EE24BTECH11027 - satwikagv

Question:

Find the equation of a circle passing through the point (7,3) having radius 3 units and whose centre lies on the line y = x - 1.

solution: From the given information, the following equations can be formulated using

Variable	Description	Value
P	point vector	(7,3)
- <i>и</i>	centre of the circle	(k, k - 1)
r	radius of the circle	3 units

TABLE 0: Variables Used

the circle equation

$$||x||^2 + 2u^{\mathsf{T}}x + f = 0 \tag{0.1}$$

$$||P||^2 + 2u^{\mathsf{T}}P + f = 0 \tag{0.2}$$

$$||u||^2 - f = r^2 \tag{0.3}$$

From (0.2) and (0.3)

$$||P||^2 + 2u^{\mathsf{T}}P + ||u||^2 = r^2 \tag{0.4}$$

Substituting from u and numerical values,

$$k^{2} + (1 - k)^{2} + 2\left(-k \quad 1 - k\right)\binom{7}{3} + ||P||^{2} - r^{2} = 0$$
(0.5)

$$2k^2 - 2k + 1 + 6 - 20k + 7^2 + 3^2 - 3^2 = 0 (0.6)$$

$$2k^2 - 22k + 56 = 0 (0.7)$$

$$k = 7, 4$$
 (0.8)

resulting in circles with centres

$$-u = \binom{7}{6} or \binom{4}{3} \tag{0.9}$$

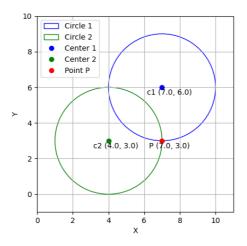


Fig. 0.1: circles passing through point P(7,3)