

Heap

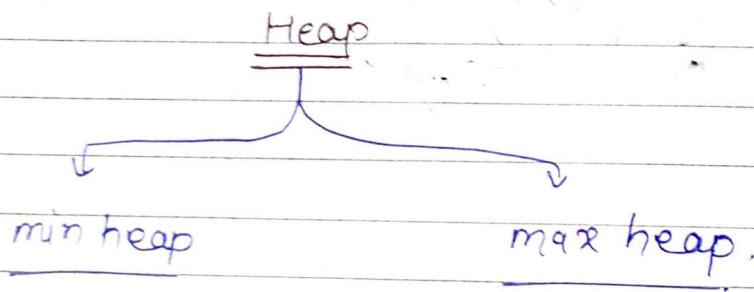


2.)

## Heap Introduction and Identification

### Identification

- (1) K.
- (2) Smallest / largest.



~~CEP~~

K + smallest  $\rightarrow$  max.

K + largest  $\rightarrow$  min.

T.C  $\Rightarrow$   $n \log k$

$n \log n \rightarrow n \log k$ .

## CODE

(1) Max heaps

```
priority_queue<int> maxh;
```

(2) Min heaps

```
priority_queue<int, vector<int>, greater<int>> minh;
```

If we want to store pairs then,

At global:

1, 15
1, 12
0, 11

```
#define pair<int, pair<int, int>> ppi;
```

6

We can replace int with ppi in heap..

2.]

$k^{\text{th}}$  smallest Element.

Given,

$$\text{arr}[2] = 7, 10, 4, 3, 20, 15$$

$$k = 3$$

$$[\text{O/P} = 7]$$

Approach 1)

Sort the array and return  
 $\text{arr}[k-1]$

But the

T.C  $\rightarrow n \log n$

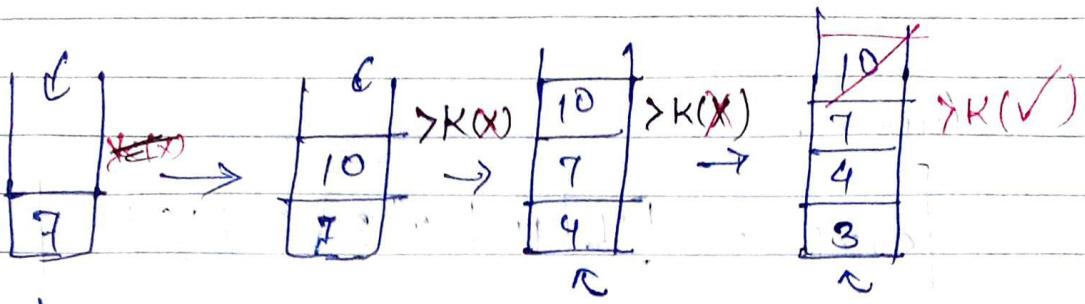
we can reduce it  
by using heap

Approach 2)

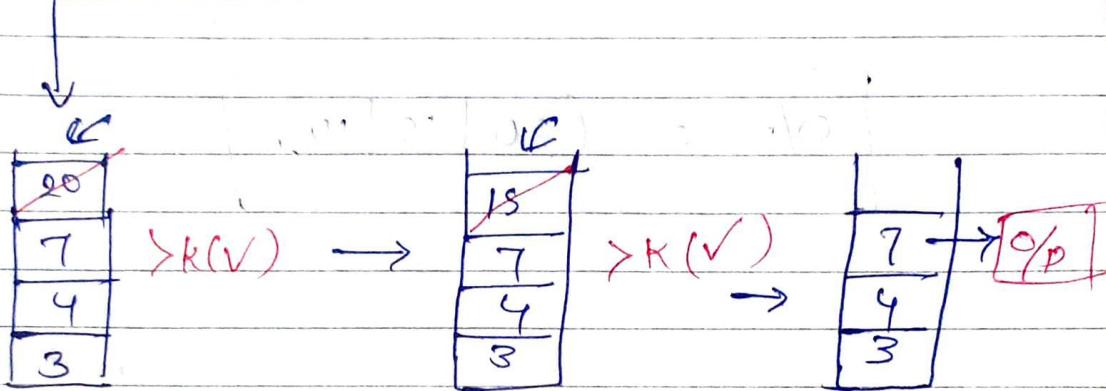
$n \log k$

3<sup>rd</sup> smallest element  $\rightarrow$  max heap

$\text{arr} \rightarrow$   
 $0 \rightarrow n-1$



max-heap



**CODE**

```
int maxHeap(int arr[], int k, int n)
```

```
{ priority_queue<int> maxh;
```

```
for (int i=0; i<n; i++)
```

```
{
```

```
    maxh.push(arr[i]);
```

```
    if (maxh.size() > k)
```

```
{
```

```
        maxh.pop();
```

```
}
```

```
}
```

```
return maxh.top();
```

# Return k largest Elements in Array.

Q.

Given,

$$\text{arr}[.] = [7 \ 10 \ 4 \ 3 \ 20 \ 15]$$

$$k = 3$$

$$\text{O/p} = [20 \ 15 \ 10]$$

~~Note~~  $k$  &  $k$  largest  $\rightarrow$  min-heap.

CODE

```
vector<int> mainHeap(int arr[], int k, int n)
```

{

```
priority_queue<int, vector<int>, greater<int> minh;
```

```
for (int i = 0; i < n; i++)
```

```
minh.push(arr[i]);
```

```
if (minh.size() > k)
```

```
minh.pop();
```

}

```
vector<int> res;
while(!minh().empty())
    res.push_back(minh.top());
    minh.pop()
```

```
return res;
```

4.

## Sort a K sorted Array

or

## Sort Nearly Sorted Array

Given,

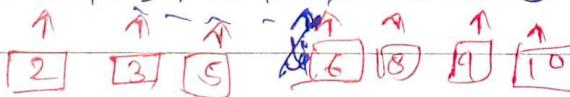
$$\text{arr} = [6 | 5 | 3 | 2 | 8 | 10 | 9]$$

$$(K=3)$$

$$\text{O/P} \Rightarrow [2 | 3 | 5 | 6 | 8 | 9 | 10]$$

means, the element at index  $i$  can be found in range  $\underline{\underline{[i-K, i+K]}}$

6, 5, 3, 2, 8, 10, 9



9
2
3
5
8

K



3
5
6
8

8
6
8
10



8
9
10



8
9
10

## CODE

```
vector<int> gork(vector<int> arr; int k, int n)
```

```
{
```

```
priority_queue<int, vector<int>, greater<int>> minh;
```

```
vector<int> res;
```

```
for(int i=0; i<n; i++)
```

```
{
```

```
minh.push(arr[i]);
```

```
if(minh.size() > k)
```

```
{
```

```
res.push_back(minh.top());
```

```
minh.pop();
```

```
}
```

```
{
```

```
while(!minh.empty())
```

```
{
```

```
res.push_back(minh.top());
```

```
minh.pop();
```

```
}
```

```
return res;
```

```
{
```

5.

## K - Closest Number

Given,

$$\text{arr}[] = [5 | 6 | 7 | 8 | 9]$$

$$K = 3$$

$$x = 7$$

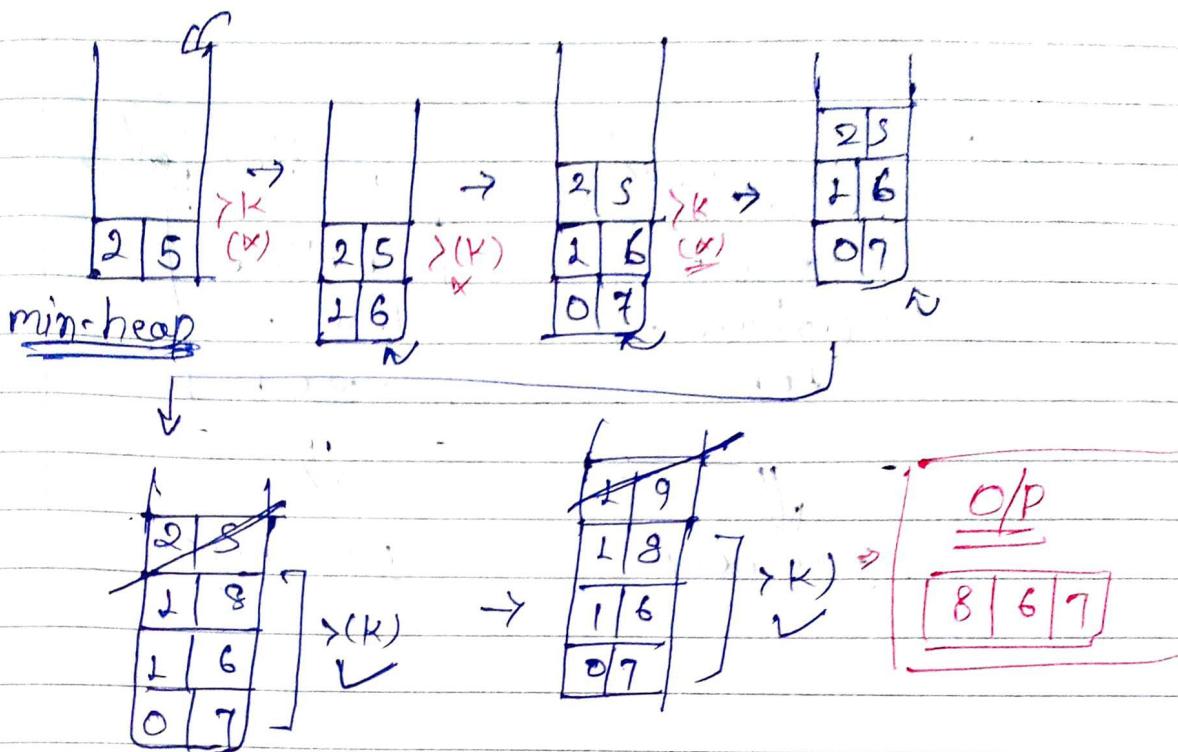
$$\text{o/p} = [6 | 7 | 8] \rightarrow \text{order doesn't matter}$$

Here we have to use key, value pair  
where key will be the absolute  
d/f. b/w  $\text{arr}[i] - x$ .

and min-heap will be used

key	value	
<u><math>\text{pair}[] : \text{arr}[i] - x</math></u>	<u><math>\text{arr}[i]</math></u>	<u>Key ↴ 0. 0 ↗ value</u> <u>min-heap</u>

Bg  $\Rightarrow$    
 $\frac{5, 6, 7, 8, 9}{-7 \ 7 \ 7 \ 7 \ 7}$   
 $\frac{}{2 \ [1 \ 0 \ 4] \ 2}$



CODE → define minh maxh

```
vector<int> kClosest(vector<int> arr, int k, int x, int n)
```

```
priority_queue<pair<int, int>> minh;
```

```
for(int i=0; i<n; i++)
```

```
    minh.push_back({abs(arr[i]-x), arr[i]});
```

```
if(minh.size() > k)
```

```
    minh.pop();
```

```
}
```

```
vector<int> res;
```

```
while(!minh.empty())
```

```
{
```

```
    res.push_back(minh.top());
```

```
    minh.pop();
```

```
return res;
```

```
}
```

6.

## Top = k Frequent Numbers

Note :-

largest freq.

largest  
greatest  
top  
max

min heap

smallest freq.

smallest  
lowest  
closest

max heap

### Problem Statement :-

Given,

arr = [2 | 1 | 1 | 3 | 2 | 2 | 4]

Frequencies ( $k=2$ )

O/P :- [1 | 2]

- 2 → 3 ✓
- 3 → 1
- 2 → 2 ✓
- 4 → 1

## Approach

By Using Unordered-map  
and  
min-heap.

unordered\_map<int, int> mp;

```
for(int i=0; i<n; i++)  
{  
    mp[arr[i]]++;  
}
```

min heap creation

priority\_queue<pair<int, int>,

vector<pair<int, int>, greater<

<pair<int, int>> min h

mp

1	3
3	1
2	2
4	1

```
for(auto i= mp.begin(); i!= mp.end(); i++)
```

{

minh.push\_back({i->second, i->first});

if(minh.size() > k)

minh.pop();

}

minh



vector<int> res;

while (!minh.empty())

Starting  
minh  
to  
res.  
vector

{

res.push\_back (minh.top()  $\rightarrow$  second);

minh.pop()

}

return res;

}.

7.

## Frequency sort

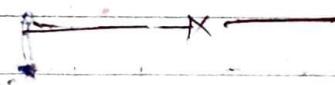
$$\underline{\text{arr}} = [2 | 2 | 2 | 3 | 2 | 2 | 4]$$



we have to sort it via max frequency.

I/O/P

$$[2 | 2 | 2 | 2 | 2 | 3 | 4]$$



Note: This Q. is same as previous (6).

arr

↓  
unordered\_map (freq, store).

↓  
max-heap (we won't check the size of k).



Store in vector



return

(CODE. is super-simple)

8.

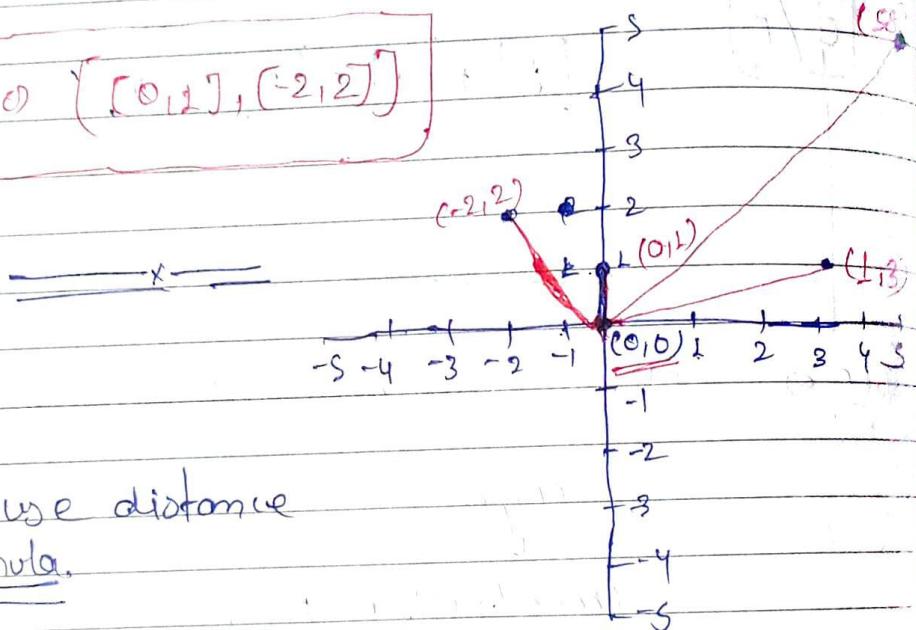
## K-Closest Points to Origin

Given,

$$\text{arr} = \begin{bmatrix} x_1 & y_1 \\ 1 & 3 \\ -2 & 2 \\ 5 & 8 \\ 0 & 1 \end{bmatrix} \quad K=2$$

Note  
order  
does  
not  
matter

O/P O  $\left[ [0, 1], [-2, 2] \right]$



We can use distance formula.

$$\text{dist.} = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

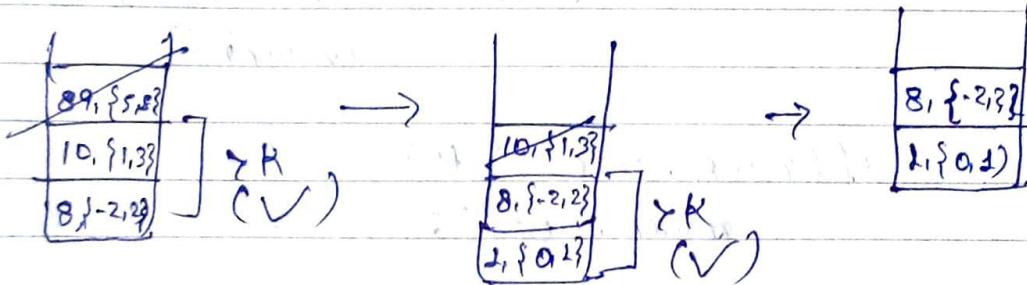
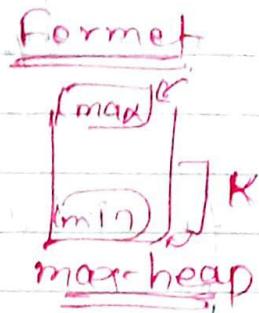
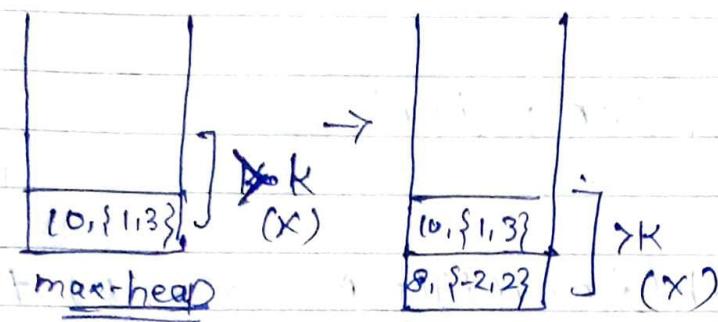
\* As we have from origin,  $(x_2, y_2) = (0, 0)$ .

$$\text{dist.} = \sqrt{x_1^2 + y_1^2}$$

As we have to compare,

$$(\sqrt{x^2 + y^2})^2 \Rightarrow x^2 + y^2$$

max-heap will be applied ⚡



only ⚡  $([-2, 2], [0, 1])$  ✓

$([0, 1], [-2, 2])$  is also accepted. ✓

i	0	1
arr[i][0]	10	15
arr[i][1]	20	25

## CODE

vector<vector<int>> res;

priority-queue<pair<int, pair<int, int>> maxh;

for(int i=0; i < n; i++)  
 {

maxh.push({arr[i][0] + arr[i][1],  
arr[i][1],  
 {arr[i][0], arr[i][1]}});

if(maxh.size() > k)  
 maxh.pop();

}

while (!maxh.empty())

{

pair<int, int> p = maxh.top().second;

res.push\_back(p);

maxh.pop();

}

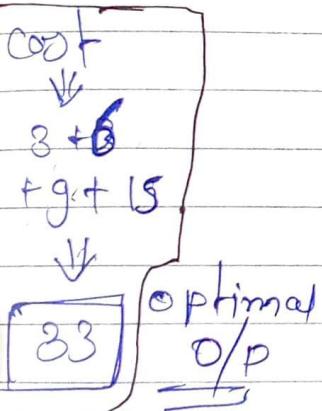
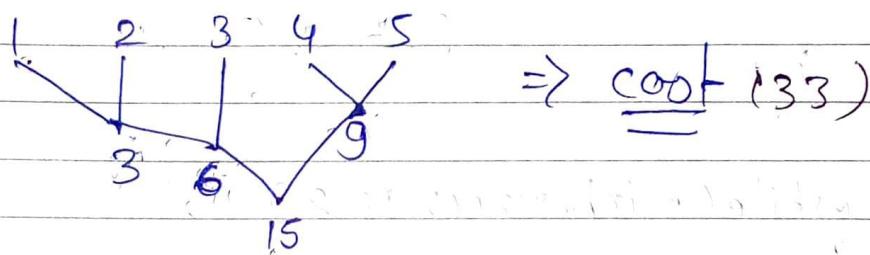
return res;

## Connect Ropes to minimize the cost

Given

$$\text{arr} = [1, 2, 3, 4, 5]$$

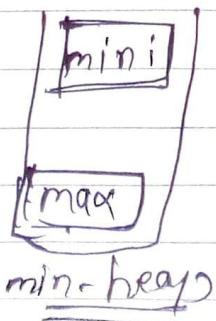
$$\text{O/P} = 33$$



Note o)

To get optimal output  
we have to add two  
smallest numbers each  
time,

min-heap is required o)



### CODE

priority-queue<int, vector<int>, greater<int>> minh;

```
for (int i = 0; i < n; i++)
```

```
    minh.push(arr[i]);
```

```
}
```

```
while (minh.size() >= 2)
```

```
{
```

```
    int first = minh.top();
```

```
    minh.pop();
```

```
    int second = minh.top();
```

```
    minh.pop();
```

```
    cost = cost + first + second;
```

```
    minh.push(first + second);
```

```
}
```

```
return cost;
```

20.

## Sum of Element

Given

arr[] : 

1	3	12	5	15	11
---	---	----	---	----	----

$$K1 = 3$$

$$K2 = 6$$

[O/P  $\Rightarrow$  23]

→ → ←

### Approach 1 ↗ sort and traverse.

2	3	5	11	12	15
---	---	---	----	----	----

↑      ↘  
3rd      6th

$$(11+12) \Rightarrow \underline{\underline{23}}$$

### Approach 2 ↗

Use maxHeap.

and

traverse.

## CODE

```
int sumElement(int arr[], int k, int n)
{
    priority_queue<int> maxh;
    for (int i=0; i<n; i++)
    {
        maxh.push(arr[i]);
        if (maxh.size() > k)
            maxh.pop();
    }
    return maxh.top();
}
```

```
int main()
{
    int first = sumElement(arr, 3, arr.size());
    int second = sumElement(arr, 6, arr.size());
    int sum = 0;
    for (int i=0; i<n; i++)
    {
        if (arr[i] > first && arr[i] < second)
            sum += arr[i];
    }
    return sum;
}
```