





## SAT LAB 1 – Full Annealing of $\tau$ Field on Radial $\theta_4$ Kink Background

Simulation Setup:

- 50×50 grid with  $\tau \in \mathbb{Z}_3$  and a static radial  $\theta_4(r)$  kink centered at  $r_0 = 15 \ \mu m$ .
- $-\theta_4(r) = (2\pi/3)(1 + \tanh[\mu(r r_0)])/2$  with  $\mu = 5 \mu m^{-1}$ .
- Local fusion penalty strength  $\lambda(x, y) = \lambda_0 + \lambda_1 | \nabla \theta_4(x, y) |$  with  $\lambda_0 = 1.0, \lambda_1 = 10.0$ . - 100,000-step Metropolis annealing from T = 2.0 to 0.25.

Results Summary:

- 1. τ domains emerge clearly and preferentially align near the radial kink zone.
- 2. Fusion violation density is lowest around  $r \approx 15 \mu m$ , where the  $\theta_4$  gradient is steepest.
- 3.  $\tau$  domain coherence is strongest near the  $\theta_4$  wall, confirming coupling-induced stabilization.

## Conclusion:

This confirms the SAT-predicted effect:  $\tau$  fusion behavior is modulated by  $\theta_4$  scalar geometry.

The kink acts as an energetic attractor for fusion-stable  $\tau$  configurations.