

Differensial tenglamalar

№1.

Qiyinlik darajasi-1

Differensial tenglama deb nimaga aytildi?

Erkli o'zgaruvchi va no'malum funksiya va uning hosilalari yoki differensiallarini bog'lovchi munosabatlar differensial tenglama deyiladi

Erkli o'zgaruvchi va no'malum funksiya bog'lovchi munosabatlar differensial tenglama deyiladi

Noma'lum funksiyani bog'lovchi munosabat differensial tenglama deyiladi

Erkli o'zgaruvchi va no'malum funksiya hosilalari yoki differensiallarini bog'lovchi munosabatlar differensial tenglama deyiladi

№2. Qiyinlik darajasi-1

Oddiy differensial tenglama deb nimaga aytildi?

Agar no'malum funksiya bitta erkli o'zgaruvchiga bog'liq bo'lsa, bunday differensial tenglama oddiy differensial tenglama deyiladi

Agar no'malum funksiya ikkita erkli o'zgaruvchiga bog'liq bo'lsa, bunday differensial tenglama oddiy differensial tenglama deyiladi

Agar no'malum funksiya uchta erkli erkli o'zgaruvchiga bog'liq bo'lsa, bunday differensial tenglama oddiy differensial tenglama deyiladi

Agar no'malum funksiya beshta erkli erkli o'zgaruvchiga bog'liq bo'lsa, bunday differensial tenglama oddiy differensial tenglama deyiladi

№3.

Qiyinlik darajasi-1

Differensial tenglama erkli o'zgaruvchiga nechta erkli o'zgaruvchiga bog'liq bo'lsa, xususiy hosila differensial tenglama deyiladi?

2 yoki undan ortiq

3 yoki undan ortiq

1 yoki undan ortiq

4 yoki undan ortiq

№4.

Qiyinlik darajasi-1

Differensial tenglamaga kirgan hosilalarning eng yuqori tartibi nima deb ataladi?

Differensial tenglama tartibi

Differensial tenglama o'lchami

Differensial tenglama o'chovi

Differensial tenglama yechimi

№5.

Qiyinlik darajasi-1

Differensial tenglamaning yechimi eki integrali deb tenglamaga qo'yganda uni ayniyatga aylantiradigan nimaga aytildi?

Har qanday differensiallanuvchi funksiyaga aytildi

Har qanday uzilishga ega bo'lgan funksiyaga aytildi

Har qanday funksionalga aytildi
Har qanday uzlusiz funksiyaga aytildi

№6.

Qiyinlik darajasi-1

Quyidagi tenglama nechanchi tartibli differensial tenglama $y'' - y' \cos x - x^2 y = 0$

2-tartibli

1-tartibli

3-tartibli

4-tartibli

№7.

Qiyinlik darajasi-1

Quyidagi differensial tenglamaning tartibini aniqlang:

$$x(1 - y^2)dx - y(1 - x^2)dy = 0$$

1-tartibli

3-tartibli

5-tartibli

0-tartibli

№8.

Qiyinlik darajasi-1

Quyidagi differensial tenglamada erkli o‘zgaruvchi nechta: $x \frac{\partial z}{\partial x} = y \frac{\partial z}{\partial y}$

2 ta

5 ta

3 ta

1 ta

№9.

Qiyinlik darajasi-2

$y = e^{Cx}$ chiziqlar oilasining differensial tenglamasini toping:

$$y = e^{\frac{xy'}{y}}$$

$$y'' = 0$$

$$y'' + y = 0$$

$$y' = \cos x$$

№10.

Qiyinlik darajasi-2

$y = \sin(x + C)$ chiziqlar oilasining differensial tenglamasini toping:

$$y^2 + y'^2 = 1$$

$$y' = y$$

$$y' = y^2$$

$$y' = \cos x(x + C)$$

№11.

Qiyinlik darajasi-2Quyidagi differential tenglamani yeching: $xydx + (x+1)dy = 0$

$y = c(x+1)e^{-x}$

$y = cx + 1$

$y = ce^x$

$y' = cxe^x$

№12.**Qiyinlik darajasi-2**Quyidagi differential tenglamani yeching: $2x^2yy' + y^2 = 2$

$y = \sqrt{2 - ce^x}$

$y = ce^x$

$y = 2 - ce^x$

$y = ce^x$

№13.**Qiyinlik darajasi-2**Quyidagi differential tenglamani yeching: $xy' + y = y^2$

$y = cxy + 1$

$y = cx - 2$

$y = cy - x$

$y = c(x - y)$

№14.**Qiyinlik darajasi-2**Quyidagi differential tenglamani yeching: $x\frac{dx}{dt} + t = 1$

$x^2 + t^2 - 2t = c$

$x = 2ct + 1$

$x = ct^2 - t$

$x^2 = ct - 1$

№15.**Qiyinlik darajasi-2**Quyidagi differential tenglamani yeching: $y' - y = 2x - 3$

$y + 2x - 1 = ce^x$

$y = cx + x^2$

$y = x + ce^x$

$y = c(x - 1)e^x$

№16.**Qiyinlik darajasi-2**Quyidagi differential tenglamani yeching: $(x^2 - 1)y' + 2xy^2 = 0$

$$y(\ln|x^2 - 1| + c) = 1, y = 0$$

$$y = c \ln(x + 1)$$

$$y = ce^x + 1$$

$$y' = \cos x(x + C)$$

№17.

Qiyinlik darajasi-2

Quyidagi differensial tenglamani yeching: $y' - xy^2 = 2xy$

$$\left| \frac{y}{y+2} \right| = ce^{x^2}$$

$$y = cx^2 + 2$$

$$y = cx^2 - 2$$

$$y = \sin(x + C)$$

№18.

Qiyinlik darajasi-2

Quyidagi differensial tenglamani yeching: $y' = 3\sqrt[3]{y^2}$

$$y = (x + c)^3, y = 0$$

$$y = cx^2 - 3x$$

$$cx = y^2$$

$$y = \cos(2x + C)$$

№19.

Qiyinlik darajasi-2

Quyidagi differensial tenglamani yeching: $(x + 2y)y' = 1$

$$x + 2y + 2 = ce^y$$

$$y = (2x - c)^2$$

$$y = ce^x + 1$$

$$y = \cos Cx$$

№20.

Qiyinlik darajasi-1

Birinchi tartibli oddiy differensial tenglamani umumiyo ko‘rinishini aniqlang

$$F(x, y, y') = 0$$

$$F(x, y, c,) = 0$$

$$\Phi(y, y') = 0$$

$$y' = f(x, y)$$

№21.

Qiyinlik darajasi-2

Birinchi tartibli differensial tenglamaga qo‘yilgan Koshi masalasini aniqlang:

$$\begin{cases} y' = f(x, y) \\ y|_{x=x_0} = y_0 \end{cases}$$

$$\begin{cases} y' = f(x, y) \\ x|_{x=x_0} = y_0 \end{cases}$$

$$\begin{cases} y' = f(x, y) \\ y'|_{x=x_0} = y_0 \end{cases}$$

$$\begin{cases} y' = f(x, y) \\ y''|_{x=x_0} = y_0 \end{cases}$$

№22.

Qiyinlik darajasi-2

Birinchi tartibli oddiy differensial tenglama umumiy yechimi ko‘rinishini aniqlang:

$$\Phi(x, y, c) = 0$$

$$F(x, y, y') = 0$$

$$y' = f(y, c)$$

$$y' = f(x, c)$$

№23.

Qiyinlik darajasi-2

O‘zgaruvchilarga ajralgan oddiy differensial tenglamani aniqlang

$$M_1(x)dx + N_1(x)dy = 0$$

$$M_1(x)dx +$$

$$+ N_1(x, y)dy = 0$$

$$M(x, y)dx + N(x, y)dy = 0$$

$$M_1(x, y)dx + N_1(x)dy = 0$$

№24.

Qiyinlik darajasi-2

O‘zgaruvchilarga ajraladigan oddiy differensial tenglamani aniqlang

$$M_1(x)N_1(y)dx +$$

$$+ M_2(x)N_2(y)dy = 0$$

$$M(x, y)dx +$$

$$+ N(x, y)dy = 0$$

$$M_1(y)dx +$$

$$+ N_1(x, y)dy = 0$$

$$M_1(x)dx +$$

$$+ N_1(x, y)dy = 0$$

№25.

Qiyinlik darajasi-3

Quyidagi differensial tenglama umumiy yechimini toping: $x(1+y^3)dx - y^2(1+x^2)dy = 0$

$$(1+x^2)^3 = e^c (1+y^3)^2$$

$$(1+x^3)^3 = \ln c (1+y^2)^2$$

$$(1+x^2)^3 = (1+y^3)^2$$

$$(1+x^2)^3 = c(1+y^3)^2$$

№26.

Qiyinlik darajasi-2

Birinchi tartibli chiziqli oddiy differensial tenglamani ko‘rinishini toping

$$y' + P(x)y = Q(x)$$

$$y' = f(x, y)$$

$$y' + P(x)z = Q(x)$$

$$M(x, y)dx + N(x, y)dy = 0$$

№27.

Qiyinlik darajasi-2

Quyidagi funksiyanibirjinsliliko‘lchovinianiqlang: $f(x) = \sqrt{x^2 + y^2}$

1-o‘lchovli

2-o‘lchovli

3-o‘lchovli

4-o‘lchovli

№28.

Qiyinlik darajasi-2

Quyidagi funksiyaning bir jinslilik o‘lchovini aniqlang: $f(x, y) = \frac{x - xy}{x + y^2}$

o‘lchovi yo‘q

2-o‘lchovli

1-o‘lchovli

0-o‘lchovli

№29.

Qiyinlik darajasi-3

$f(x, y)$ 0 o‘lchovli 1 jinsli funksiyani ko‘rinishini aniqlang:

$$f(x, y) = \varphi\left(\frac{y}{x}\right)$$

$$f(x, y) = \varphi(x + y)$$

$$f(x, y) = \varphi(xy)$$

$$f(x, y) = \varphi\left(\frac{1}{xy}\right)$$

№30 .

Qiyinlik darajasi-2

Birinchi tartibli bir jinsli differensial tenglamani yechishda qanday almashtirish bajariladi?

$$z = \frac{y}{x}$$

$$z = xy$$

$$z = x - y$$

$$z = x + y$$

№31.

Qiyinlik darajasi-3

$\frac{dy}{dx} = f\left(\frac{ax+by+c}{a_1x+b_1y+c_1}\right)$ tenglamada $\Delta = \begin{vmatrix} a & b \\ a_1 & b_1 \end{vmatrix} \neq 0$ bo'lsa, qanday almashtirish bajariladi
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$x = \alpha + u, y = \beta + v$

$x = \frac{\alpha}{u}, y = \frac{\beta}{v}$

$x = \alpha u, y = \beta v$

$x = zy$

№32.

Qiyinlik darajasi-3

$\frac{dy}{dx} = f\left(\frac{ax+by+c}{a_1x+b_1y+c_1}\right)$ tenglamada $\Delta = \begin{vmatrix} a & b \\ a_1 & b_1 \end{vmatrix} = 0$ bo'lsa, qanday almashtirish bajariladi

$z = ax + by$

$z = ax$

$z = by$

$z = ax + c$

№33.

Qiyinlik darajasi-2

Birinchi tartibli chiziqli tenglamani yechish usuli nomini aniqlang

Ixtiyorli o'zgarmasni variatsiyalash usuli
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Aniqmas koeffitsientlar usuli

Ketma-ket yaqinlashish usuli

Ketma-ket yo'qotish usuli

№34.

Qiyinlik darajasi-2

O'rniqa qo'yish usulida qanday almashtirish bajariladi?

$y = uv$

$y = u^2v$

$y = uv^2$

$y = u + v$

№35.

Qiyinlik darajasi-3

Umumlashgan bir jinsli tenglamada qanday almashtirish bajarilishini aniqlang
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$y = z^\alpha$

$y = z + x$

$y = \frac{u}{v}$

$y = uv$

№36.

Qiyinlik darajasi-3

Quyidagi tenglamaning umumi yechimini toping: $y' = \frac{y + \sqrt{x^2 - y^2}}{x}$

$$y = x \sin(\ln cx)$$

$$y = x \ln(\sin cx)$$

$$y = x \ln(\cos cx)$$

$$y = xt g(\ln cx)$$

№37.

Qiyinlik darajasi-3

Tenglamaning umumiy yechimini aniqlang: $y' + \frac{1}{x}y = \frac{\sin x}{x}$

$$y = \frac{1}{x}(c - \cos x)$$

$$y = \frac{1}{x}(c - \sin x)$$

$$y = \frac{1}{x}(c - \cos \sin x)$$

$$y = \frac{1}{x}(c - \arccos x)$$

№38.

Qiyinlik darajasi-2

Quyidagi tenglamalarni qaysi biri Bernulli tenglamasi hisoblanadi:

$$y' + P(x)y = Q(x)y^\alpha$$

$$y' + P(x)y + Q(x)y^2 = F(x)$$

$$y' + Q(x)y^2 = F(x)$$

$$y' + Q(x)y^2 = F(x)y^\alpha$$

№39.

Qiyinlik darajasi-3

Bernulli tenglamasi qanday tenglamaga keltiriladi?

Chiziqli

Bir jinsli

Eyler

Rikkati

№40.

Qiyinlik darajasi-2

Rikkati tenglamasini aniqlang

$$y' + P(x)y + Q(x)y^2 = F(x)$$

$$y' + Q(x)y^4 = F(x)$$

$$x^2 y' + P(x)y^{\frac{1}{2}} = 0$$

$$y' + P(x)y^3 = Q(x)$$

№41.

Qiyinlik darajasi-2

Rikkati tenglamasi avval qanday tenlamaga keltiriladi?

Bernulli

Lagranj

O'zgaruvchilarga ajralgan

Klero

№42.

Qiyinlik darajasi-3

Rikkati tenglamasining yechishda qanday almashtirish bajariladi

$$y = y_1(x) + z$$

$$y = uv$$

$$y = \frac{u}{v}$$

$$y = y_1(x)z$$

№43.

Qiyinlik darajasi-3

Differensial tenglama to'liq bo'lishining zaruriy va yetarli shartini aniqlang:

$$(M(x, y)dx + N(x, y)dy = 0)$$

$$\frac{\partial N}{\partial x} = \frac{\partial M}{\partial y}$$

$$\frac{\partial M}{\partial x} = \frac{\partial N}{\partial y}$$

$$\frac{\partial^2 M}{\partial x^2} = \frac{\partial^2 N}{\partial y^2}$$

$$\frac{\partial^2 M}{\partial x \partial y} = \frac{\partial^2 N}{\partial y \partial x}$$

№44.

Qiyinlik darajasi-3

Quyidagi Koshi masalasini yeching: $\begin{cases} 2x \cos^2 y dx + (2y - x^2 \sin 2y) dy = 0 \\ y|_{x=0} = 0 \end{cases}$

$$x^2 \cos^2 y + y^2 = 0$$

$$x^2 \operatorname{tg}^2 y + y^2 = 0$$

$$y^2 \cos^2 y + x^2 = 0$$

$$x^2 \sin^2 y + y^2 = 0$$

№45.

Qiyinlik darajasi-3

Quyidagi tenglama uchun integralovchi ko'paytuvchi qanday bo'ladi:

$$(x^2 - y) dx + (x^2 y^2 + x) dy = 0$$

$$\mu(x) = \frac{1}{x^2}$$

$$\mu(x) = x^2$$

$$\mu(x) = \frac{1}{x^3}$$

$$\mu(x) = x^3$$

№46.

Qiyinlik darajasi-3

Koshi masalasini yechimining mavjudlik shartini aniqlang:	$\begin{cases} y' = f(x, y) \\ y _{x=x_0} = y_0 \end{cases}$
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$f(x, y)$ – uzlucksiz

$\frac{\partial^2 f}{\partial y^2}$ – mavjud va uzlucksiz

$f(x, y)$ – 2-tartibli hosilasi mavjud
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$\frac{\partial f}{\partial y}$ – mavjud va uzlucksiz

№47.

Qiyinlik darajasi-3

Koshi masalasini yechimining yagonalik shartini aniqlang:	$\begin{cases} y' = f(x, y) \\ y _{x=x_0} = y_0 \end{cases}$
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$\frac{\partial f}{\partial y}$ – mavjud va uzlucksiz

$f(x, y)$ – 2-tartibli hosilasi mavjud
--

$\frac{\partial^2 f}{\partial y^2}$ – mavjud va uzlucksiz

$f(x, y)$ – uzlucksiz

№48.

Qiyinlik darajasi-2

$y' = \frac{y}{x}$ tenglamani $(0,0)$ maxsus nuqtasini nomini aniqlang
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dikritik tugun

Egar

Tugun

Fokus

№49.

Qiyinlik darajasi-2

$y' = \frac{2y}{x}$ tenglamani $(0,0)$ maxsus nuqtasini nomini aniqlang

Tugun

Fokus

dikritik nuqta

Markaz

№ 50.

Qiyinlik darajasi-2

$y' = -\frac{y}{x}$ tenglamani $(0,0)$ maxsus nuqtasini nomini aniqlang

Egar

Fokus

Markaz

Tugun

№51.

Qiyinlik darajasi-3

$$y' = \frac{x+y}{x-y} \text{ tenglamani } (0,0) \text{ maxsus nuqtasini nomini aniqlang}$$

Fokus

Egar

Dikritik tugun

Markaz

№52.

Qiyinlik darajasi-2

$$y' = -\frac{x}{y} \text{ tenglamani } (0,0) \text{ maxsus nuqtasini nomini aniqlang}$$

Markaz

Fokus

Dikritik tugun

Egar

№53.

Qiyinlik darajasi-2

Differensial tenglamada uning umumiy yechimidan ixtiyoriy o‘zgarmasning hech bir qiyamatida hosil qilish mumkin bo‘lmagan yechim nima deb ataladi

maxsus yechim

xususiy yechim

umumiy yechim

maxsus nuqta

№54.

Qiyinlik darajasi-3

Maxsus yechimni topish formulasini topping

$$\begin{cases} \Phi(x, y, c) = 0 \\ \Phi_c(x, y, c) = 0 \end{cases}$$

$$\begin{cases} \Phi(x, y, y', c) = 0 \\ \Phi_c(x, y, y', c) = 0 \end{cases}$$

$$\begin{cases} \Phi(x, y) = 0 \\ \Phi_c(x, y) = 0 \end{cases}$$

$$\begin{cases} \Phi(x, y', c) = 0 \\ \Phi_c(x, y', c) = 0 \end{cases}$$

№ 55.

Qiyinlik darajasi-2

Klero tenglamasini aniqlang

$$y = xy' + \psi(y')$$

$$y = xy^2 + \psi(y')$$

$$y = x + \psi(y')$$

$$y = x(y')^{-1} + \psi(y')$$

№ 56.

Qiyinlik darajasi-3

Klero tenglamasini umumiy yechimi ko‘rinishini aniqlang

$$y = cx + \psi(c)$$

$$y = x + \psi(c)$$

$$y = x(c)^{-1} + \psi(c)$$

$$y = c^2x + \psi(c)$$

№ 57.

Qiyinlik darajasi-3

Klero tenglamasini maxsus yechimini aniqlang

$$y = xp_0(x) + \psi(p_0(x))$$

$$x = y\varphi(y') + \psi(y')$$

$$x' = y\varphi(y) + \psi(y)$$

$$y = x'\varphi(y) + \psi(y')$$

№ 58.

Qiyinlik darajasi-3

Lagranj tenglamasining ko‘rinishini aniqlang

$$x = y\varphi(y') + \psi(y')$$

$$y = x\varphi(y') + \psi(y')$$

$$x' = y\varphi(y) + \psi(y)$$

$$y = y'\varphi(x) + \psi(x)$$

№ 59.

Qiyinlik darajasi-3

Lagranj tenglamasining maxsus yechimi ko‘rinishini aniqlang

$$y = x\varphi(p_0) + \psi(p_0)$$

$$y' = x\varphi(p_0) + \psi(p_0)$$

$$y = y'\varphi(p_0) + \psi(p_0)$$

$$x = y'\varphi(p_0) + \psi(p_0)$$

№ 60.

Qiyinlik darajasi-3

Quyidagi tenglamaning maxsus yechimini toping: $y = x + y'^3$

$$y = x + 1$$

$$y = x + 3$$

$$y = x + 2$$

$$y = x + 4$$

№ 61.

Qiyinlik darajasi-1

Birinchi tartibli chiziqli tenglamada $Q(x)$ qanday bo'lsa, chiziqli bir jinsli tenglama deyiladi?

$$Q(x) = 0$$

$$Q(x) \neq 0$$

$$Q(x) = 1$$

$$Q(x) = x$$

№ 62.

Qiyinlik darajasi-3

Ushbu $y = Cx^3$ chiziqlar oilasi qaysi diffirensial tenglamaning yechimi?

$$*xy' = 3y$$

$$y = e^{xy} \frac{1}{y}$$

$$y' = 3y^{\frac{2}{3}}$$

$$y = xy'$$

№ 63.

Qiyinlik darajasi-3

$y' = ax^\alpha + by^\beta$ tenglama α va β ning qanday qiymatlarida $y = z^m$ almashtirish yordamida bir jinsli tenglamaga keltiriladi

$$\frac{1}{\beta} - \frac{1}{\alpha} = 1$$

$$\alpha + \beta = 1$$

$$-\frac{1}{\alpha} - \frac{1}{\beta} = 1$$

$$\alpha - \beta = 1$$

№ 64.

Qiyinlik darajasi-3

Agary1 vay2 – birinchitartiblichiziqlitenglaningikkaturliyechimlaribo'lsa, tenglamaningumumiyyechimiy1 vay2 yordamidaqandayyoziladi?

$$y = y_1 + c(y_2 - y_1)$$

$$y = y_1 \cdot y_2$$

$$y = \frac{y_1}{y_2}$$

Yozib bo'lmaydi

№ 65.

Qiyinlik darajasi-2

Quyidagi funksiyalardan qaysi

$$y^2 dx - (xy + x^3) dy = 0$$
 tenglama uchun integrallovchi ko'paytuvchi bo'ladi?

$\frac{1}{x^3}$

$\frac{1}{y}$

$\frac{1}{x^2}$

$\frac{1}{y^2}$

№ 66.

Qiyinlik darajasi-2

Quyidagi funksiyalardan qaysi

$y(x+y)dx + (xy+1)dy = 0$ tenglama uchun integrallovchi ko‘paytuvchi bo‘ladi?

$\frac{1}{y}$

$\frac{1}{x^2}$

$\frac{1}{x^3}$

$\frac{1}{y^2}$

№ 67.

Qiyinlik darajasi-3

$e^{-x} \frac{1}{y}$ funksiya quyidagi tenglamalardan qaysi biri uchun integrallovchi ko‘paytuvchi bo‘ladi?

$y^2 dx + (e^x - y) dy = 0$

$e^{-x} xy dx - (x^2 + y^2) dy = 0$

$e^{-x} dx -$

$- (2y + xe^{-x}) dy = 0$

Hamma javoblar noto‘g‘ri

№ 68.

Qiyinlik darajasi-3

Agar $M(x, y)dx + N(x, y)dy = 0$ tenglamada $M(x, y)$ va $N(x, y)$ m-tartibli bir jinsli funksiyalar bo‘lsa, u holda integrallovchi ko‘paytuvchi qanaqa ko‘rinishda bo‘ladi?

$m(x, y) = [xM + yN]^{-1}$

$m(x, y) = xM + yN$

$m(x, y) = \frac{x + y}{M + N}$

$m(x, y) = [xN + yM]^{-1}$

№ 69.

Qiyinlik darajasi-3

Shunday egri chiziqlarni topingki, uning har bir nuqtasiga o'tkazilgan urinma koordinata o'qlari bilan birgalikda yuzasi $2a^2$ ga teng bo'lган uchburchak hosil qilsin

$$xy = \pm a^2$$

$$y = \frac{1}{a^2}$$

$$xy = \pm 2a^2$$

$$y = a^4$$

№ 70.

Qiyinlik darajasi-3

Differensial tenglamalar tuzish yo'li bilan $y = cx^2$ chiziqlar oilasiga ortogonal chiziqlar oilasini toping

$$2y^2 + x^2 = c$$

$$y = cx^{-2}$$

$$y = -cx^2$$

$$y^2 + 2x = c$$

№71.

Qiyinlik darajasi-2

Quyidagi tenglamalardan qaysi biri bir jinsli tenglama emas?

$$(x^2 + y)dx - xdy = 0$$

$$xy' \cos \frac{y}{x} = y \cos \frac{y}{x} - x$$

$$\begin{aligned} & (2x^3 - xy^2)dx + \dots \\ & + (2y^3 - x^2y)dy = 0 \end{aligned}$$

$$y' = \frac{y^3}{2(xy^2 - x^3)}$$

№72.

Qiyinlik darajasi-2

$y' + P(x)y = Q(x)$ tenglamani integrallovchi ko'paytuvchi qanaqa ko'rinishda bo'ladi?

$$e^{\int p(x)dx}$$

$$e^{-\int p(x)dx}$$

$$\int p(x)dx$$

$$e^{\int p^2(x)dx}$$

№73.

Qiyinlik darajasi-3

Agar chiziqli differensial tenglama Klero tenglamasi bo'lsa, uning integral chiziqlari oilasi nimadan iborat bo'ladi?
To‘g‘ri chiziqlar dastasi
Giperbolalar
Aylanalar
Parabolalar

№74.

Qiyinlik darajasi-3

Berilgan tenglamaning tipini aniqlang: $y \sin x + y' \cos x = 1$

Chiziqli

Bernulli

o‘zgaruvchilari ajraladigan

Rikkati

№75.

Qiyinlik darajasi-3

$y' = \frac{3y - x^2}{x}$ tenglamani yechimini aniqlang

$y = cx^3 + x^2$

$y = cx + x^2$

$y = cxe^x$

$y = cx^2 + 2x^3$

№76.

Qiyinlik darajasi-3

$(2xy + 3x^2)dx + x^2dy = 0$ tenglamaning umumiy yechimini toping

$x^2y + x^3 = c$

$x^2y + y^3 = c$

$x^3y - x = c$

$\frac{x}{y} + x^3 = c$

№77.

Qiyinlik darajasi-3

Qanday almashtirish yordamida $y' = y^2 - \frac{2}{x^2}$ tenglamani bir jinsli tenglamaga keltirish mumkin?

$y = zx^{-1}$

$y = zx$

$z = y^2$

$z = \sqrt{y}$

№78.

Qiyinlik darajasi-3

Quyidagi tenglama qaysi tipga tegishli $(x \cos y - y^2)dy + (\sin y + x)dx = 0$

to‘la differensial

Bernulli

x ga nisbatan chiziqli

hosilaga nisbatan yechilmagan

№79.

Qiyinlik darajasi-2

Boshlang‘ich shartli masala nechta yechimga ega $y' = xy - y^3$, $y(0) = 0$

1

2

3

yechimga ega emas

№80.

Qiyinlik darajasi-2

Tenglamaning tipini aniqlang $xy' = y - xe^x$

Bir jinsli

Bernulli

Chiziqli

to‘la differensial

№81.

Qiyinlik darajasi-3

Ushbu $y' = \frac{y}{3x - y^2}$ tenglamaning yechimini toping

$x = cy^3 + y^2$

$y = 3x^3 + cx^2$

$y = cx^3 + x^2$

$y = cx + x^2$

№82.

Qiyinlik darajasi-2

Ushbu $y = cx^2$ chiziqlar sinfning differensial tenglamasini toping

$xy' = 2y$

$y' = \frac{2}{x}y$

$y'x = 3y$

$y'x^2 = y^2$

№83.

Qiyinlik darajasi-1

Qaysi shart bajarilganda $y' = a(x)y^2 + b(x)y + c(x)$ Rikkati tenglamasi Bernulli tenglamasiga aylanadi?

$c(x) = 0$

$b(x) = 0$

$a(x) = 0$

$a(x) = 1$

№84.

Qiyinlik darajasi-1

Qaysi shart bajarilganda $y' = a(x)y^2 + b(x)y + c(x)$ Rikkati tenglamasi chiziqli tenglamaga aylanadi?

$a(x) = 0$

$b(x) = 0$

$c(x) = 0$

$a(x) = 1$

№85.

Qiyinlik darajasi-1

$y' = f(y) \cdot g(y)$ differensial tenglama tipini toping

O‘zgaruvchilari ajraladigan differensial tenglama

Chiziqli tenglama

Bernulli tenglamasi

Rikatti tenglamasi

№86.

Qiyinlik darajasi-1

$x' = \frac{x}{y}$ ko‘rinishga keltiruvchi differensial tenglama qanday differensial tenglama deb ataladi?

O‘zgaruvchilari ajraladigan

Chiziqli tenglamalar

Bir jinsli tenglamalar

Bernulli tenglamasi

№87.

Qiyinlik darajasi-2

$y' = p(x)y$ differensial tenglamaning umumiy yechim formulasini toping

$y = Ce^{\int p(x)dx}$

$y = \varphi(x)$

$y = e^{\int p(x)dx}$

$y = C$

№88.

Qiyinlik darajasi-2

$\varphi(x, y, C_1, C_2) = 0$ egri chiziqlar oilasining differensial tenglamasini tuzish uchun bu tenglamani necha marta diffrensiallash kerak ?

2

3

1

0

№89.

Qiyinlik darajasi-2

Agar $M(x, y)dx + N(x, y)dy = 0$ differensial tenglamada $M(x, y)$ va $N(x, y)$ bir xil tartibdagи bir jinsli funksiyalar bo'lsa tenglama turini toping?

Bir jinsli tenglamalar

O'zgaruvchilari ajraladigan tenglama

Chiziqli tenglamalar

Tuliq differensialli tenglama

№90.

Qiyinlik darajasi-1

$x' + g(t)x = f(t)x^k$ tenglamani turini aniqlang

Bernulli tenglamasi

Chiziqli tenglama

O'zgaruvchilari ajraladigan tenglama

Klero tenglamasi

№91.

Qiyinlik darajasi-1

$y' = f(x, y)$ differensial tenglama $y(x_0) = y_0$ shart bilan yechimini topishga qanday masala deyiladi?

Koshi masalasi

Chegaraviy masala

Umumi yechimni topish

Maxsus yechimni topish

№92.

Qiyinlik darajasi-1

$kx^2 + y^2 + xy' = 0$ differensial tenglamani tartibini toping

1

3

2

0

№93.

Qiyinlik darajasi-2

$y' \cdot e^{x^2} = x \cdot e^{x^2} - y$ tenglama turini aniqlang

Bir jinsli bulmagan chiziqli differensial tenglama

Bernulli tenglamasi

Klero tenglamasi

O'zgaruvchilari ajraladigan tenglama

№94.

Qiyinlik darajasi-2

Qaysi shart bajarilganda $M(t, x)dt + N(t, x)dx = 0$ tenglama to'liq differensialli bo'ladi

$$\frac{\partial M}{\partial x} = \frac{\partial N}{\partial t}$$

$$M(t, x) = x^2$$

$$N(t, x) = y$$

$$M(t, x) = N(t, x)$$

№95.

Qiyinlik darajasi-2

$y' = a(x) \cdot y^2 + b(x) \cdot y + c(x)$ Rikatti tenglamasini bitta xususiy yechimi berilgan bo'lsa, uni qanday turdag'i tenglamaga keltirish mumkin?

Bernulli tenglamasiga

O'zgaruvchilari ajraladigan tenglamaga

Chiziqli tenglamalarga

Rikatti tenglamasiga

№96.

Qiyinlik darajasi-2

Ushbu $x' + p(t)x = f(t)x^m$ Bernulli tenglamasini m ning qanday qiymatida chiziqli differensial tenglama bo'ladi?

0

1

2

-1

№97.

Qiyinlik darajasi-2

Ushbu $\frac{dx}{dt} = p(t) \cdot x + f(t) \cdot x^m$ Bernulli tenglamasi m ning qaysi qiymatida chiziqli bir jinsli differensial tenglamaga aylanadi?

1

2

3

0

№98.

Qiyinlik darajasi-1

Birinchi tartibli chiziqli differensial tenglamaning umumiy yechimi nechta ixtiyoriy o'zgarmaslarga bog'liq?

1

2

3

0

№99.

Qiyinlik darajasi-1

Birinchi tartibli chiziqli bir jinsli differensial tenglamaning umumiy yechim strukturasi qaysi?

$y = c \cdot \varphi(x)$

$y = g(x)$

$y = 1$

$y = c \cdot \varphi(x) + g(x)$

№100.

Qiyinlik darajasi-1

Birinchi tartibli chiziqli bir jinsli bo'lmasligi differensial tenglamaning umumiy yechim strukturasi qaysi?

$$y = c \cdot \varphi(x) + g(x)$$

$$y = g(x)$$

$$y = 1$$

$$y = c \cdot \varphi(x)$$

№101.

Qiyinlik darajasi-3

$y' + y = 7$ differensial tenglamaning xususiy yechimini toping

7

$7x$

e^x

0

№102.

Qiyinlik darajasi-1

Birinchi tartibli differensial tenglamaning umumiy yechimi formulasini toping

$$y = \varphi(x, C)$$

$$f(x, C) = 0$$

$$y = y(x)$$

$$x = x(y)$$

№103.

Qiyinlik darajasi-2

Birinchi tartibli $y' = \varphi\left(\frac{y}{x}\right)$ bir jinsli tenglama $y = xz$ almashtirish natijasida, qanday turdagı tenglamaga kelishini toping

O‘zgaruvchilari ajraladigan tenglamaga

Chiziqli tenglama

Bernulli tenglamasiga

To‘liq differensial tenglamaga

№104.

Qiyinlik darajasi-1

$y = xy' + \psi(y')$ differensial tenglamani turini aniqlang

Klero tenglamasi

Chiziqli tenglamalar

O‘zgaruvchilari ajraladigan tenglama

Lagranj tenglamasi

№105.

Qiyinlik darajasi-1

$y = \varphi(y')x + \psi(y')$ differensial tenglamani turini aniqlang

Lagranj tenglamasi

Chiziqli tenglamalar

O‘zgaruvchilari ajraladigan tenglama

Klero tenglamasi

№106.

Qiyinlik darajasi-2

Xarakteristik tenglamasi $\lambda^2 + 3\lambda + 2 = 0$ bo‘lgan o‘zgarmas koeffitsientli chiziqli bir jinsli tenglamani toping

$$y''+3y'+2y=0$$

$$y''+y'=0$$

$$y''+3y'=0$$

$$y''=0$$

№107.

Qiyinlik darajasi-2

$F(x, y^{(k)}, y^{(k+1)} \dots y^{(n)}) = 0$ tenglamaning tartibini pasaytirish uchun qanday almashtirish bajariladi?

$$y^{(k)} = z$$

$$y^{(k-1)} = z$$

$$y' = z$$

$$y^{(n)} = z$$

№108.

Qiyinlik darajasi-2

$F(y, y', y'', \dots, y^{(n)}) = 0 \dots (n \geq 2)$ tenglamaning tartibini pasaytirish qanday almashtirish bajariladi?

$$y' = p(y)$$

$$y^{(n+1)} = z$$

$$y^{(n)} = z$$

$$y'p = z$$

№109.

Qiyinlik darajasi-3

$F(x, y, y', \dots, y^{(n)}) = 0$ tenglamada qaysialmashtirish bajarilsa, y va uning hosilalariga nisbatan bir jinsli deyiladi

Agar y ning o‘rniga ky , y' ning o‘rniga ky' , va h.k. $y^{(n)}$ ning o‘rniga $ky^{(n)}$ qo‘yilganda tenglama o‘zgarmasa

Agar y va uning bir necha tartibli xosilalari qatnashmasa

Agar x argument qatnashmasa

Agar x ning o‘rniga kx , y' ning o‘rniga ky' , va h.k. $y^{(n)}$ ning o‘rniga $ky^{(n)}$ qo‘yilganda tenglama o‘zgarmasa

№110.

Qiyinlik darajasi-3

$$a_0 x^n y^{(n)} + a_1 x^{n-1} y^{(n-1)} + \dots$$

$$\dots + a_{n-1} y' + a_n y = 0$$

(bu yerda a_i – o‘zgarmas son) Eyler tenglamasining harakteristik tenglamasini yozing

$$a_0 \lambda(\lambda-1)(\lambda-2)\dots(\lambda-n+1) + a_1 \lambda(\lambda-1)(\lambda-2)\dots(\lambda-n+2) + \dots + a_{n-1} \lambda + a_n = 0$$

$$a_0 \lambda^{n-1} + a_1 \lambda^{n-2} + \dots + a_{n-1} = 0$$

$$a_0 \lambda^n + a_1 \lambda^{n-1} + \dots + a_{n-1} \lambda + a_n = 0$$

$$a_0 \lambda(\lambda-1) + a_1 (\lambda-1)(\lambda-2) + \dots + a_{n-1} (\lambda-n) + a_n = 0$$

№111.

Qiyinlik darajasi-3

$$a_0(x)y'' + a_1(x)y' +$$

+ $a_2(x)y = f(x)$ $x_0 \leq x \leq x_1$ tenglama uchun umumiyl chegaraviy masalani yozing

$$\alpha y'(x_0) + \beta y(x_0) = 0,$$

$$\gamma y'(x_1) + \delta y(x_1) = 0$$

$$J'(x_0) = Y_0$$

$$y(x_1) = y_1$$

$$y(x_0) = y$$

№112.

Qiyinlik darajasi-3

$a_0(x)y'' + a_1(x)y' + a_2(x)y = f(x)$ tenglama uchun umumiyl chegaraviy masalaning Grin funksiyasi ko‘rinishini yozing ($y_1(x)$ va $y_2(x)$ – tenglamani yechimlari)

$$G(x, s) = \begin{cases} a(s)y_1(x), & x_0 \leq x \leq s \\ b(s)y_2(x), & s \leq x \leq x_1 \end{cases}$$

$$G(x, s) = \begin{cases} a(s) + y_1(x), & x_0 \leq x \leq s \\ b(s)y_2(x), & s \leq x \leq x_1 \end{cases}$$

$$G(x, s) = \begin{cases} \frac{a(s)}{y_1(x)}, & x_0 \leq x \leq s \\ \frac{b(s)}{y_2(x)}, & s \leq x \leq x_1 \end{cases}$$

$$G(x, s) = \begin{cases} a(s)y_1(x), & x_0 \leq x \leq s \\ b(s)y_2(x), & s \leq x \leq x_1 \end{cases}$$

№113.

Qiyinlik darajasi-3

$y'' = f(x)$, $y(0) = 0$, $y(1) = 0$ chegaraviy masalaning Grin funksiyasini ko‘rosating

$$G(x, s) = \begin{cases} (s - 1)x \\ s(x - 1) \end{cases}$$

$$0 \leq x \leq s$$

$$s \leq x \leq 1$$

$$G(x, s) = \begin{cases} s^2 x \\ s(x + 1) \end{cases},$$

$$0 \leq x \leq s$$

$$s \leq x \leq 1$$

$$G(x, s) = \begin{cases} (s^2 - 1)x \\ s(x^2 - 1) \end{cases},$$

$$0 \leq x \leq s$$

$$s \leq x \leq 1$$

$$G(x, s) = \begin{cases} (s + 1)x \\ s(x + 1) \end{cases},$$

$$0 \leq x \leq s$$

$$s \leq x \leq 1$$

№114.

Qiyinlik darajasi-3

$$G(x, s) = \begin{cases} SinsCosx & 0 \leq x \leq s \\ SinxCoss & s \leq x \leq \pi \end{cases}$$

ko‘rinishdagi Grin funksiyasi qaysi chegaraviy masalaga tegishli?

$$y'' + y = f(x), y'(0) = 0, y(\pi) = 0$$

$$y'' + f(x), y(0) = 0, y(1) = 0$$

$$y'' - y = f(x), y'(0) = 0, y(1) = 0$$

$$\begin{aligned} y'' + y &= f(x), y'(0) = y(\pi), \\ y(1) &= 0 \end{aligned}$$

№115.

Qiyinlik darajasi-3

$y'' = \lambda y$, $y(0) = 0$, $y(l) = 0$ masalaning hos qiymati va hos funksiyalarini toping

$$\lambda_k = -\left(\frac{\pi k}{2}\right)^2,$$

$$y_k(x) = \sin \frac{\pi k}{e} x$$

$$k = 1, 2, 3$$

$$\lambda_k = \left(\frac{\pi k}{2}\right)^2,$$

$$y_k(x) = \cos \frac{\pi k}{e} x$$

$$\lambda_k = \left(\frac{2\pi}{3} k\right)^2,$$

$$y_k(x) = \sin \frac{\pi k}{e} x$$

$$\lambda_k = -\left(\frac{\pi k}{2}\right)^2,$$

$$y_k = \cos \frac{\pi k}{e} x$$

№116.

Qiyinlik darajasi-3

Agar o‘zgarmas koeffitsentli yuqori tartibli chiziqli tenglamaning o‘ng tomoni $P_m(x)e^{\gamma x}$, $(P_m(x) - ko'pxad)$ ko‘rinishida bo‘lsa, bitta hususiy yechim qaysi ko‘rinishda bo‘ladi? (Hamma javoblarda s – karralilikni bildiradi)

$$y_1 = x^s Q_m(x) e^{\gamma x}$$

$$y_1 = x^{s-1} Q_m(x) e^{\gamma x}$$

$$y_1 = x^{s+1} Q_m(x) e^{\gamma x}$$

$$y_1 = Q_{m+s}(x) e^{\gamma x}$$

№117.

Qiyinlik darajasi-2

$$a_0 x^n a y^{(n)} + a_1 x^{n-1} y^{(n-1)} + \dots$$

$\dots + a_{n-1} x y' + a_n y = f(x)$ ko‘rinishidagi Eyler tenglamasini o‘zgarmas koeffitsientli chiziqli tenglamaga keltirish uchun qanday almashtirish bajariladi? ($x > 0$ deb faraz qiling)

$$x = e^t$$

$$x = e^{-t}$$

$$x = \ln|t|$$

$$x = \ln|t| + e^t$$

№118.

Qiyinlik darajasi-3

$a_0(x)y'' + a_1(x)y' + a_2(x)y = 0$ tenglamani yechishda ushbu Ostrogradskiy -Liuvill formulasi

qo'llaniladi: $\begin{vmatrix} y_1 & y_2 \\ y'_1 & y'_2 \end{vmatrix} = C e^{-\int p(x)dx}$

bu formuladagi $p(x)$ deb nimaga teng?

$$p(x) = \frac{a_1(x)}{a_0(x)}$$

$$p(x) = -\frac{a_1(x)}{a_0(x)}$$

$$p(x) = -\frac{a_0(x)}{a_1(x)}$$

$$p(x) = a_0(x)$$

№119 .

Qiyinlik darajasi-2

Quyidagi funksiyalardan qaysi biri chiziqli bog'liq?

$$6x + 9, 8x + 12$$

$$x + 2, x - 2$$

$$\sin x, \cos x$$

$$x^2 + 2x, 3x^2 - 1, x + 4$$

№120.

Qiyinlik darajasi-2

$(2x+1)y'' + 4xy' - 4y = 0$ tenglamaning bitta xususiy yechimini toping

$$e^{-2x}$$

$$e^{-2x^2}$$

$$e^x$$

$$x^3$$

№121.

Qiyinlik darajasi-3

Ushbu $(x-a)^2 + by^2 = 1$ chiziqlar oilasi qaysi diffirensial tenglamaning yechimi?

$$(yy'' + y'^2)^2 = -y^3 y''$$

$$2yy'' + y'^2 = \sqrt{yy''}$$

$$yy'' + y'^2 = 0$$

№122.

Qiyinlik darajasi-3

Yechimni $y_1 = ax + b$ ko‘rinishda izlab, $x^2 y'' \ln x - xy' + y = 0$ tenglamaning bitta xususiy yechimini toping

$$y_1 = x$$

$$y_1 = 2x + 1$$

$$y_1 = 2x - 1$$

$$y_1 = x + 2$$

№123.

Qiyinlik darajasi-3

$y'' + 4y' + 3y = 0$ tenglamaning umumiy yechimini yozing

$$y = c_1 e^{-x} + c_2 e^{-3x}$$

$$y = c_1 e^{-x} + c_2 e^{3x}$$

$$y = c_1 e^x + c_2 e^{-3x}$$

$$y = c_1 e^x + c_2 e^{3x}$$

№124.

Qiyinlik darajasi-3

$y'' + 2y' + 10y = 0$ tenglamaning umumiy yechimini yozing

$$y = e^{-x} (C_1 \cos 3x + C_2 \sin 3x)$$

$$y = e^{3x} (C_1 \cos x + C_2 \sin x)$$

$$y = e^x (C_1 \cos 3x + C_2 \sin 3x)$$

$$y = e^{2x} (c_1 \cos 2x + c_2 \sin 2x)$$

№125.

Qiyinlik darajasi-3

$$y'' - 2y' + y = 0 \text{ tenglamaning umumiy yechimini yozing}$$

$$y = (c_1 + c_2 x)e^x$$

$$y = (c_1 + c_2 x)e^x$$

$$y = (c_1 + c_2 x^2)e^x$$

$$y = c_1 e^x + c_2 e^{-x}$$

№126.

Qiyinlik darajasi-3

$$y'' - 2y' - 3y = x^2 e^x \text{ tenglamaning bitta xususiy uchimi qanday ko'rnishda izlanadi}$$

$$y = x(Ax^2 + Bx + c)e^x$$

$$y = (Ax^2 + Bx + c)e^x$$

$$y = x^2(Ax + B)e^x$$

$$y = Ax^2 e^x$$

№127.

Qiyinlik darajasi-3

$$y'' - 4y' + 8y = \sin 2x \text{ tenglamaning bitta xususiy yechimi qaysi ko'rnishda bo'ladi?}$$

$$y = A\sin 2x + B\cos 2x$$

$$y = (Ax + B)\sin 2x + (Cx + D)\cos 2x$$

$$y = Ax^2 \sin 2x + Bx \cos 2x$$

$$y = x(A\sin 2x + B\cos 2x)$$

№128.

Qiyinlik darajasi-3

a va bning qanday qiymatlarida $y'' + ay' + by = 0$ tenglamaning yechimlari $-\infty < x < \infty$ da chegaralangan bo'ladi?

$$a = 0$$

$$b > 0$$

$$a = 0$$

$$b < 0$$

$$a > 0$$

$$b > 0$$

$$a < 0$$

$$b < 0$$

№129.

Qiyinlik darajasi-3

a va b ning qanday qiymatlarida $y'' + ay' + by = 0$ tenglamaning hamma yechimlari $x \rightarrow +\infty$ da nolga intiladi?

$a > 0$

$b > 0$

$a = 0$

$b < 0$

$a = 0$

$b > 0$

$a < 0$

$b < 0$

№130.

Qiyinlik darajasi-3

$x^3 y''' + xy' - y = 0$ Eyler tenglamasini yeching

$$y = x(c_1 + c_2 \ln|x| + c_3 \ln^2|x|)$$

$$y = c_1 + c_2 \ln|x| + c_3 \ln^2|x|$$

$$y = x^2(c_1 + c_2 \ln|x| + c_3 \ln^2|x|)$$

$$y = c_1 + c_2 x + c_3 x^2$$

№131.

Qiyinlik darajasi-3

$y''' - y' = 3(2 - x^2)$ tenglamani bitta xususiy yechimi qanday ko‘rinishda izlanadi?

$$y = (Ax^2 + Bx + C)x$$

$$y = (Ax^2 + Bx + C)x^2$$

$$y = (Ax^2 + Bx + C)e^x$$

$$y = (Ax + B)e^x$$

№132.

Qiyinlik darajasi-3

Quyidagi tenglamalardan qaysi biri Eyler tenglamasi hisoblanadi?

$$x^2 y'' - 9xy' + 21y = 0$$

$$xy'' + y' + y = 0$$

$$x^2 y'' + xy' + \frac{1}{x} y = 0$$

$$xy'' - 9y' + 21xy = 0$$

№133.

Qiyinlik darajasi-3

$$y_1 \text{ va } y_2 = c_1 y_1 \int e^{-\int p(x)dx} \frac{dx}{y_1^2}$$

funksiyalar qaysi tenglamaning ikkita chiziqli erkli yechimlari bo‘ladi?

$$\begin{aligned}y'' + y' \cdot p(x) + yQ(x) &= 0 \\y'' - y' \cdot p(x) + y^2 Q(x) &= 0 \\y'' - y' p(x) + yQ(x) &= 0 \\y'' + y' p^2(x) + yQ(x) &= 0\end{aligned}$$

№134.

Qiyinlik darajasi-3

$$\begin{aligned}y'' + 16y &= 0 \text{ tenglamaning umumiy yechimini toping} \\y &= c_1 \cos 4x + c_2 \sin 4x \\y &= ce^{-16x} \\y &= c_1 e^{4x} + c_2 e^{-4x} \\y &= c_1 e^{-4x} \cos 4x + c_2 e^{-4x} \sin 4x\end{aligned}$$

№135.

Qiyinlik darajasi-3

$$\begin{aligned}y'' + 4y &= 0 \text{ tenglamaning umumiy yechimini toping} \\y &= c_1 \cos 2x + c_2 \sin 2x \\y &= c_1 e^{2x} + c_2 e^{-2x} \\y &= ce^{-4x} \\y &= c_1 \cos 2x + c_2 x \cos 2x\end{aligned}$$

№136.

Qiyinlik darajasi-2

$$\begin{aligned}\text{Berilgan differensial tenglamaning xususiy yechimini aniqlang: } y''' - y'' &= 5x^2 + 4 \\y_1 &= \frac{5}{12}x^4 - \frac{5x^3}{3} + 7x^2 \\y_1 &= 5x^4 + 4x^2 \\y_1 &= 5x^2 + 4 \\y_1 &= ax^2 + bx + c\end{aligned}$$

№137.

Qiyinlik darajasi-2

$$\begin{aligned}\text{Berilgan tenglamaning tipini aniqlang: } (x + 3x^2)y' + xy &= 0 \\o'zgaruvchilari ajraladigan \\to'la differensial \\Bernulli \\y \text{ ga nisbatan chiziqli}\end{aligned}$$

№138.

Qiyinlik darajasi-3

$$\begin{aligned}\text{Xususiy yechimi } y_1 = xe^x \text{ bo'lgan chiziqli o'zgarmas koeffitsientli differensial tenglamani ko'rsating} \\y'' - 2y' + y = 0 \\y'' - 2y' - 3y = 0 \\y' - y = 0\end{aligned}$$

$$y'' + 2y' + y = 0$$

№128.

Qiyinlik darajasi-3

Xususiy yechimi $y_1 = x^2 e^{-x}$ bo‘lgan chiziqli o‘zgarmas koeffitsientli differensial tenglamani ko‘rsating

$$y''' + 3y'' + 3y' + y = 0$$

$$y''' - y' = 0$$

$$y'' - y = 0$$

$$y''' + 3y'' = 0$$

№129.

Qiyinlik darajasi-3

Xususiy yechimni aniqmas koeffitsientlar usuli bilan toping $y'' - 5y' + 4y = 4x^2 e^{2x}$

$$y = (ax^2 + bx + c)e^{2x}$$

$$y = x(ax^2 + bx + c)e^{2x}$$

$$y = x(ax + b)e^{2x}$$

$$y = ax^2 e^{2x}$$

№130.

Qiyinlik darajasi-2

$$y^{(n)} + a_1(x, y) \cdot y^{(n-1)} + \dots + a_{n-1}(x, y) y' + a_n(x, y) = 0 \text{ tenglama tartibini aniqlang}$$

1

2

3

n

№131.

Qiyinlik darajasi-3

$$y''' + a_1(x, y) \cdot y'' + \dots + a_n(x, y) = 0 \quad \text{differensial tenglamani turini aniqlang}$$

Birinchi tartibli *n* darajali

Chiziqli tenglamalar

Bernulli tenglamasiga

O‘zgaruvchilari ajraladigan tenglama

№132.

Qiyinlik darajasi-3

Fundamental yechimlar sistemasi $\cos x$ va $\sin x$ bo‘lgan differensial tenglamani toping

$$y'' + y = 0$$

$$y'' - y' = 0$$

$$y''' + y' = 0$$

$$y'' = 0$$

№133.

Qiyinlik darajasi-3

$y''+3y'+2y=0$ tenglamaning xarakteristik sonlarini toping

- 2, -1
- 2, 1
- 2
- 1

№134.

Qiyinlik darajasi-3

$y''+y'=0$ tenglamaning xususiy yechimini toping

- e^{-x}
- x
- x^2
- e^x

№135.

Qiyinlik darajasi-3

$y''+3y'+2y=6$ tenglamaning xususiy yechimini toping

- 3
- 0
- x
- x^2

№136.

Qiyinlik darajasi-3

- n
- 2
- 1
- 0

№137.

Qiyinlik darajasi-3

n – tartibli differensialli tenglamalarning umumiylarini yechimi nechta ixtiyorli o‘zgarmasga bog‘liq

Quyidagi differensial tenglamaning $xy''+y'^3=x^4$ tartibini toping

- 2
- 4
- 0
- 3

№138.

Qiyinlik darajasi-3

Ushbu $x^2y''-2xy'+2y=0$ Eyler tenglamasining yechimlar fundamental sistemasini toping

- x, x^2
- $1, x$
- x, x^3
- $2, x^2$

№139.

Qiyinlik darajasi-3

Quyidagi $ay''+3xy'+5y = f(x)$ Eyler tenglamasi bo‘lishi uchun a nimaga teng bo‘lishi kerak?

x²

x

1

0

№140.**Qiyinlik darajasi-3**

Agar e^{2ix} kompleks funksiya $y''+4y = 0$ tenglamaning yechimi bo‘lsa, unda uning haqiqiy yechimlari qaysi funksiyalar bo‘ladi?

sin 2x, cos 2x

2, cos x

cos x, sin 2x

cos x, sin x

№141.**Qiyinlik darajasi-3**

O‘zgarmas koefitsientli ikkinchi tartibli chiziqli bir jinsli differensial tenglamaning xususiy yechimi $e^{2x} \cos 3x$, $e^{2x} \sin 3x$ bu tenglamaning xarakteristik sonlarini toping

2 ± 3i

2,3

1 ± 2i

3 ± 2i

№142.**Qiyinlik darajasi-2** $x^2 y''+a_1 xy'+a_2 xy=0$ tenglama turini toping

Eylerning ikkinchi tartibli bir jinsl tenglamasi

Bernulli tenglamasi

O‘zgarmas koefitsientli chiziqli tenglama

Eylerning bir jinsli

№143.**Qiyinlik darajasi-2**

Ikkinci tartibli chiziqli bir jinsli differensial tenglamaning yechimlar fundamental sistemasi y_1 va y_2 bo‘lsa, umumiy yechim formulasini toping

 $y = c_1 y_1 + c_2 y_2$ $y = \varphi(x, c_1, c_2)$ $\varphi(x, y, c_1, c_2) = 0$ $y = \varphi(x, c)$ **№144.****Qiyinlik darajasi-3** $L[y] = y''+3y'-4y$ bo‘lsa, $L[e^x]$ ni toping

0

8

1

№145.

Qiyinlik darajasi-2

Xarakteristik soni 2 va 3 bo‘lgan, differensial tenglamani toping

$$y'' - 5y' + 6y = 0$$

$$y'' + y' + y = 0$$

$$y'' + y = 0$$

$$y''' = 0$$

№146.

Qiyinlik darajasi- 2

2-chi tartibli differensial tenglamaning umumiy yechimi nechta ixtiyoriy o‘zgarmaslarga bog‘liq?

2

1

3

n

№147.

Qiyinlik darajasi-3

$L[y] = y'' + 3y'$ bo‘lsa, $L[e^x]$ ni toping

$$4e^x$$

$$e^{2x}$$

$$3e^x$$

4

№148.

Qiyinlik darajasi-3

n –tartibli differensiali tenglamaning oshkormas ko‘rinishdagi umumiy yechimini toping

$$\varphi(x, y, c_1, \dots, c_n) = 0$$

$$y = \varphi(x, c)$$

$$\varphi(x, y) = 0$$

$$y = y(x)$$

№149.

Qiyinlik darajasi-3

n –tartibli differensial tenglamaning parametr ko‘rinishdagi umumiy yechimini toping

$$x = x(t),$$

$$y = y(t, c_1, c_2, \dots, c_n)$$

$$y = \varphi(x, c)$$

$$\varphi(x, y) = 0$$

$$x \varphi(x, y) = 0$$

№150.

Qiyinlik darajasi-3

$y'' + y = 0$ differensial tenglamaning yechimlarining fundamental sistemasini toping

$$\sin x, \cos x$$

e^x , e^{-x}

$\cos x$, $\sin 2x$

e^x

№151.

Qiyinlik darajasi-3

$x^k y'' + axy' + by = 0$ tenglama k ning qiymatida Eyler tenglamasi bo‘ladi

2

1

3

5

№152.

Qiyinlik darajasi-3

$L[y] = y'' + y$ bo‘lsa $L[\cos x]$ ni toping

0

$\cos 2x$

2

$\sin 2x$

№153.

Qiyinlik darajasi-3

1, x funksiyalarning Vronskiy determinantini toping.

1

0

-1

x

№154.

Qiyinlik darajasi-2

$F(x, y^{(k)}) = 0$ differensial tenglama yuqori hosilaga nisbatan yechiladigan bo‘lsa integrallash usulini toping:

k - marta ketma-ket integrallab

$x = y^{(k)}$

To‘g‘ri javob yo‘q

$y' = z$

№155.

Qiyinlik darajasi-2

$F(y, y', y'', \dots, y^{(n)}) = 0$ tenglama tartibi $y' = p(y)$ almashtirish orqali necha birlikga pasaytiriladi.

1

0

2

3

№156.

Qiyinlik darajasi-3

$\sin x, \cos x$ funksiyalarining Vronskiy determinantini toping.

- | |
|-------|
| -1 |
| 1 |
| 0 |
| cos2x |

№157.

Qiyinlik darajasi-3

$y = x^3 + C_1x + C_2$ oilaning differensial tenglamasini toping.

$$y'' = 6x$$

$$y' = 3x^2 + C$$

$$y' = f(x, y)$$

$$y'' + y = 0$$

№158.

Qiyinlik darajasi-3

Agar $W[1, \operatorname{tg}x]$ bo‘lsa ,Vronskiy determinantining $W(0)$ qiymatini toping

- | |
|----|
| 1 |
| -1 |
| X |
| 2 |

№159.

Qiyinlik darajasi-3

Vronskiy determinantining $W(0)$ qiymatini toping, agar $W[e^x, e^{-x}]$ bo‘lsa:

- | |
|----|
| -2 |
| 1 |
| -1 |
| x |

№161.

Qiyinlik darajasi-2

$x = e^t$, $y = -e^t$ funksiya quyidagi tenglamalar sistemalaridan qaysi birining yechimi bo‘ladi?

$$\dot{x} = 2x + y$$

$$\dot{y} = 3x + 4y$$

$$\dot{x} = x + y$$

$$\dot{y} = 3y - 2x$$

$$\dot{x} = x - y$$

$$\dot{y} = y - 4x$$

$$\dot{x} = x - 3y$$

$$\dot{y} = 3x + y$$

№162.

Qiyinlik darajasi-3

$$\begin{cases} y' = \frac{x}{z} \\ z' = -\frac{x}{z} \end{cases}$$

nochiziqli sistemaning umumiy yechimini ko'rsating

$$y = c_2 e^{c_1 x^2}, z = \frac{1}{2c_1 c_2} e^{-c_1 x^2}$$

$$y = c_2 e^{c_1 x}, z = \frac{1}{2c_1 c_2} e^{-c_1 x^2}$$

$$y = c_1 c_2 e^{x^2}, z = \frac{1}{2c_1 c_2} e^{-c_1 x^2}$$

$$y = c_2 e^{x^2}, z = \frac{1}{2c_1 c_2} e^{c_1 x^2}$$

№163.

Qiyinlik darajasi-3

$$\begin{cases} \dot{x} = y + 2x \\ \dot{y} = 3x + 4y \end{cases} \text{ tenglamalar sistemasini yechimini ko'rsating}$$

$$x = c_1 e^t + c_2 e^{5t}$$

$$y = -c_1 e^t + 3c_2 e^{5t}$$

$$x = c_1 e^{-t} + c_2 e^{5t}$$

$$y = -c_1 e^{-t} + 3c_2 e^{-5t}$$

$$x = c_1 e^t + c_2 e^{5t}$$

$$y = c_1 e^t + 3c_2 e^{5t}$$

$$x = c_1 e^t + 2c_2 e^{5t}$$

$$y = -c_1 e^t + 3c_2 e^{5t}$$

№164.

Qiyinlik darajasi-3

$$\begin{cases} \ddot{x} = y \\ \ddot{y} = x \end{cases} \text{ tenglamalar sistemasining nechta chiziqli bog'liqsiz yechimlari bor?}$$

4 ta

3 ta

2 ta

1 ta

№165.

Qiyinlik darajasi-2

$\frac{dx}{dt} = f(t, x, y),$	normal sistemaning umumiy yechimi nechta ixtiyoriy o'zgarmaslarga bog'liq
$\frac{dy}{dt} = g(t, x, y),$	
2	
3	
1	
0	

№166.

Qiyinlik darajasi-2

Qaysi holda normal sistema avtonom (statsionar) sistema deyiladi

Agar sistemaning o'ng tamonidagi funksiyalar oshkor holda $t - ga$ bog'liq bo'lmasa

Agar normal funksiyalar soni ikkita bo'lsa

To'g'ri javob yo'q

Agar sistemaning ung tamonidagi funksialar $t - ga$ bog'liq bo'lsa

№167.

Qiyinlik darajasi-3

$\frac{dx}{dt} = f(t, x),$	sistemanı qaysi usul bilan integrallashini toping
$\frac{dy}{dt} = g(t, y),$	

Sistema tenglamalarini har biri alohida integrallash kerak

To'g'ri javob yo'q

Bitta ikkinchi tartibli tenglamaga keltirib integrallash kerak

Integrallovchi kombinatsiya tuzib integrallash kerak

№168.

Qiyinlik darajasi-3

$\frac{dx}{dt} = f(t, x),$	sistemanı qaysi usul bilan integrallashini toping
$\frac{dy}{dt} = g(t, x, y),$	

Sistema tenglamalarini ketma-ket integrallash kerak

Sistema tenglamalarini har biri alohida integrallash kerak

Bitta ikkinchi tartibli tenglama keltirib integrallash kerak

Integrallovchi kombinatsiya tuzib integrallash kerak

№169.

Qiyinlik darajasi-3

$$\frac{dx}{dt} = p(t)x + f(t),$$

Chiziqli tenglamalar sistemasi qaysi usul bilan integrallanishini

$$\frac{dy}{dt} = g(t)x + h(t)y + e(t),$$

toping

Sistema tenglamalarini ketma-ket integrallash kerak

Sistema tenglamalarini har biri alohida integrallash kerak

Bitta ikkinchi tartibli tenglama keltirib integrallash kerak

Integrallovchi kombinatsiya tuzib integrallash kerak

№170.

Qiyinlik darajasi-2

$$\left. \begin{array}{l} \frac{dx}{dt} = f(t, x, y, z), \\ \frac{dy}{dt} = g(t, x, y, z), \\ \frac{dz}{dt} = h(t, x, y, z), \end{array} \right\}$$

normal sistema tartibini toping

3

2

1

4

№171.

Qiyinlik darajasi-2

$y''+y'+xy=0$ tenglamaning nechta differensial tenglamaning normal sistemaga keltirishini
toping

2

1

3

4

№172.

Qiyinlik darajasi-2

$$\left. \begin{array}{l} y''-z=0, \\ z''+y=0, \end{array} \right\}$$

differensial tenglamalar sistemasining tartibini toping

4

3

2

1

№173.

Qiyinlik darajasi-2

$$\left. \begin{array}{l} \frac{dx}{dt} = f(t, x, y, z), \\ \frac{dy}{dt} = g(t, x, y, z), \\ \frac{dz}{dt} = h(t, x, y, z), \end{array} \right\}$$

differensial tenglamalar sistemasining turini toping

Oddiy differensial tenglamalarning normal sistemasi

To‘g‘ri javob yo‘q

Chiziqli differensial tenglamalar sistemasi

Simmetrik ko‘rinishdagi odddiy differensial tenglamalar sistemasi

№174.

Qiyinlik darajasi-3

A matritsaning e^A ko‘rsatkichli funksiyani ko‘rsating

$$e^A = E + \frac{A}{1!} + \frac{A^2}{2!} + \frac{A^3}{3!} + \dots$$

$$e^A = E + \frac{A}{1} + \frac{A^2}{2} + \frac{A^3}{3} + \dots$$

$$e^A = A + \frac{E}{1!} + \frac{E}{2!} + \frac{E}{3!} + \dots$$

$$e^A = E - \frac{A}{1!} + \frac{A^2}{2!} - \frac{A^3}{3!} + \dots$$

№175.

Qiyinlik darajasi-3

e^A ko‘rsatkichli funksiya uchun

$$e^{A+B} = e^A \cdot e^B = e^B \cdot e^A \text{ tenglik qaysi shartda o‘rinli?}$$

$$AB = BA$$

$$AB \neq BA$$

$$AB = E$$

$$A = B + E$$

$$\frac{dX}{dt} = AX \text{ matritsali tenglamaning}$$

$$X(0) = E \text{ shartni qanoatlantruvchi yechimini toping}$$

№176.

Qiyinlik darajasi-2

$$\left. \begin{array}{l} \frac{dx}{dt} = ax + by, \\ \frac{dy}{dt} = cx + dy, \end{array} \right\}$$

differensial tenglamalar sistemasining turini toping

Chiziqli differensial tenglamalarning avtonom sistemasi

Oddiy differensial tenglamalarning normal sistemasi

Simmetrik ko‘rinishdagi oddiy differensial tenglamalar sistemasi

To‘g‘ri javob yo‘q

№177.

Qiyinlik darajasi-2

$$\left. \begin{array}{l} \frac{dx}{dt} = ax^k + by^l \\ \frac{dy}{dt} = cx^m + dy^n \end{array} \right\}$$

Differensial tenglamalar sistemasining tartibini toping:

2

1

k

n

№178.

Qiyinlik darajasi-3

Agar chiziqli bir jinsli sistemaning har bir yechimi $t \rightarrow +\infty$ da nolga intilsa, u holda nol yechim

Asimptotik turg‘un

Turg‘un, lekin asimptotik turg‘un emas

Turg‘un emas

Bunday yechim mavjud emas

№179.

Qiyinlik darajasi-3

Agar chiziqli bir jinsli sistemaning har bir yechimi $t \rightarrow +\infty$ da chegaralangan bo‘lsa u holda yechim

Turg‘un, lekin asimptotik turg‘un emas

Turg‘un emas

Asimptotik turg‘un

Bunday yechim mavjud emas

№180.

Qiyinlik darajasi-3

Agar chiziqli bir jinsli sistema hech bo‘lmaganda bitta chegaralanmagan ($t \rightarrow +\infty$ da) yechimga ega bo‘lsa, u holda nol yechim

Turg‘un emas

Turg‘un, lekin asimptotik turg‘un emas

Asimptotik turg‘un

Bunday yechim mavjud emas

№181.

Qiyinlik darajasi-3

Agar sistemaning birorta yechimi Lyapunov ma’nosida turg‘un bo‘lsa, u holda bu sistemaning

Hamma yechimlari turg‘un

Qolgan yechimlari turg'un emas
 Hamma yechimlari asimptotik turg'un
 Ba'zi yechim turg'un

№182.

Qiyinlik darajasi-3

$$\begin{cases} \frac{dx}{dt} = 2x \\ \frac{dy}{dt} = 2x + 3y \end{cases}$$

Differensial tenglamalar sistemasinin muvozanat nuqtasining turini aniqlang

Egar

Markaz

Tugilma tugun

Fokus

№183.

Qiyinlik darajasi-3

$$\begin{cases} \frac{dx}{dt} = 2x \\ \frac{dy}{dt} = x + y \end{cases}$$

Differensial tenglamalar sistemasinin muvozanat nuqtasining turini aniqlang

Tugun

Markaz

Tugun

Fokus

№184.

Qiyinlik darajasi-3

$$\begin{cases} \dot{x} = 2x + y \\ \dot{y} = 2x \end{cases}$$

0 nuqtaning tipini aniqlang

Egar

Markaz

Tugun

Fokus

№185.

Qiyinlik darajasi-3

$$\begin{cases} \dot{x} = 2x + y \\ \dot{y} = x + 3y \end{cases}$$

sistemaning muvozanat nuqtasining turini aniqlang

Tugun

Markaz

Egar

Fokus

№186.

Qiyinlik darajasi-3

$$\begin{cases} \cdot \\ x = 2x - y \\ \cdot \\ y = x \end{cases}$$

sistemaning muvozanat nuqtasining turini aniqlang

Tug‘ilma tugun

Tugun

Fokus

Egar

№187.

Qiyinlik darajasi-3

$$\begin{cases} \cdot \\ x = 3x + 2y \\ \cdot \\ y = x - 4y \end{cases}$$

sistemaning muvozanat nuqtasining turini aniqlang

Fokus

Egar

Tugun

Markaz

№188.

Qiyinlik darajasi-3

Nochiziqli sistemalarni yechishda integrallanuvchi kombinatsiyalarni topiladi Bunda teng kasrlar hossasidan foydalaniladi Agar

$$\frac{a_1}{b_1} = \frac{a_2}{b_2} = \dots = \frac{a_n}{b_n} = t \text{ bo'lsa, u holda ixtiyoriy } k_1, k_2, \dots, k_n \text{ larda}$$

$$\frac{k_1 a_1 + k_2 a_2 + \dots + k_n a_n}{k_1 b_1 + k_2 b_2 + \dots + k_n b_n} = t$$

$$\frac{k_1 b_1 + k_2 b_2 + \dots + k_n b_n}{k_1 a_1 + k_2 a_2 + \dots + k_n a_n} = t$$

$$\frac{k_1 a_1 + k_2 a_2 + \dots + k_n a_n}{k_1 b_1 + k_2 b_2 + \dots + k_n b_n} = (t+1)^2$$

$$k_1 \frac{a_1}{b_1} + k_2 \frac{a_2}{b_2} + \dots + k_n \frac{a_n}{b_n} = t$$

№189.

Qiyinlik darajasi-2

Ushbu $x^2 - y^2 = c$, va $x + y = c_2 z$ birinchi integral qaysi sistemani qanoatlantiradi?

$$\frac{dx}{y} = \frac{dy}{x} = \frac{dz}{z}$$

$$\frac{dx}{2y - z} = \frac{dy}{y} = \frac{dz}{z}$$

$$\frac{dx}{z} = \frac{dy}{xz} = \frac{dz}{y}$$

$$\frac{dx}{x} = \frac{dy}{y} = \frac{dz}{xy + z}$$

№190.

Qiyinlik darajasi-3

$y \frac{dz}{dx} - x \frac{dz}{dx} = 0$ birinchi tartibli xususiy hosilali tenglamaning umumiy yechimini ko'rsating

$$z = \varphi(x^2 + y^2)$$

$$z = \varphi(x + y)$$

$$z = \varphi(x^2 - y^2)$$

$$z = \varphi(x + y^2)$$