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Assignment-1

AI1110: Probability and Random Variables Indian Institute of Technology, Hyderabad

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Question:

One card is drawn from a well-shuffled deck of 52 cards. Find the probability of getting

- 1) A king of red colour
- 2) A face card
- 3) A red face card
- 4) The jack of hearts
- 5) A spade
- 6) The queen of diamonds

Solution:

Consider 3 random variables *X*, *Y* and *Z*, which represent the Colour, Class and Value of each card respectively.

The pmfs of each random variable are:

$$\Pr(X = i) = \frac{1}{2} \ \forall \ i \in [0, 1] \tag{1}$$

$$\Pr(Y = i) = \frac{1}{4} \ \forall \ i \in [1, 4]$$
 (2)

$$\Pr(Z = i) = \frac{1}{13} \ \forall \ i \in [1, 13]$$
 (3)

Also, the random variable pairs X,Z and Y,Z are independent.

Event	Value of X	Value of Y	Value of Z
Draw Red King	1	N/A	3
Draw Face Card	N/A	N/A	1,2 or 3
Draw Red Face Card	1	N/A	1,2 or 3
Draw Hearts Jack	N/A	3	1
Draw Spade	N/A	4	N/A
Draw Diamonds Queen	N/A	1	2
	TABLE 6		

VALUES OF X,Y,Z FOR EACH EVENT

Probability of drawing a King of Red colour:

$$Pr(X = 1, Z = 3) = Pr(X = 1) \times Pr(Z = 3)$$
$$= \frac{1}{2} \times \frac{1}{13} = \frac{1}{26}$$
(4)

2) Probability of drawing a Face Card:

$$Pr(Z = 1, 2, 3) = F_Z(3) = \frac{3}{13}$$
 (5)

3) Probability of drawing a Red Face Card:

$$Pr(X = 1, Z = 1, 2, 3) = Pr(X = 1) \times F_Z(3)$$
$$= \frac{1}{2} \times \frac{3}{13} = \frac{3}{26}$$
(6)

4) Probability of drawing the Jack of Hearts:

$$Pr(Y = 3, Z = 1) = Pr(Y = 3) \times Pr(Z = 1)$$
$$= \frac{1}{4} \times \frac{1}{13} = \frac{1}{52}$$
(7)

5) Probability of drawing a Spade:

$$\Pr(Y = 4) = \frac{1}{4} \tag{8}$$

6) Probability of drawing the Queen of Diamonds:

$$Pr(Y = 1, Z = 2) = Pr(Y = 1) \times Pr(Z = 2)$$
$$= \frac{1}{4} \times \frac{1}{13} = \frac{1}{52}$$
(9)