7-7.2-25

EE24BTECH11027 - G.V.Satwika

Problem statement

Find the equation of a circle passing through the point (7,3) having radius 3 units and whose centre lies on the line y = x - 1.

Solution I

| Variable | Description | Value |
|----------|----------------------|--|
| Р | point vector | $\begin{pmatrix} 7 \\ 3 \end{pmatrix}$ |
| _u | centre of the circle | $\binom{k}{k-1}$ |
| r | radius of the circle | 3 units |

Table: Parameters

Solution II

From the given information, the following equations can be formulated using the circle equation

$$||x||^2 + 2u^{\top}x + f = 0 \tag{1}$$

$$||P||^2 + 2u^{\top}P + f = 0 \tag{2}$$

$$||u||^2 - f = r^2 \tag{3}$$

From (2) and (3)

$$||P||^2 + 2u^{\top}P + ||u||^2 = r^2$$
 (4)

Substituting the values of u,P and r,

$$2k^2 - 2k + 1 + 6 - 20k + 7^2 + 3^2 - 3^2 = 0$$
 (5)

$$2k^2 - 22k + 56 = 0 (6)$$

$$k = 7, 4 \tag{7}$$

Solution III

resulting in circles with centres

$$-u = \begin{pmatrix} 7 \\ 6 \end{pmatrix} or \begin{pmatrix} 4 \\ 3 \end{pmatrix} \tag{8}$$

C Code I

```
#include <stdio.h>
#include <stdlib.h>
3 #include <math.h>
4 #include "/home/g-v-satwika/matgeo/codes/msoft/libs/matfun.h"
5 #include "/home/g-v-satwika/matgeo/codes/msoft/libs/geofun.h"
6
7 int main() {
      double **P = createMat(1, 2); // Create a point vector for P
8
     P[0][0] = 7; // x-coordinate of point P
     P[0][1] = 3; // y-coordinate of point P
10
      double r = 5; // Given radius
12
      // Final equation: 2k^2 - 22k + 40 = 0
       double **CM=createMat(3,1); //coefficient matrix
14
       CM[0][0]=2: // Coefficient for k^2
15
       CM[1][0] = -22; // Coefficient for k
16
       CM[2][0] = 56: //constant term
17
18
     // Solve the quadratic equation to get two values of k
```

C Code II

```
double **K=createMat(2,1);
      K=Matquad(CM[0][0],CM[1][0],CM[2][0]);
      double k1=K[0][0]:
      double k2=K[1][0];
      // Create two separate vectors for the two centers
24
      double **center1 = createMat(1, 2);
      double **center2 = createMat(1, 2);
26
      center1[0][0] = k1; // Center 1: (k1, k1-1)
28
      center1[0][1] = k1-1;
29
      center2[0][0] = k2; // Center 2: (k2, k2-1)
      center2[0][1] = k2-1;
      // Write the centers to a file
34
      FILE *file = fopen("circle.txt", "w");
      if (file == NULL) {
36
          fprintf(stderr, "Error opening file for writing.\n");
37
          return 1;
```

C Code III

```
39
      }
40
      // Write the two centers to the file
      fprintf(file, "C1(%.2f, %.2f)\n", center1[0][0], center1[0][1]);
41
      fprintf(file, "C2(%.2f, %.2f)\n", center2[0][0], center2[0][1]);
42
      fprintf(file, "P(7.00,3.00)");
43
      fclose(file);
44
      // Free the allocated memory
45
     /* for (int i = 0; i < 1; i++) {
46
          free(center1[i]);
47
          free(center2[i]);
48
          free(P[i]);
49
      free(center1):
      free(center2);
      free(P);*/
      freeMat(center1,1);
54
      freeMat(center2,1);
      freeMat(P,1);
56
      freeMat(CM,3);
```

C Code IV

```
freeMat(K,2);
return 0;
}
```

Python Code I

```
1 import numpy as np
2 import matplotlib.pyplot as plt
 # Function to extract points from the file
 def read_points_from_file(filename):
     points = []
6
      with open(filename, 'r') as file:
7
          for line in file:
8
              # Split line by parentheses and commas
              line = line.strip()
              point = line[line.find('(')+1 :
     line.find(')')].split(',')
              points.append((float(point[0]), float(point[1])))
12
      return points
13
15 # Function to plot a circle given the center and radius
def plot_circle(ax, center, radius, color, label):
```

Python Code II

```
circle = plt.Circle(center, radius, color=color, fill=False,
     label=label)
     ax.add_artist(circle)
18
# Function to label a point with its coordinates
def label_point(ax, point, label):
     ax.annotate(f'{label} {point}', (point[0], point[1]),
     textcoords="offset points", xytext=(10,-10), ha='center')
# Reading points from 'circle.txt'
points = read_points_from_file('circle.txt')
c1 = points[0] # First center point
c2 = points[1] # Second center point
p = points[2] # Point on the circle
30 # Given radius
radius = 3
```

Python Code III

```
# Create the plot
fig, ax = plt.subplots()
36 # Plot the circles
plot_circle(ax, c1, radius, 'blue', 'Circle 1')
plot_circle(ax, c2, radius, 'green', 'Circle 2')
40 # Plot the points c1, c2, and p
ax.plot(c1[0], c1[1], 'bo', label='Center 1')
ax.plot(c2[0], c2[1], 'go', label='Center 2')
ax.plot(p[0], p[1], 'ro', label='Point P')
# Label the points with their coordinates
label_point(ax, c1, 'c1')
17 label_point(ax, c2, 'c2')
label_point(ax, p, 'P')
```

Python Code IV

```
49
50 # Set plot limits to ensure the full circles are shown
si # Find the min and max coordinates to include the entire circle
s2 all_x = [c1[0] - radius, c1[0] + radius, c2[0] - radius, c2[0] +
     radius]
ss all_y = [c1[1] - radius, c1[1] + radius, c2[1] - radius, c2[1] +
     radius]
# Set limits with some padding
ax.set_x \lim(\min(all_x) - 1, \max(all_x) + 1)
ax.set_ylim(min(all_y) - 1, max(all_y) + 1)
# Set equal scaling and labels
ax.set_aspect('equal', 'box')
ax.set_xlabel('X')
ax.set_ylabel('Y')
ax.legend()
```

Python Code V

```
# Show the plot
plt.grid(True)
plt.savefig("circle_plot.png");
plt.show()
```

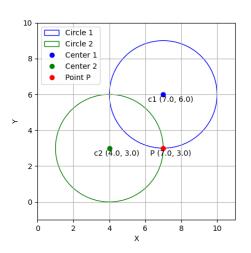


Figure: Plot of y(x)