## EE24BTECH11027 - satwikagv

## **Question:**

Find the equation of a circle passing through the point (7,3) having radius 3 units and whose centre lies on the line y = x - 1.

## **Solution:**

Variable	Description	Value
P	point vector	$\binom{7}{3}$
- <i>u</i>	centre of the circle	$\binom{k}{k-1}$
r	radius of the circle	3 units

TABLE 0: Variables Used

From the given information, the following equations can be formulated using the circle equation

$$||x||^2 + 2u^{\mathsf{T}}x + f = 0 \tag{0.1}$$

$$||P||^2 + 2u^{\mathsf{T}}P + f = 0 \tag{0.2}$$

$$||u||^2 - f = r^2 \tag{0.3}$$

From (0.2) and (0.3)

$$||P||^2 + 2u^{\mathsf{T}}P + ||u||^2 = r^2 \tag{0.4}$$

Substituting the values of u,P and r,

$$2k^2 - 2k + 1 + 6 - 20k + 7^2 + 3^2 - 3^2 = 0 ag{0.5}$$

$$2k^2 - 22k + 56 = 0 ag{0.6}$$

$$k = 7, 4$$
 (0.7)

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resulting in circles with centres

$$-u = \binom{7}{6} or \binom{4}{3} \tag{0.8}$$

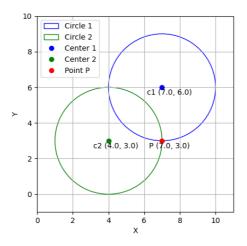


Fig. 0.1: circles passing through point P(7,3)