

# C1W3\_Assignment

December 13, 2020

## 1 Week 3 Assignment: Implement a Quadratic Layer

In this week's programming exercise, you will build a custom quadratic layer which computes  $y = ax^2 + bx + c$ . Similar to the ungraded lab, this layer will be plugged into a model that will be trained on the MNIST dataset. Let's get started!

### 1.0.1 Imports

```
[1]: import tensorflow as tf
from tensorflow.keras.layers import Layer

import utils
```

### 1.0.2 Define the quadratic layer (TODO)

Implement a simple quadratic layer. It has 3 state variables:  $a$ ,  $b$  and  $c$ . The computation returned is  $ax^2 + bx + c$ . Make sure it can also accept an activation function.

#### `__init__`

- call `super(my_fun, self)` to access the base class of `my_fun`, and call the `__init__()` function to initialize that base class. In this case, `my_fun` is `SimpleQuadratic` and its base class is `Layer`.
- `self.units`: set this using one of the function parameters.
- `self.activation`: The function parameter `activation` will be passed in as a string. To get the tensorflow object associated with the string, please use `tf.keras.activations.get()`

**build** The following are suggested steps for writing your code. If you prefer to use fewer lines to implement it, feel free to do so. Either way, you'll want to set `self.a`, `self.b` and `self.c`.

- `a_init`: set this to tensorflow's `random_normal_initializer()`
- `a_init_val`: Use the `random_normal_initializer()` that you just created and invoke it, setting the `shape` and `dtype`.

- The `shape` of `a` should have its row dimension equal to the last dimension of `input_shape`, and its column dimension equal to the number of units in the layer.
- This is because you'll be matrix multiplying  $x^2 * a$ , so the dimensions should be compatible.
- set the dtype to 'float32'
- `self.a`: create a tensor using `tf.Variable`, setting the `initial_value` and set trainable to `True`.
- `b_init`, `b_init_val`, and `self.b`: these will be set in the same way that you implemented `a_init`, `a_init_val` and `self.a`
- `c_init`: set this to `tf.zeros_initializer`.
- `c_init_val`: Set this by calling the `tf.zeros_initializer` that you just instantiated, and set the `shape` and `dtype`
  - `shape`: This will be a vector equal to the number of units. This expects a tuple, and remember that a tuple `(9,)` includes a comma.
  - `dtype`: set to 'float32'.
- `self.c`: create a tensor using `tf.Variable`, and set the parameters `initial_value` and `trainable`.

**call** The following section performs the multiplication  $x^2a + xb + c$ . The steps are broken down for clarity, but you can also perform this calculation in fewer lines if you prefer.

- `x_squared`: use `tf.math.square()`
- `x_squared_times_a`: use `tf.matmul()`.
- If you see an error saying `InvalidArgumentError: Matrix size-incompatible`, please check the order of the matrix multiplication to make sure that the matrix dimensions line up.
- `x_times_b`: use `tf.matmul()`.
- `x2a_plus_xb_plus_c`: add the three terms together.
- `activated_x2a_plus_xb_plus_c`: apply the class's `activation` to the sum of the three terms.

```
[2]: # Please uncomment all lines in this cell and replace those marked with `# YOUR_
      ↪CODE HERE`.
      # You can select all lines in this code cell with Ctrl+A (Windows/Linux) or_
      ↪Cmd+A (Mac), then press Ctrl+/ (Windows/Linux) or Cmd+/ (Mac) to uncomment.
```

```
class SimpleQuadratic(Layer):

    def __init__(self, units=32, activation=None):
        '''Initializes the class and sets up the internal variables'''
        # YOUR CODE HERE
        super(SimpleQuadratic, self).__init__()
        self.units=units
        self.activation=tf.keras.activations.get(activation)

    def build(self, input_shape):
        '''Create the state of the layer (weights)'''
```

```

        # a and b should be initialized with random normal, c (or the bias)
        ↪with zeros.
        # remember to set these as trainable.
        # YOUR CODE HERE
        a_init=tf.random_normal_initializer()
        a_init_val=a_init(shape=(input_shape[-1],self.units),dtype="float32")
        self.a=tf.Variable(initial_value=a_init_val,trainable=True)

        b_init=tf.random_normal_initializer()
        b_init_val=b_init(shape=(input_shape[-1],self.units),dtype="float32")
        self.b=tf.Variable(initial_value=b_init_val,trainable=True)

        c_init=tf.zeros_initializer()
        c_init_val=c_init(shape=(self.units,),dtype="float32")
        self.c=tf.Variable(initial_value=c_init_val,trainable=True)

    def call(self, inputs):
        '''Defines the computation from inputs to outputs'''
        # YOUR CODE HERE
        return self.activation(tf.matmul(tf.math.square(inputs),self.a)+tf.
        ↪matmul(inputs,self.b)+self.c)

```

Test your implementation

```
[3]: utils.test_simple_quadratic(SimpleQuadratic)
```

All public tests passed

Train your model with the SimpleQuadratic layer that you just implemented.

```

[4]: # THIS CODE SHOULD RUN WITHOUT MODIFICATION
     # AND SHOULD RETURN TRAINING/TESTING ACCURACY at 97%+

mnist = tf.keras.datasets.mnist

(x_train, y_train),(x_test, y_test) = mnist.load_data()
x_train, x_test = x_train / 255.0, x_test / 255.0

model = tf.keras.models.Sequential([
    tf.keras.layers.Flatten(input_shape=(28, 28)),
    SimpleQuadratic(128, activation='relu'),
    tf.keras.layers.Dropout(0.2),
    tf.keras.layers.Dense(10, activation='softmax')
])

model.compile(optimizer='adam',
              loss='sparse_categorical_crossentropy',
              metrics=['accuracy'])

```

```
model.fit(x_train, y_train, epochs=5)
model.evaluate(x_test, y_test)
```

Downloading data from <https://storage.googleapis.com/tensorflow/tf-keras-datasets/mnist.npz>

11493376/11490434 [=====] - 0s 0us/step

Train on 60000 samples

Epoch 1/5

60000/60000 [=====] - 12s 208us/sample - loss: 0.2760 - accuracy: 0.9178

Epoch 2/5

60000/60000 [=====] - 12s 198us/sample - loss: 0.1352 - accuracy: 0.9594

Epoch 3/5

60000/60000 [=====] - 12s 198us/sample - loss: 0.1019 - accuracy: 0.9684

Epoch 4/5

60000/60000 [=====] - 12s 198us/sample - loss: 0.0829 - accuracy: 0.9741

Epoch 5/5

60000/60000 [=====] - 12s 197us/sample - loss: 0.0698 - accuracy: 0.9778

10000/10000 [=====] - 1s 68us/sample - loss: 0.0746 - accuracy: 0.9778

[4]: [0.07460902843918885, 0.9778]

[ ]: