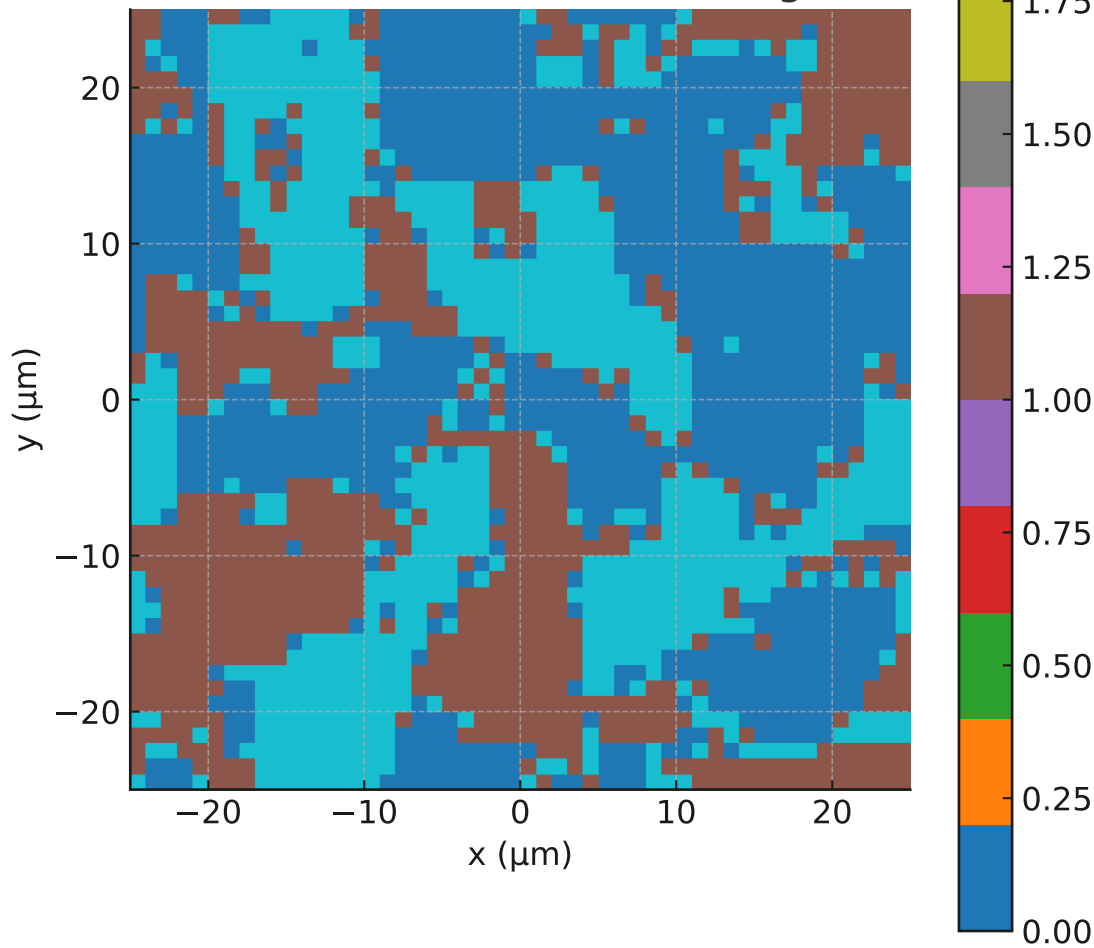
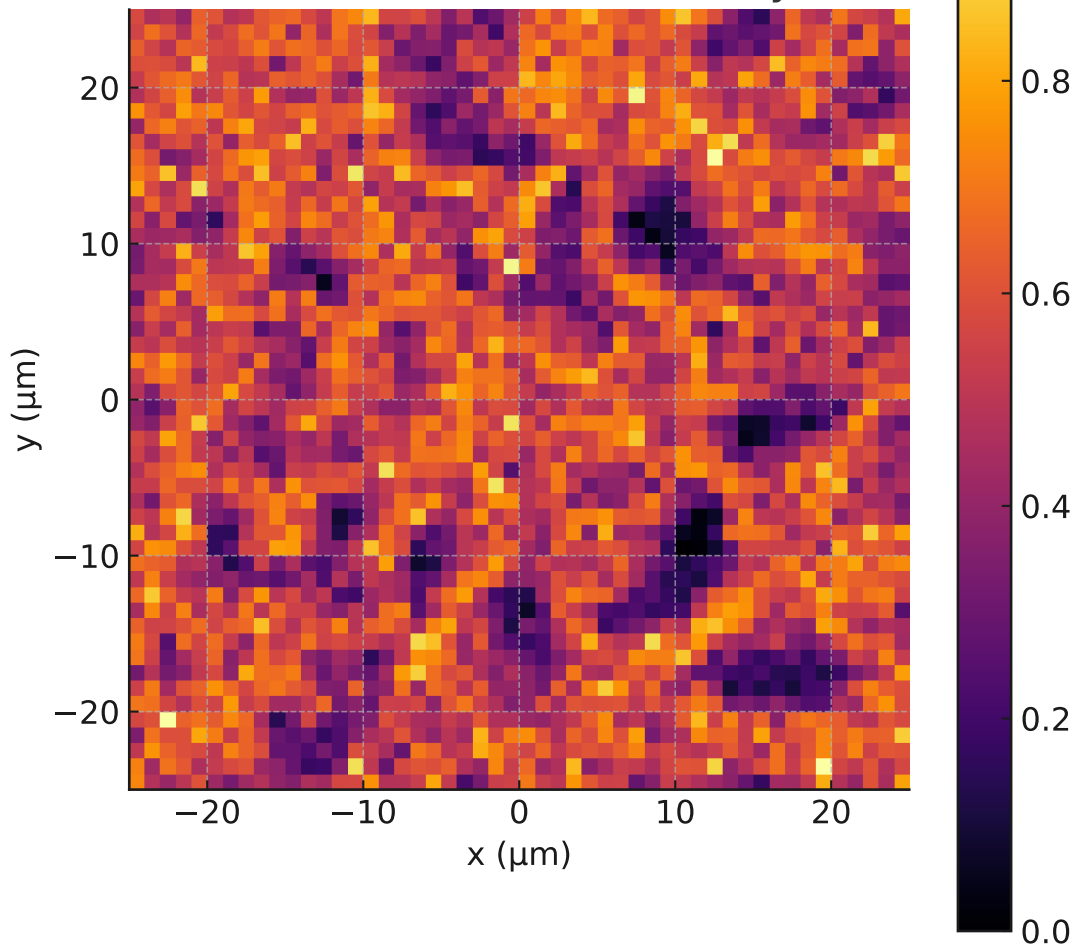


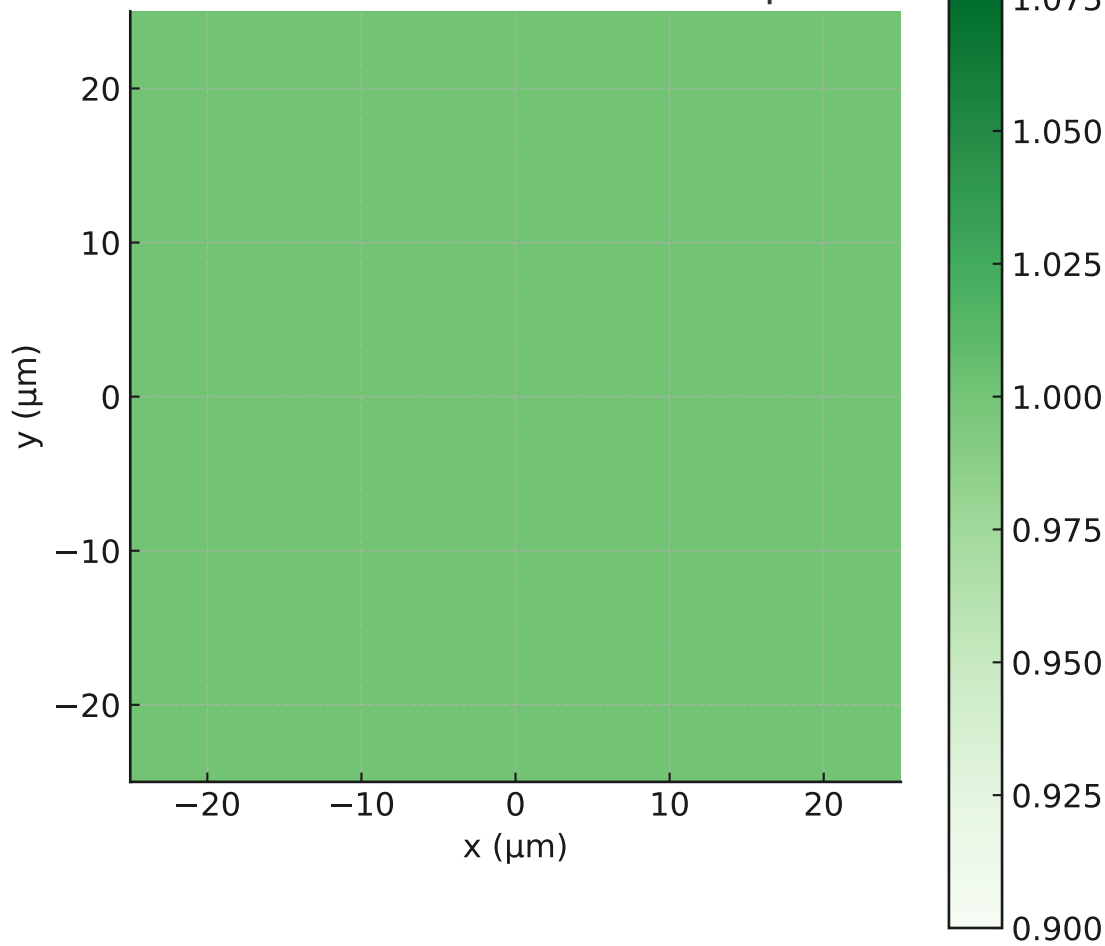
τ Field After Full Annealing



τ Fusion Violation Density



τ Domain Coherence Map



SAT LAB 1 – Full Annealing of τ Field on Radial θ_4 Kink Background

Simulation Setup:

- 50×50 grid with $\tau \in \mathbb{Z}_3$ and a static radial $\theta_4(r)$ kink centered at $r_0 = 15 \mu\text{m}$.
- $\theta_4(r) = (2\pi/3)(1 + \tanh[\mu(r - r_0)])/2$ with $\mu = 5 \mu\text{m}^{-1}$.
- Local fusion penalty strength $\lambda(x, y) = \lambda_0 + \lambda_1 \cdot |\nabla \theta_4(x, y)|$ with $\lambda_0 = 1.0$, $\lambda_1 = 10.0$.
- 100,000-step Metropolis annealing from $T = 2.0$ to 0.25 .

Results Summary:

1. τ domains emerge clearly and preferentially align near the radial kink zone.
2. Fusion violation density is lowest around $r \approx 15 \mu\text{m}$, where the θ_4 gradient is steepest.
3. τ domain coherence is strongest near the θ_4 wall, confirming coupling-induced stabilization.

Conclusion:

This confirms the SAT-predicted effect: τ fusion behavior is modulated by θ_4 scalar geometry. The kink acts as an energetic attractor for fusion-stable τ configurations.