## EE24BTECH11027 - satwikagv

## **Question:**

Find the equation of a circle passing through the point (7,3) having radius 3 units and whose centre lies on the line y = x - 1.

## solution:

Variable	Description
P	point vector
- <i>и</i>	centre of the circle
r	radius of the circle

TABLE 0: Variables Used

From the given information, the following equations can be formulated using the circle equation

$$||x||^2 + 2u^{\mathsf{T}}x + f = 0 \tag{0.1}$$

$$||P||^2 + 2u^{\mathsf{T}}P + f = 0 \tag{0.2}$$

$$u = \begin{pmatrix} -k \\ 1 - k \end{pmatrix} \tag{0.3}$$

$$||u||^2 - f = r^2 \tag{0.4}$$

(0.5)

where

$$p = \binom{7}{3}, r = 3 \tag{0.6}$$

(0.7)

From (0.2) and (0.4)

$$||P||^2 + 2u^{\mathsf{T}}P + ||u||^2 = r^2 \tag{0.8}$$

(0.9)

Substituting from (0.3) and numerical values,

$$k^{2} + (1 - k)^{2} + 2(-k \quad 1 - k)\binom{7}{3} + ||P||^{2} - r^{2} = 0$$
 (0.10)

$$2k^2 - 2k + 1 + 6 - 20k + 7^2 + 3^2 - 3^2 = 0 ag{0.11}$$

$$2k^2 - 22k + 56 = 0 ag{0.12}$$

$$k = 7, 4$$
 (0.13)

(0.14)

resulting in circles with centres

$$-u = \begin{pmatrix} 7 \\ 6 \end{pmatrix} or \begin{pmatrix} 4 \\ 3 \end{pmatrix} \tag{0.15}$$

(0.16)

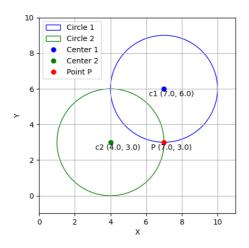


Fig. 0.1: circles passing through point P(7,3)