer & Friedman 1976]

- aka. **zero-one algorithm**
- Detects all **SAF**
- Detects  $\langle \uparrow/0 \rangle$  TF, not  $\langle \downarrow/1 \rangle$
- Does NOT detect all AF, CF
- Complexity is  **$4N$**

## MSCAN

1. **Write zero** to every cell
2. **Read zero** from every cell
3. **Write one** to every cell
4. **Read one** from every cell



|       | SAF | AF | TF  | CF | Complexity |
|-------|-----|----|-----|----|------------|
| MSCAN | D   | -  | 1/2 | -  | 4N         |

D: all detected  
- : not all detected