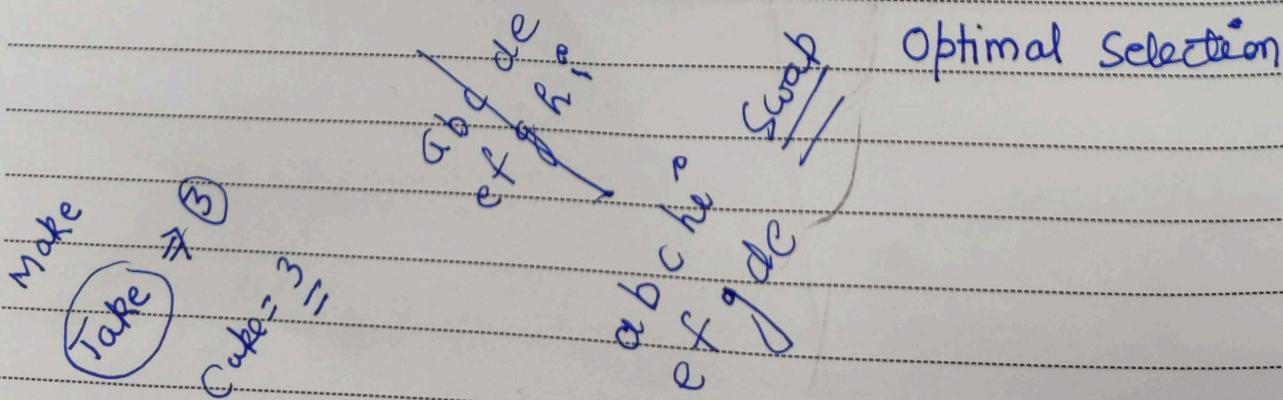
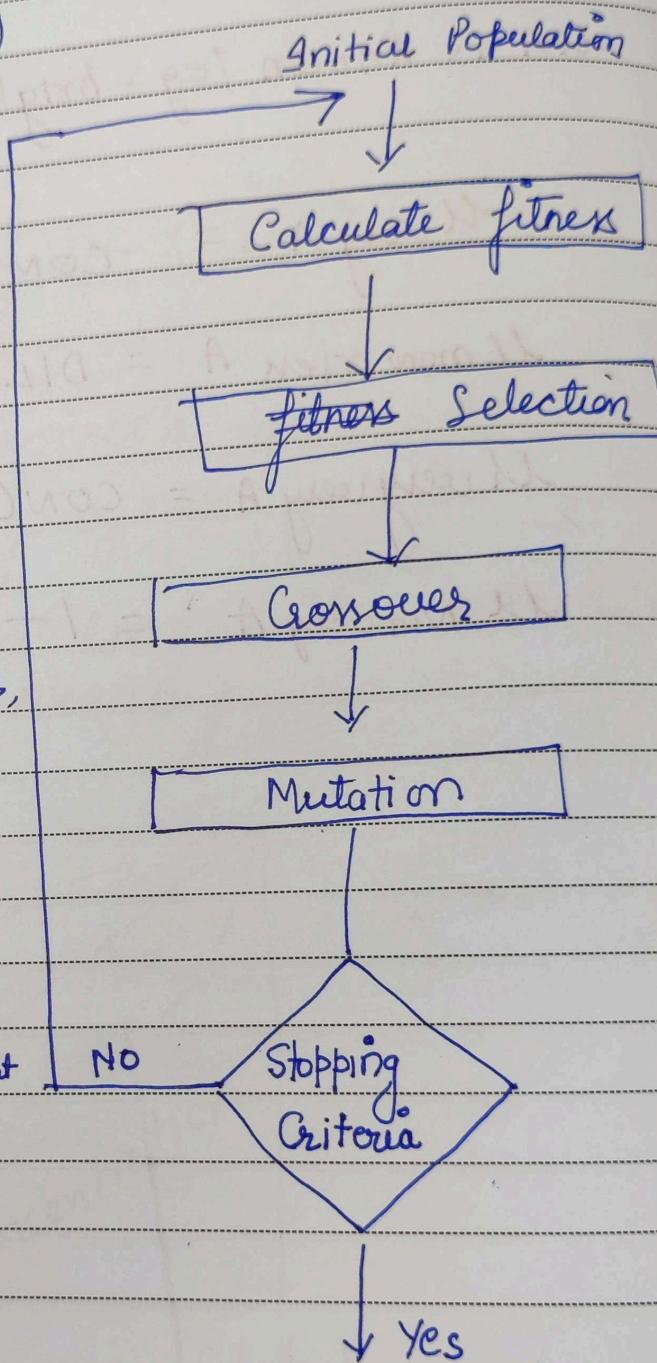
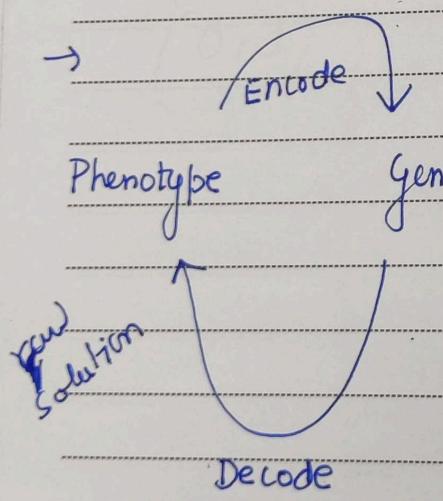


## Genetic Algorithm (John Holland)

- Abstraction of Real biological Evaluation
- Solve Complex Problems (like NP Hard)
- Focus on Optimization
- population of possible Solutions for a given problem
- From a group of individuals, the best will survive.



$$4x + 8 = 0$$

$$2y = 0$$

$$x = -2, 0$$

$$2 \times 4 + 0 = 16 + 0$$

$$8 + 0 - 1 =$$

Some benchmark optimization problems.

- ↳ Travelling Salesman Problem
- ↳ Knapsack Problem
- ↳ Graph Colouring Problem
- ↳ Job Machine Assignment Problem
- ↳ Coin change Problem
- ↳ Binary search tree construction problem



Proposed Approach :-

We presume that all the sensors are homogeneous and stationary and their location is known.

### a) Sensing Coverage representation

A set of sensor nodes in a target area A is delineated as

$S = \{s_1, s_2, \dots, s_m\}$ , where  $s_i$  is located at coordinates  $\{a_i, b_i\}$ , where  $i$  varies from 1 to M

Let P be the set of POC's distributed over the area A.

If N is no. of POC's then  $\{p_1, p_2, \dots, p_N\}$   
where POC  $p_j$  is situated at  $[a_j, b_j]$ , where j varies from 1 to N.

N

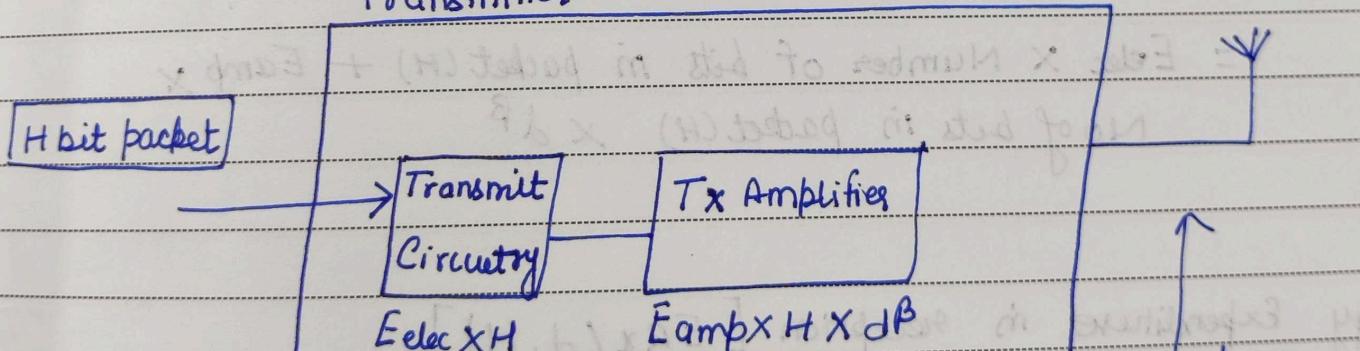
A binary coverage variable  $c_{ij}$  which signifies whether sensor  $s_i$  covers the POC  $p_j$  is defined below.

$$c_{ij} = \begin{cases} 1 & \text{if } (a_i - a_j)^2 + (b_i - b_j)^2 \leq R_a^2 \\ 0 & \text{otherwise.} \end{cases}$$

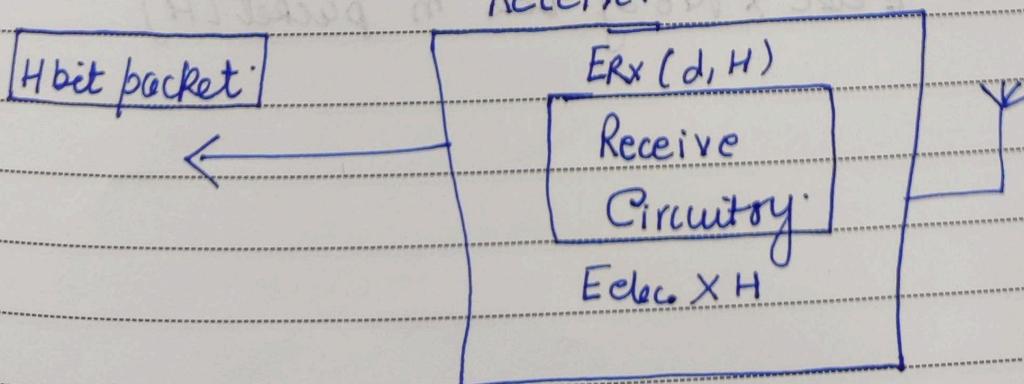
(b) Energy disbursement Model :-

we exploit the model illustrated by Heinzelman to compute the power disbursement for both kind of communication (transmission as well as reception)

Transmitter



Receiver



"The energy disbursement model".

In above fig. transmit circuitry or receives circuitry consumes  $E_{elec}$  nano joules energy in transmission or reception of per bit.

Energy expenditure in the power amplification of each bit is depicted by  $E_{amp}$ .

$\beta$  exponent of path loss.

As a result, when a transmitter transmits a packet of  $H$  bits to the receiver, the overall energy expenditure can be determined as follows

Energy Expenditure in Transmission  $[E_{Tx}(d, H)]$

$$= E_{elec} \times \text{Number of bits in packet } (H) + E_{amp} \times \\ \text{No of bits in packet } (H) \times d^\beta$$

Energy Expenditure in reception  $[E_{Rx}(d, H)]$

$$= E_{elec} \times \text{No of bits in packet } (H)$$

Problem formulation :-

to locate such specific set of sensor nodes such that each POC is covered by at least one node.

Optimization model:-

$$\text{Min } \sum \text{cost}_i \cdot a_i \quad i = 1, 2, 3, 4 \dots M$$

Subject to

$$\sum c_{ij} \cdot a_i \geq 1 \quad j = 1, 2, 3 \dots N$$

$$x_i = 0 \text{ or } 1 \quad i \in [1, M]$$



## "Absolute sensing - Area Coverage Using extended Genetic Algo."

Coverage of the proposed ASceGA includes 2 optimized strategies: the GA extended approach to determining the sensor node schedule and the stir up proposal.

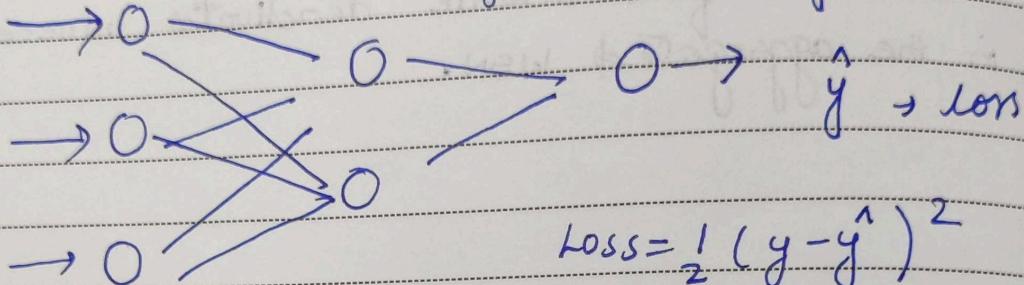
The first scheme deactivates unnecessary nodes in the aggregated WSN.

$\Leftarrow$ : Optimizers:  $\rightarrow$

$f_1 f_2$

## 1) Gradient Descent

optimizers  
Input layer      hidden layer      o/p layer



Aim:  $\rightarrow$  To reduce Loss  
with optimizers

to reduce update weights in back.  
propagation -

$$w_{\text{new}} = w_{\text{old}} - \eta \frac{dL}{dw_{\text{old}}}$$

Gradient descent

1) Epoch

2) Iteration

$\rightarrow$  dataset 10K Records  
I have to train my model for 20 epochs,  
10K records

$$\text{Loss} = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$



Everyone P2  
focus

$f_1, f_2, \dots, y$

$\dots, y_1$

$y_2$

$\vdots$

$y_{10K}$

In Every epoch  $10^k$   
records will be taken  $\rightarrow$

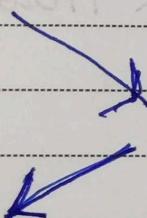
Front

back

{ Epoch      Complete  
dataset is  
taken }

what if my dataset becomes 1 million records?

1 million

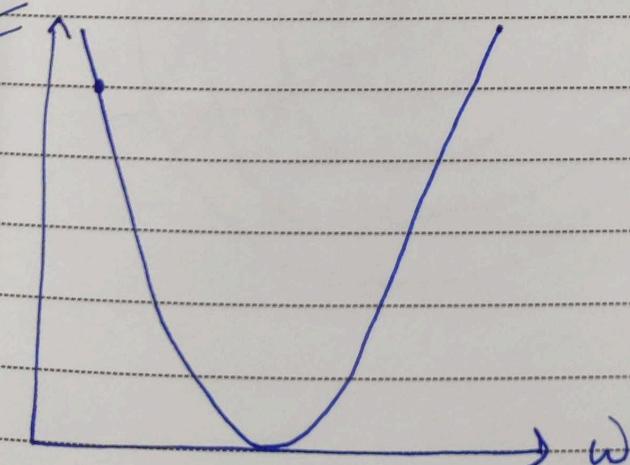


→ Huge RAM

→ weight updation will take time

→ Convergence will be slow.

Loss



More Resource  
Computationally  
expensive

so what do we  
do?

stochastic G.D.

Instead taking all records

take only 1 record: →

do Front →

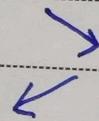
back ↙

$$\text{Loss} = \frac{1}{2} (y - y')^2$$

For every epoch

(10K)

I have to do 10K iterations



20 epoch.

$$\rightarrow 20 \times 10K.$$

↓  
Convergence is slow

Less  
Computationally  
expensive

Minibatch SGD: →

10k records  
for every epoch : Researchers take  
some batch size  
say 1000

20 Epoch

Epoch ①

how many iterations

$$\frac{10k}{K} = 10 \text{ iterations}$$

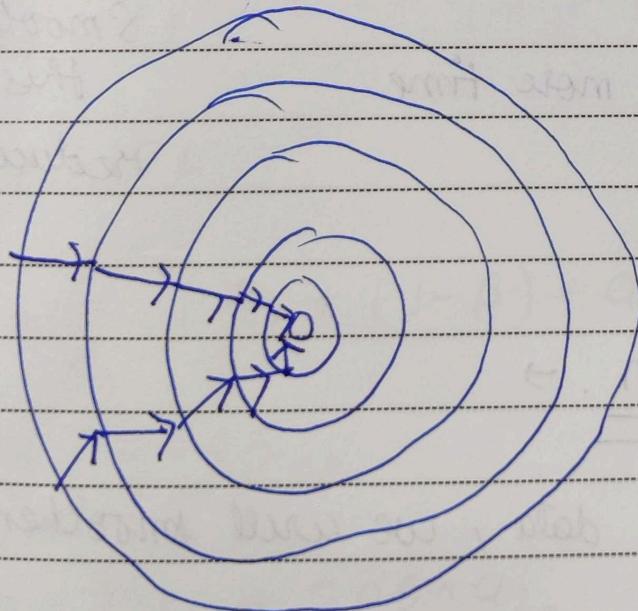
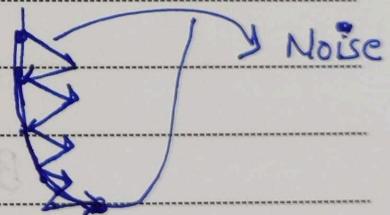
10 forward and

10 backward propagations

Epoch ②

→ 10 iteration.

mini batch SGD

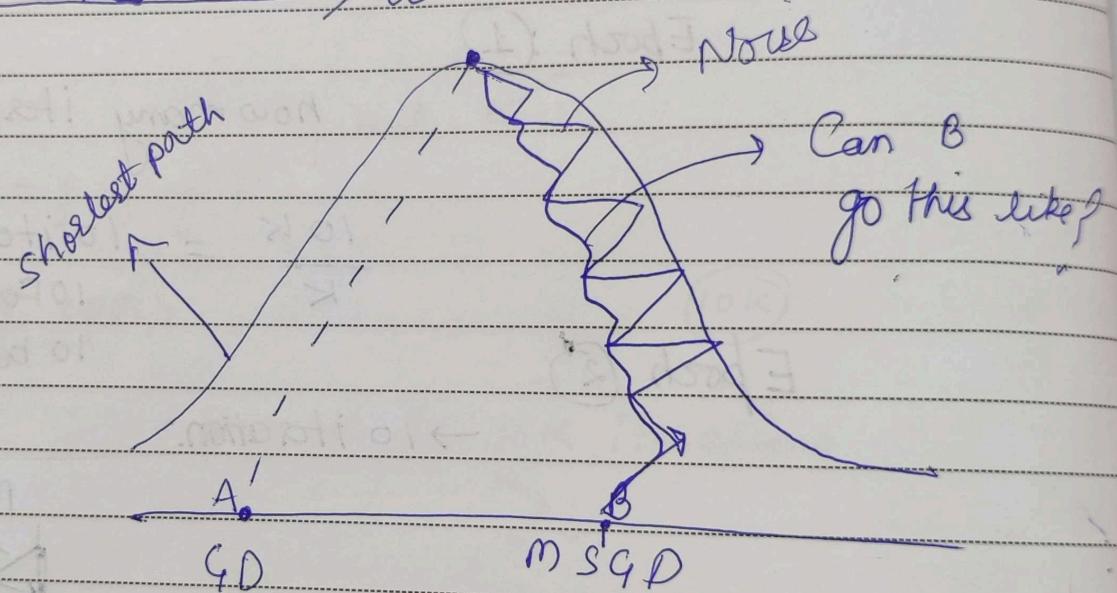
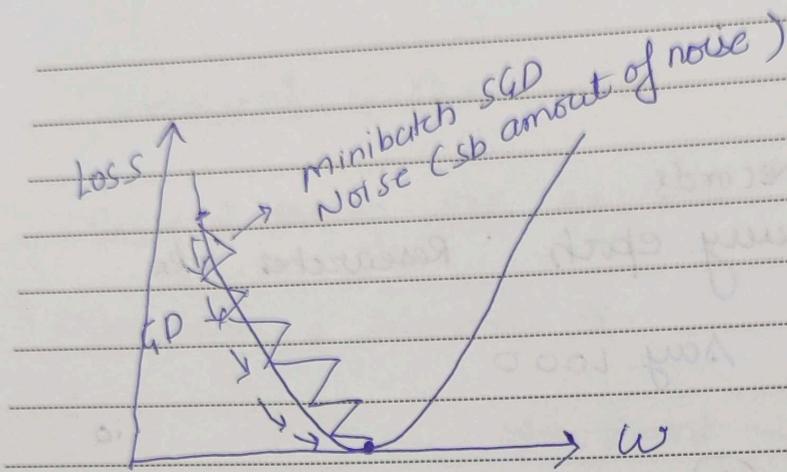


GD whole dataset

SGD 1 record

MiniBatch → Batch size

6:30 pm  
  
~~7:00~~ PM



B will take more time  
 sb GPS to B

Smoothing  
 this  
 Reducing Noise

SGD with momentum: →

Noisy data, we will smoothen

$$w_{new} = w_{old} - \eta \frac{\partial L}{\partial w_{old}}$$

$$w_t = w_{t-1} - \eta \frac{\partial L}{\partial w_{t-1}}$$

momentum says: in order to smoothen, we will compute expo weighted average.

Exponential weighted Average:  $\rightarrow$

$t_1$	$t_2$	$t_3$	$t_4$	$\dots$	$t_n$	date time
$a_1$	$a_2$	$a_3$	$a_4$	$\dots$	$a_n$	series data

$$V_t = a_1$$

$$V_{t_1} = a_1$$

$$V_{t_2} = \beta V_{t_1} + (1-\beta) * a_2$$

$$\text{say } \beta = .95$$

$$= .95a_1 + 0.05 * a_2$$

$\beta$  is hyperparameter  
how much importance you  
want to give to  
previous data

ARIMA  $\Rightarrow$  Smoothing concept

$$\beta = 1$$

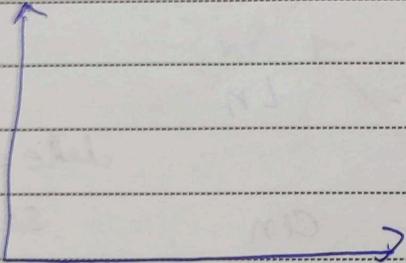
$$= \alpha_1 + \alpha_2$$

give more importance to  $\alpha_2$  (next value)

$$V_{t+3} = \beta V_{t+2} + (1-\beta)\alpha_3$$

$$= \beta(\beta V_{t+1} + (1-\beta)\alpha_2) + (1-\beta)\alpha_3$$

Exponential avg.



$\Rightarrow$

Exponential Weighted average

$$w_t = w_{t-1} - \eta v_{dw}$$

↑  
exponential weighted avg.

$$b_t = b_{t-1} - \eta v_{db}$$

$$v_{dw} = \beta v_{dw,t-1} + (1-\beta) \times \frac{\partial L}{\partial w}$$

$$V_{t+1} = \beta V_t + (1-\beta) \cdot \alpha_2$$

### Implementation details

Initially  $V_{d\omega} = 0$   $V_{db} = 0$

On iteration and no inside epoch

Compute  $d\omega, db$  on the current mini batch

$$V_{d\omega t} = \beta V_{d\omega t-1} + (1-\beta) \frac{\partial L}{\partial \omega t}$$

$$V_{db t} = \beta V_{db t-1} + (1-\beta) \frac{\partial L}{\partial b t}$$

$$\omega = \omega - \eta V_{d\omega} V_{d\omega}$$

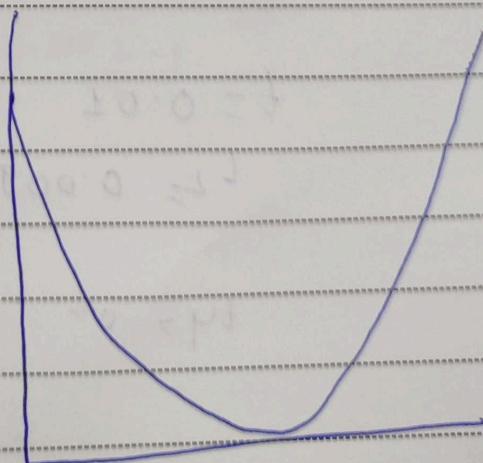
$$b = b - \eta V_{db} V_{db}$$

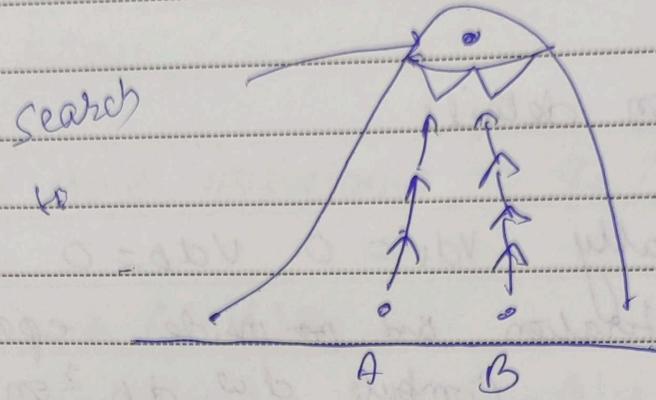
④

Adaptive ~~Adagrad~~ gradient descent

$\eta = \text{fixed}$

N





weight updation formula

$$w_t = w_{t-1} - \eta \frac{\partial L}{\partial w}$$

$$w_t = w_{t-1} - \eta \underbrace{\frac{\partial L}{\partial w}}_k$$

$$\eta = \frac{m}{\sqrt{\eta t + \epsilon}} \leftarrow \text{initial learning rate}$$

$$= \sum_{j=1}^k$$

$$\leq \frac{n}{\sqrt{\eta t + \epsilon}} \quad \text{Good fitting}$$

$$t = 0.01$$

$$L_2 = 0.009 \quad L_3 = 0.0$$

$$ty = 0.0$$

$$\gamma + \sum_{i=1}^t \left( \frac{\partial L}{\partial w_t} \right)^2$$

divide by big no.  $\eta'$  will reduce

we need to reduce learning rate

disadvantage: After some time

$\eta'$  is very very big no  
if deep N. N.

{ .01 } starting  
.0000001 (learning rate) Now

disadvantage:-

$\eta'$  is becoming very very high

(5) and

Adadelta with RMSROP

weight update

~~Homemade~~

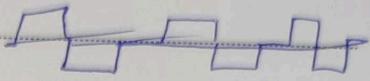
$$\begin{aligned} \eta' &= \eta \\ &\quad \sqrt{S_{dw} + \epsilon} \\ &= \beta \quad \downarrow \\ S_{dw}' &= \beta S_{dw} + \epsilon \end{aligned}$$



Adam

Adaptive Momentum

Action



Adaptive "

Momentum  
RMSProp

combine

$v_{dw}$   $v_{db}$   $s_{dw}$   $s_{db}$

$$\frac{\partial L}{\partial w}, \frac{\partial L}{\partial b}$$

using current minibatch

$$V_L = \beta_1 v_{dw} + (1 - \beta) \frac{\partial L}{\partial w}$$

$$v_{dw} = \beta_1 v_{dw} + (1 - \beta) \frac{\partial L}{\partial w}$$

$$s_{db} = \beta_2 s_{db} + (1 - \beta) \left( \frac{\partial L}{\partial b} \right)^2$$

$$s_{db} = \beta_2 s_{db} +$$

Bias Correction

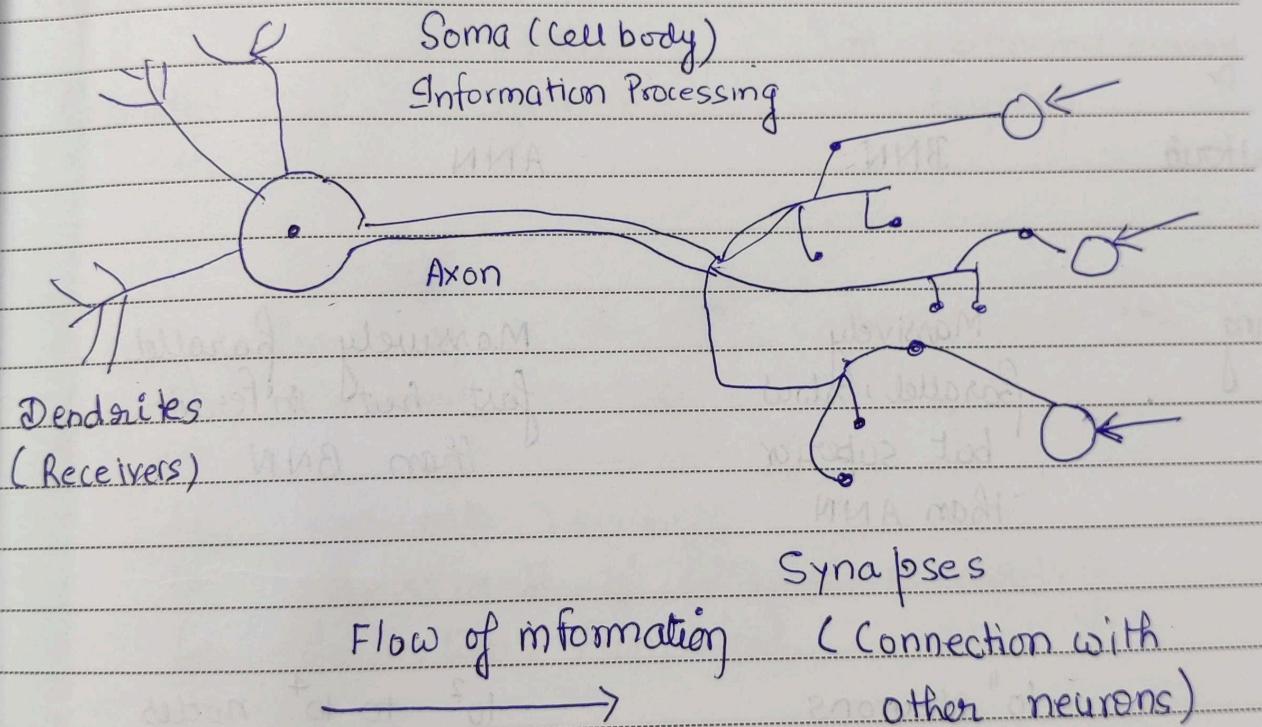
initial LR

$$\left\{ \begin{array}{l} w_t = w_{t-1} - n \times \frac{v_{dw}}{\sqrt{s_{dw}} + \epsilon} \\ b_t = b_{t-1} - n \times \frac{v_{db}}{\sqrt{s_{db}} + \epsilon} \end{array} \right. \quad \left. \begin{array}{l} \text{Adam} \\ \rightarrow \text{Smoothing factor} \\ \rightarrow \text{RMSprop} \end{array} \right.$$

## Biological Neuron

A nerve cell neuron is a special biological cell that processes information.

According to an estimation, there are huge number of neurons, approximately  $10^{11}$  with numerous interconnections, approximately  $10^{15}$



Dendrites:-

Soma:-

Axon:-

Synapses



## ANN vs BNN

BNN

Soma

Dendrites

Synapse

Axon

ANN

Node

Input

Weights or interconnections

Output

Criteria

BNN

ANN

Processing

Massively parallel, slow  
but superior than ANN

Massively parallel,  
fast but inferior than BNN

Size

$10^9$  Neurons

$10^2$  to  $10^4$  nodes

and

$10^{15}$  fmtr

Connections

Learning

They can tolerate ambiguity

Very precise, structured and formatted data is required to tolerate ambiguity.

Fault tolerance

Performance  
degrades with  
even partial  
damage

it is capable of  
robust performance, hence  
has the potential to be  
fault tolerant.

Storage

Stores the  
information  
in synapse

Stores the information  
in continuous memory  
locations.

Capacity

Processing of ANN depends upon the  
following 3 building blocks

- ↳ Network Topology
- ↳ Adjustments of weights or learning
- ↳ Activation Functions

Network Topology is the arrangement of a network along with its nodes and connecting lines. According to the topology, ANN can be classified as

### Feedforward Network

Single layer feedforward Network

Multilayer feedforward Network

Feedback Network: →

a feedback network has feedback paths, which means the signal can flow in both directions using loops. following types

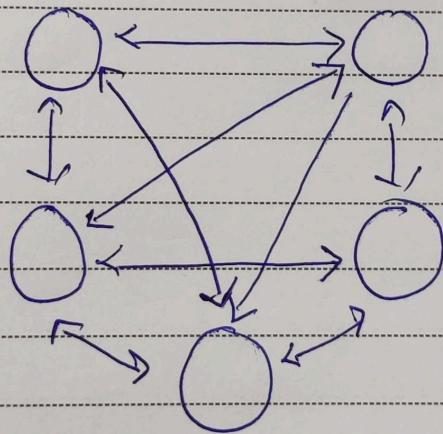
Recurrent Networks

2 types.

Fully recurrent Network:-

It is simple

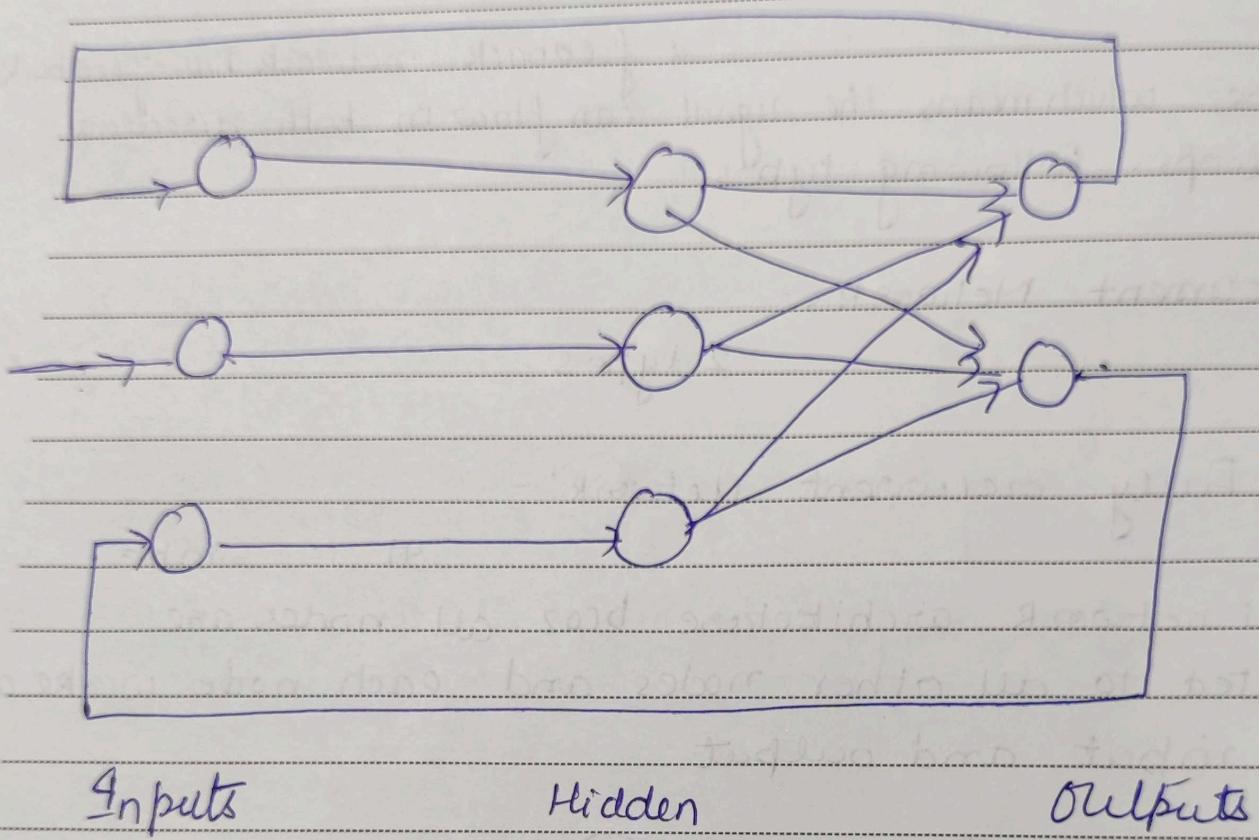
neural network architecture bcoz all nodes are connected to all other nodes and each node works as both input and output.



Jordan Network

It is closed loop network

in which the output will go to the input again as feedback as shown





<: Adjustments of weights or learning : →

Learning in artificial neural network, is the method of modifying the weights of connections between the neurons of a specified network.

Learning can be classified into 3 categories : →

Supervised learning

Unsupervised " "

Reinforcement "

Activation function :-

Activation function

## Advantages: →

1. ANN has the ability to learn and model non linear and complex relationships as many relationships between input and output are non linear.

2. After training , ANN can infer unseen relationships from unseen data , and hence it is generalized.

3.

Unlike many machine learning models , ANN does not have restrictions on datasets → data should be ~~symmetric~~ Gaussian dist<sup>n</sup> or any other dist.

## Applications

1. Image Processing and Character Recognition
2. Forecasting
3. Credit Rating
4. Fraud Detection
5. Portfolio Management

```
import numpy as np  
import pandas as pd  
from keras.models import Sequential  
from keras.layers import Dense
```

```
model = Sequential()  
model.add(Dense(12, input_dim=8, activation='relu'))  
model.add(Dense(8, activation='relu'))
```

Compiling Keras model:

fit

```
model.compile('loss = 'binary_crossentropy'  
              , optimizer = 'adam', metrics = ['accuracy'])
```

Fitting the Keras model

```
model.fit(x, y, epochs=50, batch_size=50)
```

(5) Evaluate Keras Model | (6) Make Predictions

```
accuracy = model.evaluate(x, y)  
print("Accuracy: {}% of predictions rounded = [round(x[0]) for x in predictions]
```

```
predictions = model.predict(x)
```

```
predictions]
```

Loss function and its type :

Loss helps us to understand how much the predicted value differ from actual value.

Function used to calculate the loss is called as "Loss function".

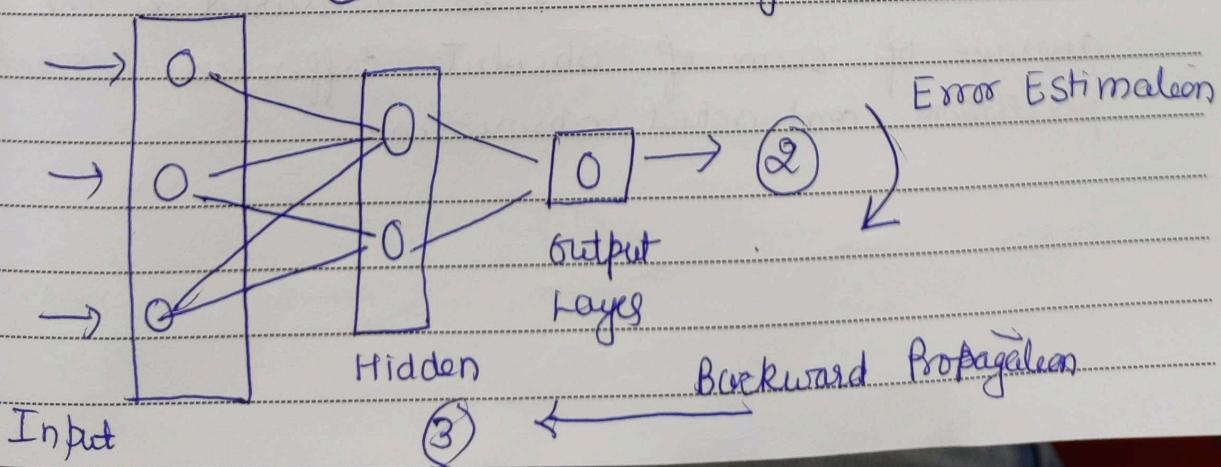
Loss function is a method of evaluating "How well your algorithm models your dataset".

If your predictions are totally off, your loss function will output a higher number.

If they are pretty good, it will output a lower number. As you tune your algorithm to try and improve your model, your loss function will tell you if you are improving or not.

LOSS FUNCTION are helpful to train a neural Network.

① → Forward Propagation



## Types of Loss function

1. Regression Loss Function
2. Binary Classification loss functions
3. Multi class Classification Loss Functions

### 1) Regression Loss Function

Regression models deals with predicting a continuous value for example given floor area, no of rooms, size of rooms, predict the price of room. Loss function used in regression problem are called "Regression Loss Function".

Most used Regression loss function are below:-

#### 1.1 Mean Absolute Error (MAE) / L1 Loss function :

Mean absolute error, is measured as the average of sum of absolute differences between predictions and actual observations.

- It measures the average "magnitude" of errors in a set of predictions "without considering their directions".
- Robust to outliers.
- MAE output ranges between 0 and  $\infty$
- Derivatives of ~~MAE~~ MAE are not continuous, making it inefficient

MAE is also known as "Least Absolute Deviations" or "LAD".

$$\text{Loss} = \frac{\sum_{i=0}^n |y_i - \hat{y}_i|}{n}$$

MAE LOSS

## Mean Square Error (MSE) / L2 Loss Function:-

Mean square error, is measured as the avg of sum of squared differences between predictions and actual observations.

It measures the average "magnitude" of errors in a set of predictions, "without considering their "directions".

less robust to outliers

MSE loss is stable than MAE.

L2 Loss ranges between 0 and  $\infty$ .

Derivatives of MSE are continuous, making it efficient to find the ~~solution~~ solution.

"MSE is the most commonly used regression loss function"

$$\text{Loss} = \frac{\sum_{i=0}^n (y_i - \hat{y}_i)^2}{n}$$

### 1.3. Root Mean Square Error (RMSE) | RMS Error :-

Root mean square error is the extension of MSE - measured as the average of square root of sum of squared differences between predictions and actual observations.

$$RMSE = \sqrt{\frac{\sum_{i=1}^N (\text{Predicted}_i - \text{Actual}_i)^2}{N}}$$



1.4

Mean Bias Error: →

MBE is less commonly used in practice.

MBE is similar

Hebbian learning rule, perceptron learning rule

Delta learning rule, Widrow Hoff Learning rule

Connection learning rule, winner take all  
Learning all.

Supervised learning

Unsupervised learning

Reinforcement learning

## L1 Fundamentals of Neural Networks

McCulloch and Pitts

Supervised learning  
Classification  
Regression

L2 Perceptions

Linear classification

L6

Hebbian learning  
and  
Associative Memory

L3 L4 Feed forward multiple layer  
networks and Backpropagation

Perception

Unsupervised  
learning

L5 Recurrent Neural  
Networks (RNN) Sequence and  
temporal data

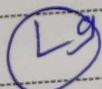
L8

Convolutional  
Neural  
Networks  
(CNN)

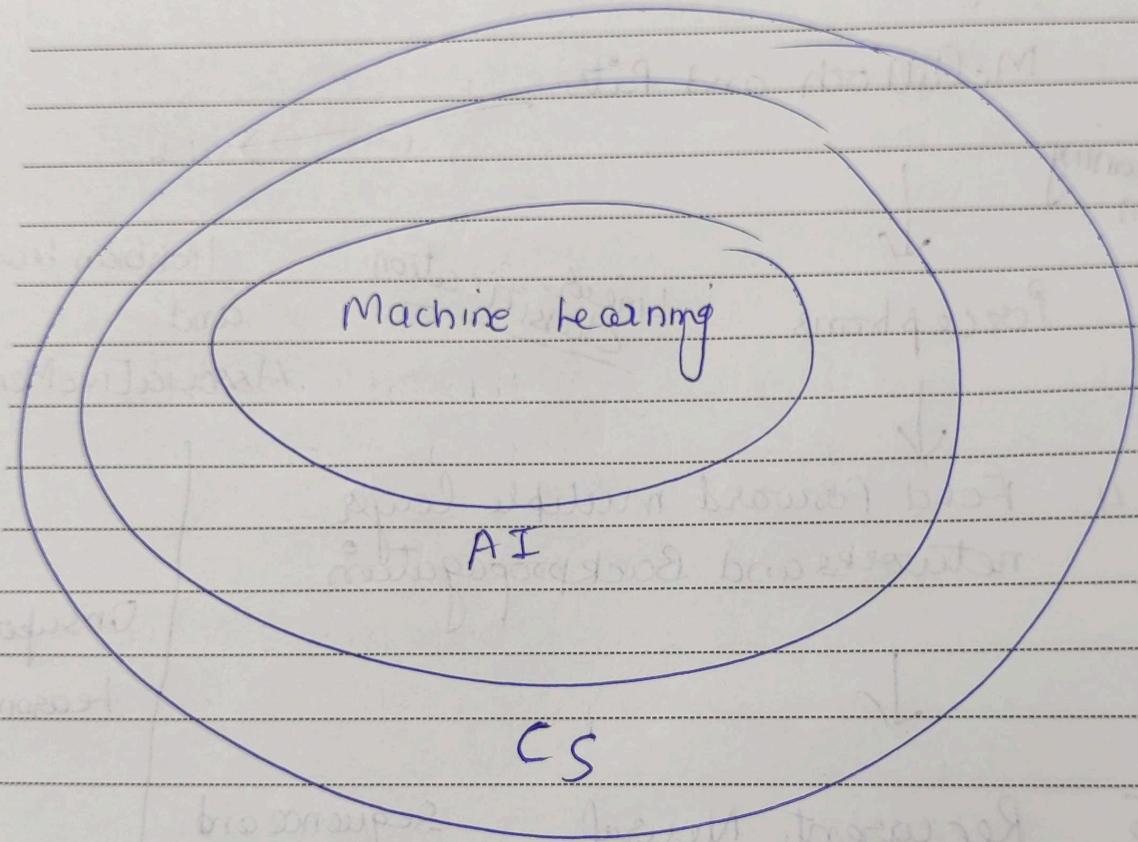
L7 Hopfield Networks  
and

Boltzmann  
machines

Deep learning



Development of ANN  
field



## Perceptrons

The perceptron is an algorithm for learning a linear binary classifier in the form of the threshold function that maps its input  $X$ , a real valued vector, to a single output binary value  $Y$ .

In the context of neural networks, a perceptron is a single artificial neuron using the Heaviside step function as the activation  $f$ .

As a linear classifier, the single layer perceptron is the simplest feed forward neural network.

$$y_j = \begin{cases} 1 & \text{if } w^T x = \sum w_{ij} * x_{ij} > \theta \\ 0 & \text{otherwise} \end{cases}$$

$$i = 1 - N$$

$w$  is a real valued vector,  $j \neq$  of iteration

The binary value of  $f(x)$  is used to classify a data item as either a positive or a negative instance.

## Intuitions for Perceptron Learning

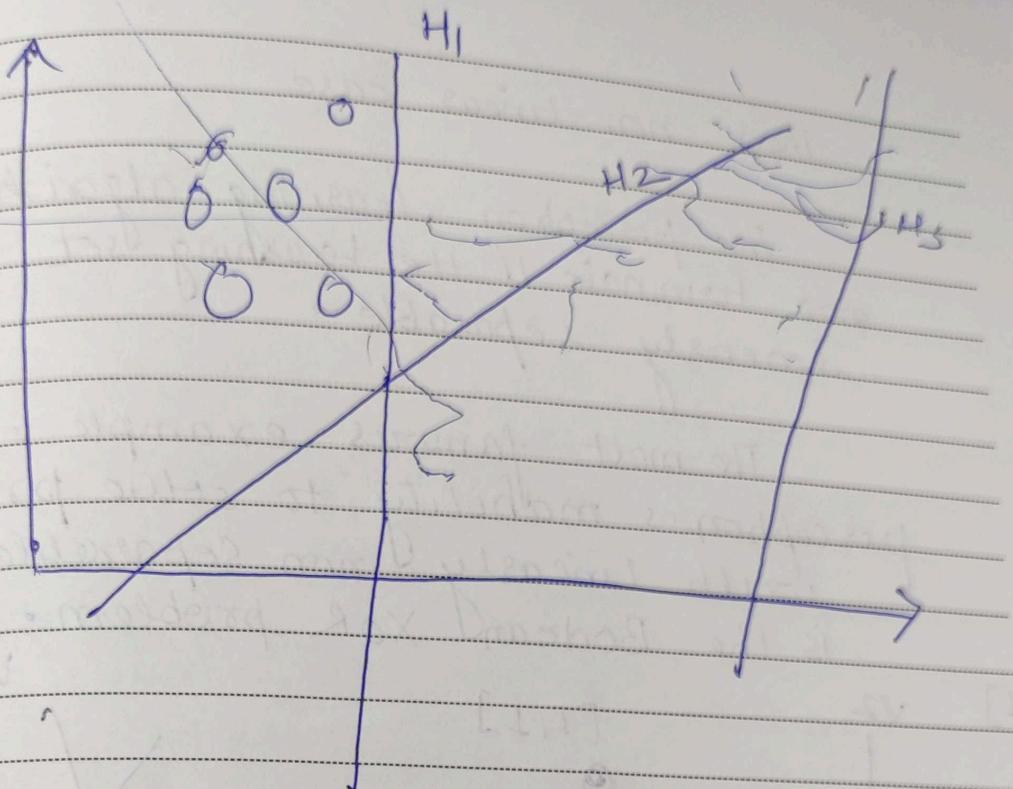
A perceptron is a linear classifier that tries to find a hyperplane in the space spanned by its input.

The adjustments of weights corresponds to changes in orientation of hyperplane.

The adjustments of bias corresponds to changes in the hyper plan intercepts with axes of the space.

For a 2 dimensional space the perceptron corresponds a line in the plane, the orientation of which is decided by the weights and the intercepts of which are decided by the bias.

An optimal perceptron finds a hyperplane (eg line) that best separates the data items.



which problems can a perceptron solve?

- Binary Classification for linearly separable instance spaces.

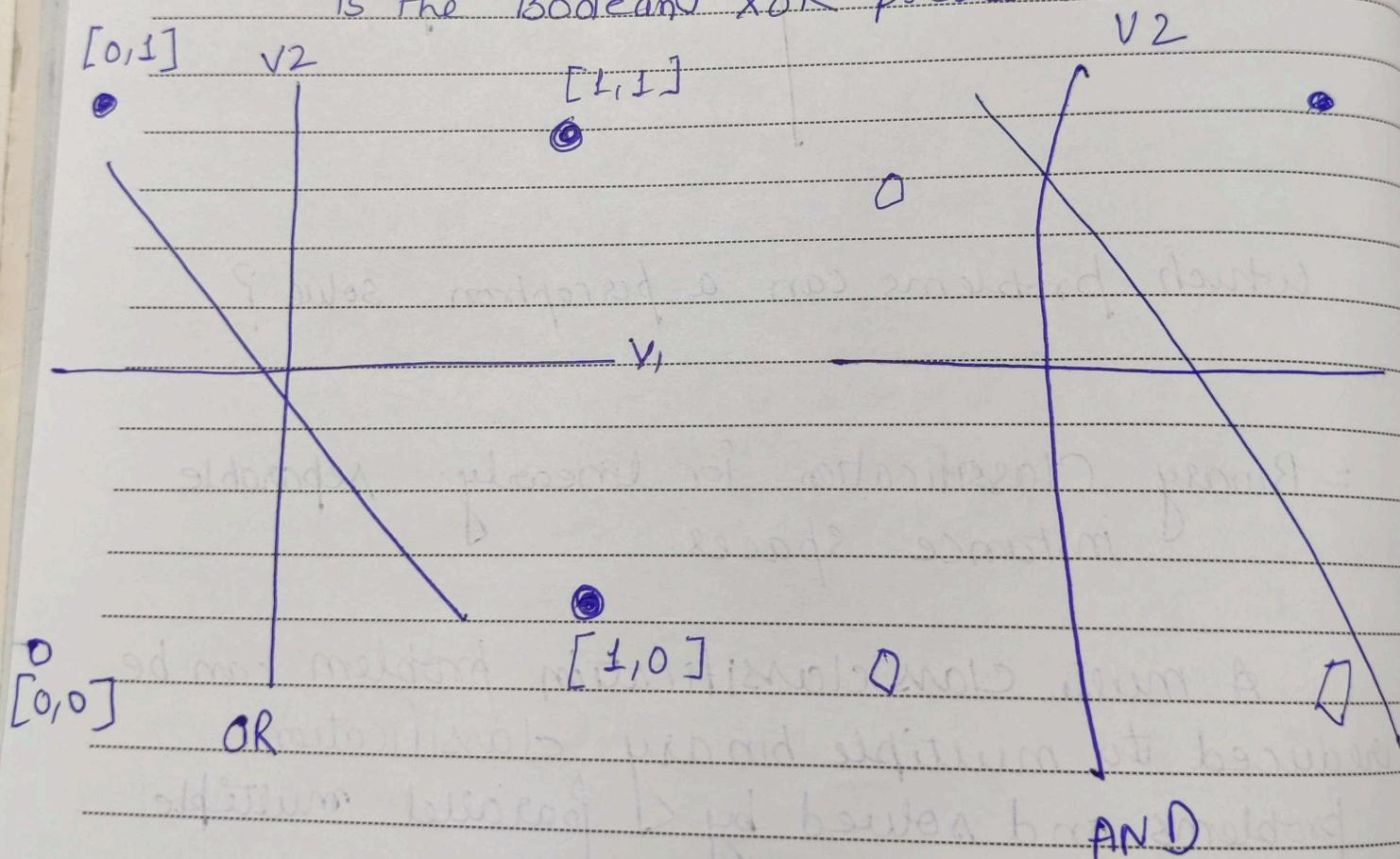
A multi class classification problem can be reduced to multiple binary classification problems and solved by  $\geq$  parallel multiple perceptrons.

As a perceptron only has binary output, regression cannot be performed.

Then non-linear case

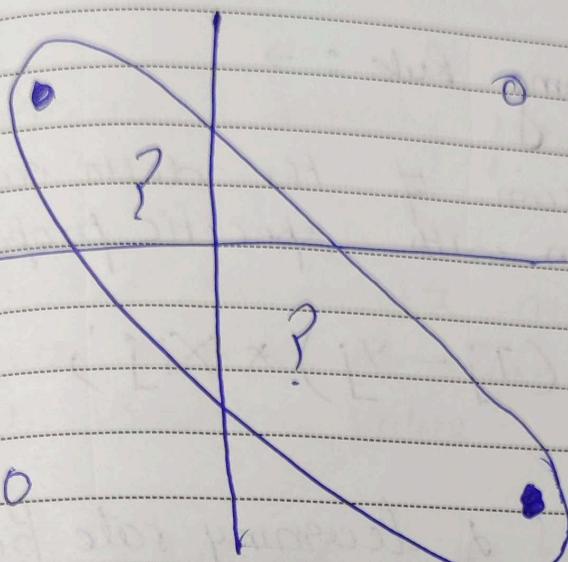
The perceptron learning algorithm does not terminate if the learning set is not linearly separable.

The most famous example of the perceptron's inability to solve problems with linearly non-separable vectors is the Boolean XOR problem.





$v_2$



XOR

Perceptron learning Rule :  $\rightarrow$

A simpler version of the delta rule  
for ONE neuron with specific properties

$$w_{ij+1} = w_{ij} + \alpha * (T_j - Y_j) * x_{ij}$$

of learning rate Parameter

$y_j = x_{ij} w_{ij}$ ,  $i = \text{input}$ ,  $j = \text{iteration}$ .

$T = \text{target}$

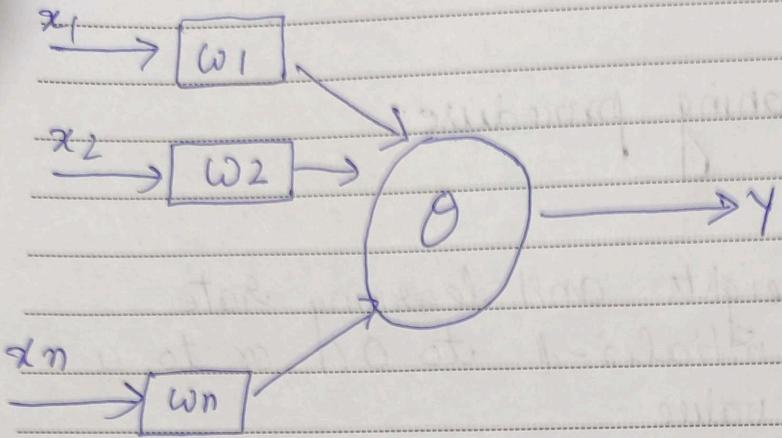
The threshold can also be learned by  
transforming it to a bias = -threshold  
and completing the data items with an  
extra input  $x_{0j} = 1$  and corresponding  
weight  $w_{0j} = \text{bias}$

steps in a learning procedure:-

Initialise the weights and learning rate  
Weights may be initialised to 0/1 or to a  
small random value.

For each example  $j$  in the dataset, perform  
the following steps until total training set error  
ceases to improve.

- Calculate the output
- Calculate the new weights



$$y_j = 1 \text{ if } W * x + B = (\text{Sum } w_{ij} * x_{ij}) > \theta$$

$$i = 1 \dots n$$

Otherwise  $y = 0$

$$w_{ij+1} = w_{ij} + \alpha * (T_j - y_j) * x_{ij} \quad \alpha = 0.2$$

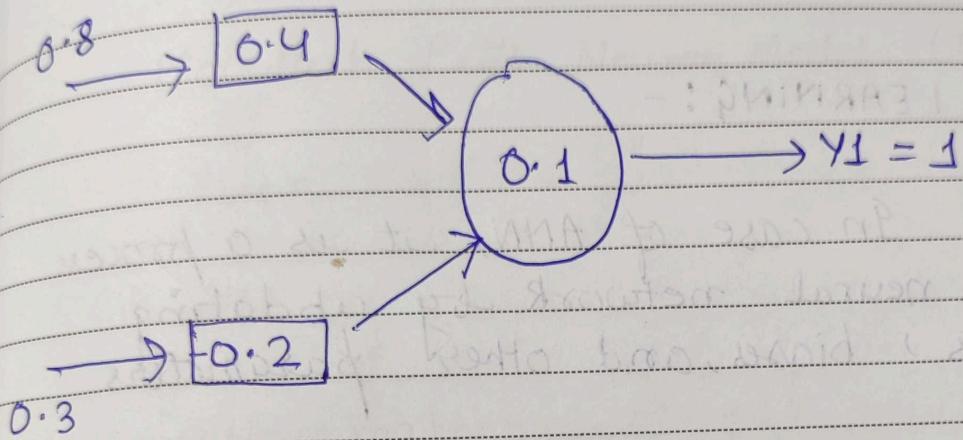
delta weight

$$x_{ii} =$$

$$\alpha = 0.2$$



$$\begin{aligned}x_{11} &= 0.8 & T_1 &= 0 \\x_{21} &= 0.3 & \omega_{11} &= 0.4 \\&& \omega_{21} &= -0.2\end{aligned}$$



$$\begin{aligned}& 0.4 \times 0.8 + (-0.2 \times 0.3) \\& = 0.32 - 0.06 \\& = 0.26 > 0.1\end{aligned}$$

$$\rightarrow Y_1 = 1$$

$$\begin{aligned}\omega_{12} &= 0.4 + 0.2 * (0-1) * 0.8 \\&= 0.24\end{aligned}$$

$$\omega_{22} = -0.2 + 0.2 * (0-1) * 0.3 = -0.26$$

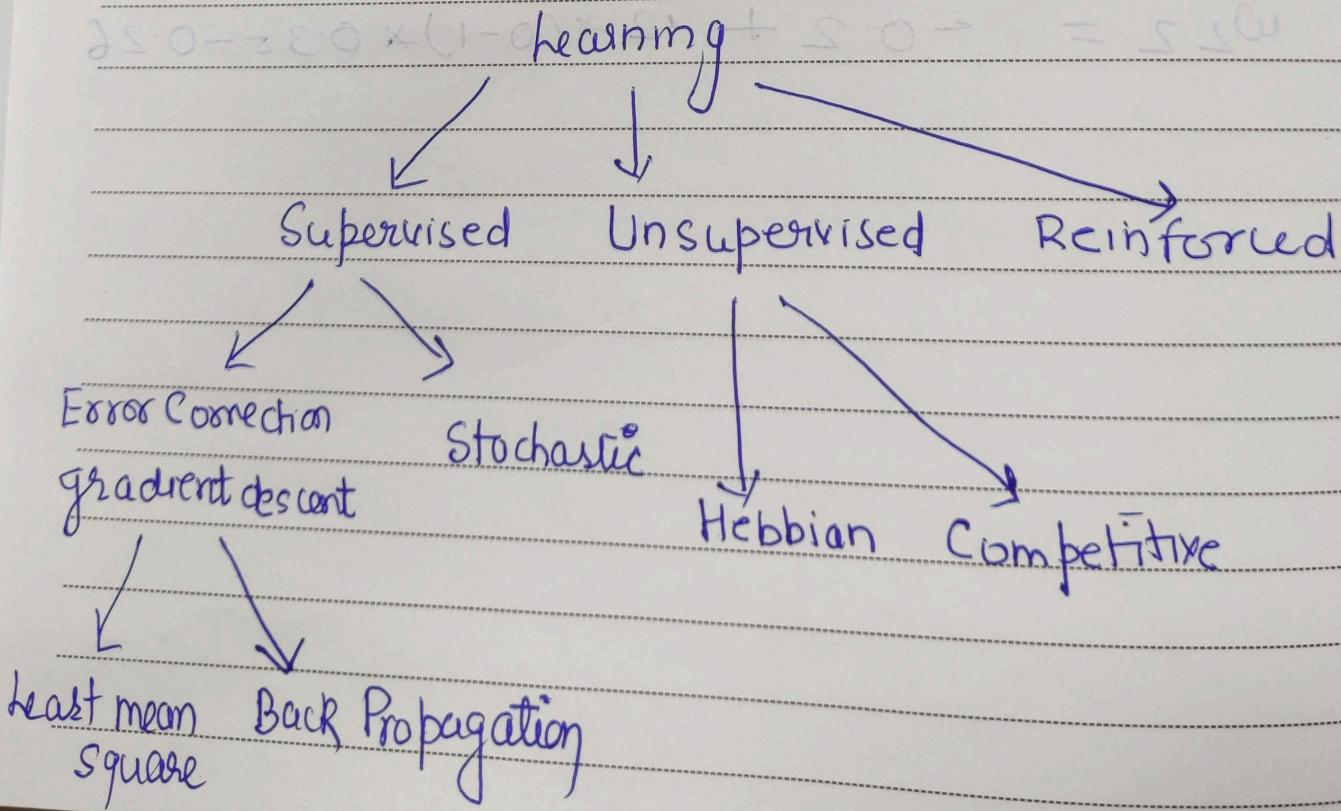
## CONCEPT OF LEARNING :-

In case of ANN, it is a process of modifying neural network by updating its weights, biases, and other parameters if any.

During the learning, the parameters of the networks are optimized and as a result process of curve fitting.

It is then said that the network has passed through a learning phase.

## Types of Learning



## McCulloch-Pitts Neuron Model (MCP)

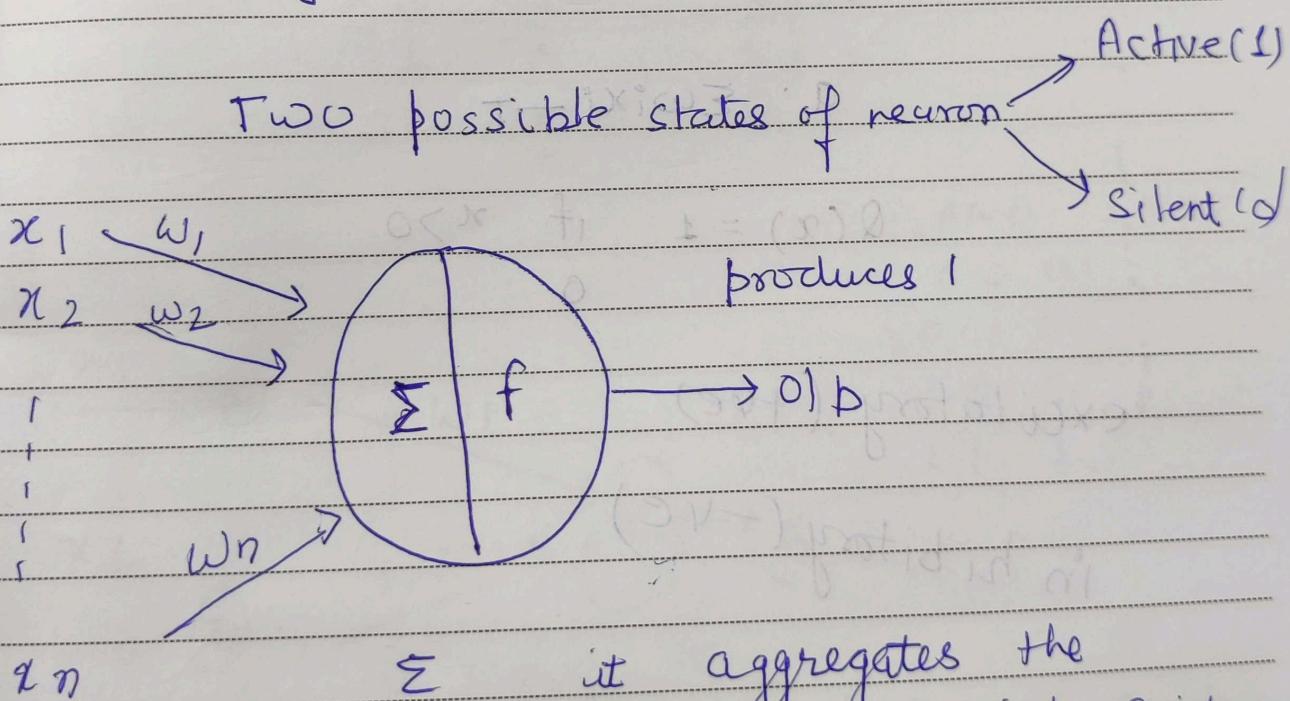
### Linear threshold Gate Model

in 1943 by Warren McCulloch and Walter Pitts

First mathematical model of biological neuron.

Basic building block of neural netw.

Directed (Graph)-weight graph is used for connecting neurons



$\Sigma$  it aggregates the weighted input into single numeric value.

$$f \text{ produces the O/p using threshold (T)}$$
$$\begin{cases} 1 & \text{if } X > T \\ 0 & \text{if } X < T \end{cases}$$
$$\Sigma x_1 w_1 + x_2 w_2 + \dots + x_n w_n ] X$$

BIAS / threshold :

Minimum value of weighted active input for a neuron to fire.

If effective I<sub>lp</sub> is larger than T,  
then o<sub>lp</sub> → 1 else 0

o<sub>lp</sub>  
f(a)

$$a = \sum w_i x_i - T$$

$$Q(x) = 1 \text{ if } x > 0$$

1 onward 0

excitatory (+ve)

inhibitory (-ve)

$$\theta > nw - p$$

Implement ANDNOT function using McCulloch-Pitts neuron (Binary data)

$x_1$	$x_2$	$y$
0	0	0
0	1	0
1	0	1
1	1	0

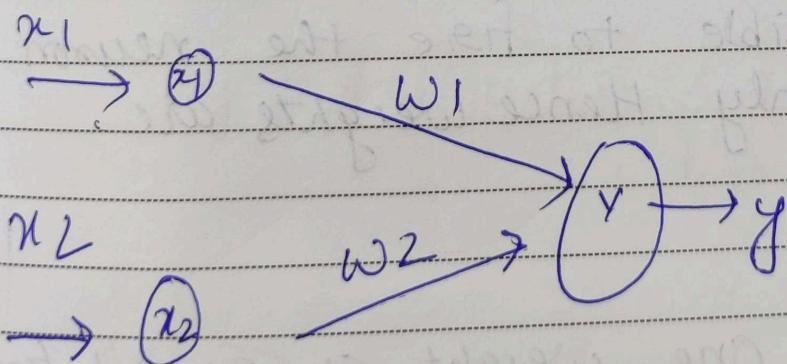
AND      NOT

0 0 0

0 1 0

1 0 0

1 1 1



Case 1: Assume both weights are excitatory

$$w_1 = w_2 = 1$$

$$\theta > nw - p$$

$$\geq 2 \times 1 - 0$$

$$\theta > 2$$

$$y_{in} = x_1 w_1 + x_2 w_2$$

for inputs

$$(0,0) \quad y_{in} = 0 \times 1 + 0 \times 1 = 0$$

$$(0,1) \quad y_{in} = 0 \times 1 + 1 \times 1 = 1$$

$$(1,0) \quad y_{in} = 1 \times 1 + 0 \times 1 = 1$$

$$(1,1) \quad y_{in} = 1 \times 1 + 1 \times 1 = 2$$

$$f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} \geq 2 \\ 0 & y_{in} < 2 \end{cases}$$

It is not possible to fire the neuron with  $w_1(1,0)$  only. Hence weights are not suitable.

Case 2: Assume one weight as excitatory and others as inhibitory

$$w_1 = 1, w_2 = -1$$

$$(0, 0)$$

$$(0, 1)$$

$$(1, 0)$$

$$(1, 1)$$

$$\begin{aligned}y_{in} &= 0x_1 + 0x_2 - 1 = 0 \\&= 0x_1 + 1x_2 - 1 = -1 \\&= 1x_1 + 0x_2 - 1 = 1 \\&= 1x_1 + 1x_2 - 1 = 0\end{aligned}$$

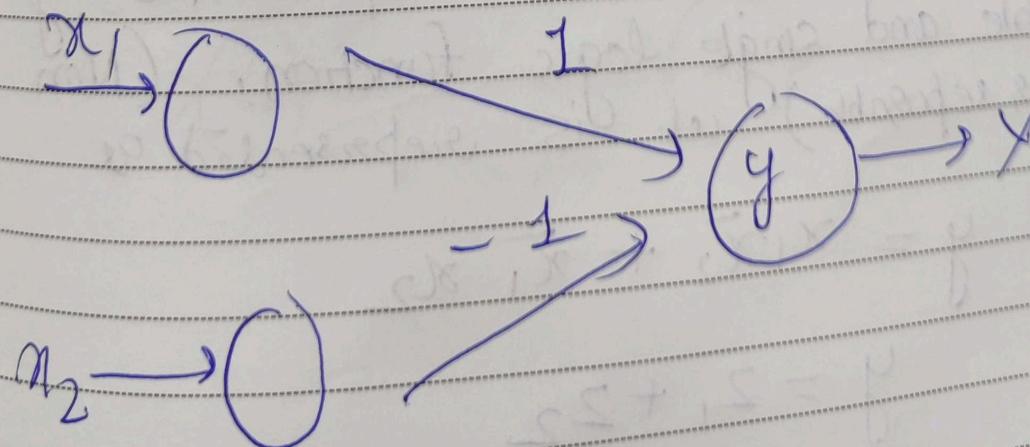
It is possible to fire the neuron  
with IP  $(1, 0)$  only

$$0 > mw - b$$
$$2 \times 1 - 1$$

$$0 > 1$$

Output of Neuron

$$y = f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} \geq 1 \\ 0 & \text{if } y_{in} < 1 \end{cases}$$



PN-①



Implement XOR function using McCulloch - Pitts Neuron

$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	0

Consider the truth table for XOR function

The MP neuron has no particular training algo.

In MP neuron, only analysis is being performed

XOR function cannot be represented by simple and single logic function, (Non linear separable) let it is represented as

$$y = x_1 \bar{x}_2 + \bar{x}_1 x_2$$

$$y = z_1 + z_2$$



(2)

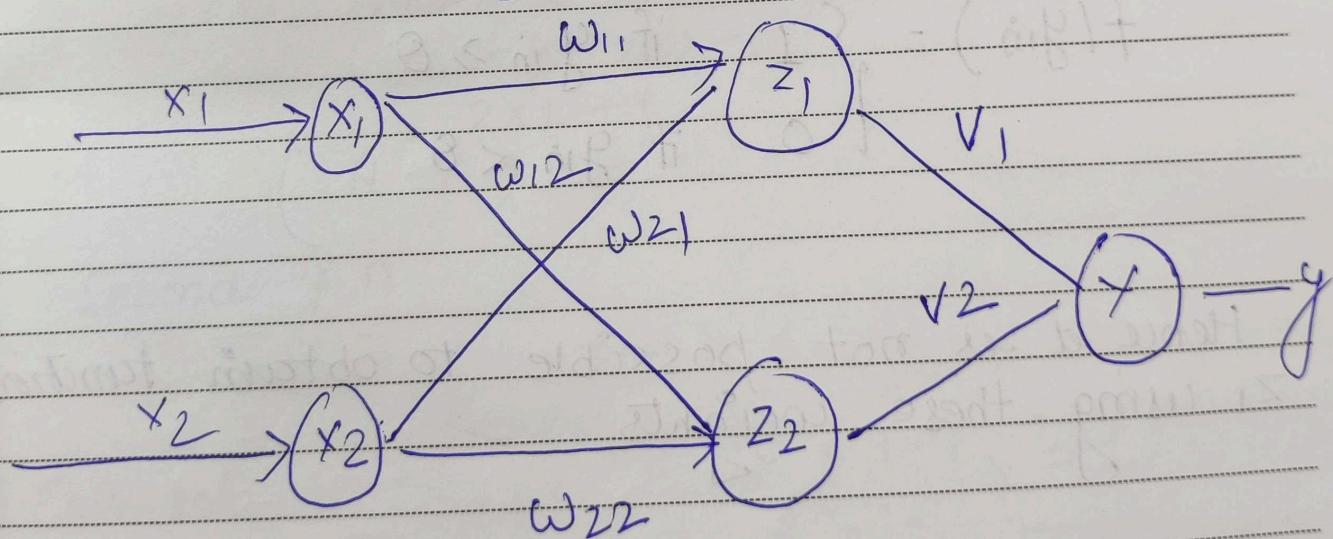
where

$$z_1 = x_1 \bar{x}_2 \quad \text{function 1}$$

$$z_2 = \bar{x}_1 x_2 \quad \text{function 2}$$

$$Y = z_1 \text{ OR } z_2 \quad \text{function 3}$$

A single layer net is not sufficient to represent the XOR function. We need to add an intermediate layer is necessary.



③

### First Function

$$z_1 = x_1 x_2$$

Truth table for function  $z_1$

1 0 1

$$w_{11} = w_{21} = 1$$

$$(0,0) z_{1,in} \quad 0 \times 1 + 0 \times 1 = 0$$

$$(0,1) \quad 0 \times 1 + 1 \times 1 = 1$$

$$(1,0) \quad 1 \times 1 + 0 \times 1 = 1$$

$$(1,1) \quad 1 \times 1 + 1 \times 1 = 2$$

$$f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} \geq 0 \\ 0 & \text{if } y_{in} < 0 \end{cases}$$

Hence it is not possible to obtain function  $z_1$  using these weights

(4)

Assume the weights are initialized to

$$\omega_{11} = 1, \omega_{21} = -1$$

Calculate the net impulse,

$$(0,0) Z_{11n} = 0 \times 1 + 0 \times -1 = 0$$

$$(0,1) Z_{12n} = 0 \times 1 + 1 \times -1 = -1$$

$$(1,0) Z_{11n} = 1 \times 1 + 0 \times -1 = 1$$

$$(1,1) Z_{12n} = 1 \times 1 + 1 \times -1 = 0$$

What should be threshold value

$$\theta = \text{nw} - p$$

$$2 \times 1 - 1$$

$$(\theta = 1)$$

Second  $f^n$

$$Z_2 = x_1, x_2$$

Assume

$$\omega_{12} = \omega_{22} = 1$$

Calculate net impulse

$$(0,0)$$

$$6 \quad *$$

$$\boxed{0 \ 1 \ 1}$$

$$(0,1)$$

$$1 \quad \checkmark$$

} free in

$$(1,0)$$

$$1 \quad \checkmark$$

3 cases

$$(1,1)$$

$$2 \quad \checkmark$$

⑤

$$w_{11} = -1, w_{22} = 1$$

Calculate the net inputs

$$(0,0) = 0 \times -1 + 0 \times 1 = 0$$

$$(0,1) = 0 \times -1 + 1 \times 1 = 1$$

$$(1,0) = 1 \times -1 + 0 \times 1 = -1$$

$$(1,1) = 1 \times -1 + 1 \times 1 = 0$$

$$\theta = 2 - 1 \\ = 1$$

$\theta = 1$  then neuron fires

Third function

$$y = z_1 (\text{OR}) z_2$$

$$\begin{array}{ccccc} x_1 & x_2 & y & z_1 & z_2 \\ \hline 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 1 & 0 & 1 & 1 & 0 \\ 1 & 1 & 0 & 0 & 0 \end{array}$$

0	0	0	0	0
0	1	1	0	1
1	0	1	1	0
1	1	0	0	0

(6)

Truth table

$$y_{in} = 2_1 v_1 + 2_2 v_2$$

Assume the weights are initialized to

$$v_1 = v_2 = 1$$

Calculate the net inputs

$$(0,0) \quad 0 + 0 = 0$$

$$(0,1) \quad 0 + 1 = 1$$

$$(1,0) \quad 1 + 0 = 1$$

$$(1,1) \quad 1 + 1 = 2$$

$$\begin{matrix} 0 \\ 1 \\ 1 \\ 0 \end{matrix}$$

$$f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} \geq \theta \\ 0 & \text{if } y_{in} < \theta \end{cases}$$

 $\theta = 1$ , then the neuron fires

(7)



OR gate

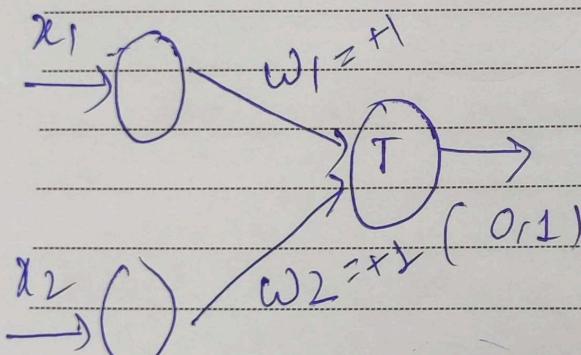
AND gate

 $x_1 \ x_2 \ y$ 

0	0	0
0	1	1
1	0	1
1	1	1

 $x_1 \ x_2 \ y$ 

0	0	0
0	1	0
1	0	0
1	1	1



$$w_1 = +1, w_2 = +1$$

we should set  
threshold?

so that above  
conditions are  
satisfied.

$$w_1 = +1, w_2 = +1$$

so

$$T > 1/2$$

$$(0,0) = 0 \times 1 + 0 \times 1 = 0$$

$$(0,1) = 0 \times 0 + 1 \times 1 = 1$$

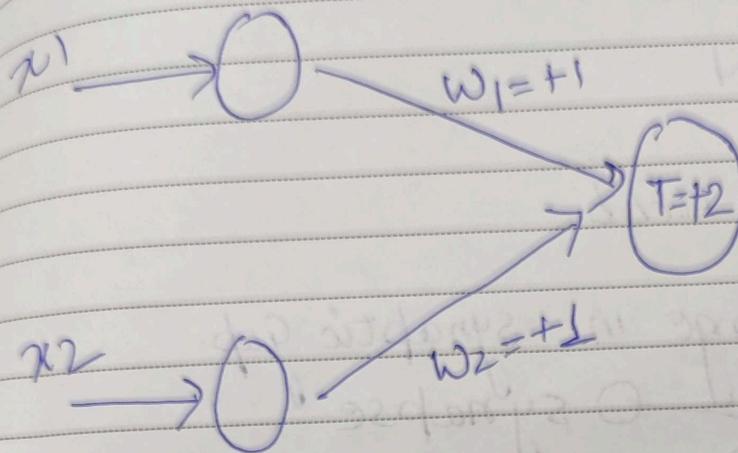
$$(1,0) = 1 \times 1 + 0 \times 0 = 1$$

$$(1,1) = 1 \times 1 + 1 \times 1 = 2$$

$T > 1/2$

Can we put threshold = 1  
and get final answer

(8)



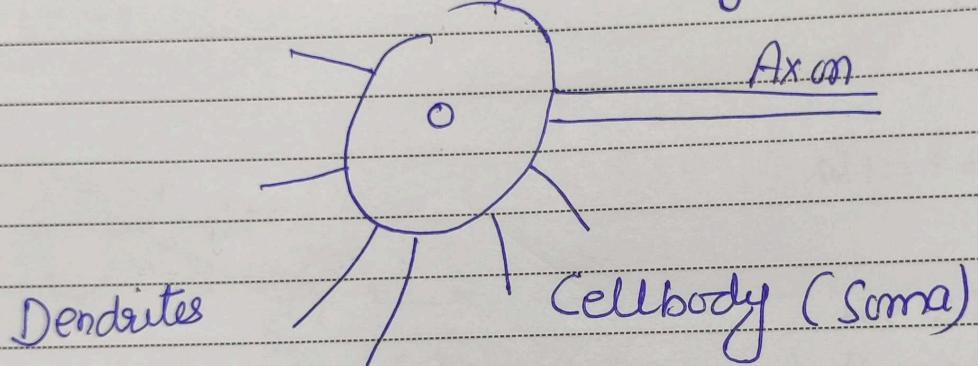
## Hebb Network / Hebbian rule

ANN

In 1949, Donald Hebb

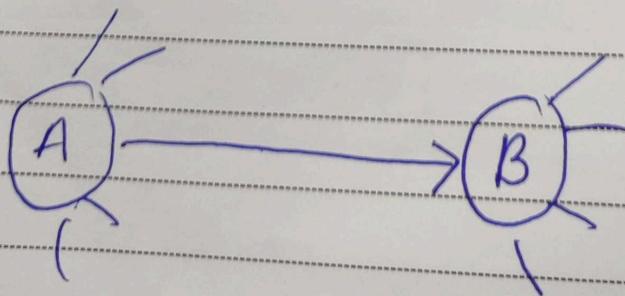
⇒ learning ⇒ change in synaptic gap.

synapse



Hebb rule:

when an axon of cell A is near enough to excite cell B repeatedly / permanently firing it, then growth / metabolic change takes place in both of the cells.





- unsupervised algo  
Pattern association, pattern categorization,  
and pattern classification

Hebb law

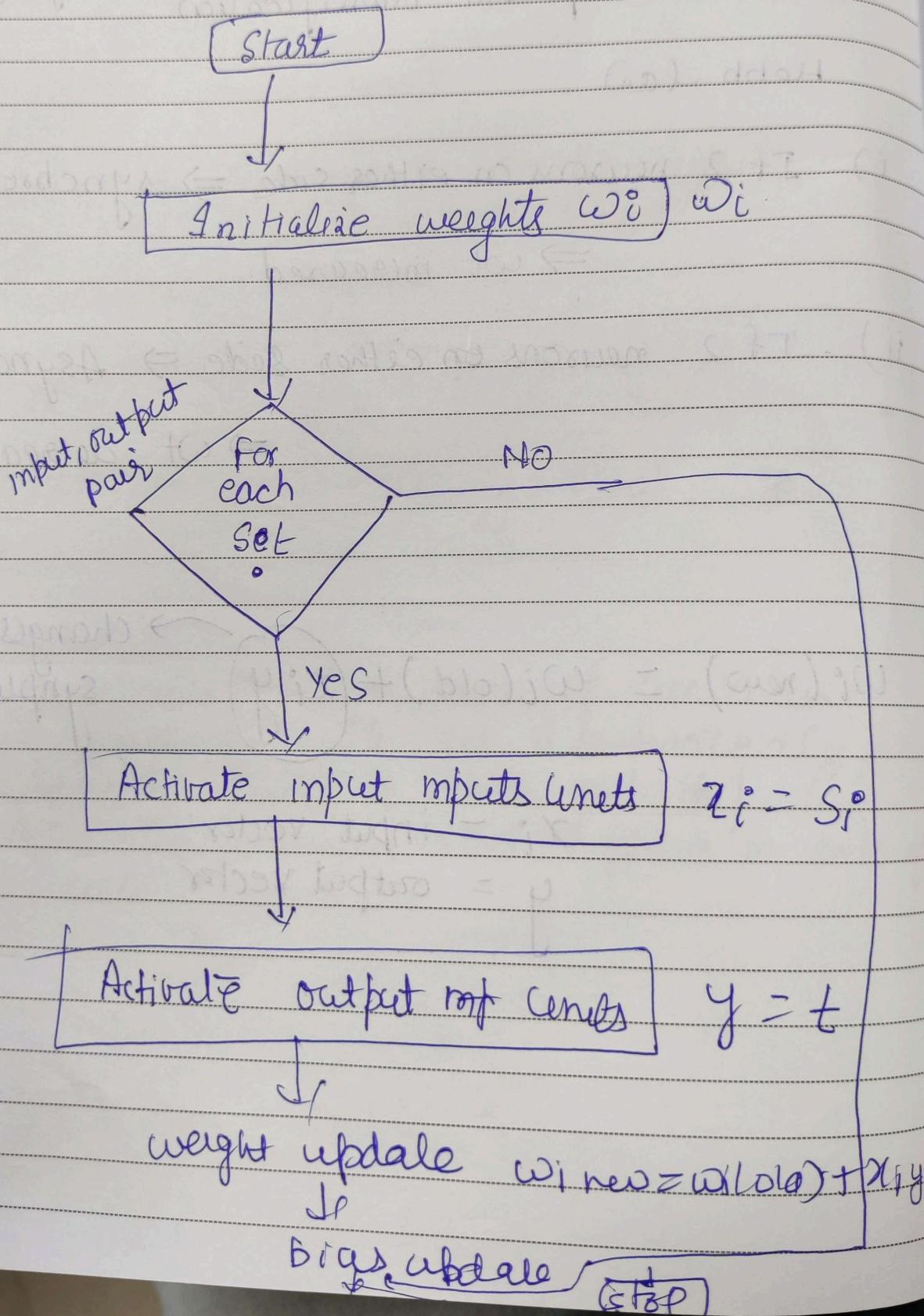
- i) If 2 neurons on either side  $\Rightarrow$  synchronously  
 $\Rightarrow$  wt. increased
- ii) If 2 neurons on either side  $\Rightarrow$  Asynchronously  
 $\Rightarrow$  wt. decreased

$$w_i(\text{new}) = w_i(\text{old}) + (x_i \cdot y) \quad \begin{matrix} \rightarrow \text{changes} \\ \text{synaptic gap} \end{matrix}$$

$$\begin{aligned} x_i &= \text{input vector} \\ y &= \text{output vector} \end{aligned}$$



## Flowchart



## Training Algo

Step 0: Initialize the weights and bias

Step 1 for each training ip and ob pair  
perform step 2 to 4

Step 2  $x_i = s_i$  (activation)

Step 3  $y = f$  (activation)

Step 4 wt update

$$w_i^{\text{new}} = w_i^{\text{old}} + x_i y$$

$$b^{\text{new}} = b^{\text{old}} + y$$

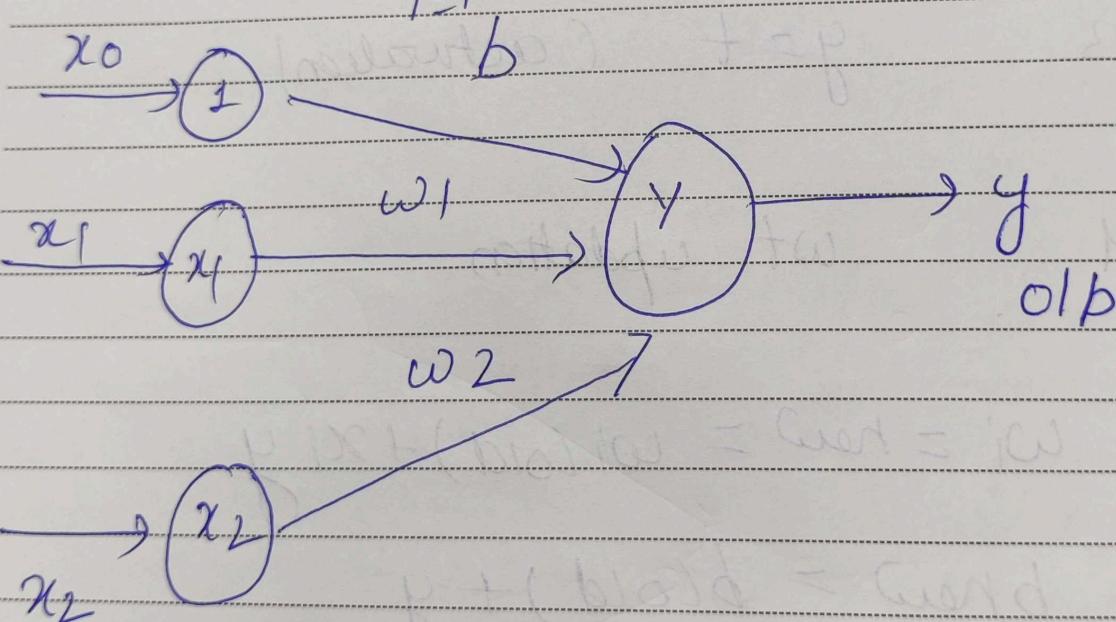
## Linear Separability

A decision line is drawn to separate positive and negative responses.

$$y_m = b + \sum_{j=1}^n x_j w_j$$

Requirement for the response of the net is

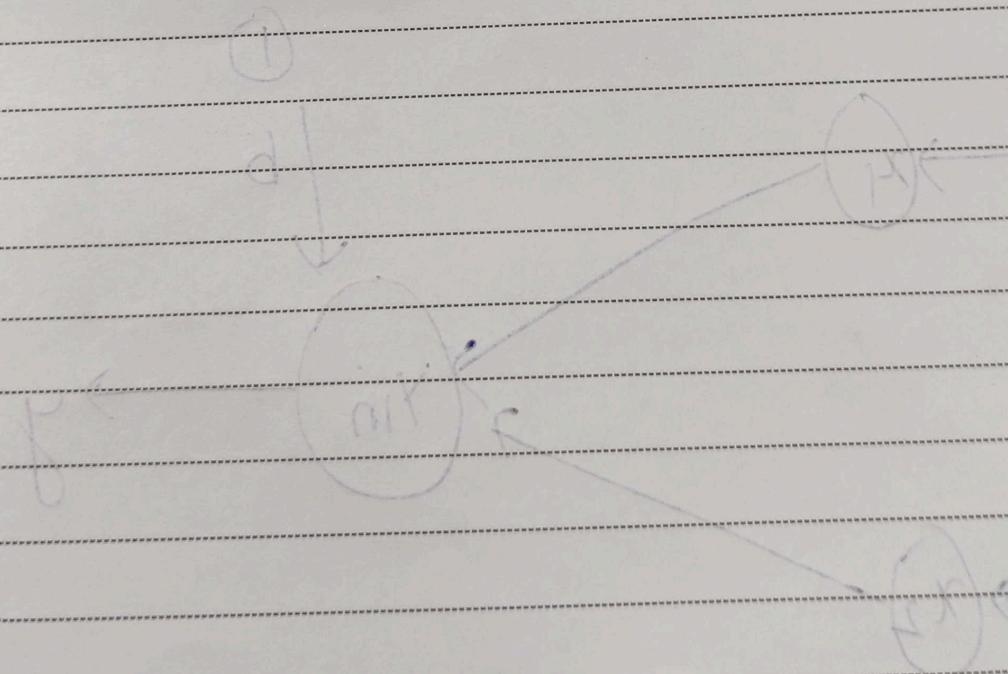
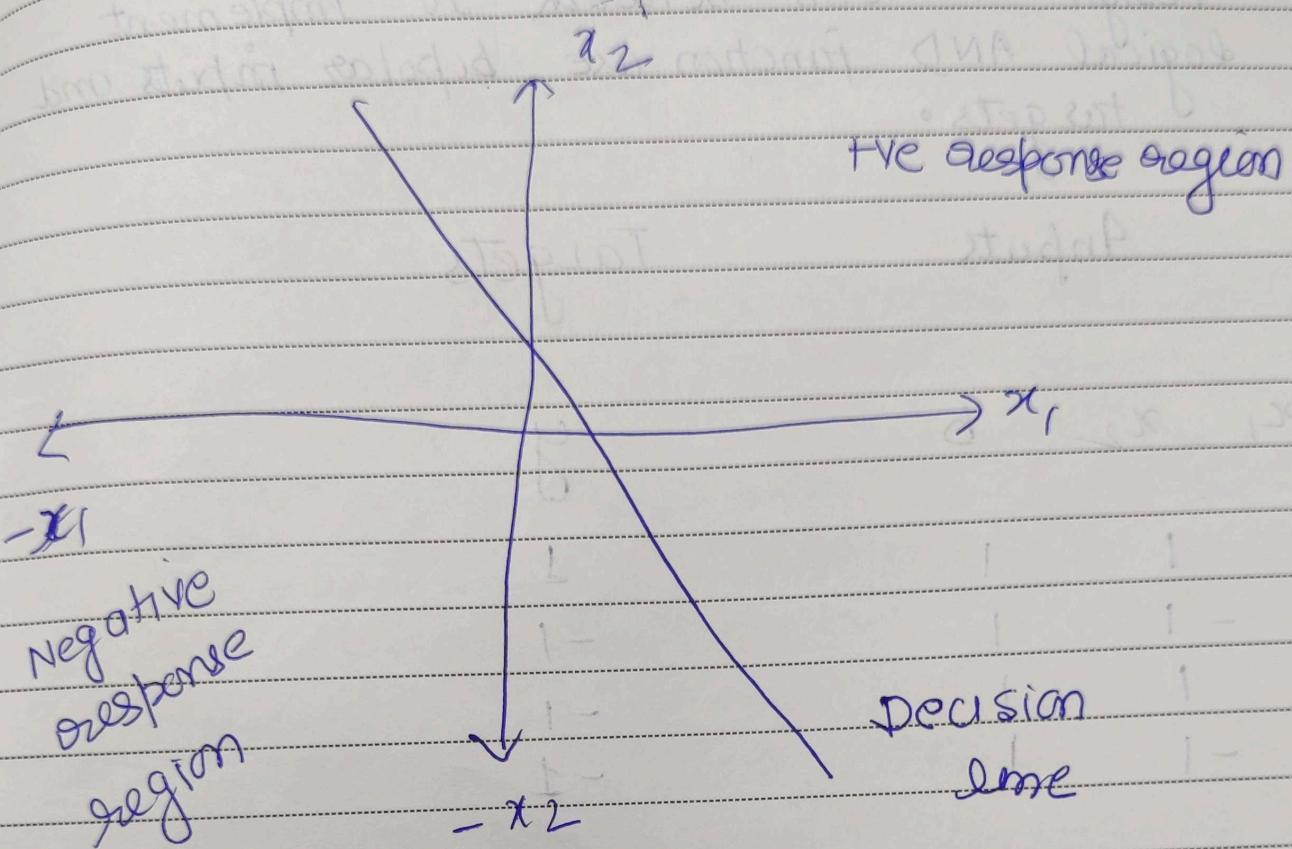
$$b + \sum_{i=1}^n x_i w_i = 0$$



$$b + x_1 w_1 + x_2 w_2 = 0$$

$$x_2 = -\frac{w_1}{w_2}$$

$$x_1 = -\frac{b}{w_2}$$



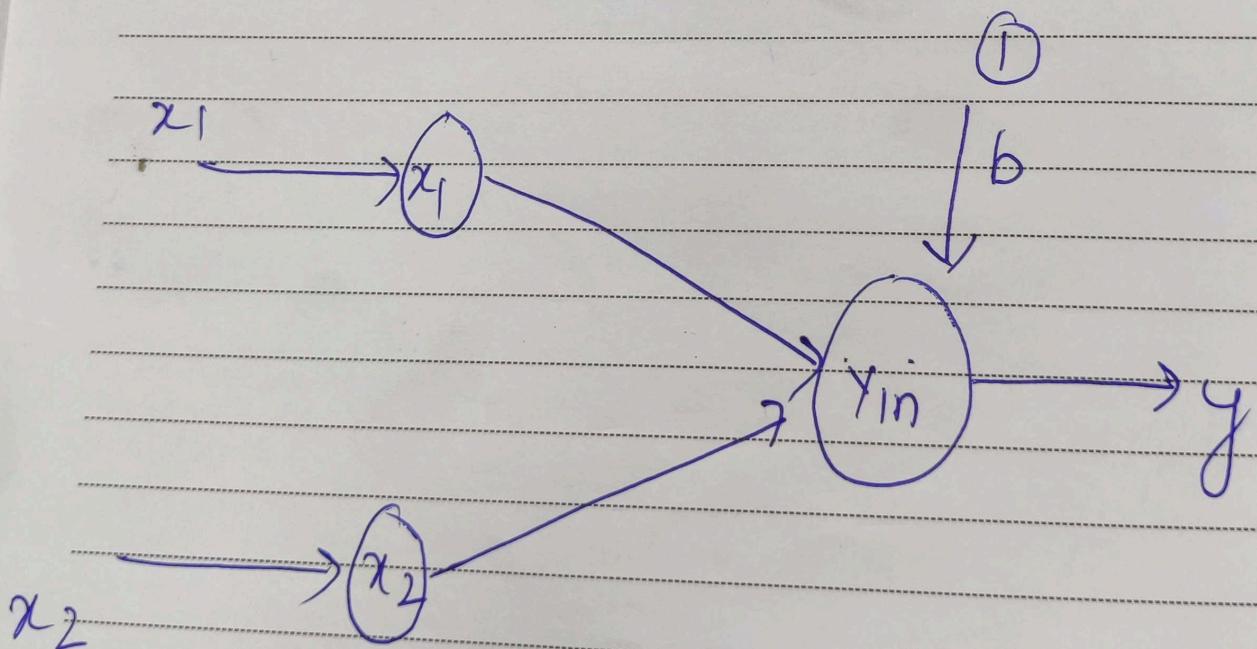


Q. Design a Hebb network to implement logical AND function use bipolar inputs and targets.

Inputs

Targets

$x_1$	$x_2$	$b$	$y$
1	1	1	1
1	-1	1	-1
-1	1	1	-1
-1	-1	1	-1



$$\omega_{i\text{ new}} = \omega_{i\text{ (old)}} + \Delta \omega$$

xi y

$$y = b + x_1 w_1 + x_2 w_2$$

$$w_1 = w_2 = b = 0$$

We have to train

Inputs			y	weight changes			New weight		
$x_1$	$x_2$	b	g	$\Delta w_1$	$\Delta w_2$	$\Delta b$	$w_{1\text{ new}}$	$w_{2\text{ new}}$	$b_{\text{new}}$
1	1	1	1	1	1	1	0+1 =1	6+1 =7	0+1 =1
1	-1	1	-1	-1	1	-1	1+(-1) =0	1+1 =2	1+(-1) =0
+1	1	1	-1	1	-1	-1	0+1 =1	2+(-1) =1	0+(-1) =-1
-1	-1	1	-1	1	1	-1	1+1 =2	1+1 =2	-1+(-1) =-2

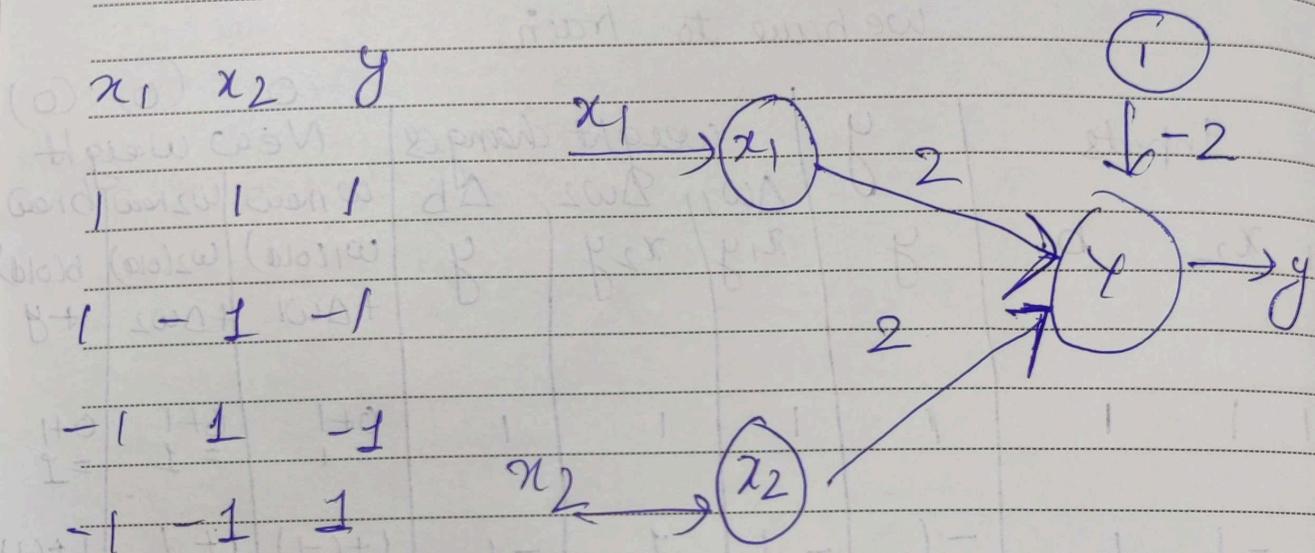


Final weights are

$$w_1 = 2$$

$$w_2 = 2$$

$$b = -2$$



(ii)

$$y = b + x_1 w_1 + x_2 w_2$$

$$= -2 + (1)(2) + (1)(2)$$

$$= -2 + 2 + 2$$

$$y = 2$$

Design a Hebb Network, find the weights required to perform the classification of the given input pattern.

+ . .	+ . +
+ . .	+ . +
+ + +	+ + +

'L'

$$Z^1 = 1$$

'U'

$$U^1 = 0$$

The pattern is shown as  $3 \times 3$  matrix form in the squares. The "+" symbol represent the value "1" and empty squares indicates "-1". Consider "L" belongs to class so target value is 1 and "U" does not belong to the members of class (so target value is 0).

Step 1

 $w_1$ 

I

 $x_1 \ x_2 \ x_3$ 

1 -1 -

1 -1

Target

y  
1  
-1

Inputs

 $x_1 \ x_2 \ x_3 \ x_4 \ x_5 \ x_6 \ x_7 \ x_8 \ x_9$   
 1 1 1 1 1 1 1 1 1
 

Pattern

L U

 $w_1$   
(0) $w_1(0|0)$   
 $+ \Delta w_1$ 

0 + 1 = 1

1 + -1 = 0

Step 1

$$w_1 = w_2 = w_3 = w_4 = w_5 = w_6 = w_7 = w_8 = w_9 = 0$$

$$b = 0$$

Inputs									b	y	weight changes			
$x_1$	$x_2$	$x_3$	$x_4$	$x_5$	$x_6$	$x_7$	$x_8$	$x_9$		$\Delta w_1$	$\Delta w_2$	$\Delta w_3$	$\Delta w_4$	
1	-1	-1	1	-1	-1	1	1	1	1	$x_5y$	$x_2y$	$x_3y$	$x_4y$	
1	-1	1	1	-1	1	1	1	1	-1	1	-1	-1	1	

$\Delta w_5$	$\Delta w_6$	$\Delta w_7$	$\Delta w_8$	$\Delta w_9$	$\Delta b$
$x_5y$	$x_6y$	$x_7y$	$x_8y$	$x_9y$	
-1	-1	1	1	1	1
1	-1	-1	-1	-1	-1

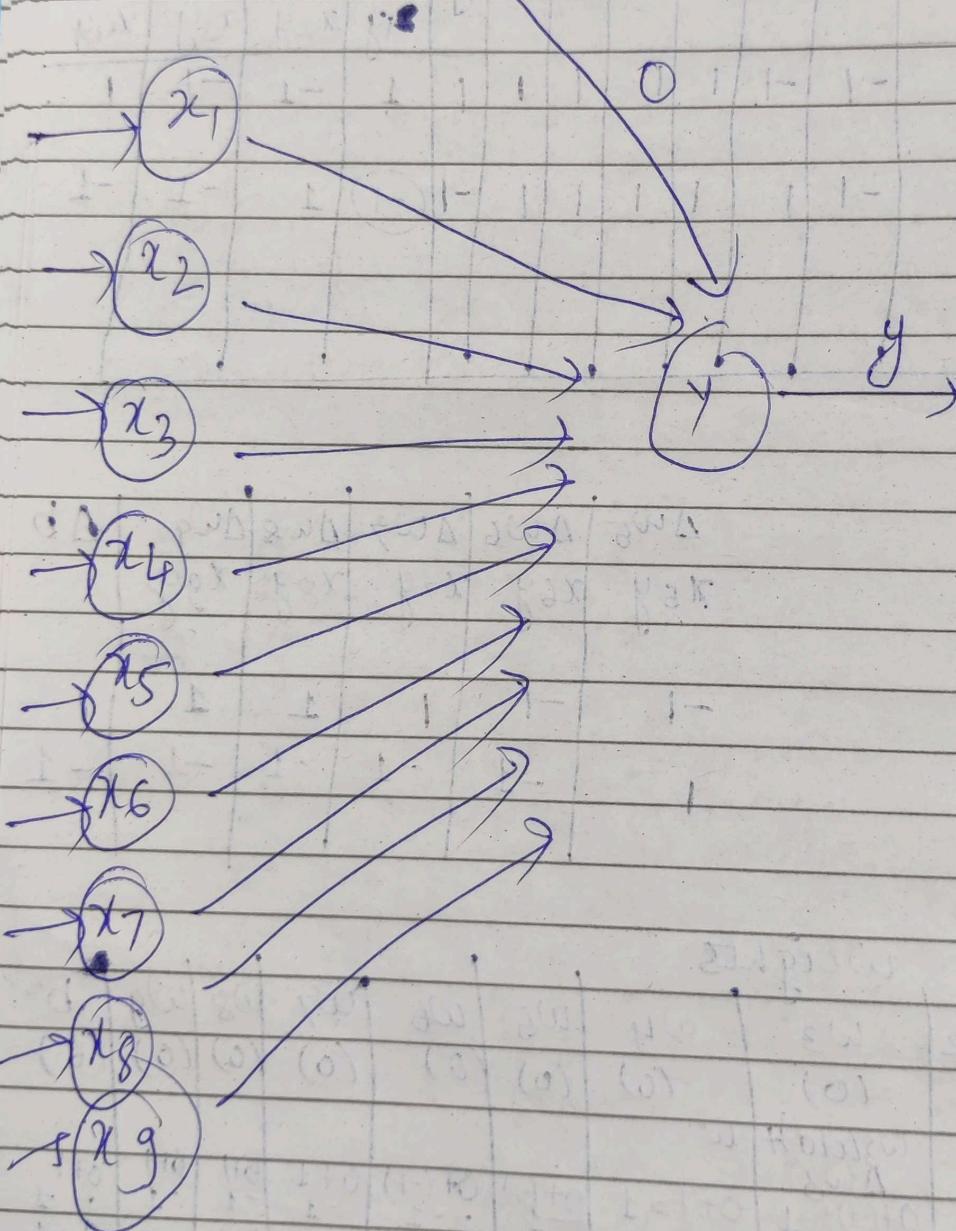
New weights									B
$w_1$ (0)	$w_2$ (0)	$w_3$ (0)	$w_4$ (0)	$w_5$ (0)	$w_6$ (0)	$w_7$ (0)	$w_8$ (0)	$w_9$ (0)	
$w_1(0) + \Delta w_1$ $0 + 1 = 1$	$w_2(0) + \Delta w_2$ $0 + (-1) = -1$	$w_3(0) + \Delta w_3$ $0 + (-1) = -1$	$w_4(0)$	$w_5(0)$	$w_6(0)$	$w_7(0)$	$w_8(0)$	$w_9(0)$	
$1 + 1 = 2$	$-1 + (-1) = -2$	$-1 + (-1) = -2$	$0 + 1 = 1$	$0 + (-1) = -1$	$0 + 1 = 1$	$0 + (-1) = -1$	$0 + 1 = 1$	$0 + (-1) = -1$	
$1 + -1 = 0$	$-1 + 1 = 0$	$-1 + -1 = -2$	$1 - 1 = 0$	$-1 + 0 = -1$	$-1 + 1 = 0$	$-1 + -1 = -2$	$1 - 1 = 0$	$0 + 0 = 0$	

wnew

$$[0 \ 0 \ -2 \ 0 \ 0 \ -2 \ 0 \ 0 \ 0]$$

$$b=0$$

(1)



$$1 - 1 - 1 \mid 1 - 1 - 1 \mid \mid \mid b = 0$$

$$1x_0 + -1x_0 + -1x_{-2} + 1x_0 + -1x_0 + -1x_{-2} \\ + 1x_0 + 1x_0 + 1x_0 + 0$$

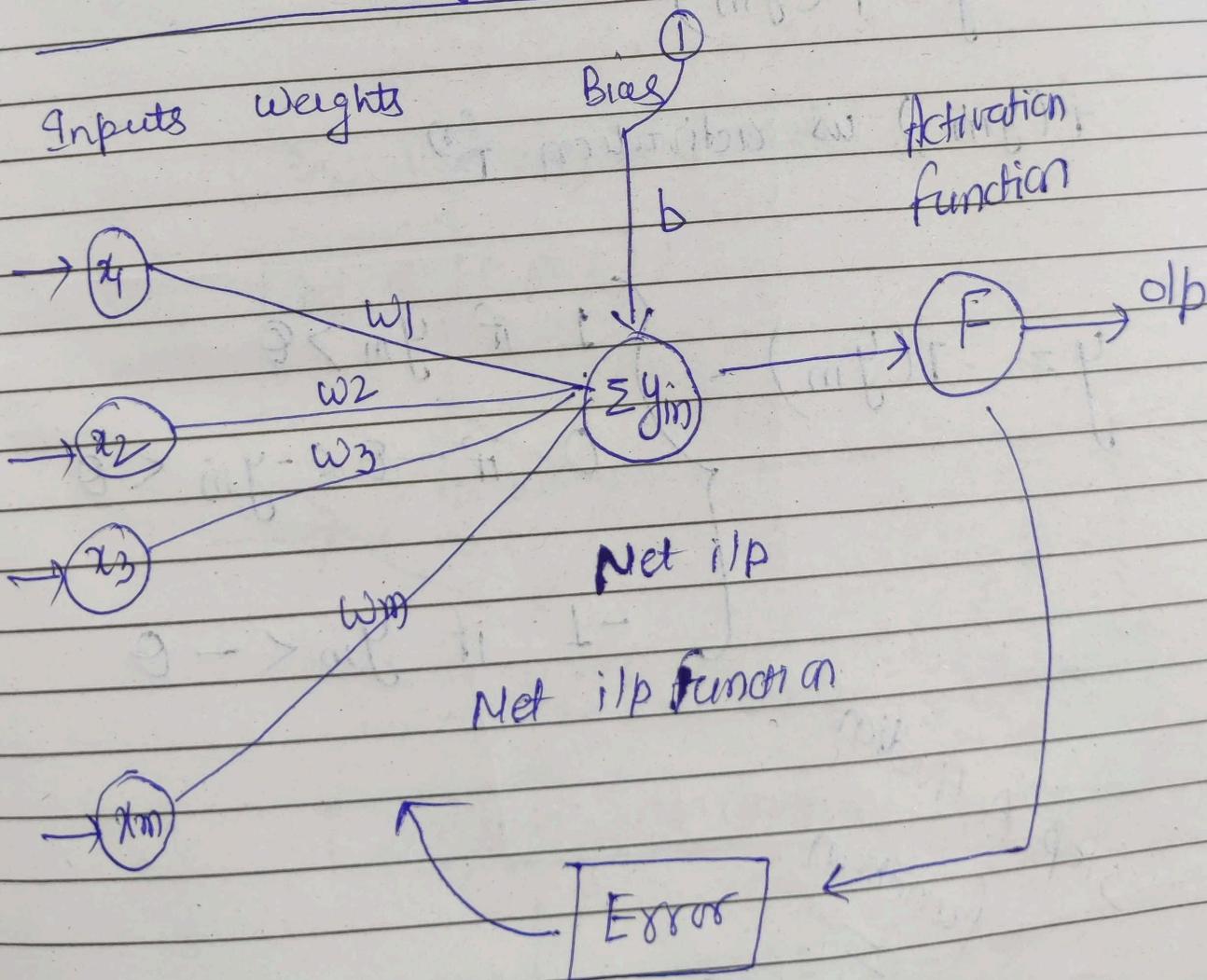
$$y = 4 \quad \checkmark$$

$$[1 - 1 \mid 1 - 1 \mid \mid \mid \mid] \quad \text{Second set} \\ b = 0$$

$$y = -2 - 2 = -4 \quad (-\text{ve value})$$

## Supervised Learning Network

- Perceptron networks come under single layer feed forward networks → simple Perceptrons
- Simplest form of Neural Network is able to classify data into two classes.
- Introduced by Frank Rosenblatt in 1957



2 types of Perceptrons

i) Single layers

(ii) Multi Layers

- 2 or more layers

$$y_{in} = x_1 w_1 + x_2 w_2 - \dots - x_n w_n + b$$

$$y = f(y_{in})$$

$f(y_{in})$  is activation function

$$y = f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} > \theta \\ 0 & \text{if } -\theta \leq y_{in} < \theta \\ -1 & \text{if } y_{in} < -\theta \end{cases}$$

Step Activation  
function

the weight updation

if  $y \neq t$  then

learning rate

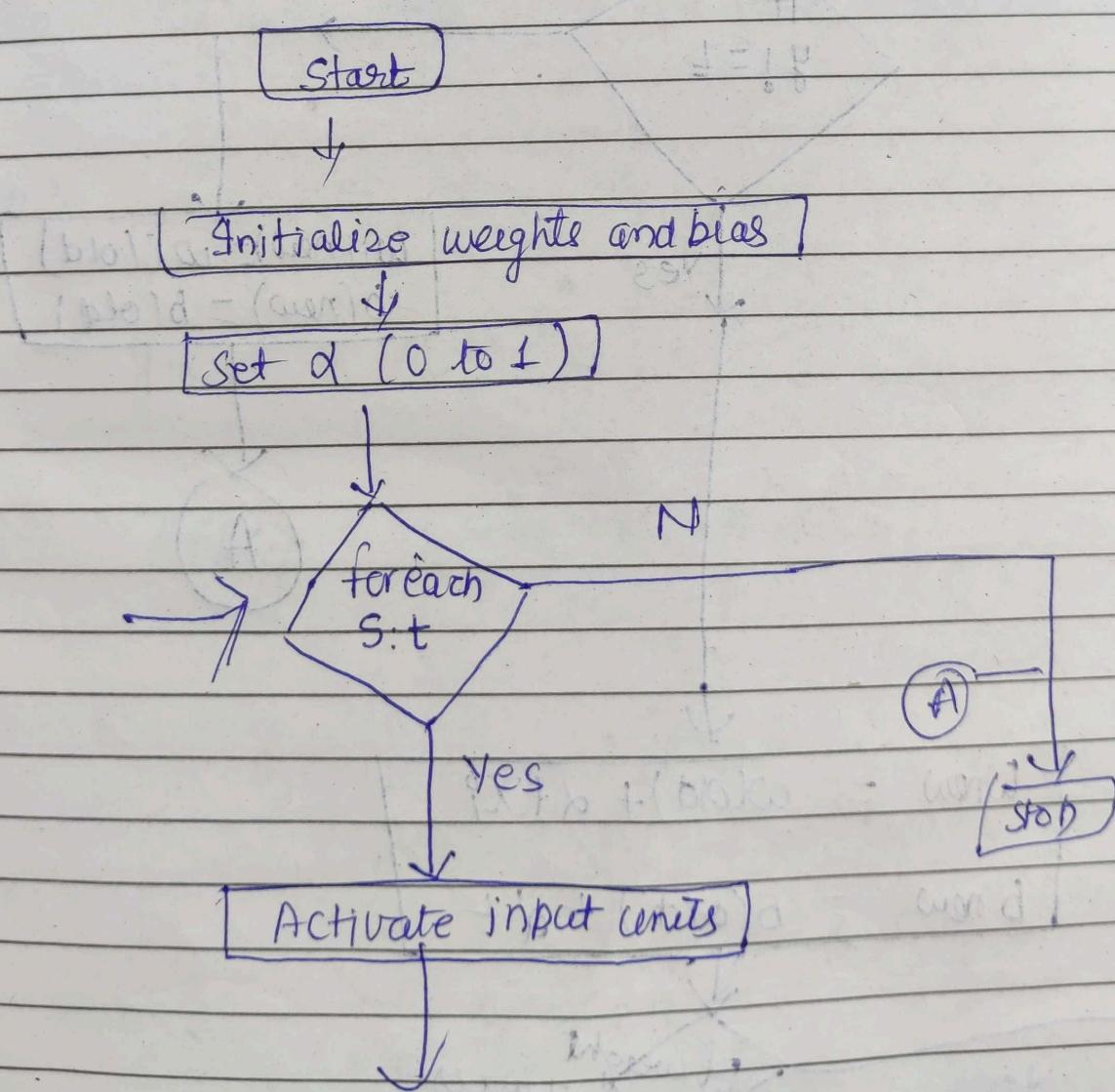
$$w(\text{new}) = w(\text{old}) + d \cdot t \cdot x$$

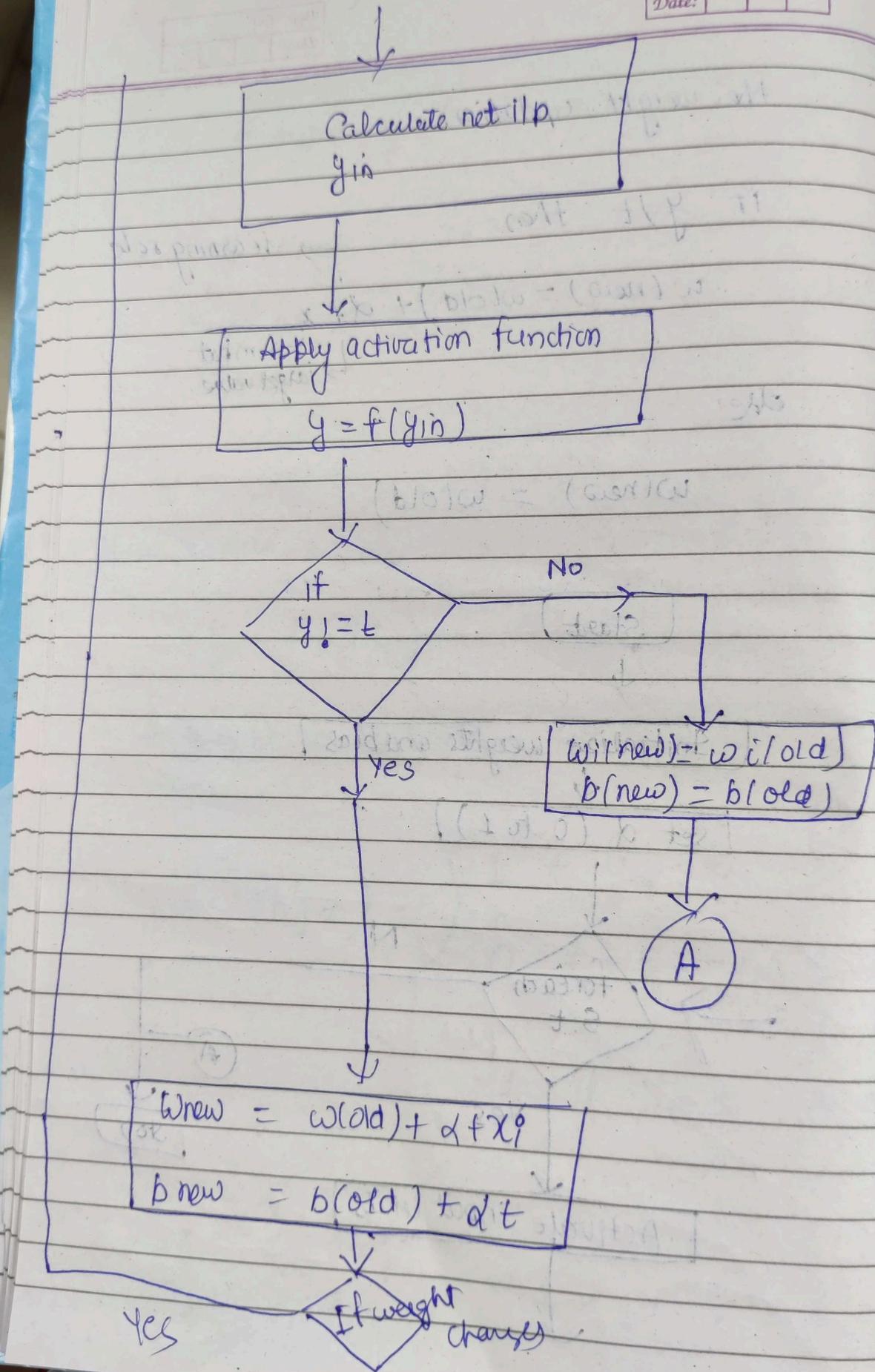
$d$  without mid point  $\rightarrow m_{\text{bat}}$

$t$  target value

else

$$w(\text{new}) = w(\text{old})$$





Step 0

Step 1

Step 2

Step 3

## (Training Algorithm.)

Step 0 :

Initialize weights and bias

$$\alpha = 1$$

Step 1 Perform step 2-5 until final stopping condition is false

Step 2 Perform step 3-4 for each training pair

Step 3 Calculate the o/p

$$y_{in} = b + \sum_{i=1}^n x_i w_i$$

Apply activation function

$$y = f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} > \theta \\ 0 & \text{if } -\theta \leq y_{in} \leq \theta \\ -1 & \text{if } y_{in} < -\theta \end{cases}$$

Step 4 : weight and bias adjustment

if  $y \neq t$  then

$$w_i(\text{new}) = w_i(\text{old}) + \alpha t x_i$$

$$b(\text{new}) = b(\text{old}) + \alpha t(1)$$

else

$$w_i(\text{new}) = w_i(\text{old})$$

$$b(\text{new}) = b(\text{old})$$

Step 5

$$w_i x_i + b = \text{out}$$

$$3 \times \text{out} - 3 \times b = (\text{out}) + \gamma$$

$$3 \rightarrow \text{out} - b + \gamma$$

## Testing Algorithm

Step 0:

The initial weights to be used here  
are taken from training algo

Step 1: For each training ip vector  $x$  to be  
classified

perform steps 2-3

Step 2 Set activations

$$y_{in} = b + \sum_{i=1}^n x_i w_i$$

$$y = f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} > \theta \\ 0 & \text{if } -\theta \leq y_{in} \leq \theta \\ -1 & \text{if } y_{in} < -\theta \end{cases}$$

Problem:

Implement AND function using  
Perceptron networks for bipolar inputs and targets

Epoch	Inputs	Target	Calculated weight changes			New weights
			$\Delta \omega_1$	$\Delta \omega_2$	$\Delta b$	
1	$x_1 = 1$ $x_2 = 1$	1	$-1$	$-1$	-1	$\boxed{-1}$
2	$x_1 = -1$ $x_2 = 1$	-1	$-1$	$-1$	-1	$\boxed{-1}$
3	$x_1 = 1$ $x_2 = -1$	-1	$-1$	$-1$	-1	$\boxed{-1}$
4	$x_1 = -1$ $x_2 = -1$	-1	$-1$	$-1$	-1	$\boxed{-1}$

New weights	$w_1$	$w_2$	$b$	$b_{old} + \Delta b$
	$w_{old} + \Delta w_1$	$w_{old} + \Delta w_2$	$b_{old} + \Delta b$	
$0+1$	$0+1$	$0+1$	$0+1$	$=1$
$1+1=0$	$1+1=2$	$1-1=0$	$0-1=-1$	
$0+1$	$2-1$	$0-1$	$-1$	$=1$

$$w_1 = -1, w_2 = 1, b = -1$$

Epoch 2

Input  
 $x_1$   
 $x_2$

Target

Net input  
 $y_1 = \omega_1 x_1 + \omega_2 x_2 + b$

Calculated  
Output  
 $y_1 = 0$

Desired  
Output  
 $y_1 = -1$

Weight  
change  
 $\Delta w_1 = -1$ ,  
 $\Delta w_2 = 1$ ,  
 $\Delta b = -1$

$$\begin{array}{l}
 \text{Input} \quad x_1 \quad x_2 \quad b \\
 \text{Target} \quad -1 \\
 \text{Net input} \quad \omega_1 x_1 + \omega_2 x_2 + b \\
 \text{Calculated Output} \quad y_1 = 0 \\
 \text{Desired Output} \quad y_1 = -1 \\
 \text{Weight change} \quad \Delta w_1 = -1, \Delta w_2 = 1, \Delta b = -1 \\
 \text{Error} \quad y_1 - \text{Desired} = -1 - (-1) = 0 \\
 \text{Update rule} \quad \omega_{1,2} \leftarrow \omega_{1,2} + \eta \cdot \Delta \omega_{1,2} \\
 \text{New weights} \quad \omega_1 = -1 + 1 = 0, \omega_2 = 1 + 1 = 2, b = -1 + -1 = -2 \\
 \text{Final output} \quad y_1 = \omega_1 x_1 + \omega_2 x_2 + b = 0 \cdot 1 + 2 \cdot 1 + -2 = 0
 \end{array}$$

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$$E_{\text{final}} = \omega_1 = 0, \omega_2 = 1, b = -2$$

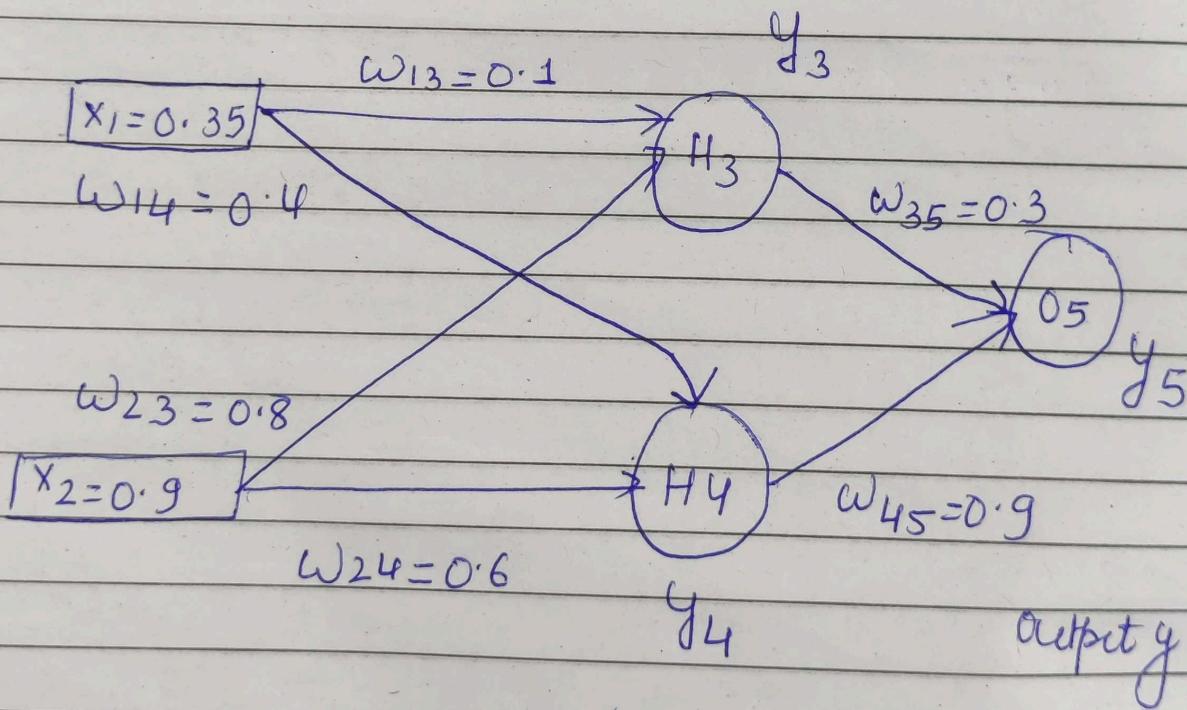
$$F_{\text{max}} \text{ or } b = \omega_1 = 4, \omega_2 = -1$$
$$F_{\text{max}} \text{ or } b = \omega_1 = \omega_2 \neq 1, b = -1$$

$y_1 = b + \omega_1 x + \omega_2 x^2$

## Back Propagation

Assume that the neurons have a sigmoid activation function, perform a forward pass and a backward pass on the network.

Assume that the actual output of  $y$  is 0.5 and learning rate is 1. Perform another forward pass.



→ Forward pass: compute output for  $y_3, y_4$  and  $y_5$

$$a_j = \sum_i w_{ij} * x_i + (2.0 * b_0)$$

$$y_j = F(a_j) = \frac{1}{1 + e^{-a_j}}$$

$$a_1 = (w_{13} * x_1) + (w_{23} * x_2)$$

$$= (0.1 * 0.35) + (0.8 * 0.9) = 0.755$$

$$y_3 = f(a_1) = \frac{1}{1 + e^{-0.755}} = 0.68$$

$$a_2 = w_{14} * x_1 + w_{24} * x_2$$

$$= 0.4 * 0.35 + 0.6 * 0.9 = 0.68$$

$$y_4 = f(a_2) = \frac{1}{1 + e^{-0.68}}$$

$$= 0.6637$$

$$\begin{aligned}
 a_3 &= (\omega_{35} * y_3) + (\omega_{45} * y_4) \\
 &= (0.3 * 0.68) + (0.9 * 0.6637) \\
 &= 0.801
 \end{aligned}$$

$$\begin{aligned}
 y_5 &= f(a_3) = \frac{1}{1+e^{-0.801}} \\
 &= 0.69 \text{ (Network output)}
 \end{aligned}$$

$$\text{Error} = Y_{\text{target}} - y_5$$

$$= -0.19$$

Try to update weights

- Each weight changed by

$$\Delta w_{ji} = n \delta_j o_i$$

$$\delta_j = o_j (1 - o_j) (t_j - o_j) \text{ if } j \text{ is an output unit}$$

$$\delta_j = o_j (1 - o_j) \sum_k \delta_k w_{kj} \eta \text{ if } j \text{ is a hidden unit}$$

where  $\eta$  is a constant called learning rate

$t_j$  is the correct teacher output for unit  $j$

$\delta_j$  is the error measure for unit  $j$

Backward pass

compute  $\delta_3$ ,  $\delta_4$  and  $\delta_5$

for output unit

$$\delta_5 = y(1-y)(y_{\text{target}} - y)$$

$$= 0.69(1-0.69)(0.5-0.69)$$

$$= -0.0406$$

For hidden unit

$$\delta_3 = y_3(1-y_3) w_{35} * \delta_5$$

$$= 0.68(1-0.68) * (0.3 * -0.406)$$

$$= -0.00265$$

$$\delta_4 = y_4(1-y_4) w_{45} * \delta_5$$

$$= -0.6637 * (1-0.6637) * (0.9 * (-0.0406))$$

$$= -0.0082$$

Compute New weights

$$\Delta w_{ji} = \eta \delta_j$$

$$\Delta w_{45} = \eta \delta_5 y_4 = 1 * -0.0406 * 0.6637 = -0.0269$$

$$w_{45}(\text{new}) = \Delta w_{45} + w_{45}(\text{old}) \\ = -0.0269 + 0.9 = 0.8731$$

$$\Delta w_{14} = \eta \delta_4 x_1 = 1 * -0.0082 * 0.35 = -0.00287$$

$$w_{14}(\text{new}) = \Delta w_{14} + w_{14}(\text{old}) = -0.00287 + 0.4 \\ = 0.3971$$

## Evolutionary Algorithms

The algorithms, which follow some biological and physical behaviours:-

Biologic behaviours:-

1. Genetic and Evolution → Genetic Algorithms (GA)
2. Behaviour of ant colony → Ant Colony optimization (ACO)
3. Human nervous system → ~~Artificial~~ Artificial Neural Network (ANN)

In addition to that there are some algorithms inspired by some physical behaviours:-

Physical behaviours:-

- 1) Annealing process → Simulated Annealing (SA)
- 2) Swarming of particle → Particle Swarm optimization (PSO)
- 3) Learning → Fuzzy logic (FL)

## Genetic Algorithm

It is a subset of evolutionary algo-

rmor's subset division of optimization

1) Ant Colony Optimization

2) Swarm Particle Optimization

Models biological processes :-

1) Genetics

2) Evolution

Initial population  $\leftarrow$  initial random search

(MMA) Selection Process

Randomly select traits of initial pop

Individuals based on selected traits

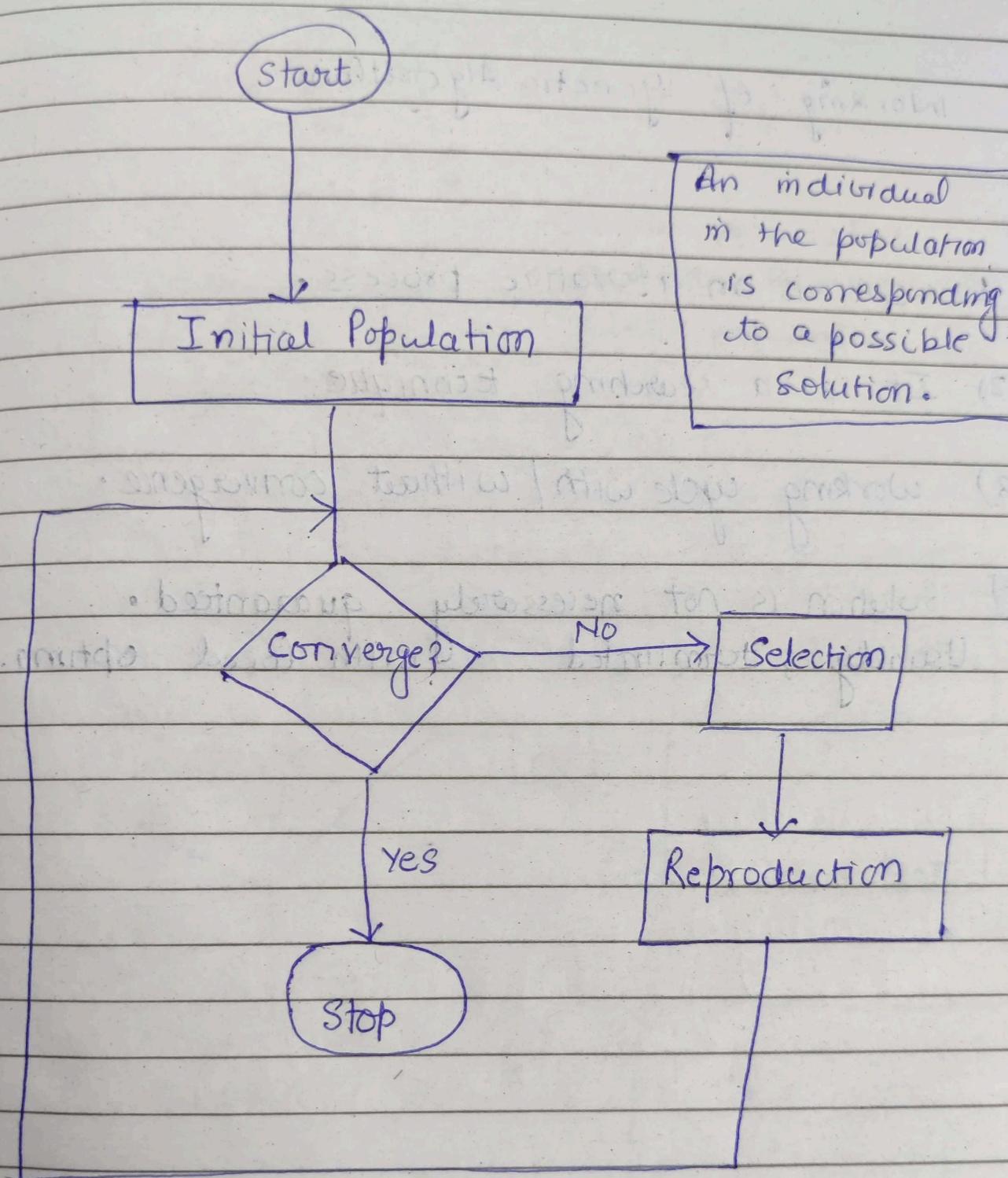
→ crossover operation

Individuals  $\leftarrow$  random parents

(M2) mutation

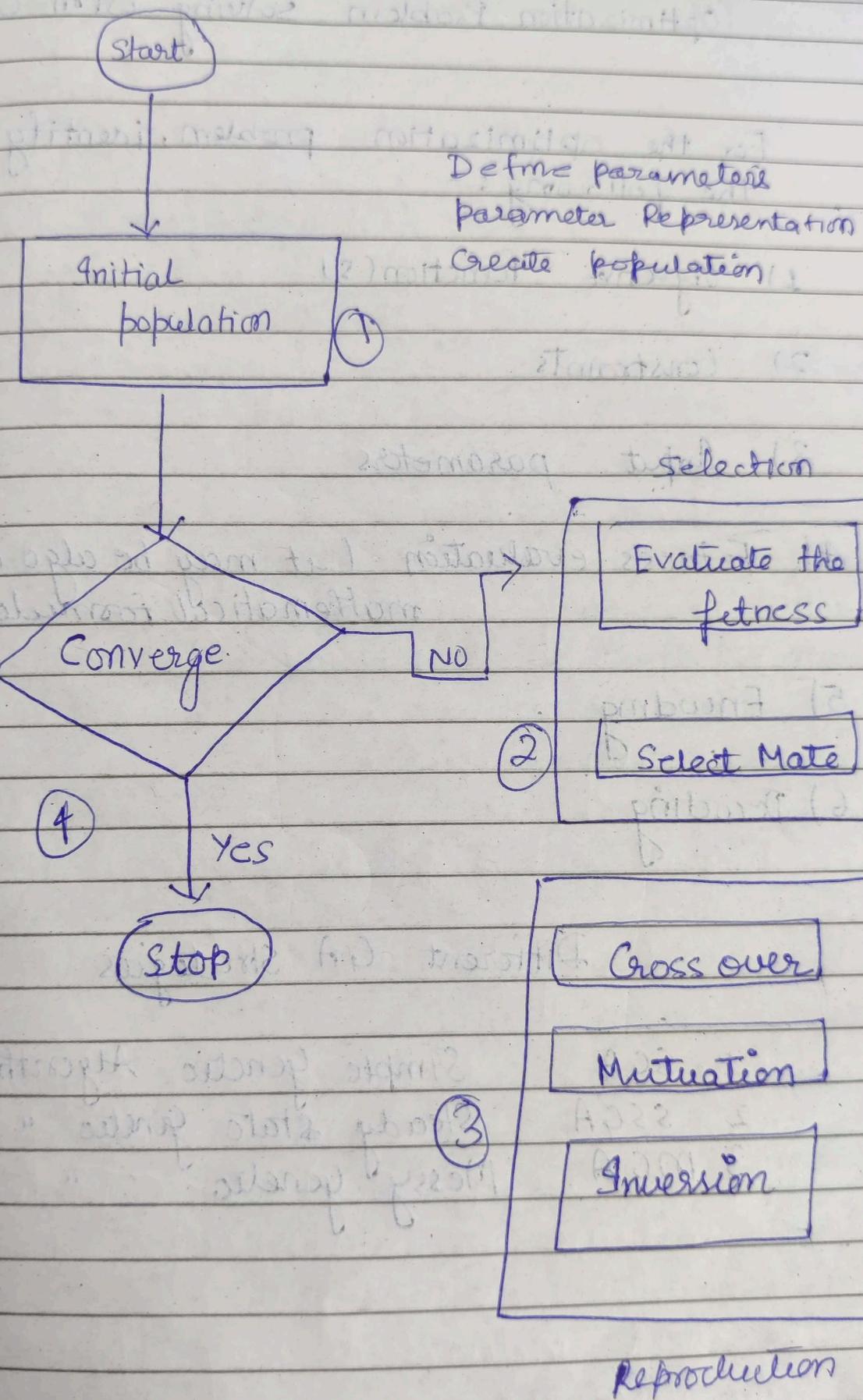
Individuals  $\leftarrow$  altered random parents

→ selection process



## Working of Genetic Algorithm

- 1) GA is an iterative process.
- 2) It is a searching technique.
- 3) Working cycle with / without convergence.
- 4) Solution is not necessarily guaranteed.  
Usually, terminated with local optima.



## (Optimization Problem solving with GA)

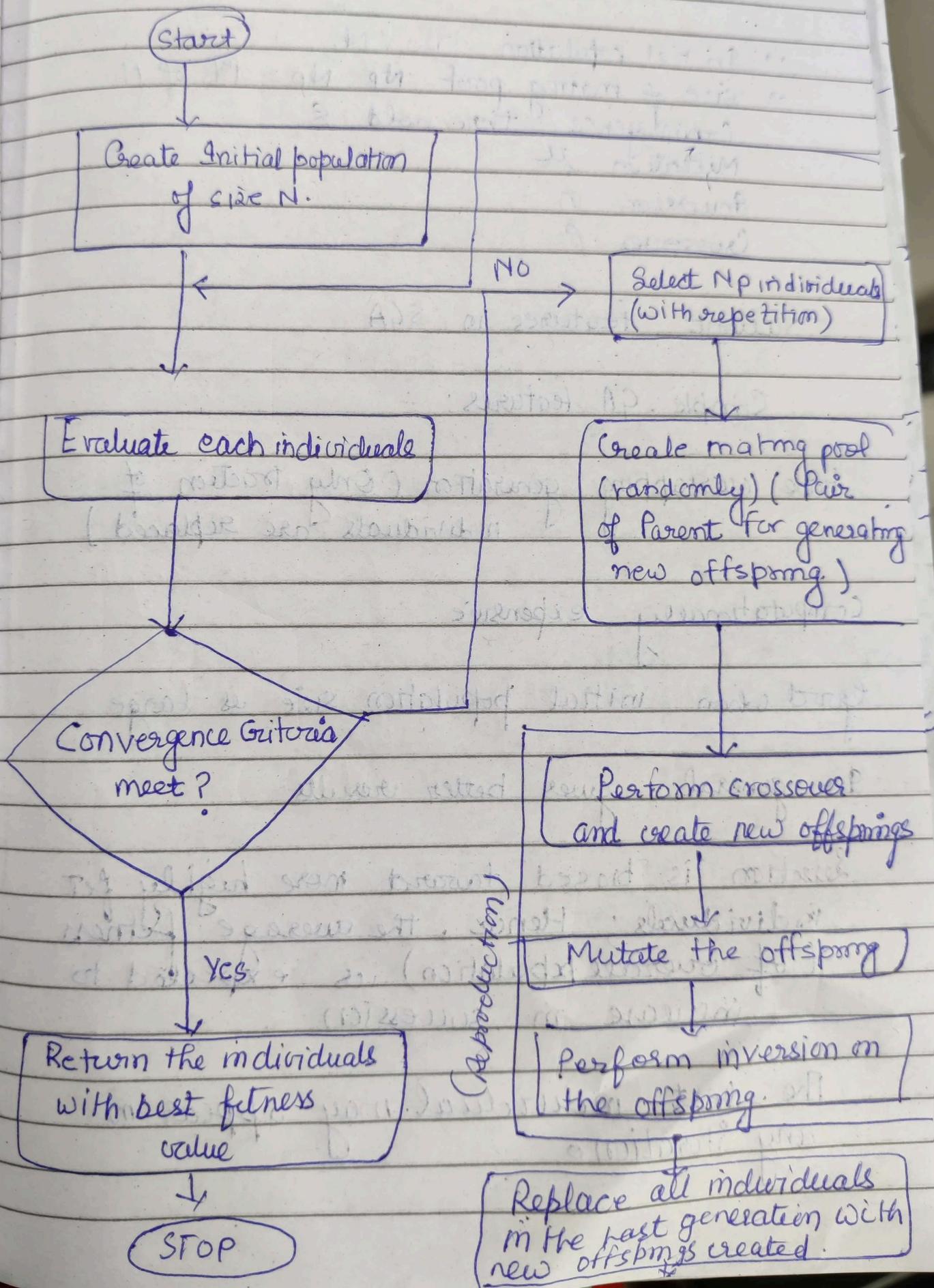
For the optimization problem, identify the following :-

- 1) Objective function(s)
- 2) Constraints
- 3) Input parameters
- 4) Fitness evaluation (it may be algo or mathematical formula)
- 5) Encoding
- 6) Decoding

### Different GA Strategies

1. SGA Simple Genetic Algorithm
2. SSGA Steady State Genetic "
3. MGA Messy Genetic "

## Simple GA



~~genetic algo'~~  
~~Probabilistic~~  
~~search;~~  
~~random~~  
~~search;~~

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## SGA parameters

- Initial population size :  $N$
- Size of mating pool  $N_p$ :  $N_p = P\%$  of  $N$
- Convergence threshold  $S$
- Mutation  $\mu$
- Inversion  $\eta$
- Crossovers  $\rho$

## Salient features in SGA

### Simple GA features:

Have overlapping generation (Only fraction of individuals are replaced)

Computationally expensive

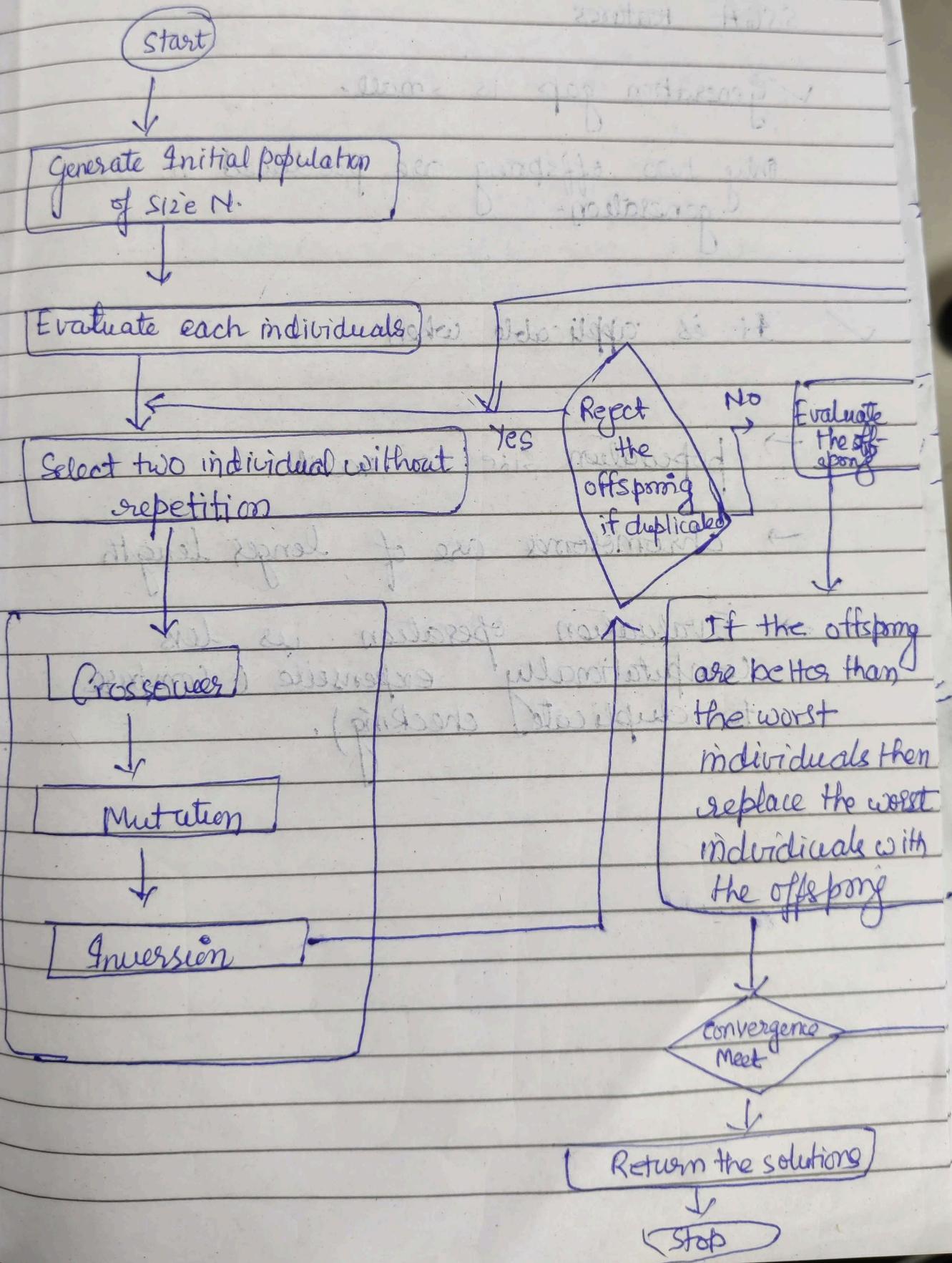
Good when initial population size is large

In general, gives better results

Selection is biased toward more highly fit individuals; Hence, the average fitness (of overall population) is expected to increase in succession.

The best individual may appear in any iteration.

## Steady State Genetic Algorithm (SSGA)



## Lecture - 16

Following are the GA operators in Genetic Algorithms:-

Encoding

Convergence test

Mating pool

Fitness Evaluation

Crossover

Mutation

Inversion

(1)

(2)

## Encoding Schemes

- ↳ Binary encoding      Binary GA
- ↳ Real value encoding
- ↳ Order encoding      Permutated GA
- ↳ Tree encoding

(1) Individual      is a single solution  
(2) Population      set of individuals